Part D. Name three benefits of including functional style programming in Java

- Programs are more compact: easier to write, and easier to read/understand
- Programs are thread-safe
- Easier to demonstrate correctness of functional programs
- Easier to test; less likely that a test of a subroutine will fail tomorrow if it passed today since there are no side effects

Part E. Express the functions defined below using Church's lambda notation:

```
i. f(x) = x + 2x2 => \lambda x.x + 2x2

ii. g(x,y) = y - x + xy => \lambda xy.y - x + xy

iii. h(x,y,z) = z - (x + y) => \lambda xyz. z - (x + y)
```

Part F. For each lambda expression below, name the parameters and the free variables.

```
//parameters are marked in blue; free variables are marked in red
Runnable r = () ->
{
    int[][] products = new int[s][t];
    for (int i = 0; i < s; i++) {
        for(int j = i + 1; j < t; j++) {
            products[i][j] = i * j;
        }
    }
}

ii.
//parameters are marked in blue; free variables are marked in red
BiFunction<Double, Double, Double> f = (double u, double v) → [ba cosux sinvx dx]
```

(Note: the right hand side of the "→" is mathematical notation, not Java, but it can be converted to a large block of Java code having the same free variables. See lecture code to review the BiFunction functional interface.)

```
iii.
  //parameters are marked in blue; free variables are marked in red
Comparator<String> comp = (s, t) ->
  {
    if(ignoreCase == true) {
        return s.compareToIgnoreCase(t);
    } else {
        return s.compareTo(t);
    }
}
```