

## Grid Detection Dataset

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### Dataset description

The dataset contains multiple image sequences of varying difficulty.

- seq1/img0000-img0500.jpg: Easy, majority of grid visible in each image.
- seq2/img0000-img0310.jpg: People walking past camera.
- seq3/img0000-img0250.jpg: Viewing from outside surrounding net.

The camera is approximately level with the ground in seq1 and seq2, but substantially tilted in seq3. The camera height is between 1 and 2 meters.

### Camera model

Modeling fisheye lenses is not part of the curriculum, so we provide an appropriate camera model. The model is equivalent to the OpenCV fisheye model with a single radial distortion coefficient. Python and Matlab implementations of the projection equations described below is included in the dataset.

#### *Fisheye projection*

The model is best understood by rewriting camera coordinates  $(X, Y, Z)$  using spherical coordinates:

$$X = \lambda \sin \theta \cos \phi \quad (1)$$

$$Y = \lambda \sin \theta \sin \phi \quad (2)$$

$$Z = \lambda \cos \theta \quad (3)$$

Here,  $\lambda$  is the distance of the point from the center of projection,  $\theta$  is its angle against the optical axis, and  $\phi$  is its angle around the optical axis. The projection of the point into the fisheye image is then given by

$$u = c_x + f\theta(1 + k\theta^2) \cos \phi \quad (4)$$

$$v = c_y + f\theta(1 + k\theta^2) \sin \phi \quad (5)$$

where  $f, c_x, c_y, k$  are the fisheye model parameters (included in the dataset).

### *Converting from and to rectilinear projection*

If we rewrite the equations for a rectilinear projection (ideal pinhole) using spherical coordinates, the projection of a point into the image is given by

$$u = c_x + f \tan \theta \cos \phi \quad (6)$$

$$v = c_y + f \tan \theta \sin \phi \quad (7)$$

To convert a point in a rectilinear image into a point in the original fisheye image, you can use the procedure from exercise 2. First, invert the rectilinear projection to obtain  $\theta, \cos \phi, \sin \phi$ . Then, project back into the fisheye image using the projection equations.

To go the other way, converting a point in the fisheye image to a point in a rectilinear image, you need to invert the fisheye equations to find  $\theta, \cos \phi, \sin \phi$ . Doing this algebraically requires solving a cubic polynomial in  $\theta$ , which can be tricky. Instead, you can solve for  $\theta$  using numerical root finding, e.g. Newton-Raphson iteration (see Wikipedia).