

# Advanced Digital Signal Processing: Imaging and Image Processing



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## Exercise 4: Image Formation

Due date: 29.06.2015

### Problem 1 – Backprojection

In this exercise, you will implement a reconstruction algorithms for the simulated images in exercise 3. Before the image is reconstructed, the space of the final image has to be discretized.

- a) Given the sampling frequency  $f_s$  and the wave propagation speed  $c$ , find a plausible value for the distance  $d_s$  between neighboring elements (resolution) in the discretized image.

The image  $I$  is reconstructed by

$$I(x, y) = \sum_{l=1}^{N_l} ss_l(t_d(x, y)).$$

where  $ss_l(t)$  is the modulated received pulse compressed signal. The position in the scene is denoted by  $x_l \leq x \leq x_h$  and  $y_l \leq y \leq y_h$ . For the implementation, proceed as follows.

- b) For each ping and position in the discretized image space, compute the distances to the sensors,  $d_x(x, y)$ ,  $d_y(x, y)$ , and the corresponding time delays  $t_d(x, y)$ .
- c) Next, modulate the phase of  $ss_l(t_d(x, y))$  by computing

$$ss_l(t_d(x, y)) = ss_{l,b}(t_d(x, y)) \exp\{j2\pi f_c t_d(x, y)\}. \quad (1)$$

Finally, compute  $I(x, y)$ .

Note:  $ss_{l,b}(t_d(x, y))$  is the baseband signal corresponding to  $ss(\tau_d(x, y))$ .

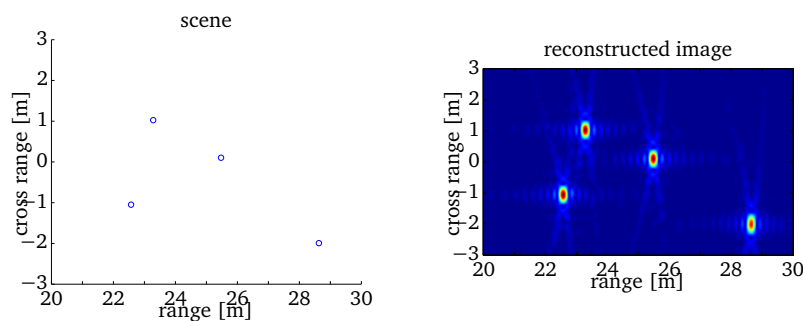


Figure 1: Original scene (left) and reconstruction (right).