
PyThermal Documentation

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Dinesh Pinto, St. Stephen's College

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`class main.System(initial_values, lattice_a, lattice_b)`

`__init__(initial_values, lattice_a, lattice_b)`
Generates metadata about the system.

Parameters

- **initial_values** – List of initial state values of the system
- **lattice_a** – Lattice sites in A
- **lattice_b** – Lattice sites in B

`__weakref__`
list of weak references to the object (if defined)

check_existence (*names*)
Checks whether variables exists on hard disk. Generally deprecated for try-except statements.

Parameters **names** – list of names of variables

Returns Boolean list whether files exists on hard disk

check_system ()
Runs checks to make sure all inputs are valid.
:raises Value errors for invalid inputs

folder_path
The naming convection is as follows: P[Total no. of particles] D[Dimensionality of lattice] A[No. of sites in A] B[No. of sites in B]

Returns Path for storing program output

static plotting_metadata ()
Stores metadata for Matplotlib plots.

Returns Filename of images

Returns Image titles

Returns y axis labels

Returns x axis labels

Returns y axis limits

`main.main_states(initial_values, chosen_eigenstates, lattice_a, lattice_b)`

Contains function calls to determine the density matrix of a subsystem in its energy basis and compare the

diagonal/off-diagonal elements. Uses time() module to time execution of various functions and output to standard output.

Parameters

- **chosen_eigenstates** – Eigenstates for which to compute DM's
- **initial_values** – List of initial values for system initial_values = [Total no. of particles(nop), Dimension of lattice(ndims)]
- **lattice_a** – List of sites in A
- **lattice_b** – List of sites in B

Returns True if execution successful

`main.main_time(initial_values, chosen_eigenstate, t_initial, t_final, t_steps, lattice_a, lattice_b)`

Contains functions to time evolve the entire system (both sub-lattices) starting in an initial state where all particles are in one sub-lattice. Possible issues.

Parameters

- **initial_values** – List of initial values for system initial_values = [Total no. of particles(nop), Dimension of lattice(ndims)]
- **chosen_eigenstate** – Initial state for time evolution
- **t_initial** – Starting time
- **t_final** – Ending time
- **t_steps** – No. of steps
- **lattice_a** – List of sites in A
- **lattice_b** – List of sites in B

Returns True if execution successful

ROUTINES

`routines.position_states` (*lat, nop, del_pos=None*)

Returns position states for a given lattice and number of particles. Parameter `del_pos` can be used to delete lattice sites.

Parameters

- **lat** – Array of lattice sites
- **nop** – Nop of particles in lattice
- **del_pos** – Lattice sites to delete

Returns Positions states

Returns Total no. of states

`routines.distribute` (*n_items, n_processes, i*)

Defines a starting and stopping point for a particular task to be allocated to a process. Returns a (start, stop) tuple.

Parameters

- **n_items** – Total no. of items
- **n_processes** – Total no. of processes
- **i** – Process no. (not same as PID)

Returns Start & Stop point index in no. of items

`routines.hamiltonian_parallel` (*lattice, ndims, nop*)

Wrapper for `_hamiltonian`. Creates multiple processes, each of which calls `_hamiltonian` simultaneously. Defines a global ‘ham’, which is a multiprocessing array interfaced with ctypes and reshaped to generate an empty (filled with zeros) hamiltonian array.

Parameters

- **lattice** – Lattice used
- **ndims** – Dimensionality of lattice
- **nop** – No. of particles

Returns Hamiltonian matrix

`routines.diagonalize` (*h*)

Calculates eigenvectors and eigenvalues used Pade algorithm (see SciPy documentation).

Control threads using OpenMP. Link to lower level OpenBLAS (Basic Linear Algebra Subroutines) written in Fortran for parallel processing.

Parameters **h** – Matrix

Returns Real array of eigenvalues

Returns Complex array of eigenvectors

`routines.ncr(n, r)`

No. of combinations of k items taken from n items.

Parameters

- **n** – Total no. of items
- **r** – No. of items chosen

Returns Total no. of combinations

`routines.sum_ncr(n, k)`

Calculates $nC0 + nC1 + \dots + nCr$.

Parameters

- **n** – Total no. of items
- **k** – No. of items chosen

Returns Sum of combinations

`routines.relabel(e_states, nop, nol_b, lat_a)`

The state is $|\psi\rangle_{AB} = \sum_{i, n, \mu} a_{i_n \mu} |i_n \mu\rangle$ where the product state is written as $|i_n \mu\rangle$. Refer to “The Density Matrix using Relabelled States.pdf”

Parameters

- **lat_a** – Sub-lattice B
- **e_states** – Eigenstates
- **nop** – No. of particles
- **nol_b** – No. of lattice sites in B

Returns Array of relabelled states

`routines.rho_a_pbasis(label, e_vec, nos, nol_a, nop)`

Calculates density matrix for sub-lattice A. Error checks density matrix (trace should be 1.0). Warning raised if trace differs by $1(+/-)0.1$.

Parameters

- **label** – Relabelled states
- **e_vec** – Eigenvectors
- **nos** – No. of states
- **nol_a** – No. of lattice sites in A
- **nop** – No. of particles

Returns Density matrix of sub-lattice A

`routines.rho_b_pbasis(label, e_vec, nos, nol_b, nop)`

Calculates density matrix for sub-lattice B. Error checks density matrix (trace should be 1.0). Warning raised if trace differs by $1(+/-)0.1$.

Parameters

- **label** – Relabelled states

- **e_vec** – Eigenvectors
- **nos** – No. of states
- **no_l_b** – No. of lattice sites in B
- **nop** – No. of particles

Returns Density matrix of sub-lattice B

`routines.h_block_diagonal` (*lat_b, n_dim, nop*)

Creates a block diagonal matrix containing the hamiltonian (for various no. of particles) of B placed in blocks along the diagonal.

Parameters

- **lat_b** – Lattice sites in B
- **n_dim** – No. of dimensions
- **nop** – No. of particles

Returns Block diagonal matrix

`routines.transform_basis` (*rho_pbasis, e_vecs_bd*)

Transforms DM from position basis to DM in energy basis.

Parameters

- **rho_pbasis** – Rho in position basis
- **e_vecs_bd** – Eigenvectors of block diagonal hamiltonian

Returns Rho in energy basis

`routines.naive_thermal` (*rho*)

Compare maximum diagonal and off diagonal terms in density matrix. Note: Makes copy of DM (bypass will destroy original DM)

Parameters **rho** – Density matrix in energy basis

Returns Max diagonal element

Returns Max off-diagonal element

`routines.initial_sublattice_state` (*e_vec, label, nos, nop, e_vec_num*)

Returns a normalized initial state with all particles in one sub-lattice. Control which sub-lattice is used by passing appropriate eigenvectors (i.e. eigenvectors of the chosen sub-lattice) as an argument.

Parameters

- **e_vec** – Eigenvectors of either sub-lattice
- **label** – Array of relabelled states
- **nos** – No. of states
- **nop** – No. of particles
- **e_vec_num** – Initial eigenvector chosen

Returns Normalized initial state

`routines.trace_squared` (*rho*)

Calculate the trace of the square of the density matrix.

Parameters **rho** – Density matrix

Returns Trace of the square of the density matrix

`routines.vn_entropy_b (psi_t, label, nos, nol_b, nop)`

Calculates Von-Neumann entropy as $S = -\text{tr}(\rho * \ln(\rho))$. Also calculates trace of square of density matrix (measure of entanglement). Uses a filter to suppress ‘WARNING: The logm input matrix may be nearly singular’. Wraps loop in `tqdm` for progress bar.

Parameters

- **psi_t** – Psi(t)
- **label** – Relabelled states
- **nos** – No. of states
- **nol_b** – No. of lattice sites in B
- **nop** – No. of particles

Returns Real Von-Neumann entropy

Returns Trace of density matrix of B

`routines.time_evolution (psi_0, h, nos, timesteps)`

Psi evolved as $|\Psi(t)\rangle = \exp(-i * h * t)|\Psi(0)\rangle$. Uses matrix exponential for computation.

Parameters

- **psi_0** – Initial state
- **h** – Hamiltonian matrix
- **nos** – No. of states
- **timesteps** – Array of times

Returns Array of Psi(t)

`routines.avg_particles (psi_t, timesteps, labels, nop)`

Calculates the average number of particles in sub-lattices A and B.

Parameters

- **psi_t** – Array of psi at various times
- **timesteps** – Array of times
- **labels** – Relabelled states
- **nop** – Total no. of particles

Returns Avg. particles in sub-lattice A

Returns Avg. particles in sub-lattice B

OUTPUT

`output.status (time_taken=0.0)`

Prints current status (execution time) of program execution. Note: Times returned from here are not true measures of algorithm speed. For rigorous function time testing use the `timeit` module.

Parameters `time_taken` – Block execution time

`output.warning (*objects)`

Handles non-fatal warnings. Output to `stderr`.

Parameters `objects` – Objects

`output.write_file (path, filename, data=None, fmt='%18e')`

Checks if output directory exists, if not, creates it. Writes arrays/lists to the disk. Performs IO using NumPy. Possible switch in future to the more robust Pandas (dependant code must be unaffected).

Parameters

- **path** – Folder path to write to
- **filename** – Name of file (include extension)
- **data** – Data to be written
- **fmt** – Format specifier

`output.write_image (path, filename)`

Checks if output directory exists, if not, creates it. Then writes to disk. Writes images to the disk. Performs IO using Matplotlib.

Parameters

- **path** – Folder path to write to
- **filename** – Name of file (including extension)

`output.read_file (path, filename, dtype=<class 'numpy.float64'>)`

Reads data from files stored locally. Performs IO using NumPy. Possible switch in future to the more robust Pandas (dependant code must be unaffected).

Parameters

- **path** – Path to folder
- **filename** – Name of file
- **dtype** – Data type of file

Returns Array of read data

Raise IOError if file not found

`output.plot_write(x, y, title=None, y_label=None, x_label=None, y_limit=None, path=None, filename=None, checkbox=None)`

Generate graphs using Matplotlib. Uses `write_image()` to save to hard disk. Checkbox can be used to control plot display during execution.

Parameters

- **x** – x axis
- **y** – y axis
- **title** – Graph title
- **y_label** – y axis label
- **x_label** – x axis label
- **y_limit** – y axis limits
- **path** – Path for saving file
- **filename** – Name of file
- **checkbox** – Show images during execution(1) or not(0)

ABOUT

about **.about** (*test=True*)

Checks dependencies and return version numbers for PyThermal. Tests NumPy and SciPy. Checks OpenBLAS for Numpy.

Parameters **test** – Run tests for NumPy and SciPy

`gui.fetch(values, values2)`

Prints data stored in entries for debugging purposes.

Parameters

- **values** – List storing initial values
- **values2** – List storing sub-lattices A and B

`gui.graphical_interface(base)`

Base layout for text fields and their labels. The order in which they are placed matters. This may be addressed in a future update.

Parameters **base** – Root

Returns List of entries

`gui.execute(initial_values, optional_values)`

Calls `main()` from `main.py`.

Parameters

- **optional_values** – List of optional values
- **initial_values** – List of initial values

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