

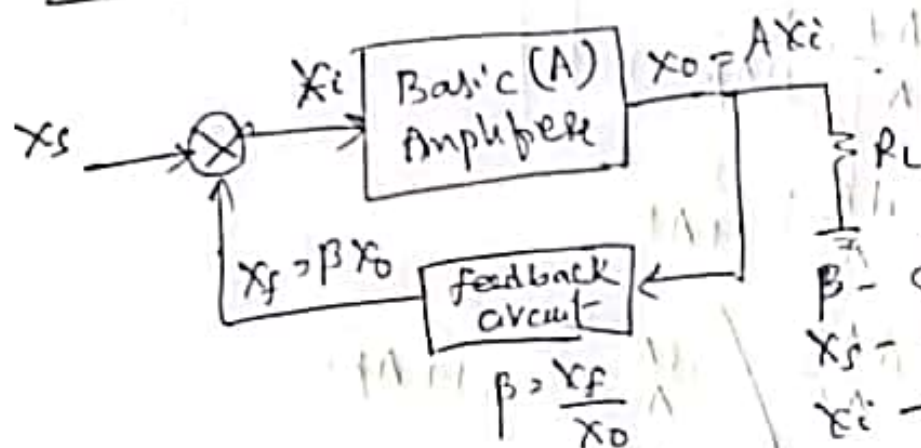
Negative feedback Amplifiers

(1)

Advantages.

1. Improves stability
 2. Increases Bandwidth
 3. Increases I/p Impedance
 4. Decreases o/p Impedance
 5. Reduces Noise and distortion.
- But Gain decreases.

Negative feedback amplifiers



These signals cause no voltage or current

β - feedback factor
 X_s - Source signal
 X_i - I/p signal to amplifier
 X_f - feedback signal
 X_o - o/p signal
 A - gain without feedback

$$X_i = X_s - X_f$$

$$A = \frac{X_o}{X_i}$$

$$A_f = \frac{X_o}{X_s} = \frac{X_o}{X_i + X_f} = \frac{AX_i}{X_i + \beta X_o} = \frac{AX_i}{X_i + A\beta X_i}$$

A_f - gain with negative feedback

$$A_f = \frac{A}{1 + A\beta}$$

Stabilization of Gain in Negative feedback Amplifier

$$A_f = \frac{A}{1+AB}$$

Differentiate w.r.t A

$$\frac{dA_f}{dA} = \frac{(1+AB) - AB}{(1+AB)^2} = \frac{1}{(1+AB)^2}$$

$$\text{But } \frac{A_f}{A} = \frac{1}{1+AB}$$

$$\frac{dA_f}{dA} = \frac{A_f}{A} \cdot \frac{1}{1+AB}$$

$$\frac{dA_f}{A_f} = \frac{dA}{A} \cdot \frac{1}{1+AB}$$

$$\text{Sensitivity } \frac{dA_f/A_f}{dA/A} = \frac{1}{1+AB}$$

$$\text{Desensitivity} = (1+AB)$$

The % change in gain with feedback (due to temperature variations) reduced by $(1+AB)$ times compared to without feedback.

R_{if} — Input Impedance with feedback
 R_i — " " without feedback

$$R_{if} = R_i (1+AB)$$

$$\text{If } R_{of} = \frac{R_o}{1+AB}$$

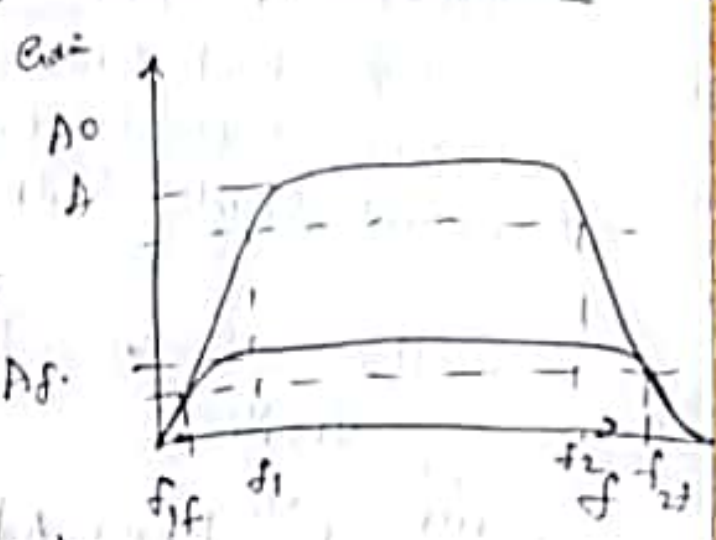
where R_{of} — o/p Impedance with feedback

R_o — o/p Impedance without feedback

Frequency Response of Negative Feedback Amplifier

$f_2 - f_1$ - Bandwidth with out feedback

$f_{2f} - f_{1f}$ - Bandwidth with feedback



So with feedback the gain decreases (A_f) but Bandwidth increases.

Distortion reduces $D / (1 + A\beta)$

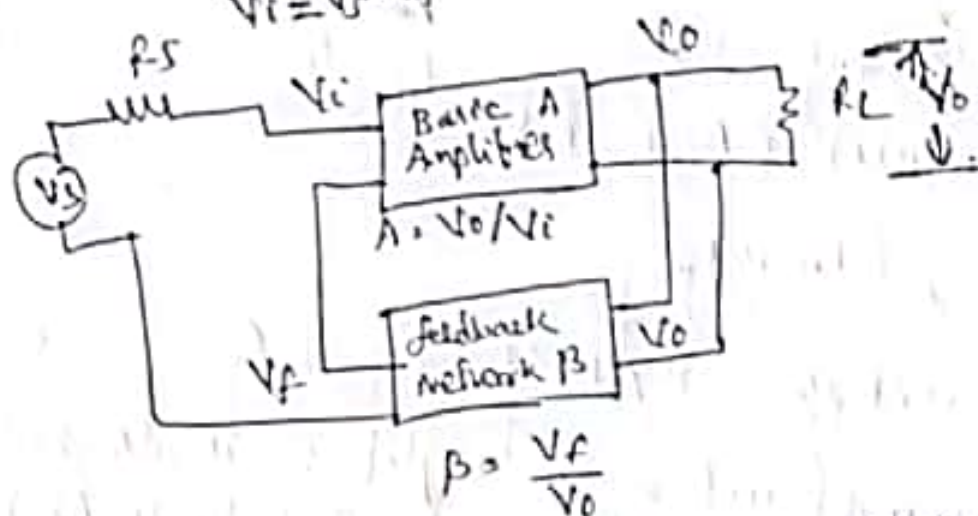
Noise produced within an amplifier is also reduced by negative feedback again by a factor $(1 + A\beta)$

Output Current So gain decreases

Four Basic feedback topologies are

1. Voltage Series feedback Amplifier.
2. Voltage Shunt feedback Amplifier.
3. Current Series feedback Amplifier.
4. Current Shunt feedback Amplifier.

1) Voltage Series feedback Amplifier



Sampling Signal o/p Voltage V_o (I/p to feedback w/w)
 mixing signal V_f voltage f.o/p from feedback w/w

A part of o/p voltage fed back to i/p decreases
 i/p voltage V_i ($V_i = V_s - V_f$) known as
 Voltage Series feedback Amplifier. In this
 Gain decreases as i/p voltage is decreased due to
 feedback.

→ R_{if} Increases
 R_{of} decreases.

Frequency Response of Negative feedback Amplifier (3)

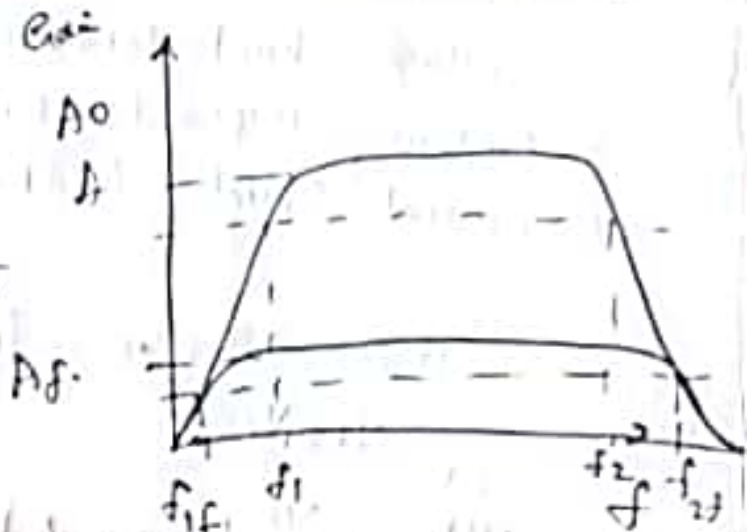
$f_2 - f_1$ - Bandwidth
without feedback

$f_{2f} - f_{1f}$ - Bandwidth with
feedback

So with feedback the
gain decreases (A_f) but
Bandwidth increases.

Distortion reduces $D / (1 + A\beta)$

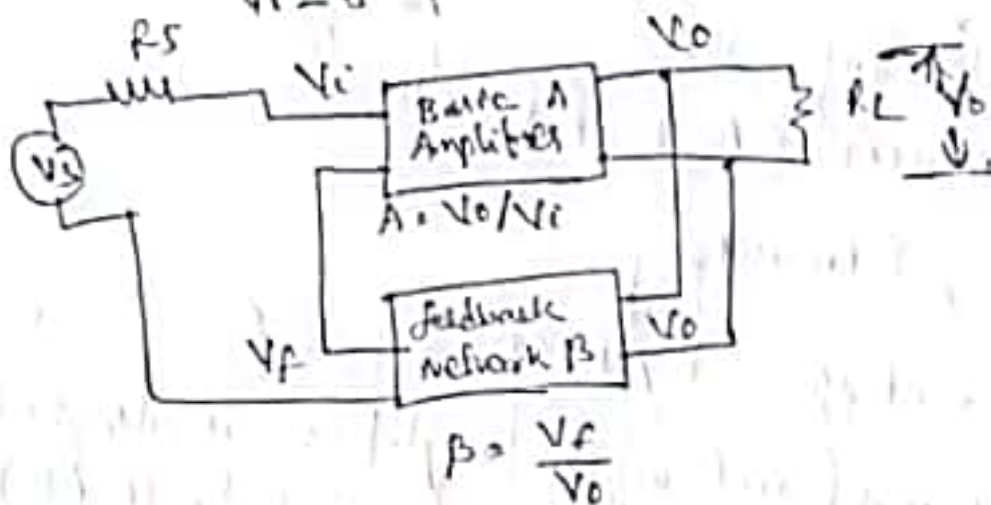
Noise produced within an amplifier is also reduced
by negative feedback again by a factor $(1 + A\beta)$



Four Basic feedback topologies are

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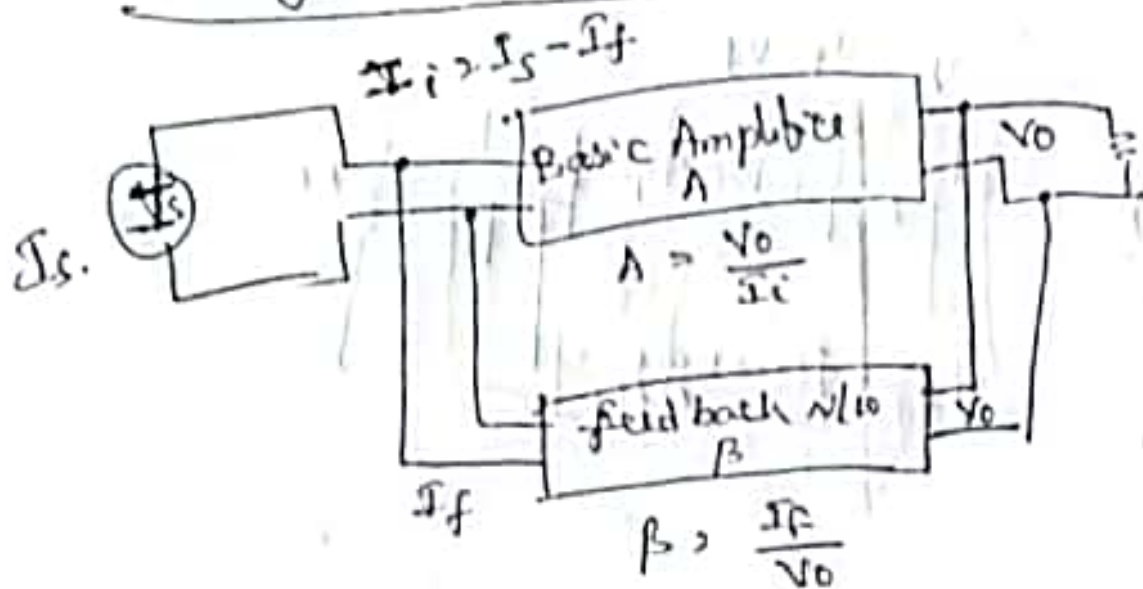
1) Voltage Series feedback Amplifier



Sampling Signal o/p Voltage V_o (I/p to feedback/w)
 mixing signal V_f voltage (o/p from feedback/w)

A part of o/p voltage fed back to i/p decreases
 i/p voltage V_i ($V_i = V_s - V_f$) known as
 Voltage Series feedback Amplifier. In this
 Gain decreases as i/p voltage is decreased due to
 feedback.
 \rightarrow R_{if} Increases
 R_{of} decreases.

2. Voltage Shunt Feedback Amplifier 5



Sampling Signal — Voltage V_o
 mixing Signal — Current I_f
 Gain A — Transresistance — V_o / I_i
 β — Trans conductance $\frac{I_f}{V_o}$

o/p Resistance decreases.

i/p Resistance decreases

(Note: Both sides shunt connection)

I_s — Source current

I_f — feedback current

V_o — o/p voltage

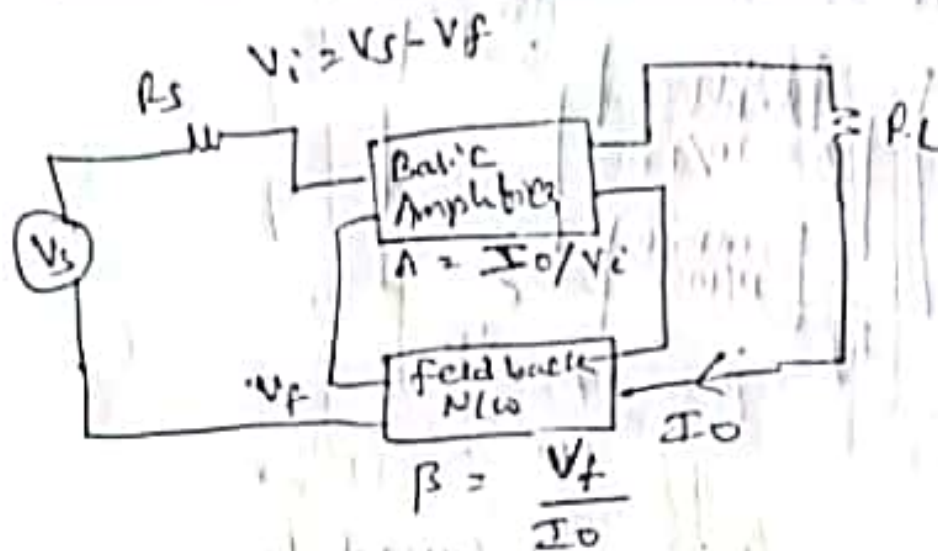
A part of o/p voltage feedback to i/p decreases

i/p current known as voltage shunt

feedback amplifies. As i/p current decreases
 o/p current decreases o/p voltage V_o also decreases
 So Gain decreases.

Current Series feedback Amplifier

(6)



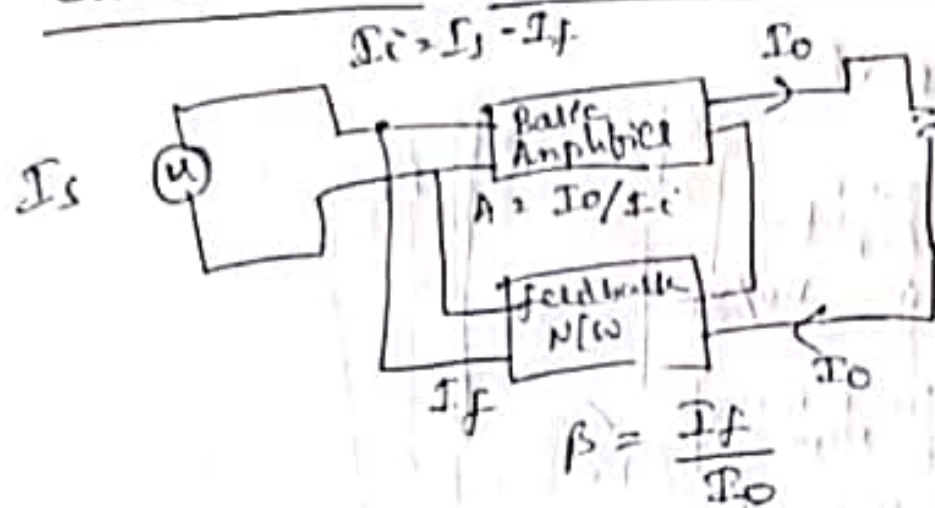
A part of o/p current feedback to i/p decreases i/p voltage known as Current series feedback amplifier. Gain in current series feedback amplifier is $A = I_o / V_i$ known as Transconductance. β reciprocal of A .

$\beta = \frac{V_f}{I_o}$ In current series feedback

Input Resistance and o/p Resistance both increases.

Current Shunt-feedback Amplifier

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The sampling signal is o/p current I_o
mixing signal is I_f .

A part of o/p current fed back to I/p decreases
I/p current ($I_i = I_s - I_f$) and gain so.
It is known as Current shunt feedback amplifier.

O/p Resistance increases.

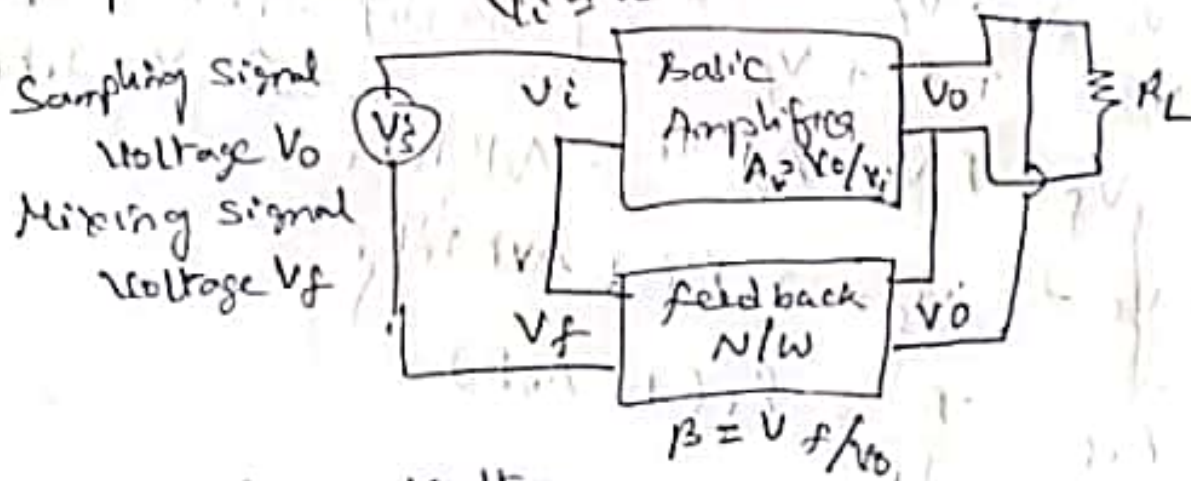
I/p Resistance decreases with feedback

(Note at o/p series connection, at i/p shunt connection)

Voltage Series Feedback Amplifier

In voltage series feedback Amplifier output of op output voltage feedback to i/p decreases i/p voltage and voltage gain (V_o/V_s).

The block diagram of voltage series feedback amplifier shown in fig.



V_s - Source voltage

V_o - o/p voltage

V_i - i/p voltage to the Amplifier.

A_v - The gain of the amplifier without feedback

$$A_v = \frac{V_o}{V_i}$$

A_{vf} - The voltage gain of the amplifier with feedback

$$V_s = V_i + V_f$$

$$A_v = \frac{V_o}{V_i} \quad B = \frac{V_f}{V_o}$$

$$A_{vf} = \frac{V_o}{V_s} = \frac{V_o}{V_i + V_f} = \frac{A_v V_i}{V_i + B V_o} = \frac{A_v V_i}{V_i + A_v B V_i}$$

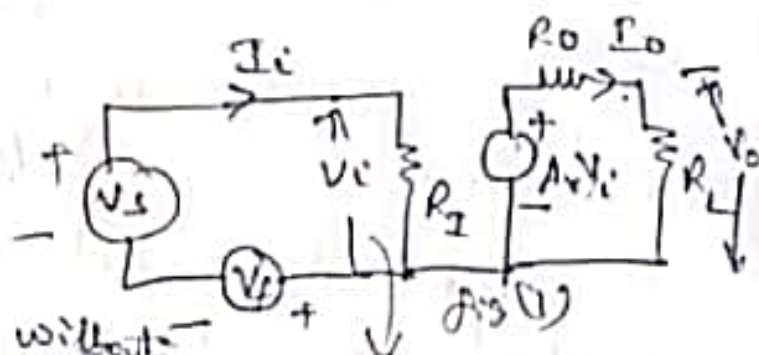
$$A_{vf} = \frac{A_v}{1 + A_v B}$$

o/p output - I/p - Input (2)

The Thevenin Equivalent Circuit to find

R_{if}

R_{if} - I/p Impedance with feedback



R_i - I/p Impedance without feedback

$$V_s = V_i + V_f \quad \text{feedback}$$

$$V_s = I_i R_i + V_f \quad \left(\begin{array}{l} \text{The drop across } R_i = V_i \\ V_i = I_i R_i \end{array} \right)$$

$$V_f = \beta V_o = A_v \beta V_i = A_v \beta I_i R_i$$

$$\text{so } V_s = V_i + V_f = I_i R_i + A_v \beta I_i R_i$$

$$R_{if} = \frac{V_s}{I_i} = R_i (1 + A_v \beta)$$

R_{of} - o/p Impedance with feedback

In the above dig remove R_L . Connect Voltage source V at o/p and set $V_s = 0$.

$$V_i = -V_f ; V_o = V$$

$$I = \frac{V - A_v V_i}{R_o} = \frac{V + A_v V_f}{R_o}$$

$$I = \frac{V + A_v \beta V}{R_o} = \frac{V (1 + A_v \beta)}{R_o} \Rightarrow R_{of} = \frac{V}{I}$$

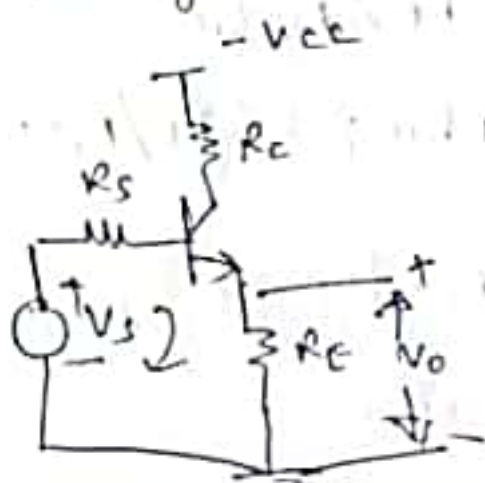
$$R_{of} = \frac{R_o}{1 + A_v \beta}$$

with feedback R_{of} decreases.

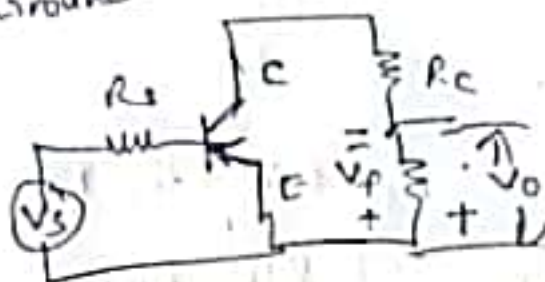
$$\text{If } R_L \text{ included } R_{of} = \frac{R_o'}{1 + A_v \beta} \text{ where } R_o' = R_o \parallel R_L$$

The Emitter follower is an example for voltage series feedback amplifier.

(3)



Draw the hybrid model of this circuit. Connect $-V_{CC}$ to Ground



The voltage drop across R_E is V_o as well as V_f

In Fig (1)

$$V_s = I_B R_s + V_{BE} + I_E R_E$$

$$I_E R_E = V_s - I_B R_s - V_{BE}$$

So $I_E R_E = V_o$ \uparrow $V_{BE} \downarrow$ This is voltage series feedback principle.

The voltage gain $A_v = \frac{V_o}{V_s} \quad \text{--- (1)}$

$$V_o = h_{fe} I_B R_E \quad \text{--- (2)}$$

$$V_s = I_B (R_s + h_{ie}) \quad \text{--- (3)}$$

② & ③ substitute in $A_v = \frac{V_o}{V_s} \quad \text{--- (1)}$

$$A_v = \frac{V_o}{V_s} = \frac{h_{fe} R_E}{R_s + h_{ie}}$$

$$\beta = \frac{V_f}{V_o} \frac{V_o}{V_s} ; \quad V_f = V_o \quad \beta = 1$$

$$D = 1 + A_v \beta = 1 + \frac{h_{fe} R_E}{R_s + h_{ie}}$$

$$D = \frac{R_s + h_{ie} + h_{fe} R_E}{R_s + h_{ie}}$$

The gain with feedback A_{vf}

$$A_{vf} = \frac{A_v}{D} = \frac{h_{fe} R_E / (R_s + h_{ie})}{R_s + h_{ie} + h_{fe} R_E / (R_s + h_{ie})}$$

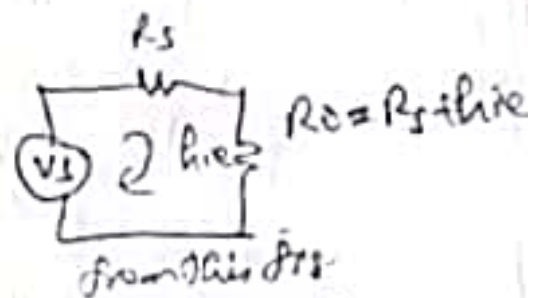
$$D = 1 + A_v B$$

$$A_{vf} = \frac{h_{fe} R_E}{R_s + h_{ie} + h_{fe} R_E}$$

$R_s + h_{ie} \ll h_{fe} R_E$

$$A_{vf} = \frac{h_{fe} R_E}{h_{fe} R_E} \approx 1$$

$$R_{if} = \frac{R_i (1 + A_v B)}{1} = R_i D$$



$$R_{if} = (R_s + h_{ie}) D = (R_s + h_{ie}) \frac{(R_s + h_{ie} + h_{fe} R_E)}{(R_s + h_{ie})}$$

$$R_{if} = R_s + h_{ie} + h_{fe} R_E$$

$$R_{of} = \frac{R_o}{D} \quad R_o = R_E$$

$$R_{of} = R_E (R_s + h_{ie}) / (R_s + h_{ie} + h_{fe} R_E)$$

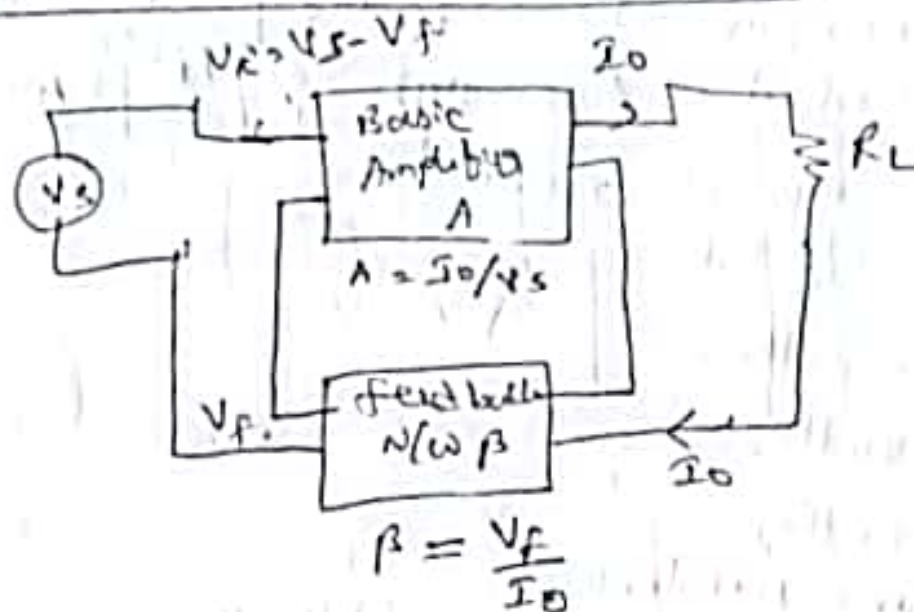
$$\lim_{R_E \rightarrow \infty} R_{of} = \frac{R_E (R_s + h_{ie})}{R_s + h_{ie} + h_{fe} R_E}$$

$$= \frac{R_E (R_s + h_{ie})}{R_E (R_s + h_{ie} + h_{fe})} = \frac{R_s + h_{ie}}{h_{fe}}$$

So in emitter follower OIP impedance increases and OIP impedance decreases.

Current Series feedback amplifiers

①



In current series feedback amplifier, a part of output current fed back to i/p i.e. decreases i/p voltage and transconductance $I_o / V_s = G_{MF}$

Sampling signal is current
mixing signal is Voltage

The characteristics of current series feedback amplifier are

1. G_{MF} decreases
2. Bandwidth increases.
3. I/p Impedance and output impedance both increases.
4. Noise / distortion decreases.
5. Stability improves.

It is also known as Transconductance amplifier.

In current series feedback amplifier
 The Thevenin's equivalent
 circuit preferred at i/p side
 The Norton's equivalent circuit
 preferred at o/p side.



- V_s - Source voltage
- V_i - i/p voltage
- V_o - o/p voltage
- R_s - Source resistance
- R_i - I/p resistance without feedback
- R_o - o/p resistance without feedback
- G_m - I_o / V_i Transconductance
- $R_i = \infty$ $V_i = V_s$
- $R_o = \infty$ $I_o = I_L = G_m V_i$

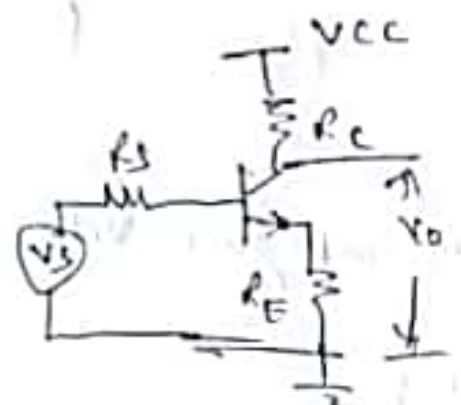


fig. CE amplifier without
 bypass capacitor
 with feedback
 decreases.

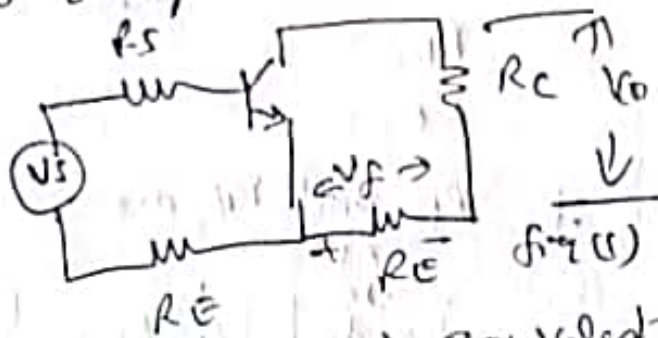
This works as current series feed
 back amplifier.
 The current flowing through R_E
 in I_E produces $I_E R_E = V_f$
 decreases i/p voltage V_{BE} (V_i)

$$\beta = \frac{V_f}{I_o} = -\frac{I_o R_E}{I_o} = -R_E$$

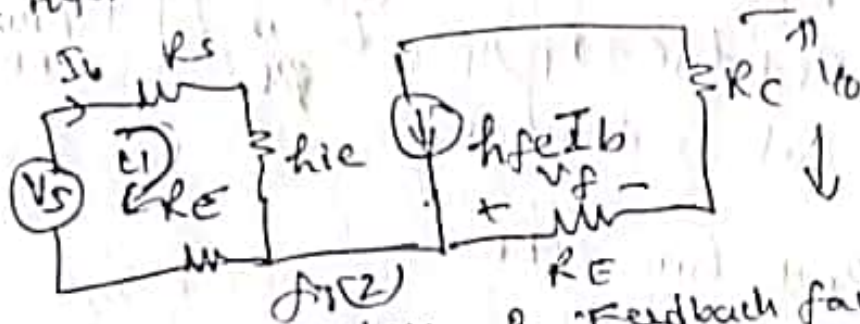
where β is feedback factor.

As V_i decreases the Gain
 known as Transconductance G_m f

To analyze this Equivalent circuit



The Hybrid model Equivalent of this is



$\beta = -R_E$ where β Feedback factor.

When $R_C = \infty$ $R_s = 0$ $V_i = V_s$

Trans conductance $G_M = \frac{I_o}{V_i} = \frac{-h_{fe} I_b}{V_s}$

In loop 1 $V_s = I_b (R_s + h_{ie} + R_E)$

$G_M = \frac{I_o}{V_s} = \frac{-h_{fe}}{R_s + h_{ie} + R_E}$ (1); $\beta = -R_E$

$D = 1 + \beta G_M = 1 + \frac{h_{fe} R_E}{R_s + h_{ie} + R_E}$

$G_{MF} = \frac{G_M}{D}$

$G_{MF} = \frac{-h_{fe}}{R_s + h_{ie} + (1 + h_{fe}) R_E}$

then $G_{MF} = -\frac{1}{R_E}$

So R_E stable resistor the transconductance G_{MF} stabilized with feedback.

In fig (2) $I_o = G_{MF} V_s = \frac{-h_{fe} V_s}{R_s + h_{ie} + (1 + h_{fe}) R_E} = -\frac{V_s}{R_E}$

So o/p current depends on V_s and R_E .

The voltage gain with feedback $A_{Vf} = \frac{I_o R_L}{V_s}$

$$A_{Vf} = \frac{G_m V_s R_L}{V_s} = -\frac{R_L}{R_E}$$

Voltage gain is stable if R_E and R_L are stable.

In i/p loop

$$V_s = I_b (R_s + h_{ie} + R_E)$$

R_i with out feedback is

$$\frac{V_s}{I_b} = R_s + h_{ie} + R_E$$

$$R_{if} = R_i (1 + G_m R_E) = R_i D = (R_s + h_{ie} + R_E) \times D$$

$$= \cancel{R_s + h_{ie} + R_E} \times \frac{R_s + h_{ie} + (1 + h_{fe}) R_E}{\cancel{R_s + h_{ie} + R_E}}$$

$$\text{So } R_{if} = R_s + h_{ie} + (1 + h_{fe}) R_E$$

with feedback i/p impedance increased.

R_{of} - o/p resistance with feedback

$$R_o = \infty \quad R_o' = R_L$$

$$R_{of}' = R_o' \frac{1 + \beta G_m}{1 + \beta G_m}$$

$$G_m = \lim_{R_L \rightarrow 0} G_m$$

$$= \lim_{R_L \rightarrow 0} \frac{-h_{fe}}{R_s + h_{ie} + R_E} = G_m$$

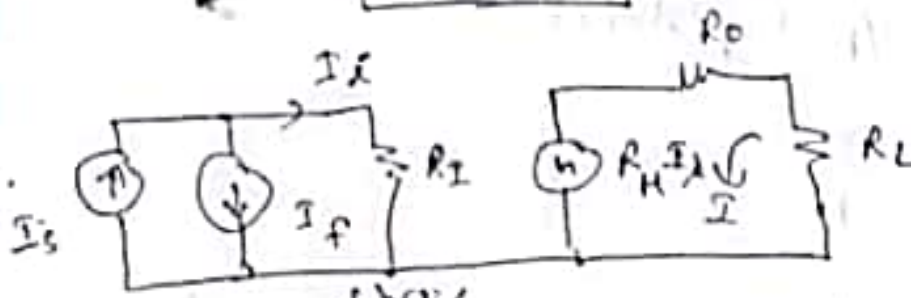
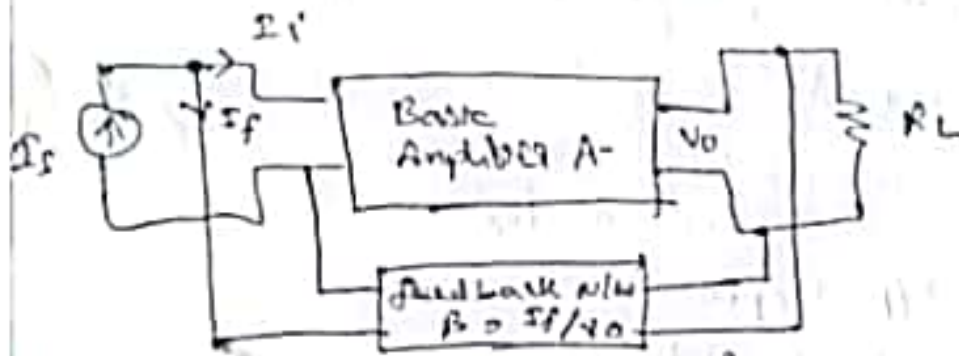
$$R_{of}' = R_L \frac{1 + \beta G_m}{1 + \beta G_m} = R_L$$

R_{of}' o/p resistance with feedback including R_L .

R_L - Load Resistance

Voltage Shunt feedback Amplifier.

①



with feedback Transmittance $= \frac{V_o}{I_s} = \frac{V_o}{I_i + I_f}$

$$R_{Hf} = \frac{V_o}{I_i + \beta V_o} = \frac{V_o}{I_i} \cdot \frac{1}{1 + \beta \frac{V_o}{I_i}} = \frac{R_H}{1 + \beta R_H}$$

$\frac{V_o}{I_i} = R_H$ - Transmittance without feedback

$R_{Hf} = \lim_{R_L \rightarrow \infty} R_H$ - open circuit transmittance

Input resistance with feedback (R_{if})

$$R_{if} = \frac{V_i}{I_s} = \frac{V_i}{I_i + I_f} = \frac{V_i}{I_i + \beta V_o} = \frac{V_i}{I_i + \beta R_H I_i}$$

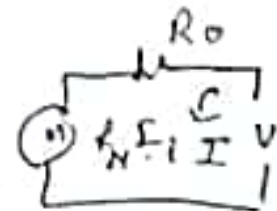
$$R_{if} = \frac{V_i}{I_i} \cdot \frac{1}{1 + \beta R_H} = \frac{R_i}{1 + \beta R_H}$$

R_i - i/p resistance without feedback

R_{of} o/p resistance with feedback. At $I_s = 0$ $R_L \rightarrow \infty$

connected V at o/p. i.e. (2)

$$I = \frac{V - R_H I_i}{R_o} \quad \begin{matrix} I_s = 0 \\ I_i = -I_f \end{matrix}$$



Voltage shunt feedback amplifier

①

Collector to base bias in CE amplifier works as voltage shunt feedback amplifier.

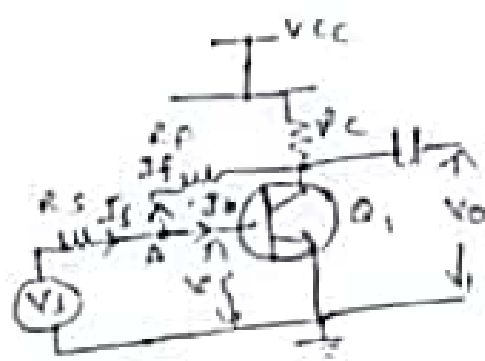
The transistor in CE configuration.

if applied b/w base and emitter

if taken b/w collector and emitter.

R_c collector resistor R_s source resistor.

R_f feedback resistor b/w collector and ~~emitter~~ base of the transistor.



As V_o increases the if current I_b decreases.

At node A Kirchhoff's current law applied.

$$I_s = \frac{V_i}{R_s}$$

$$I_b = I_s - I_f$$

V_i small $V_i \ll 0$

$$\frac{V_i - V_o}{R_f} = I_f$$

$$-\frac{V_o}{R_f} = I_f$$

$$\boxed{V_o \uparrow \rightarrow I_f \uparrow \rightarrow I_b \downarrow}$$

$$\boxed{\beta = \frac{I_f}{V_o} = -\frac{1}{R_f}} \quad \text{--- (1)}$$

β = feedback factor

It has gain A without feedback $A = R_M$

reciprocal of β ($A = \frac{1}{\beta}$ by definition)

A gain of the amplifier = $\frac{V_o}{I_i}$

- Transresistance amplifier

$$A = \frac{V_o}{I_i}$$

$$R_{MF} = \frac{R_M}{1 - \beta R_M}$$

R_{MF} - Transresistance with feedback

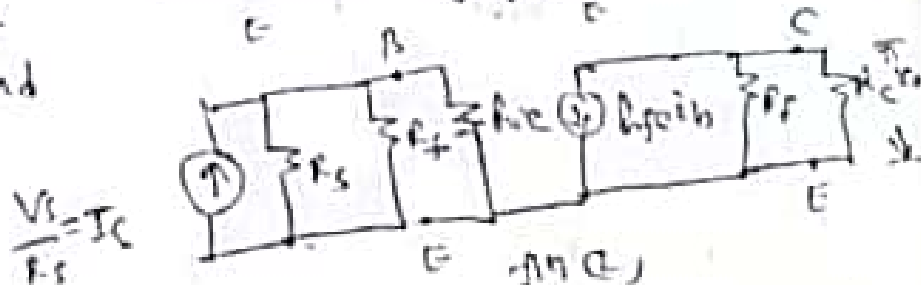
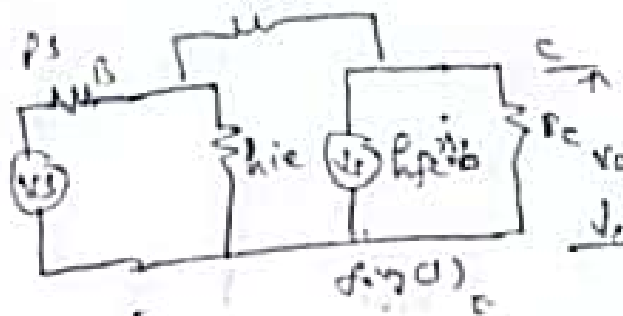
R_M - Transresistance without feedback

$$\left[\begin{array}{l} A = R_M \\ A_f = A + \beta \\ \frac{A}{1 - \beta A} = \frac{R_M}{1 - \beta R_M} \end{array} \right]$$

2
To analyze this hybrid model is used.

R_f can be split towards i_b side and o/p side using Millers theorem.

For simplification R_f connected towards i/p and o/p side in fig 2



Now to analyze it

R_{in} , β , R_{Mf} , R_{zf} , R_{of} , A_{vf} derivation from Hybrid parameters.

$\beta = i_b$ feedback factor $\frac{I_f}{V_o}$

To find R_M $\beta = -\frac{1}{R_f}$ - (1)

$$R_M = \frac{V_o}{I_i} = \frac{V_o}{I_c}$$

$$R_f \parallel R_C = R_C' = \frac{R_f R_C}{R_f + R_C}$$

$$V_o = -h_{fe} i_b R_C' \quad \text{--- (2)}$$

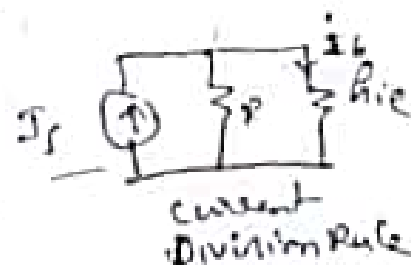
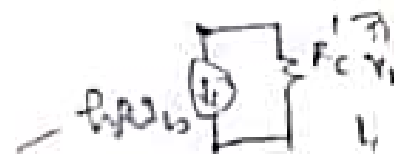
$$R_s \parallel R_f = R = \frac{R_s R_f}{R_s + R_f}$$

$$i_b = \frac{I_c \cdot R}{R + h_{ie}} \quad \text{--- (3)}$$

Substitute (3) in (2)

$$V_o = \frac{-h_{fe} I_s R R_C'}{R + h_{ie}}$$

$$R_M = \frac{V_o}{I_s} = \frac{-h_{fe} R_C' R}{R + h_{ie}} \quad \text{--- (4)}$$



Current Division Rule

$$R_{Mf} = \frac{R_M}{1 + \beta A_{vf}}$$

$$= \frac{-h_{fe} R_C' R}{R + h_{ie}} \cdot \frac{1}{1 + \left(\frac{-h_{fe} R_C' R}{R + h_{ie}} \right) \left(\frac{-1}{R_f} \right)}$$

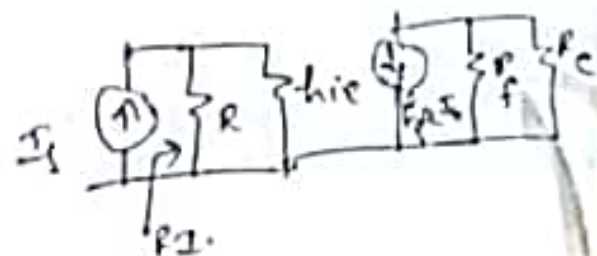
$$R_{Mf} = \frac{-h_{fe} R_C' R}{(R + h_{ie}) R_f + h_{fe} R_C' R} \quad \text{--- (5)}$$

(3)

mid R_{sf} at i/p side

$$R = R_f || R_s$$

$$R_s = R || h_{ie} = \frac{R h_{ie}}{R + h_{ie}} \quad (6)$$



with feedback $R_{sf} = \frac{R_s}{1 + \beta R_M} \quad (7)$

Output R_{of}

$$R_c = \infty$$

$$R_{in} = R_c \rightarrow \infty \quad R_M = \frac{-h_{fe} R_c R}{R + h_{ie}} \quad (8)$$

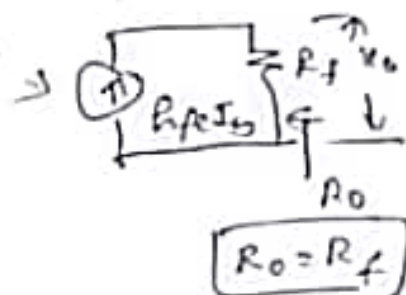
$$R_c' = R_f || R_c$$

$$R_c = \infty \text{ now}$$

replace $R_c' = R_f$ in (8)

$$R_M = \frac{-h_{fe} R_f R}{R + h_{ie}} \quad (9)$$

In o/p now



$$R_{of} = \frac{R_o}{1 + \beta R_M}$$

substitute now

$$R_o = R_f$$

$$R_M \text{ from (9) in } R_{of}$$

$$\beta = -\frac{1}{R_f}$$

$$R_{of} = \frac{R_f}{1 + \beta R_M} = \frac{R_f}{1 + \frac{1}{R_f} \frac{h_{fe} R_f R}{R + h_{ie}}}$$

$$\downarrow R_{of} = \frac{R_f (R + h_{ie})}{R + h_{ie} + h_{fe} R} \quad \text{As } R \text{ is high}$$

In voltage shunt feedback amplifiers

$$R_{sf} \downarrow \quad R_{of} \downarrow$$

$$R_{of}' = R_{of} || R_c \quad (\text{including external } R_c)$$

the gain of the amplifier

$$A_{vf} = \frac{V_o}{V_s} = \frac{V_o}{I_s \cdot R_s} = \frac{R_{mf}}{R_s}$$

So in voltage shunt feedback amplifier
voltage gain decreases with feedback.

R_{if} and R_{of} decreases.

It is known as Transresistance Amplifier.

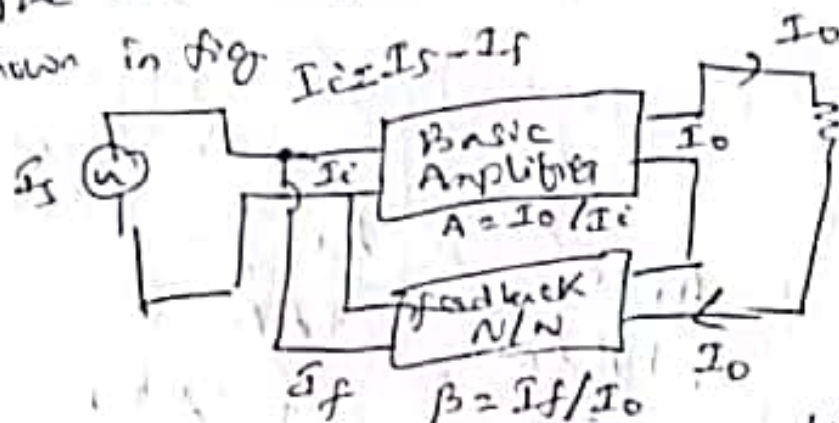
$$R_{of} = R_{of} \parallel R_c$$

Current shunt feedback amplifier

①

In Current shunt feedback amplifier a part of o/p current fed back to i/p, decrease i/p current and current gain I_o/I_i .

The block diagram of current shunt feedback amplifier shown in fig.



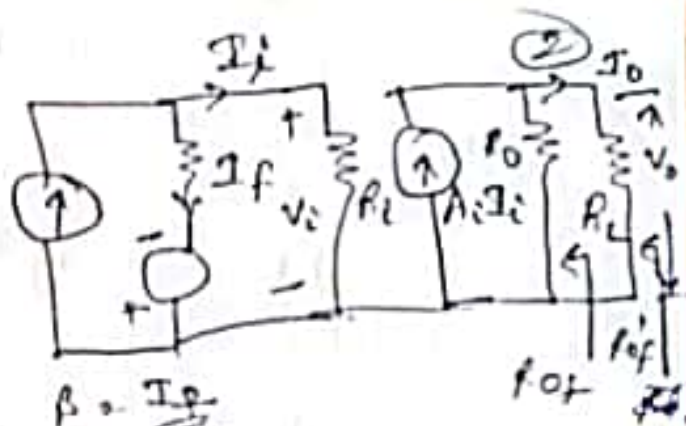
In current shunt feedback amplifier, the sampling current is I_o . mixing signal is current (I_f).
The current gain without feedback $A_1 = I_o/I_i$
feedback factor $\beta = I_f/I_o$.

The o/p impedance increases and i/p impedance decreases.

The characteristics of current shunt feedback amplifier

1. Sampling and mixing signal both are current.
2. The current gain with feedback A_{if} decreases.
3. Bandwidth increases.
4. Noise/Distortion decreases.
5. Stability of gain
6. i/p Impedance decreases; o/p impedance increases.

A_i - Short-circuit current gain
 A_i - The current gain without feedback
 A_{if} - The current gain with feedback



$$A_{if} = \frac{I_o}{I_s}$$

$$A_i = \frac{I_o}{I_i}$$

$$\beta = \frac{I_f}{I_o}$$

$$A_i I_i = I_o$$

$$I_s = I_i + I_f$$

$$A_{if} = \frac{A_i I_i}{I_i + I_f} = \frac{A_i I_i}{I_i + \beta A_i I_i} = \frac{A_i}{1 + A_i \beta}$$

from o/p loop $I_o = A_i I_i \frac{R_o}{R_o + R_L}$ ($R_L = 0$) $I_o = A_i I_i \frac{R_o}{R_o}$
 $A_i = \frac{I_o}{I_i}$

$$A_i = \frac{R_o}{R_L} A_i$$

$$\text{If } R_L = 0 \quad A_{if} = \frac{A_i}{1 + A_i \beta}$$

Input Impedance $R_{if} = \frac{V_i}{I_s} = \frac{I_i R_i}{I_i + I_f} = \frac{I_i R_i}{I_i + \beta A_i I_i}$

$$\text{So } R_{if} = \frac{R_i}{1 + A_i \beta}$$

Input impedance R_{if} decreases with feedback.

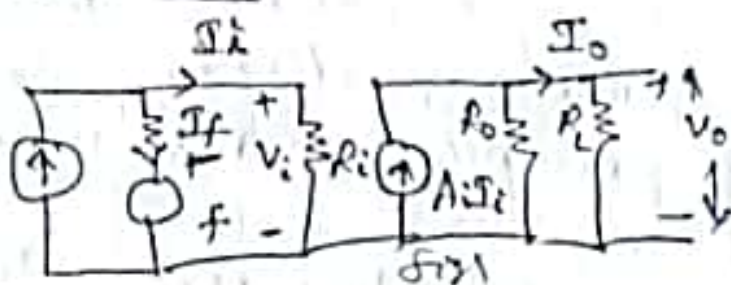
O/p Resistance with feedback (R_{of})

(3)

Set $I_s = 0$ remove R_L

Connect V at o/p.

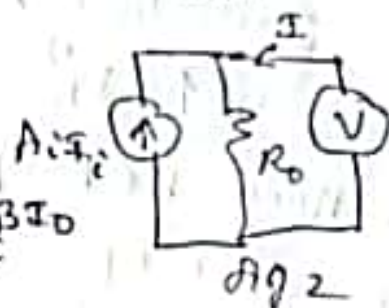
Then o/p current $I_o = I$ I_s



$$I = \frac{V}{R_o} - A_i I_i \text{ from fig 2}$$

Since $I_s = 0$ $I_i = -I_f$

$$\text{So } I = \frac{V}{R_o} + A_i I_f = \frac{V_o}{R_o} + A_i \beta I_o$$



$$I = \frac{V}{R_o} - A_i \beta I$$

$$I(1 + A_i \beta) = \frac{V}{R_o} \Rightarrow \frac{V}{I} = R_o(1 + A_i \beta) = R_{of}$$

$$\boxed{R_{of} = R_o(1 + A_i \beta)}$$

$$R_{of}' = R_{of} \parallel R_L = \frac{R_L R_o(1 + A_i \beta)}{R_L + R_o(1 + A_i \beta)} = \frac{R_L R_o(1 + A_i \beta)}{R_L + R_o + R_o A_i \beta}$$

Divide N & D with $R_o + R_L$

$$R_{of}' = \frac{R_o R_L}{R_o + R_L} (1 + A_i \beta)$$

$$1 + \frac{R_o A_i \beta}{R_o + R_L}$$

$$\left[\because \frac{A_i R_o}{R_o + R_L} = A_i \right]$$

SE, $R_L = \infty$ then $A_i = 0$

$$R_{of}' = \frac{R_o \parallel R_L (1 + A_i \beta)}{1 + 0} = \frac{R_o \parallel R_L (1 + A_i \beta)}{1 + 0}$$

$$= R_{of}' = R_o' (1 + A_i \beta) \text{ where } R_o' = R_o \parallel R_L$$

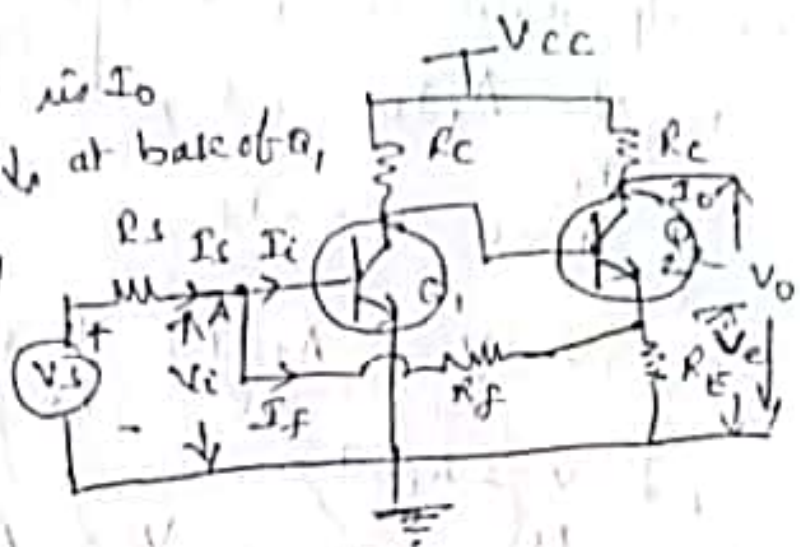
The two stage RC coupled amplifier with feedback resistor R_f b/w Q_1 (base) and Q_2 (emitter) decrease the current gain (A_{if}). The current through R_f decreases, i/p base current I_i as I_o o/p current increases.

Q_2 collector current is I_o
 $I_o \uparrow \Rightarrow I_f \uparrow \Rightarrow I_b \approx I_i \downarrow$ at base of Q_1

At Node KCL apply

$$I_s = I_i + I_f$$

$$I_i = I_s - I_f$$



$$I_f = \text{current through } R_f = \frac{V_i - V_{e2}}{R_f}$$

where V_i - i/p voltage at base of Q_1

V_{e2} - emitter voltage at Q_2

I_f - feedback current

V_i - in in millivolts

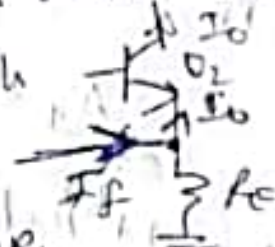
V_{e2} - o/p voltage at emitter of Q_2

If V_i neglected. $I_f = -\frac{V_{e2}}{R_f}$

R_E - emitter resistance of Q_2

The voltage drop across $R_E = (I_o - I_f)R_E$

Note: I_o is the current through R_E



$$I_f = \frac{(I_o - I_f)R_E}{R_f}$$

$$I_f R_f + I_f R_E = I_o R_E \Rightarrow I_f (R_f + R_E) = I_o R_E$$

$$\beta = \frac{I_o}{I_i} = \frac{R_E}{R_f + R_E}$$

The current gain $A_I = \frac{-I_{C2}}{I_S}$

$$A_I = - \frac{I_{C2}}{I_{B2}} \times \frac{I_{B2}}{I_{C1}} \times \frac{I_{C1}}{I_{B1}} \times \frac{I_{B1}}{I_S}$$

$$- \frac{I_{C2}}{I_{B2}} = -h_{fe} \quad \text{--- (1)}$$

$$\frac{I_{C1}}{I_{B1}} = h_{fe}$$

$$\frac{I_{B2}}{I_{C1}} = - \frac{R_{C1}}{R_{C1} + R_{i2}} \quad \text{--- (2)} \quad R_{i2} = h_{ie} + (1+h_{fe})(R_E \parallel R_F)$$

$$\frac{I_{B1}}{I_S} = \frac{R}{R + h_{ie}} \quad \text{--- (3)} \quad \text{where } R = R_S \parallel (R_F + R_E) \Rightarrow \text{by current division}$$

Substitute (1), (2), (3), (4) in A_I Equation the gain of amplifier w/o feedback is obtained

$$A_{If} = \frac{A_I}{1 + A_I \beta} \quad \beta = \frac{R_E}{R_F + R_E}$$

~~$$R_{if} = \frac{R_S (1 + A_I \beta)}{1}$$~~

$$R_{if} = \frac{R_i}{1 + A_I \beta}$$

$$R_{of} = R_o \frac{1 + \beta A_i}{1 + \beta A_I} = R_o = R_{C2}$$

