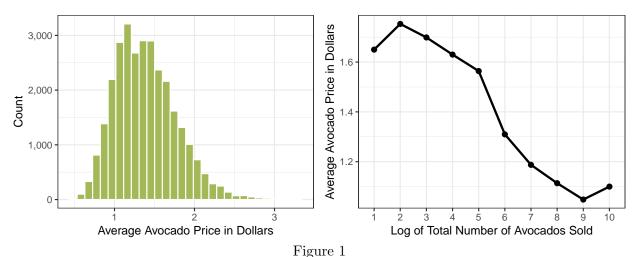
Predictive Model for Average Avocado Prices December 16, 2020

Executive Summary:

Introduction: Avocado is a fruit that is originated from southern America. This fruit is extremaly health and have a lot of benefits and nutritions. Individuals can use avocados with any other ingridients to complete a meal such as toast and salad. In addition, avocados can also be used to make healthy oil or desserts like avocado ice cream or smoothie. Knowing the fact that avocados are health for a human body, avocados have been the rise of American's new favorites fruits since the last decade. The amount of avocados have been sold in America are higher and higher everyday. With this being said, knowing the variables that cause the price of avocados to go up and down would benefits all consumers and restaurants owner. For example, a restaurants that have avocado toast or guacamole on their menu would have a better understanding of where to get cheaper avocados to maximize their profit. Knowing the cost of avocado can also help restaurants owner create budget for their restaurant and cost of a dish on their menu. In addition, individuals who like avocado would also know where and when to get type of avocado they desire. There are many questions asked in favor of these issues including 1) What factor impact the average price of avocados? 2) Are characteristics of an avocado important in pricing decision? 3) How good is the model? 4) How can we improve the model? and 5) How can we implement the model for the consumer to gain easy access? This analysis will attempt to answer all these questions by starting with a variable data analysis, developing the model using a multiple linear regression, assessing the quality of the model, and providing significant results of the model. The purpose of this model is to predict the average avocado prices using various variables provided in the dataset.

Methods: A dataset was retrieved from Kaggle, a website that have input and output from scientists and college students. This dataset has a large sample size of 30,021 observations from 2015 to 2020. The data was originally collected from the Hass Avocado Broad (HAB) website. There are no missing values for all the variables in the dataset. This dataset has historical data of avocado prices and characteristics. The dataset contains two time series columns including date of observation and vear of observation, one characteristic variable including type of the avocado, and one geographical variable. In addition, there are eight quantitative predictors including total number of avocados sold, total number of avocados with Price Look-Up (PLU) code 4046 sold, total number of avocados with PLU code 4226 sold, total number of avocados with PLU code 4770 sold, total number of bags sold, total number of small bags sold, total number of large bags sold, and total number of extra large bags sold. There are 54 distinct geographical regions of where the avocados are from with different average prices for different time of the year. The goal of this analysis is to find the relationship between predictors and average avocado prices. To build a model with average avocado price, a multiple linear regression with significant predictors will be used. Before building a model, we will explore how each variable impact the average of avocado prices. Then, using the "best" model, we will predict the avocado price to validate our model. The data will be splitted into a .75/.25 proportion train/test set. All analysis will be done in R Studio with version 3.6.2.

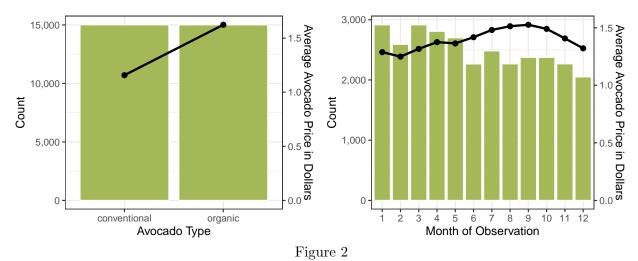
Exploratory Data Analysis: Before building a model, it is important to explore the distribution of average avocado prices and the relationship of it with each of the predictor. The target variable average price have an approximately normal distribution, see Figure 1.1. With a normal distribution assumption, a multiple linear regression can be applied. The price of avocados range from \$0.44 to \$3.25 with an average of \$1.35 for each avocado. In terms of predictors, a descriptive statistics was constructed for all continuous variable in the dataset, see Table A2 in the Appendix. All continuous variable are right skewed with an extremely large maximum value compare to the means and the third interquatile ranges. This signifies a log-transformation is needed for all continuous predictors to minimize skewness effect. In addition, the values of the continuous variables will be smaller and easier to analyze.



Total number of avocados sold is the number that have been sold in each location and each time of the year. Economically, the price of avocado will be lower if there are more supply. On the other hand, the price will be higher if there is a shortage in avocado. On a consumer side, a cheaper avocado would be more like to be bought than a more expensive one. This leads to a higher sells in avocados if the price is cheaper. Figure 1.2 shows a negative relationship between average avocado price and the log-transformation of total number of avocados sold. The rest of the article will use log of total number of avocados sold, unless otherwise specify. In Figure 1.2, the total number of avocados sold were sorted from smallest to highest and divided into 10 equal buckets. The first bucket contains the smaller number of avocados solds. The last bucket contains the highest number of avocados sold. A negative relationship indicates the average price will be cheaper if there are more avocado sold. However, the price will be more expensive if there are less avocado sold. This have proven the points of less supply lead to higher price. Likewise, higher price of avocados leads to less consumpsion. Therefore, the amount of avocado sold will be less. This variable would contribute significant impact in the model to predict the average of avocado prices.

The type of the avocado is also a signicant factor that would change the price of an avocado. In this dataset, there are two types of avocados including conventional and organic. Conventional avocados are traditional growing method that majority of the countries do. The price of conventional avocado would be more likely to be cheaper since the cost of growing conventional avocados are

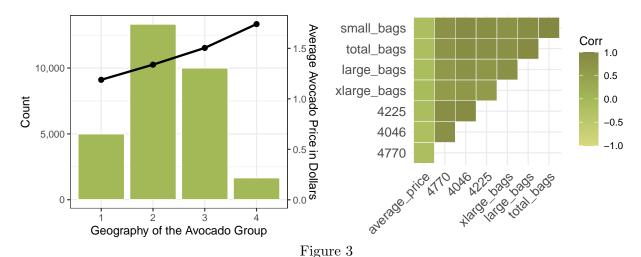
cheaper. On the other hand, organic avocados are growed without using any chemical, fertilizers, pesticides, or other artificial agents. Without a booster, organic avovados take longer to grow and easier to be eaten by insects. Therefore, the price of organic avocado would be considered more expensive. Figure 2.2 depicts the relationship of average avocado price with avocado types. As seen in the plot shown using a black line, organic avocados have a higher average price than conventional avocado. This indicates that an organic avocado would cause the price to be higher compared to a conventional avocado. Furthermore, this variable, type of avocado, have a balance proportion (shown using two bars). With a balance proportion, the predictive model would be more unbiased. Therefore, type of avocados would contribute a significant impact in predicting the price of avocados.



Month of observation is the time where the avocado is observed. Time of the year is important for fruits and vegitables because majority of the fruit only grow in a certain months or their season. Therefore, we would expect to have more avocados during avocado season and less avocados otherwise. As mentioned before, the price of avocado would be more like to increase if there are less avocados in supply. This means that, the average price would increase during non-avocado seasons and decrease during avocado seasons. Figure 2.2 shows a plot of average avocado price by month of observation with its frequency. As one can see, avocado seasons can be assume to be between January and May with the highest number of observations. On the other hand, non-avocado seasons are likely to be in between the month of June to December with lower number of avocados observed. In addition, a black line depicts lower average prices from January to May and higher prices from June to December. This indicates that during avocados season, the price of avocados are lower because there are more avocados in supply. On the other hand, the low supply of avocados from June to December causes the average price to go up. Therefore, this variable month of the year could contribute significant relationship with average price in the linear regression model.

Last but not least, location of the avocados sold could also be significant to the model. The geography of the avocado is the region or city the avocado is sold. Different cities and states have different living expenses resulting in different prices of the avocados. For example, the living expenses in California is higher than Texas. Thus, the price of avocados in California cities would be higher than the prices of avocados in Texas. Figure 5.1 depicts a relationship between average avocado prices and geographical location. This variables is sorted from smallest to highest average

price and assign four geographical group. The first geographical group sells cheapest avocados. The regions in the first group include Cincinnati, Columbus, Dallas, Houston, Nashville, New Orleans, Phoenix, Roanoke, and South Central. Furthermore, the last geographical group sells the most expensive avocados. Those regions include Hartford, New York, and San Francisco. Knowing the location of the market, the model can provide more variation of the average price.



Other variables like total number of avocados with Price Look-Up (PLU) code 4046 sold, total number of avocados with PLU code 4770 sold, total number of bags sold, total number of small bags sold, total number of large bags sold, and total number of extra large bags sold also have a strong negative relationship with the average prices. However, the correlation of all the continuous independent variable are very high, majority above .80, see Figure 5.2. If all high correlated variables are used within the same model, multicolinarity issues will arise. This leads the coefficients of each predictors to be unstable. Therefore, only total number of avocados sold will be use in the model. Total volume would describe total number of all different categories added up. In other words, the variables total number of avocados with Price Look-Up (PLU) code 4046 sold, total number of avocados with PLU code 4226 sold, total number of avocados with PLU code 4770 sold, total number of bags sold, total number of small bags sold, total number of large bags sold, and total number of extra large bags sold are a component of total volume. Using just one variable total volume alone would be good enough to cover the details of each components. Other variables did not mentions in the exploratory analysis have little to no relationship with average avocado prices.

Model Fitting/Inferences:

Conclusion:

Term	Coef	SdError	F-Stat	pValue	2.5% CI	97.5% CI
(Intercept)	1.228	0.018	70.111	0.000	1.193	1.262
$\log_{-}total_{-}volume$	-0.029	0.001	-23.237	0.000	-0.031	-0.026
month2	-0.037	0.008	-4.712	0.000	-0.052	-0.021
month3	0.031	0.008	4.066	0.000	0.016	0.045
month4	0.094	0.008	12.402	0.000	0.079	0.109
month5	0.080	0.008	10.502	0.000	0.065	0.095
month6	0.134	0.008	16.547	0.000	0.118	0.149
month7	0.198	0.008	25.137	0.000	0.182	0.213
month8	0.223	0.008	27.667	0.000	0.207	0.239
month9	0.242	0.008	30.527	0.000	0.227	0.258
month10	0.192	0.008	24.207	0.000	0.176	0.207
month11	0.113	0.008	13.961	0.000	0.097	0.129
month12	0.026	0.008	3.202	0.001	0.010	0.043
typeorganic	0.367	0.005	67.379	0.000	0.356	0.377
${\it geography_bins2}$	0.160	0.005	33.397	0.000	0.150	0.169
${\it geography_bins3}$	0.309	0.005	61.764	0.000	0.299	0.318
${\it geography_bins4}$	0.563	0.008	69.124	0.000	0.547	0.579

Table 1: Summary regression of final model

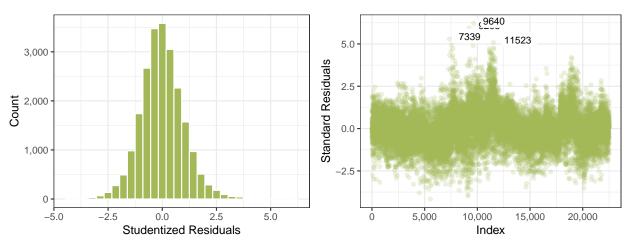


Figure 4

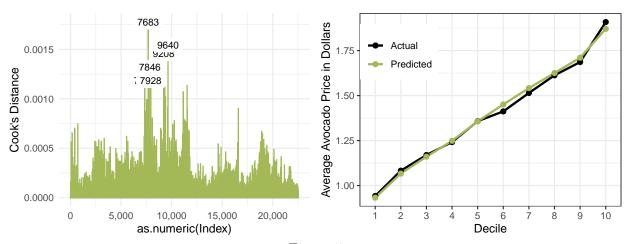


Figure 5

$\underline{\textbf{Introduction}}:$

Appendix A: Supplemental Tables

Table 2: Summary Statistics for all numerical independent features

Statistic	N	Mean	St. Dev.	Min	Pctl(25)	Pctl(75)	Max
		1,100,11	20. 20		1 001(20)	1 001(10)	1,1011
$total_volume$	30,021	$939,\!255$	3,813,519	85	14,299	489,803	63,716,144
4046	30,021	$299,\!107$	1,289,108	0	783	$115,\!156$	22,743,616
4225	30,021	284,901	1,169,078	0	2,814	140,947	20,470,573
4770	30,021	21,629	100,919	0	0	$5,\!424$	2,546,439
total_bags	30,021	$333,\!534$	1,415,618	0	8,374	$159,\!174$	31,689,189
$small_bags$	30,021	232,126	950,503	0	$5,\!956$	112,938	20,550,407
large_bags	30,021	95,185	467,210	0	352	36,068	13,327,601
xlarge_bags	30,021	$6,\!223$	$38,\!137$	0	0	560	1,022,564

	Model	Number of	MSE	Adj.R.squared	F.statistics	AIC
		Features				
1	Initial Model	16.000	0.062	0.572	1879.873	1421.841
2	Stepwise Model	16.000	0.062	0.572	1879.873	1421.841
3	Model with Interaction	78.000	0.060	0.588	413.437	598.507
	Terms					
4	Stepwise Model with	77.000	0.060	0.588	418.808	597.053
	Interaction Terms					

Table 3: Regression validation metrics including MSE, R-squared adjusted, and AIC

	GVIF	Df	$GVIF^{(1/(2*Df))}$
log_total_volume	2.713	1.000	1.647
month	1.007	11.000	1.000
type	2.673	1.000	1.635
geography_bins	1.031	3.000	1.005

Table 4

Appendix B: R Code

```
1 #### Packages ####
3 library (magrittr)
4 library (tidymodels)
5 library (lubridate)
6 library (corrplot)
7 library (MASS)
8 library (broom)
9 library (car)
10 library (tidyverse)
12
13 #### Parameters ####
14
  avocado_color <- "#A3B958"
16
17
18 #### Functions ####
19
  Explore Variable \leftarrow function (df, xvar, count = TRUE, x_axis) {
20
2.1
    group_df <- df %>%
22
       group_by({{xvar}}) %%
23
       summarise (average_price = mean (average_price),
24
                 count = n(),
25
                  .groups = "drop")
26
27
    ratio <- max(group_df$count) / max(group_df$average_price)
28
29
    if (count == TRUE) {
30
      p \leftarrow ggplot(group\_df, aes(x = factor(\{\{xvar\}\}), group = 1)) +
31
         geom_bar(aes(y = count), stat = "identity", fill = avocado_color, col = "white}
32
         geom_point(aes(y = average_price * ratio), size = 2, color = "black") +
33
         geom_line(aes(y = average_price * ratio), size = 1, color = "black") +
34
         scale_y_continuous (sec.axis = sec_axis (~./ratio, name = "Average Avocado Price
       in Dollars"),
                              label = scales::comma
36
37
      y_lab <- "Count"
38
39
40
    } else {
41
       p \leftarrow ggplot(group_df, aes(x = \{\{xvar\}\}, group = 1)) +
         geom_point(aes(y = average_price), size = 2, color = "black") +
42
43
         geom\_line(aes(y = average\_price), size = 1, color = "black")
44
       y_lab <- "Average Avocado Price in Dollars"
45
46
47
    p +
       labs(y = y_lab, x = x_axis) +
49
       theme_bw()
50
51
ValidationTable <- function(fit, model_type){
```

```
mod <- fit
54
     fit _summary <- tibble (Model = model_type,
                             "Number of Features" = length((coef(mod) \% \% names())[-1]),
56
                             MSE = mean(mod\$residuals^2),
57
                             Adj.R. squared = summary(mod)  adj.r. squared,
58
                             F. statistics = summary (mod) $ fstatistic [[1]],
59
                             AIC = AIC \pmod{1}
60
     return (fit _summary)
61
62
63
   #### Data ####
   avocado <- read_csv("data/avocado-updated-2020.csv")
66
67
68
   # descriptive statistics of the data
70
   summary(avocado %>%
71
              select_if(is.numeric))
72
73
74
75 # add deciles to continuous response
76
   avocado %%%
77
78
     mutate (
       total_volume_bins = as_factor(cut(total_volume, breaks = 10,
79
                                            include.lowest = TRUE, labels = FALSE)),
80
       "4046_bins" = as_factor(cut(`4046`, breaks = 10,
81
                                     include.lowest = TRUE, labels = FALSE)),
82
       "4225_bins" = as_factor(cut('4225', breaks = 10,
83
                                     include.lowest = TRUE, labels = FALSE)),
       "4770_bins" = as_factor(cut(`4770`, breaks = 10,
85
                                     include.lowest = TRUE, labels = FALSE)),
86
       total_bags_bins = as_factor(cut(total_bags, breaks = 10,
87
                                          include.lowest = TRUE, labels = FALSE)),
88
       small_bags_bins = as_factor(cut(small_bags, breaks = 10,
89
90
                                          include.lowest = TRUE, labels = FALSE)),
91
       large_bags_bins = as_factor(cut(large_bags, breaks = 10,
                                          include.lowest = TRUE, labels = FALSE)),
92
       xlarge_bags_bins = as_factor(cut(xlarge_bags, breaks = 10,
93
                                           include.lowest = TRUE, labels = FALSE)))
94
95
   # add month
96
97
   avocado %
98
99
     mutate(month = factor(month(date)))
100
   # feature engineer
102
103
   price_by_location <- avocado %>%
105
     group_by(geography) %>%
     summarise (average_price = mean (average_price),
106
                .groups = "drop") %%
107
     mutate(average_price_bins = cut(average_price, breaks = 4,
108
                                        include.lowest = TRUE, labels = FALSE)) %>%
109
```

```
dplyr::select(geography, geography_bins = average_price_bins) %%
110
     distinct()
112
   avocado ‰%
113
     left_join(price_by_location, by = "geography") %>%
114
     modify_at("geography_bins", as_factor)
115
   # log tranformation of total_volume
118
119
   avocado %
120
     mutate(log_total_volume = log(total_volume)) %%
     mutate(log_total_volume_bins = as_factor(cut(log_total_volume, breaks = 10,
                                                      include.lowest = TRUE, labels = FALSE
123
       )))
124
   #### Explore ####
126
127
     target variable: average_avocado price
128
   ggplot(avocado, aes(average_price)) +
130
     geom_histogram(fill = avocado_color, bins = 30, col = "white") +
131
     theme_bw() +
     labs(x = "Average Avocado Price in Dollars", y = "Count") +
133
     scale_y_continuous(label = scales::comma)
134
135
136
   # continuous predictors
137
138
   Explore Variable (avocado, total_volume_bins, count = FALSE,
139
                    x_axis = "Total Number of Avocados Sold")
140
   ExploreVariable (avocado, log_total_volume_bins, count = FALSE,
141
                    x_axis = "Log of Total Number of Avocados Sold")
142
143
   Explore Variable (avocado, `4046_bins`, count = FALSE,
144
                    x_axis = "Total Number of Avocados with PLU 4046 Sold")
145
146
   Explore Variable (avocado, `4225_bins`, count = FALSE,
                    x_{axis} = "Total Number of Avocados with PLU 4225 Sold")
147
   {\tt ExploreVariable\,(avocado\,,~`4770\_bins\,`,~count} = {\tt FALSE},
148
                    x_{axis} = "Total Number of Avocados with PLU 4770 Sold")
149
   ExploreVariable(avocado, total_bags_bins, count = FALSE,
                    x_axis = "Total Number of Bags Sold")
   ExploreVariable (avocado, small_bags_bins, count = FALSE,
                    x_{axis} = "Total Number of Small Bags Sold")
153
   Explore Variable (avocado, large_bags_bins, count = FALSE,
154
                    x_axis = "Total Number of Large Bags Sold")
155
   ExploreVariable (avocado, xlarge_bags_bins, count = FALSE,
156
                    x_axis = "Total Number of Extra Large Bags Sold")
157
158
159
   #
    categorical predictors
160
161
   Explore Variable (avocado, type, count = TRUE,
                    x_axis = "Avocado Type")
162
   Explore Variable (avocado, year, count = TRUE,
163
                    x_axis = "Year of Observation")
164
```

```
ExploreVariable (avocado, month, count = TRUE,
                     x_axis = "Month of Observation")
166
   ExploreVariable (avocado, geography, count = FALSE,
167
                     x_{-axis} = "Geography of The Avocado") +
168
     coord_flip()
169
   ExploreVariable (avocado, geography_bins, count = TRUE,
170
                     x_axis = "Geography of the Avocado Group")
172
173
   # correlation
174
175
176
   corr_table <- avocado %>%
     dplyr::select(total_volume, '4046', '4225', '4770', total_bags, small_bags,
177
                     large_bags, xlarge_bags, average_price) %>%
178
     cor()
179
180
   corr_table %>%
181
     \{.[order(abs(.[, 1]), decreasing = TRUE)\}
182
        order(abs(.[, 1]), decreasing = TRUE)] %%
183
     corrplot(method = "number", type = "upper")
184
185
186
   #### Model Development ####
187
188
189
   # select significant variables
190
   avocado ‰%
191
     dplyr::select (average_price,
192
                     log_total_volume,
193
                     month,
194
                     type,
195
                     geography_bins)
196
197
198
199 # split data into train and test set
200
201
   set . seed (123)
   avocado_split <- initial_split (avocado, strata = average_price)
203
204
   avocado_train <- training(avocado_split)
205
206
   avocado_test <- testing(avocado_split)
207
208
210
   # Initial model with all predictors
211
   init_fit \leftarrow lm(average_price^-.,
212
                    data = avocado_train)
213
214
215
216 # variable selection using stepAIC
217
   step_fit <- stepAIC(init_fit , direction = "both", trace = FALSE)</pre>
219
220
```

```
221 # interaction
222
   int_fit <- lm(average_price ~ .*.,
223
224
                  data = avocado_train)
226
   # variable selection for interaction model
227
228
   int_step_fit <- stepAIC(int_fit , direction = "both", trace = FALSE)</pre>
229
230
231
232
   # generate iteration log
233
   init_fit_summary <- ValidationTable(init_fit, "Initial Model")</pre>
   step_fit_summary <- ValidationTable(step_fit, "Stepwise Model")</pre>
236 int_fit_summary <- ValidationTable(int_fit, "Model with Interaction Terms")
   int_step_fit_summary <- ValidationTable(int_step_fit, "Stepwise Model with
       Interaction Terms")
238
   bind_rows(init_fit_summary,
239
              step_fit_summary,
240
              int_fit_summary,
241
              int_step_fit_summary) %>%
242
243
     modify_if(is.numeric, round, 3)
244
245
246 # final model
247
   final_fit <- init_fit
248
249
   final_fit %>%
250
     tidy() %>%
251
     modify_if(is.numeric, round, 3)
252
253
254
   #### Model Diagnostic ####
255
256
   # add rownames
258
   avocado_train %
259
     rownames_to_column()
260
261
   # Residuals
262
   avocado_train %
264
265
     mutate(predict = predict(final_fit),
             rstudent = rstudent(final_fit))
266
267
268
269 ## Influential Observations
270 ## Cook's D plot
271 ## identify D values > 4/(n-p-1) as a guide;
272 ## Cook and Weisberg recommend 0.5 and 1 (R uses these guides in default diagnostic
       plots below)
cutoff \leftarrow 4/((nrow(avocado_train) - length(final_fit $coefficients) - 2))
```

```
275
   diag <- augment(final_fit) %>%
     mutate(Index = 1: nrow(.))
277
   diag %>%
     mutate(high\_cooksd = case\_when(
280
        .cooksd > cutoff ~ 1, TRUE ~ 0),
281
       col_stdresid = case_when(
282
          . std. resid > 0  1,
283
          . std. resid < 0 \ \tilde{} \ 0),
284
       high_hat = case_when(
285
         . hat > .1 ~1,
         TRUE \tilde{} 0))
287
288
   ## cook's distant ggplot
289
290
   ggplot(diag, aes(x = as.numeric(Index), y = .cooksd)) +
291
     geom_bar(stat = "identity", col = avocado_color) +
     labs(y = "Cook's Distance") +
293
     theme_minimal() +
294
     geom\_label(data = diag \%\% filter(.cooksd > cutoff + .001),
295
                 aes(label = Index), label.size = NA, size = 3) +
296
     scale_x_continuous(label = scales::comma)
297
298
300 ## Normality of Residuals
301
   ggplot(diag, aes(x = .std.resid)) +
302
     geom_histogram(bins = 30, col = "white", fill = avocado_color) +
303
     theme_bw() +
304
     labs (x = "Studentized Residuals",
          y = "Count") +
306
     scale_y_continuous(label = scales::comma)
307
308
309
   # studentize residual plot
310
311
312
   ggplot(diag, aes(x = Index, y = .std.resid)) +
     geom_point(alpha = 0.2, col = avocado_color) +
313
     labs(y = "Standard Residuals", x = "Index") +
314
     theme_bw() +
315
     theme(legend.position = "none") +
316
     geom_label(data = diag \%\% filter(.std.resid > 5 | .std.resid < -5),
317
                 aes(label = Index), label.size = NA, size = 3, hjust = -.25, vjust = .3) +
     scale_x_continuous(label = scales::comma)
319
320
321
   # outlier and influential points
322
323
324
   diag %>%
325
     filter(.std.resid > 5 \mid .std.resid < -5 \mid .cooksd > cutoff + .001) \%
326
     dplyr::select(average_price, log_total_volume, month, type, geography_bins)
327
328
329 ## VIF
330 ## vif score seem very close to 1
```

```
vif(final_fit) # closer to 1 the better; 5-10 is moderate
332
333
   #### Predictions
334
335
   # Account for sigma^2
336
337
   sd_fit <- sd(final_fit$resid)</pre>
338
339
340
341
   # predict
342
   avocado_test %
343
     mutate(average_price_preds = predict(final_fit, newdata = .))
344
345
346
347
   # errors
348
   avocado_test %
349
     mutate(average_price_error = average_price - average_price_preds)
350
351
   mse <- mean(avocado_test $ average_price_error)^2
352
353
354
355 # create lift chart
356
   avocado_test %%%
357
     mutate(average_price_decile = ntile(average_price_preds, n = 10))
358
359
   decile_price <- avocado_test %%
360
     group_by(average_price_decile) %>%
361
     summarise (Actual = mean (average price),
362
                Predicted = mean(average_price_preds),
363
                .groups = "drop") %%
364
     gather (key, price, -average_price_decile)
365
366
367
   ggplot (decile_price,
          aes (x = factor (average_price_decile), y = price,
368
               group = key, color = key) +
369
     geom_line(size = 1) +
370
     geom_point(size = 2) +
371
     theme_bw() +
372
     scale\_color\_manual(values = c("black", avocado\_color)) +
373
     labs(x = "Decile",
374
          y = "Average Avocado Price in Dollars") +
     theme(legend.title = element_blank(), legend.position = c(0.15,.8))
```

Listing 1: Appendix of Code