

## CHI-square Test :-

→ The chi-square test for Goodness of fit tests claims about population proportions [categorical variables]

→ It is a non-parametric test that is performed on categorical data. [ordinal, nominal data]

Ex:- There is a population of Male who likes different color of bike

	<u>Theory</u>	
yellow Bike	$\frac{1}{3}$	} population proportions
orange Bike	$\frac{1}{3}$	
Red Bike	$\frac{1}{3}$	



Theoretical  
categorical distribution.

we will pick sample data. → in order to test the above claim

	<u>Sample</u>
Yellow Bike	22
orange Bike	17

Red Bike	59
↓	
observed categorical distribution.	

→ According to chi-square, with the help of sample data we need to come to conclusion on population proportions given. and this test is called Goodness of fit.

→ In 2010 census of the city, the weight of the individuals in a small city were found to be the following.

weight	<50 kg	50-75	>75
	20%	30%	50%

In 2020, weight of  $n=500$  individuals were sampled,  
Below are the results.

<50	50-75	>75
140	160	200

using  $\alpha = 0.05$ , would you conclude the population differences of weights has changed in last 10 years?

Ans) In 2010  
Expected

<50 kg	50-75	>75
20%	30%	50%

In 2020  
when,  $n=500$   
observed

<50	50-75	>75
140	160	200

In 2010  
Expected

<50 kg	50-75	>75
$500 \times 0.2$ $= 100$	$500 \times 0.3$ $= 150$	$500 \times 0.5$ $= 250$

① Null hypothesis ( $H_0$ ): The data meets the expectation

Alternate hypothesis  $H_1$ : The data does not meet the expectation.



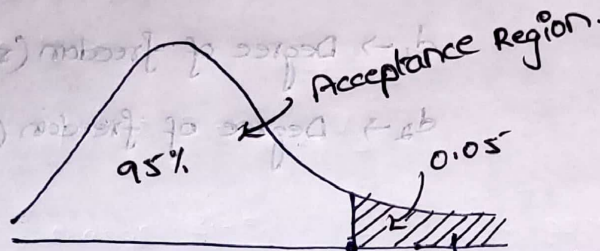
②  $\alpha = 0.05$   $C.I = 95\%$

③ Degree of freedom

$dof = k - 1 = 3 - 1 = 2$

④ Decision Boundary:

→ usually chi-square distribution is a right-skewed distribution.



Rejection Region.

critical value  
= 5.991

chi-square Test  $\chi^2 > 5.991$  { Reject the null hypothesis }

from chi-square table.

⑤ calculate chi square test statistics

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

O - Observed  
E - Expected.

$$= \frac{(140 - 100)^2}{100} + \frac{(160 - 150)^2}{150} + \frac{(200 - 250)^2}{250}$$

$$\chi^2 = 26.67$$

$\chi^2 > 5.991$  { Reject the null hypothesis }

The weights of population has changed.

## F-distribution

The F-distribution with  $d_1$  and  $d_2$  degrees of freedom is the distribution of

$$x = \frac{s_1/d_1}{s_2/d_2}$$

$s_1 \rightarrow$  independent Random variables

$s_2 \rightarrow$  independent Random variable

$d_1 \rightarrow$  Degree of freedom ( $s_1$ )

$d_2 \rightarrow$  Degree of freedom ( $s_2$ )

F-Test  $\rightarrow$  variance Ratio test {comparing the variance between 2 groups}

Q) The following data shows the no. of bulbs produced daily for some days by 2 workers A and B.

A	B
40	39
30	38
38	41
41	33
38	32
35	39
40	
34	

can we consider based on the data worker B is

more stable <sup>or not</sup> and efficient

$$\alpha = 0.05, 95\% \text{ C.I.}$$

$$F_{0.05, 6, 7}$$

A) null hypothesis  $H_0: \sigma_1^2 = \sigma_2^2$

Alternate hypothesis  $H_1: \sigma_1^2 \neq \sigma_2^2$

$$n_1 = 6, n_2 = 8$$



$x_1$	$\bar{x}$	$(x_1 - \bar{x})^2$
40	37	9
30	37	49
38	37	1
41	37	16
38	37	1
35	37	4
$\bar{x}_1 = 37$		$\sum (x_i - \bar{x})^2 = 80$

$$s_1^2 = \frac{\sum_{i=1}^n (x_i - \bar{x}_i)^2}{n-1}$$

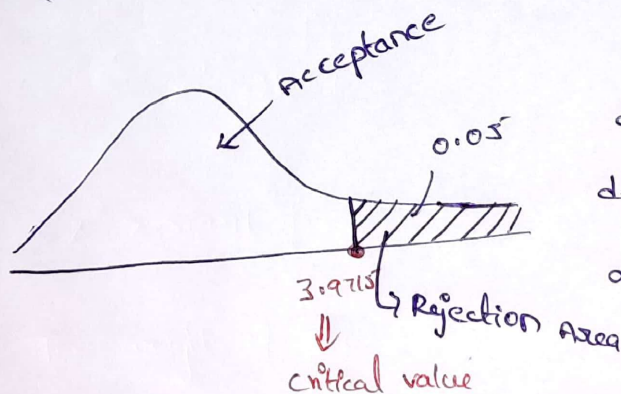
$$= \frac{80}{5} = 16$$

$x_2$	$\bar{x}_2$	$(x_2 - \bar{x})^2$
39	37	4
38	37	1
41	37	16
33	37	16
32	37	25
39	37	4
40	37	9
34	37	9
$\bar{x}_2 = 37$		$\sum (x_i - \bar{x}_2)^2 = 84$

\* Variance Ratio [F-test]

$$F = \frac{s_1^2}{s_2^2} = \frac{16}{12} = 1.33$$

\* Decision Rule:- [F-distribution]  $\rightarrow$  is also a right-skewed distribution.



$$df_1 = 6 - 1 = 5$$

$$df_2 = 8 - 1 = 7$$

$$\alpha = 0.05$$

$\Rightarrow$  F-test  $> 3.9715$  {Reject null hypothesis}

Is  $1.33 > 3.9715 \Rightarrow$  false.

we fail to reject the null hypothesis.

worker A  $\approx$  worker B