Algorithms and Distributed Systems 2023/2024 (Lecture One)

MIEI - Integrated Master in Computer Science and Informatics

MEI - Master in Computer Science and Informatics

Specialization block

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NOVA SCHOOL OF SCIENCE & TECHNOLOGY

Lecture structure:

- Understand what is a distributed system.
- Modeling a distributed system.
 - General system model.
 - Fault model.
 - Timing assumption.
- Understanding the role of an algorithm.
 - Point-to-Point Communication Algorithms.
- The Broadcast Problem
 - Best effort broadcast.
 - Reliable broadcast.

"A distributed system is a network that consists of autonomous computers that are connected using a distribution middleware. They help in sharing different resources and capabilities to provide users with a single and integrated coherent network." — Technopedia.

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Note: our goal, as designers of distributed systems and distributed algorithms is to work to ensure that there are definitions that don't depend on failure!

This might be a more honest answer!

A more honest and focused answer:

A distributed system is composed by a set of **processes** that are interconnected through some **network** where processes seek to achieve some form of **cooperation** to execute tasks towards a **common goal**.







Why do we want to distribute things anyways?

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Fault-Tolerance (also known as dependability): If I use N machines to support my system and f (f < N) fail, then my system can still operate.

Concurrency (or more processing/storage power):
 If instead of using 1 machine to run my system, I use N machines (N >> 1) then I will have N times more resources and, hopefully, my system will be (close to) N times faster.

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- Fault-Tolerance: It is necessary to consider what you do when a machine fails or becomes unreachable (and they will).
- Concurrency: It is necessary to consider the possible orderings of events.
- No global clock: In other words, no way of synchronising via time.

Reasoning about Distributed Systems.

 You can probably guess that distributed systems are complex.

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- And our task is to understand how they might behave and how we can build them to operate correctly (and efficiently).

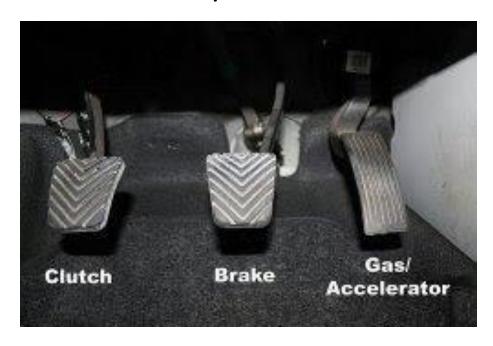
Reasoning about Distributed Systems.

- You can probably guess that distributed systems are complex.
- And our task is to understand how they might behave and how we can build them to operate correctly (and efficiently).
- Uh oh...



- Somewhat "less intelligent" example:
 - How do you reason about a car?

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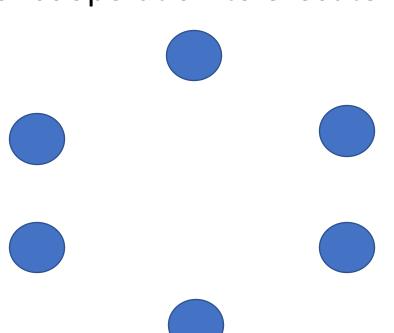


Key insight:

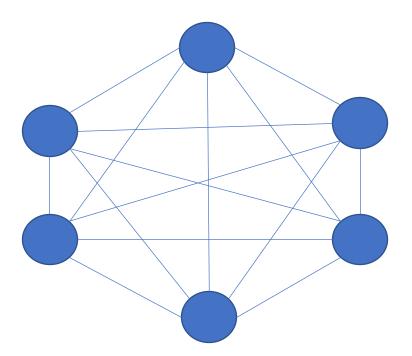
We need **abstractions** for talking about all kinds of systems

A distributed system is composed by a set of **processes** that are interconnected through some network (via **links**) where processes seek to achieve some form of cooperation to execute tasks.

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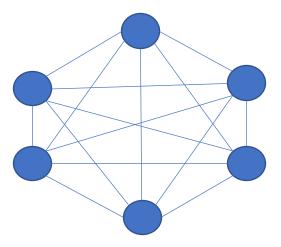


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More formally:

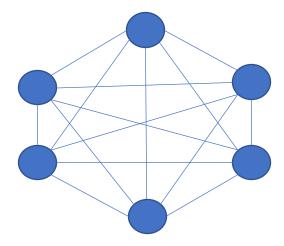
- Processes computational elements:
 - Abstracts the notion of machine/node.
- Network Graph G=(V,E), in which V is the set of processes, E represents the communication channels (i.e., links) between pairs of processes.



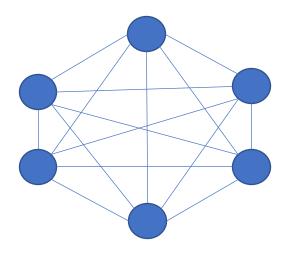
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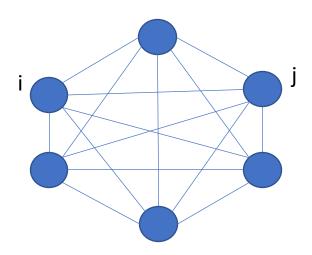
In general, we will consider a complete graph, where every process is connected to every other by a bidirectional link.



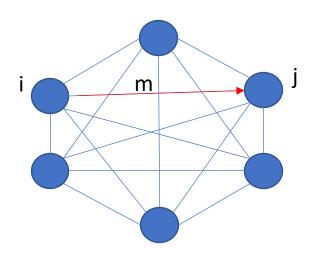
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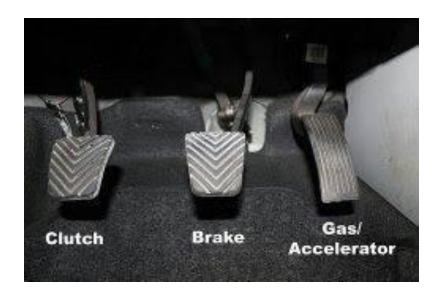
More formally:

- Processes communicate through the exchange of Messages, belonging to an alphabet M plus the special symbol null, which captures a non-existent message.
- Notation: send_i(j,m,arg₁, arg₂, ..., arg_n)
 - Process i send message m with arguments arg₁ to arg_n to process j.

m

We are done right?

- We are done right?
- Not quite, back to our somewhat "less intelligent" example:
 - How do you reason about a car?









tributed system



ewhat "less inteligent"







- We are done right?
- Not quite...
- Some extra things must be considered.
 - Timing assumptions.
 - Internal model of the process.
 - (Process) Fault model.
 - Network model,

Examples

- Client-server web interactions
- Audio streaming
- Stock-exchange trading

Timing assumptions

Two fundamental models

Synchronous System:

 Assumes that there is a known upper bound to the time required to deliver a message through the network and for a process to make all computations related with the processing of the message.

Asynchronous System:

• There are *no assumptions* about the time required to deliver a message or process a message.

Timing assumptions

- This might look like not a big deal but, there are strong implications here:
 - In a synchronous system you can **detect** when a process fails (in some particular fault models).
 - In a synchronous system you can have protocols **evolve** in synchronous steps (Why is that?)
 - In an asynchronous system there are some problems that have **no solution**.

Timing assumptions

The "real world" is **asynchronous**, so why is it that we sometimes consider the synchronous model?

- The synchronous model is easier to reason about
- More efficient solutions can be devised in the synchronous model

Internal Model of the Process

- Each process has a unique identifier: i ∈ V
- Internally each process has (classical model):
 - states_i set of (valid) states for process i
 - Inputs and outputs that are special state variables (which allow the process to get information from outside and export information to the outside)
 - init_i initial state for process i
 - Fundamentally, a process is a **deterministic automaton**.

Beyond Synchrony and Asynchrony

- There is a (more) practical system model that in some sense stands between these two extremes.
- The **partially synchronous** model (or *eventually synchronous* model).
- In this model the system is considered to be asynchronous, but it is assumed that eventually (meaning for sure at some time in the future that is unknown) the system will behave in a synchronous way for long enough (for something good to happen).

- Synchronous Model: Execution in rounds.
- Transition of the process (internal) state based on two functions:
 - trans_i: states_i x [M U {null}] V --> states_i
 - msgs_i: states_i --> [M U {null}] v
- In each round a process will:
 - Sends a message (potentially different) to all processes.
 - Receives a message from all processes.
 - Apply trans_i over the received messages to determine its following state.

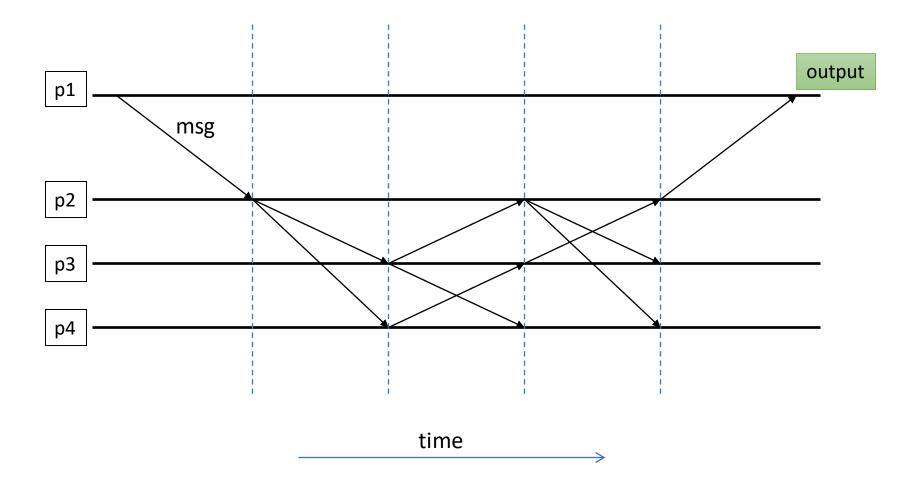
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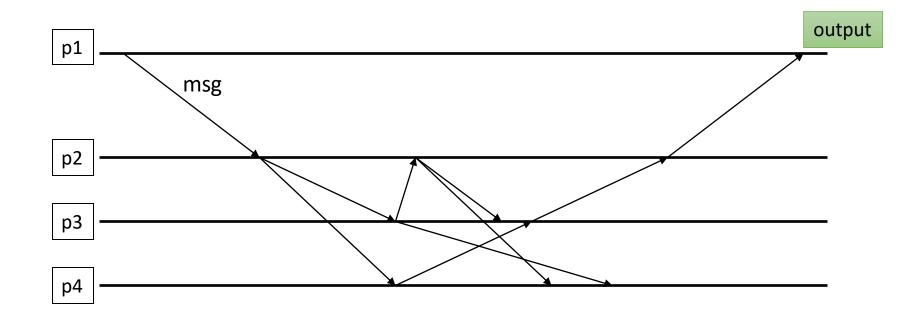
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- Asynchronous Model: Execution is not based on rounds.
- Transition of the process state based on two functions:
 - trans_i: states_i x M U {null} --> states_i
 - msgs_i: states_i --> {M U {null}}
- Since there is no notion of rounds:
 - A transition of state is triggered by the reception of a single message (notice that the transition can be S --> S)
 - Transitioning to a state (even if the same) can trigger the generation (and transmission) of a new set of messages.

Example of an execution in the synchronous model:



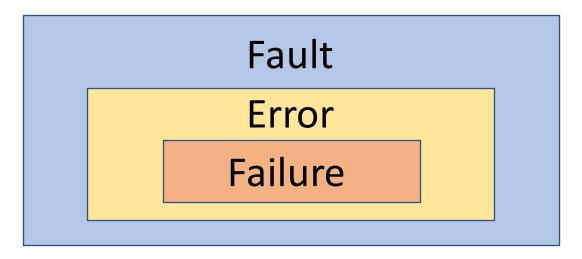
Example of an execution in the asynchronous model:



time

Fault Model

- Faults lead processes to deviate from their expected behavior.
- Classical Model:



- Example: Sector in the hard disk is damaged (fault);
 - -> Sector is accessed (Error) -> File is lost (Failure)

Fault Model (cont.)

- This classical model usually has a recursive implication.
- The failure of a component of a process (or system)
 might imply a fault in another component (or
 different process in the system).
- Going back to the previous example, the failure of the file system (file damaged) might lead to a fault in the load of the operative system, which might result in the failure of the operative system.

- A process that never fails, is considered **correct**.
- Correct processes never deviate from their expected/prescribed behavior.
 - It executes the algorithm as expected and sends all messages defined by it.
- Failed (or Faulty) processes might deviate from their prescribed behavior in different ways.
 - The *unit of failure* is the process, meaning that when it fails, all its component fail at the same time.
- The (possible/considered) behaviors of a faulty process is defined by the process fault model.

- Crash Fault Model:
 - When a process fails it stops sending any messages (from that point onward).
 - This is the fault model that we will consider most of the times.

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Fail-Stop Model:

 Similar to the crash model, except that upon failure the process "notifies" all other processes of its own failure (only possible when considering a synchronous system).

- Byzantine (or Arbitrary) Fault Model:
 - A failed process might deviate from its protocol in any arbitrary way.
 - Examples:
 - Duplicate Messages;
 - Create invalid messages;
 - Modify values received from other processes.
 - Why is this relevant?
 - Can capture memory corruption;
 - Can capture software bugs;
 - A malicious attacker that controls a process.

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 - Why is this relevant?
 - Can capture memory corruption;
 - Can capture software bugs;
 - A malicious attacker that controls a process.
 - This is not something that we will delve into here:
 - The Confiabilidade de Sistemas Distríbuidos (CSD) course deals with these challenges.

- The Network Model captures the assumptions made concerning the links that interconnect processes.
- Namely it captures what can go wrong in the network regarding:
 - Messages sent between processes being lost.
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Some of the weird phenomena in the network can be understood in the **Architectures and Protocols of Computer Networks (APRC)** course.

How to model the network?

We need abstractions like we had with the timing and fault models

In principle, we make a set of assumptions about the network operates

Some models *closer* to reality than others

Network Model (a starting point)

Fair Loss Model

- A model that captures the possibility of messages being lost (albeit in a fair way)
- Properties:
 - FL1 (Fair-Loss): Considering two correct processes *i* and *j*; if *i* sends a message to *j* infinite times, then *j* delivers the message infinite times.
 - FL2 (Finite Duplication): Considering two correct processes *i* and *j*; if *i* sends a message *m* to *j* a finite number of times, then *j* cannot deliver *m* infinite times.
 - FL3 (No Creation): If a correct process *j* delivers a message *m*, then *m* was sent to *j* by some process *i*.

Network Model (moving on...)

Stubborn Model

- A stronger model that assumes that processes communicate in a stubborn way, to prevent message loss.
- Properties:
 - SL1 (Stubborn Delivery): Considering two correct processes *i* and *j*; if *i* sends a message to *j*, then *j* delivers the message an infinite number of times.
 - SL2 (No Creation): If a correct process j delivers a message m, then m was sent to j by some process i.

Network Model (better now)

Perfect Link Model (also called Reliable):

- A stronger model that assumes the links between processes are well-behaved.
- Properties:
 - PL1 (Reliable Delivery): Considering two correct processes i and j; if i sends a message to j, then j eventually delivers m.
 - PL2 (No Duplication): No message is delivered by a process more than once.
 - PL3 (No Creation): If a correct process j delivers a message m, then m was sent to j by some process i.

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 - The perfect link model makes it easier to reason about algorithms design...
 - ...but more importantly, these abstractions can be built on top of one another using **distributed algorithms**.

• Our property of the property

What is this dark sorcery that you speak?

• Oul profrections of the contraction of the contra

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- What is this dark sorcery that you speak?
- Wait for the lab today to discover...

Don't forget that the perfect link abstraction does not state anything about time

Algorithms Specification and Properties

 Did you noticed that when discussing these network models (i.e., abstractions) I have defined them in terms of a set of properties?

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- Why do we tend to think in terms of properties?

Algorithms Specification and Properties

- Did you noticed that when discussing these network models (i.e., abstractions) I have defined them in terms of a set of properties?
- **Algorithms** (that instantiate these abstractions) also provide a set of **properties** (if correct, those of the abstraction they implement).
- Why do we tend to think in terms of properties?
- Quick answer: Because algorithms are composable, and the design of an algorithm depends on the underlying properties provided by other algorithms.

Algorithms Specification and Properties

What does these properties capture?

- The correctness criteria for the algorithm (and for any implementation of that algorithm).
- It defines restrictions to (all) valid executions of the algorithm.

Two fundamental types of properties:

- Safety
- Liveness

Safety Properties

Conditions that must be enforced at any (and all) point of the execution

 Intuitively, preventing bad things that should never happen.

Relevant aspects:

- The trace of an empty execution is always safe (do nothing and you shall do nothing wrong).
- The prefix of a trace that does not violate safety, will never violate safety.

Liveness Properties

Conditions that should be enforced at some point of an execution (but not necessarily always).

Intuitively, good things that should happen eventually.

Relevant aspects:

 One can always extend the trace of an execution in a way that will respect liveness conditions (if you haven't done anything good yet, you might do it in the future).

Safety VS Liveness Properties

 Correct algorithms will have (most of the times) both Safety and Liveness properties.

- Some properties however are hard to classify within one of these classes, and they might mix aspects of safety and liveness
 - Usually, one can decompose these properties in simpler ones through conjunctions.

Modelling distributed systems

Models that handle:

- Networks
- Timing
- Faults

Currently, we do not have any constructions that actually **operate** within these models

Let's now start to think about concrete problems...

 Now that we have covered the rules of the game, we can start to think on how to solve problems (within a particular set of rules).

The Broadcast Problem

- Informally: A process needs to transmit the same message m to N other processes (where N is every process in the system including himself).
- Let's assume that the complete set of processes in the system is known a-priori: π
- Let's assume we have access to the Perfect Point-to-Point Link Abstraction.
- Let's assume an asynchronous system (no rounds, no failure detection).

The Broadcast Problem

Wait... How do you specify an algorithm again?

 I have sort of told you before, through a deterministic automaton...

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Wait... How do you specify an algorithm again?

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Ok let's simplify this...

ALGORITHM

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You need an Interface for this to be used (think of APIs)

ALGORITHM

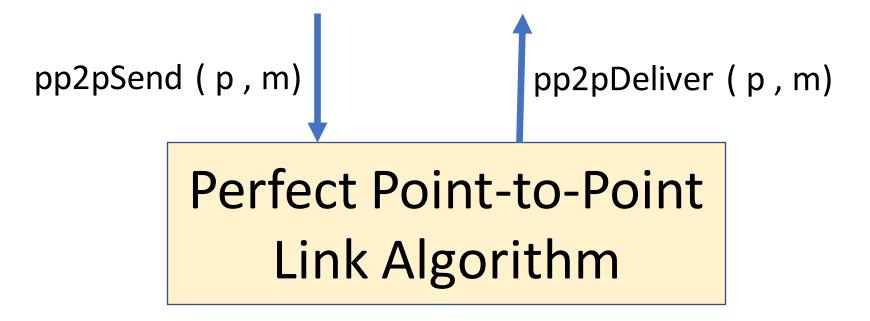
You need an Interface for this to be used (think of APIs)

Perfect Point-to-Point Link Algorithm

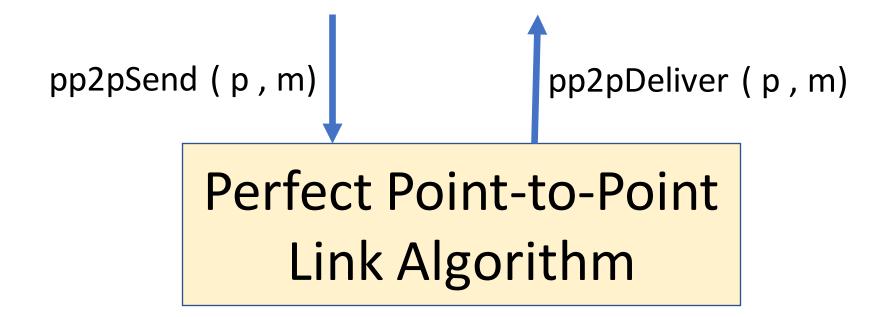
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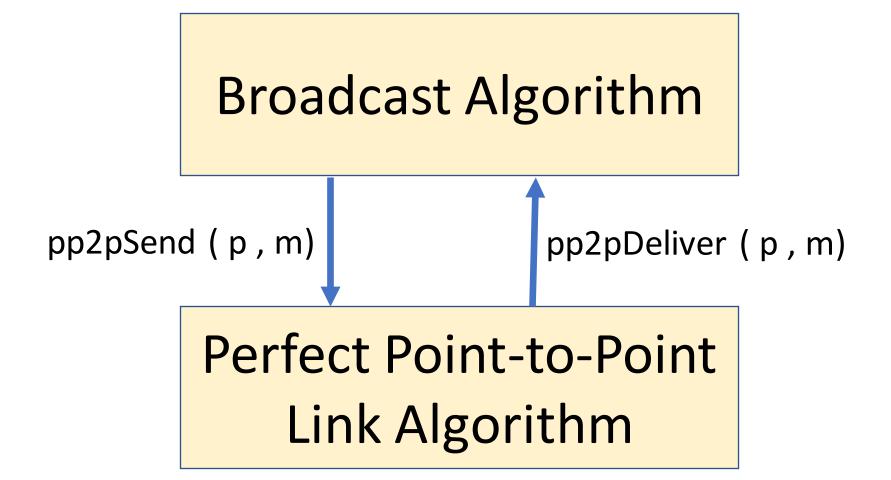
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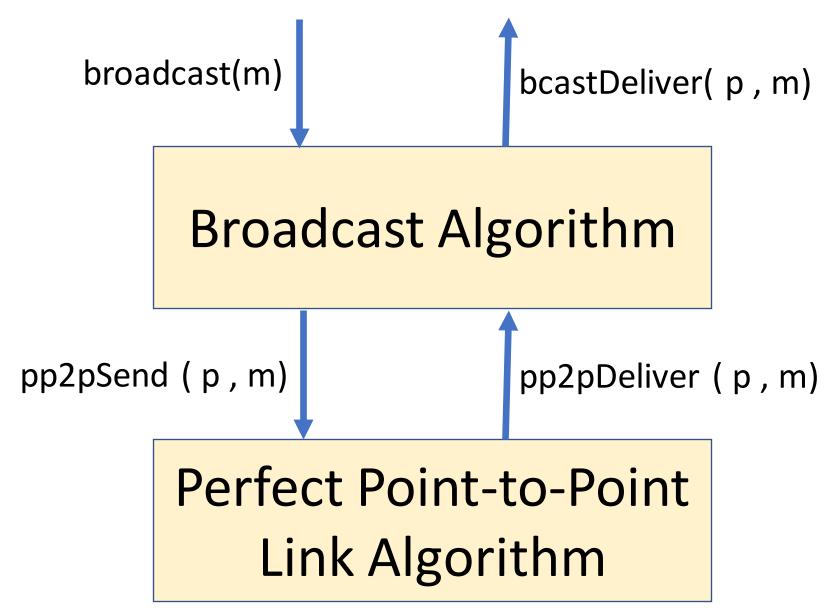


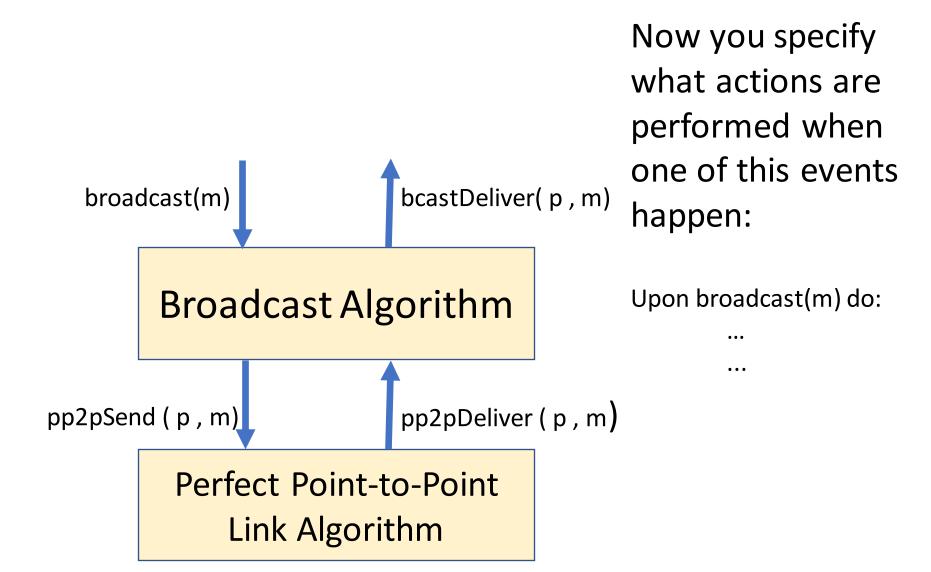
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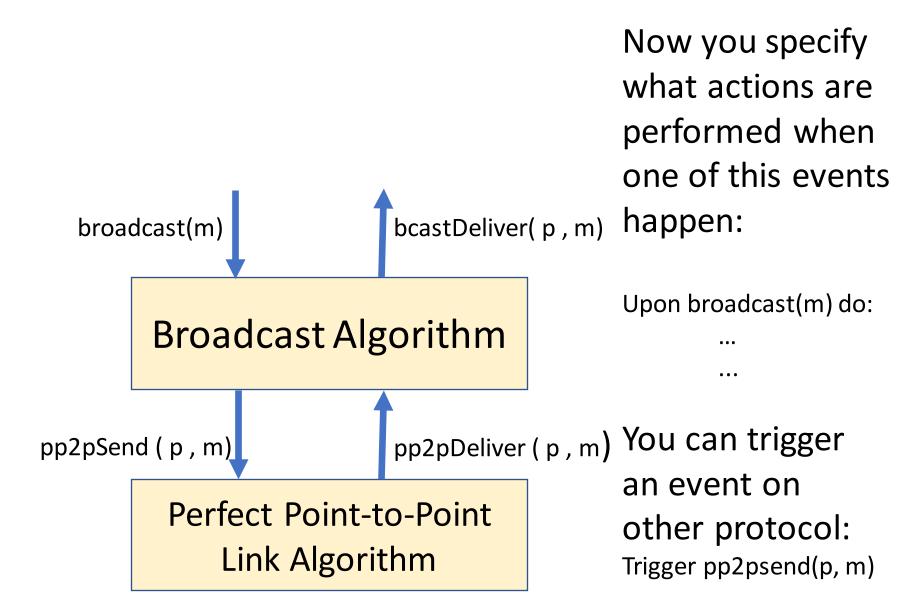




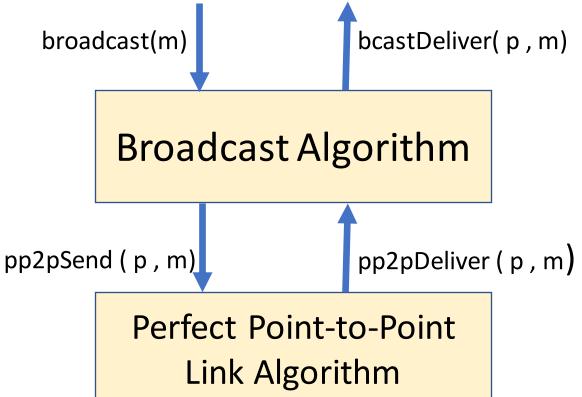
broadcast(m) **Broadcast Algorithm** pp2pDeliver (p,m) pp2pSend (p,m) Perfect Point-to-Point Link Algorithm







There is a special event called **Init** where you can initialize the **local** state of the **algorithm**



Now you specify what happens when one of this events happen:

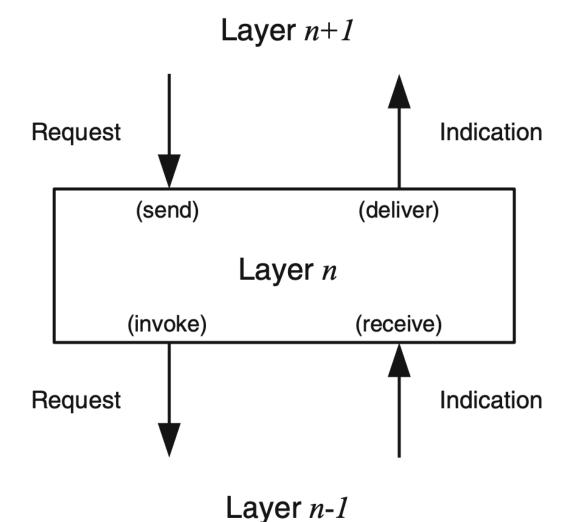
Upon broadcast(m) do:

• •

You can trigger an event on another protocol:

Trigger pp2psend(p, m);

Layering (Broadcasts)

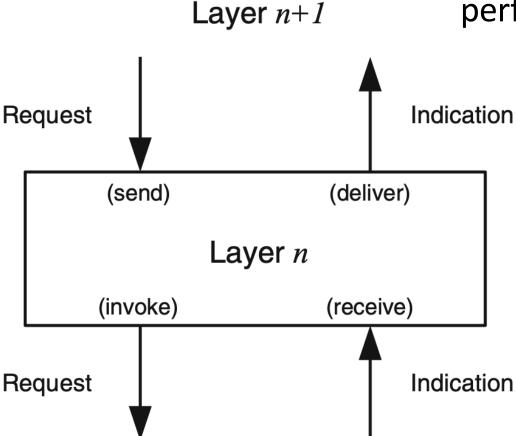


Two important distinctions:

- Requests
- Indications

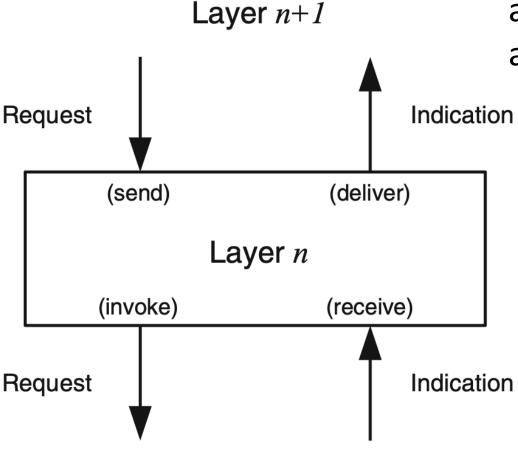
Requests

Requests inform the *next* layered algorithm to perform some action.



Layer *n-1*

Indications



Indications inform the *previous* layered algorithm that the action was performed.

Layer *n-1*

Back to the Broadcast problem...

What is the simplest solution that you can think of?

Think like this:

- I am a process; someone asks me to send a message to everyone (including me)
- I know everyone already so basically what do I do?

Back to the Broadcast problem...

What is the simplest solution that you can think of?

Solution:

Just go ahead and send the message to everyone, one at a time. When you get one of these messages, you just deliver it to the upper layer.

Back to the Broadcast Problem:

Good... that works... (Sort of)

- That is the solution for the Best Effort Broadcast.
- Best Effort Broadcast:
 - BEB1 (Best-Effort validity): For any two correct processes
 i and *j*, every message broadcasted by *i* is eventually
 delivered by *j*.
 - BEB2: (No Duplication): No message is delivered more than once.
 - BEB3: (No Creation): If a correct process j delivers a message m, then m was broadcast by some process i.

Best Effort Broadcast

State: (could be omitted)

Upon Init do: (could be omitted)

```
Upon bebBroadcast( m ) do
    forall p ∈ π
    trigger pp2pSend( p, m);
```

Upon pp2pDeliver (p , m) do
 trigger bebDeliver(p, m);

Best Effort Broadcast

Not so great right?

 What happens if a process fails while sending messages to all the other processes?

Best Effort Broadcast

• Not so great right?

 What happens if a process fails while sending messages to all the other processes?

Answer not everyone gets the message...

- Let's make this somewhat stronger and more interesting...
- Reliable Broadcast:
 - RB1 (Validity): If a correct process i broadcasts message m, then i eventually delivers the message.
 - RB2 (No Duplications): No message is delivered more than once.
 - RB3 (No Creation): If a correct process j delivers a message m, then m was broadcast to j by some process i.
 - RB4 (Agreement): If a message m is delivered by some correct process i, them m is eventually delivered by every correct process j.

How do you think we could solve this problem? Remember that we can use the Best Effort Broadcast Algorithm to solve this one...

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```
State:
             delivered //set of message ids that were already delivered.
Upon Init do:
             delivered ← {};
Upon rbBroadcast( m ) do
             trigger rbDeliver(m);
             mid \leftarrow generateUniqueID(m);
             delivered ← delivered U {mid};
             trigger bebBroadcast( { mid, m } );
Upon bebDeliver(p, { mid, m } ) do
             if ( mid ∉ delivered ) then
                           delivered ← delivered U {mid};
                           trigger rbDeliver(m);
                           trigger bebBroadcast(mid, m);
```

In all fairness in the Literature: Eager Reliable Broadcast

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                           trigger rbDeliver(m);
                           trigger bebBroadcast(mid, m);
```

In all fairness in the Literature: Eager Reliable Broadcast

trigger bebBroadcast(mid, m);

```
State:
             delivered //set of message ids that were already delivered.
Upon Init do:
                                                          Why is this solution correct?
            delivered ← {}:
Upon rbBroadcast( m ) do
            trigger rbDeliver(m);
             mid ← generateUniqueID(m);
             delivered ← delivered U {mid};
            trigger bebBroadcast( { mid, m } );
Upon bebDeliver(p, { mid, m } ) do
            if ( mid ∉ delivered ) then
                          delivered ← delivered U {mid};
                         trigger rbDeliver(m);
```

To show the correctness of the algorithm we must check each property individually. For each we have me make a (rational) argument that the algorithm enforces it.

Reliable Broadcast:

- RB1 (Validity): If a correct process i broadcasts message m, then i eventually delivers the message.
- RB2 (No Duplications): No message is delivered more than once.
- RB3 (No Creation): If a correct process j delivers a message m, then m was broadcast to j by some process i.
- RB4 (Agreement): If a message m is delivered by some correct process i, them m is eventually delivered by every correct process j.

In all fairness in the Literature: Eager Reliable Broadcast

State:

delivered //set of message ids that were already delivered.

This solution consumes a lot of messages (not being nice for the network nor processors)!

In fact, it costs $O(|\pi|^2)$ total messages to execute.

• Ideally we would design a Reliable Broadcast solution that resulted in $O(|\pi|)$ messages

• See Lab 01!

Summary of Lecture

Why are distributed systems required?

The importance of abstractions

Idealised models for describing distributed algorithms

Concrete examples of broadcasting messages

Quiz!!1!



Question 1

Which p2p link model allows for the loss of messages?

Fair loss

Stubborn

Perfect

Answer 1

Which p2p link model allows for the loss of messages?

Fair loss

Stubborn

Perfect

Question 2

In the synchronous model, it is impossible to tell when a process has failed?

True

False

Answer 2

In the synchronous model, it is impossible to tell when a process has failed?

True

False

Question 3

Which fault model allows a process to keep sending and delivering a subset of the messages it receives?

Crash fault

Omission fault

Fail-stop

Answer 3

Which fault model allows a process to keep sending and delivering a subset of the messages it receives?

Crash fault

Omission fault

Fail-stop