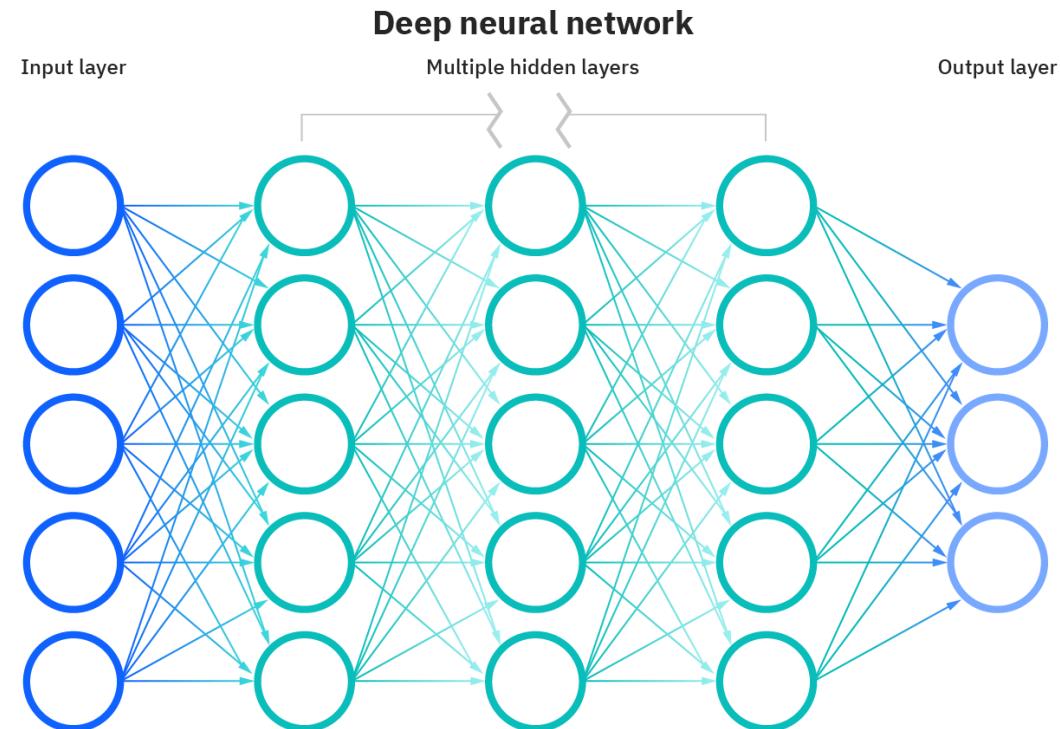


Deep Learning

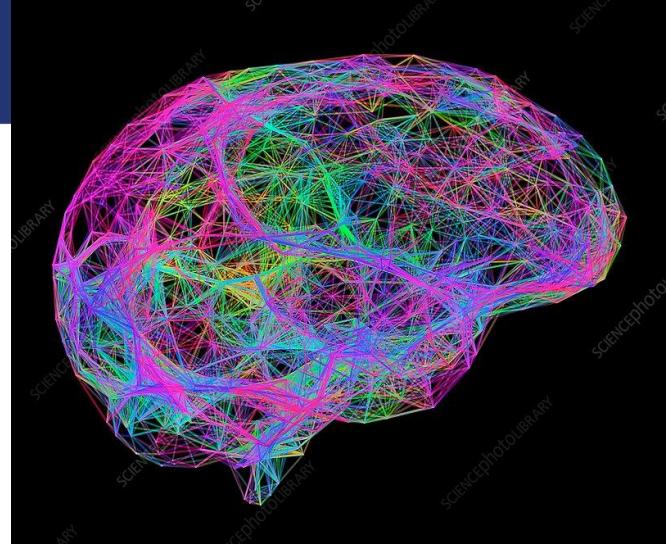
Neural Networks



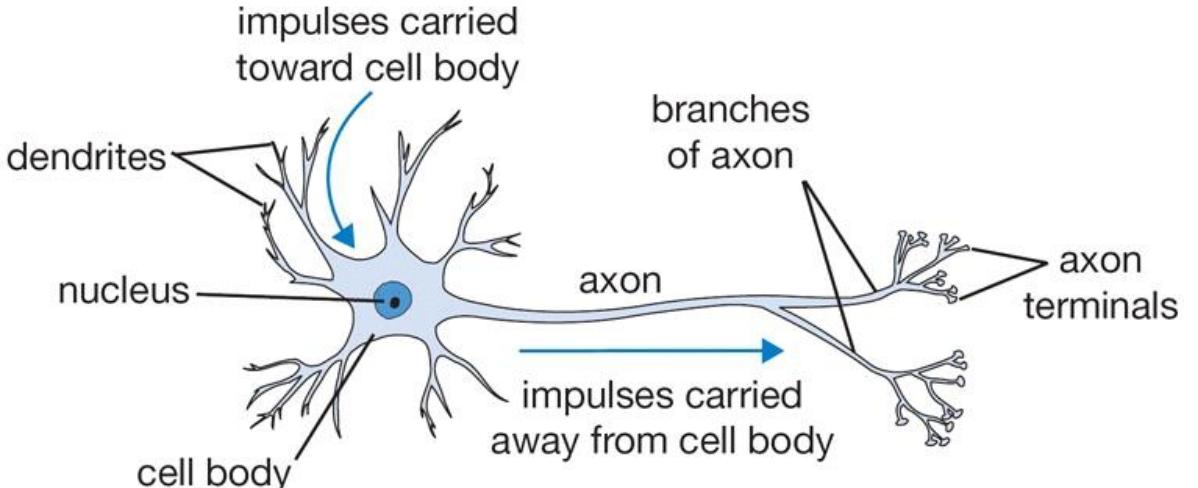
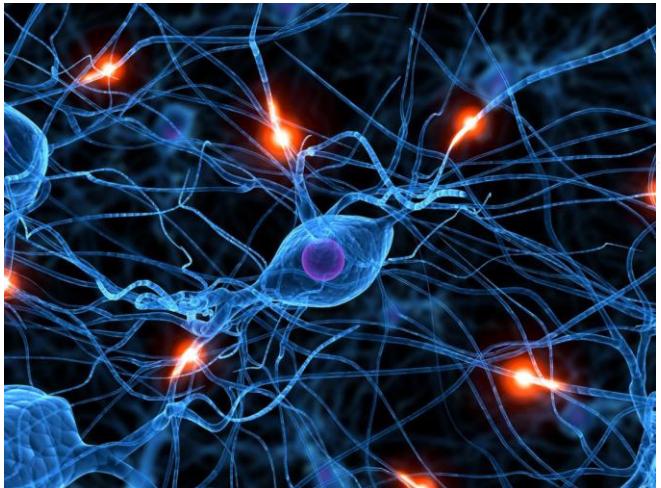


DEEP LEARNING – A NEW PROMISE

Biological Motivation



- There are ~86B neurons in our brain
- Neurons are connected to other neurons through an axon
- The structure resemble to a network, where information is passed from one neuron to another



Geoffrey Hinton (2016)



2021

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FAULTY IMAGE

AI has a long way to go before doctors can trust it with your life



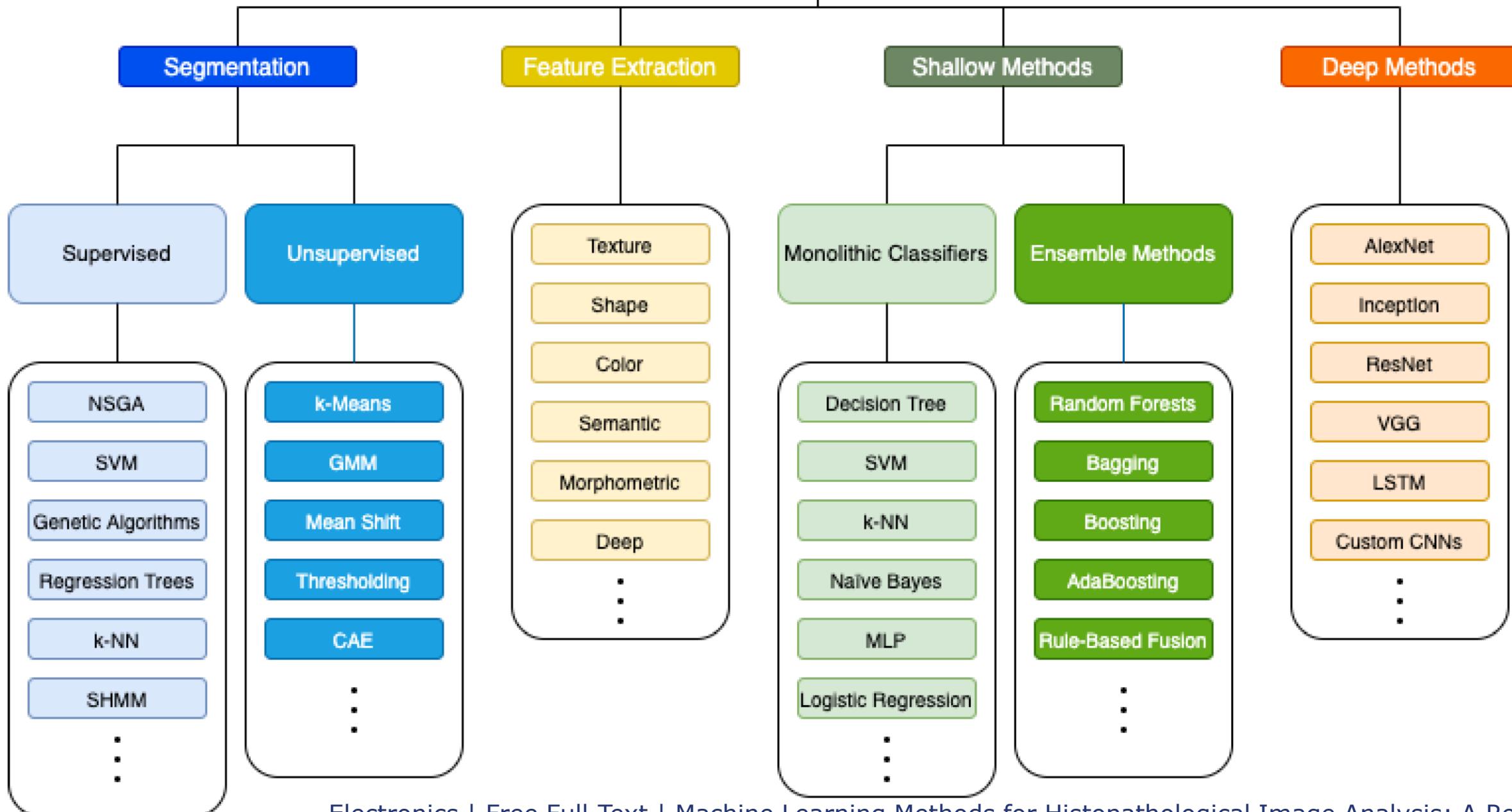
A hand points at a chest X-ray image, which shows the ribcage and lungs. The image is labeled 'ID 208727' on the left and 'CHEST Im. #1 22:24:06' on the right. The hand is dark-skinned and appears to be pointing towards a specific area of the lung field.

Job security.

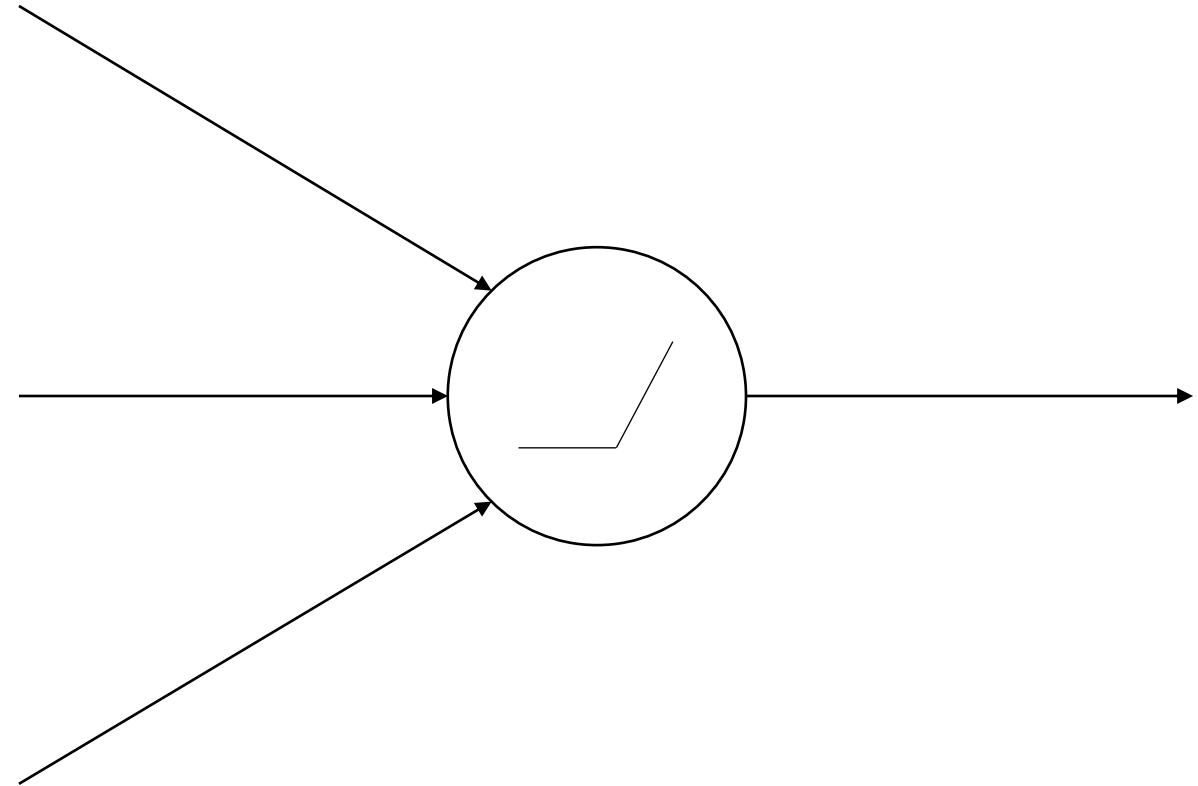
By Gary Smith and Jeffrey Funk | Published June 4, 2021

Image: REUTERS/Luke MacGregor

ML Methods for HI Analysis

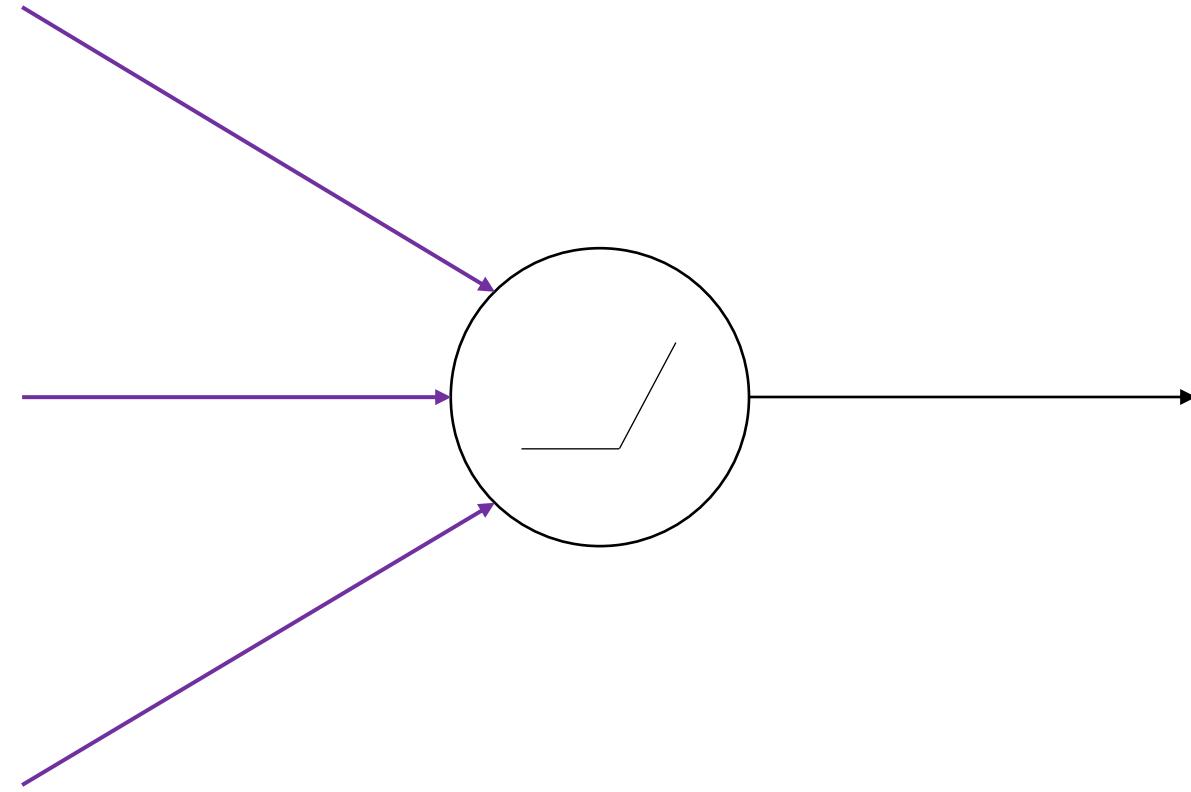


Neuron (Perceptron)



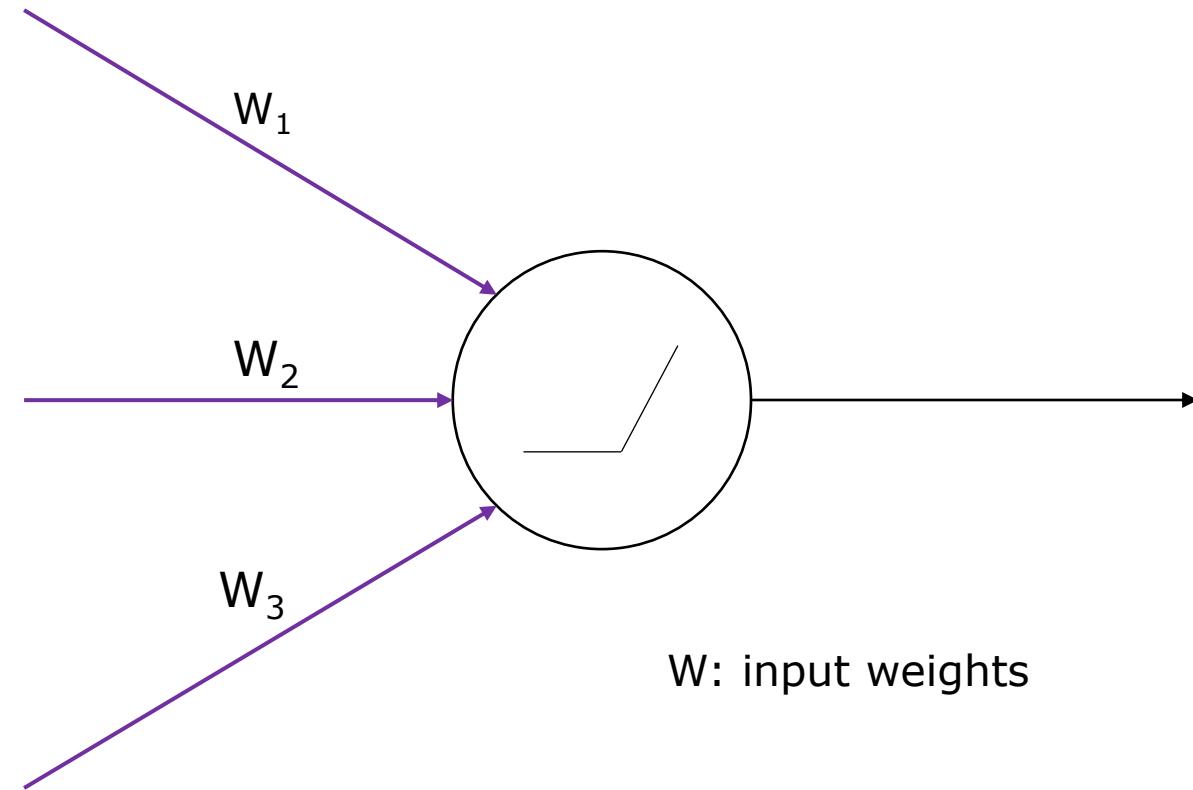
Neuron (Perceptron)

**Input
synapses**



Neuron (Perceptron)

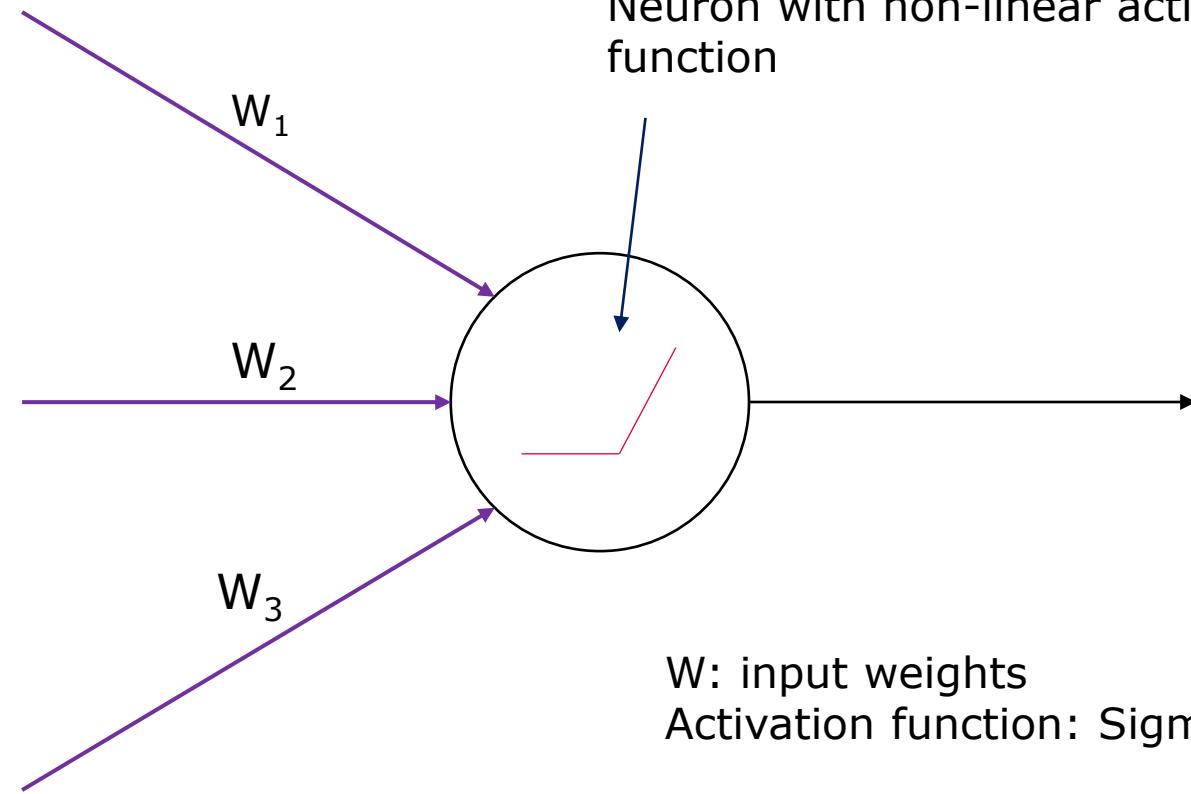
**Input
synapses**



w : input weights

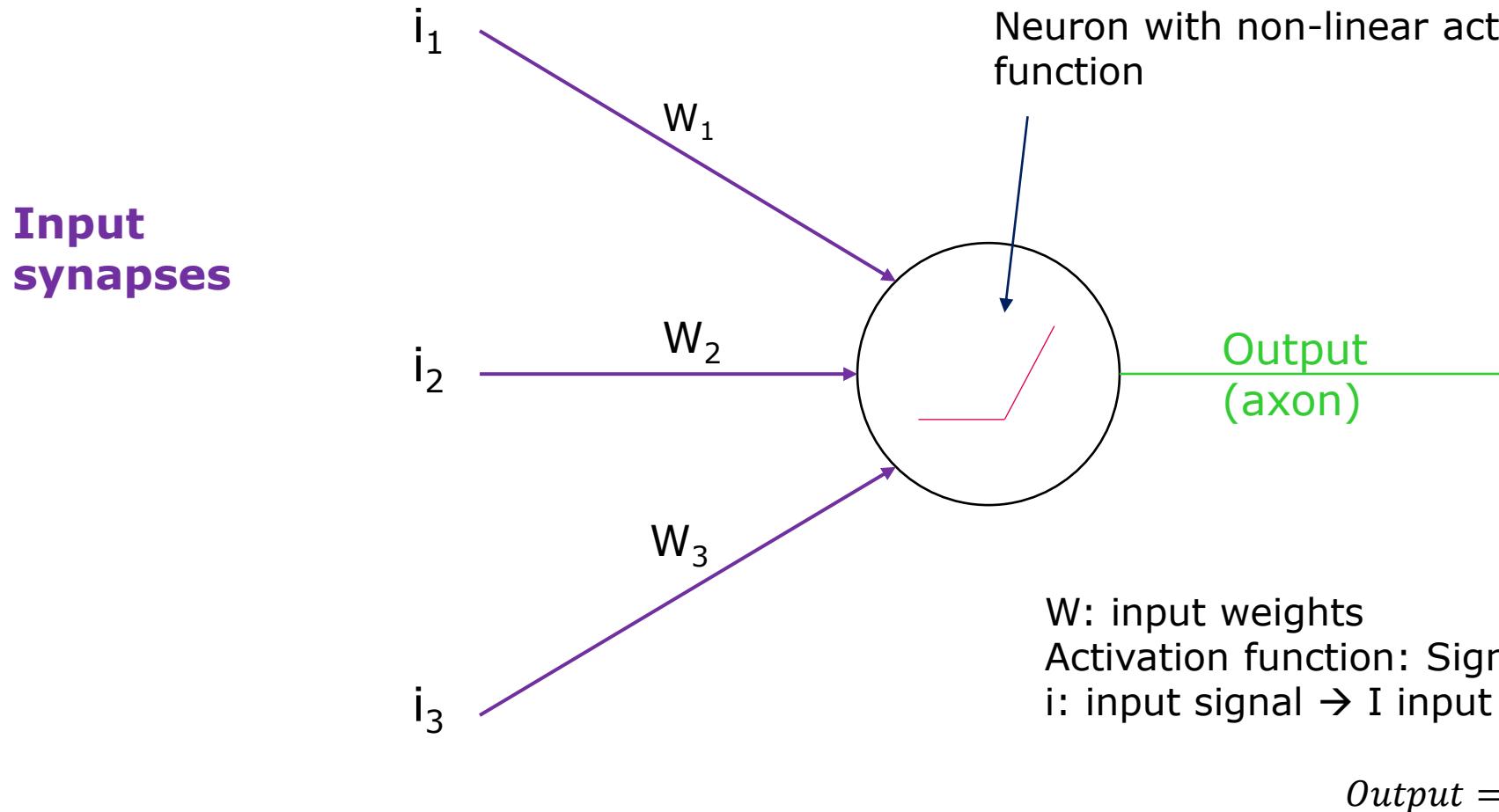
Neuron (Perceptron)

**Input
synapses**

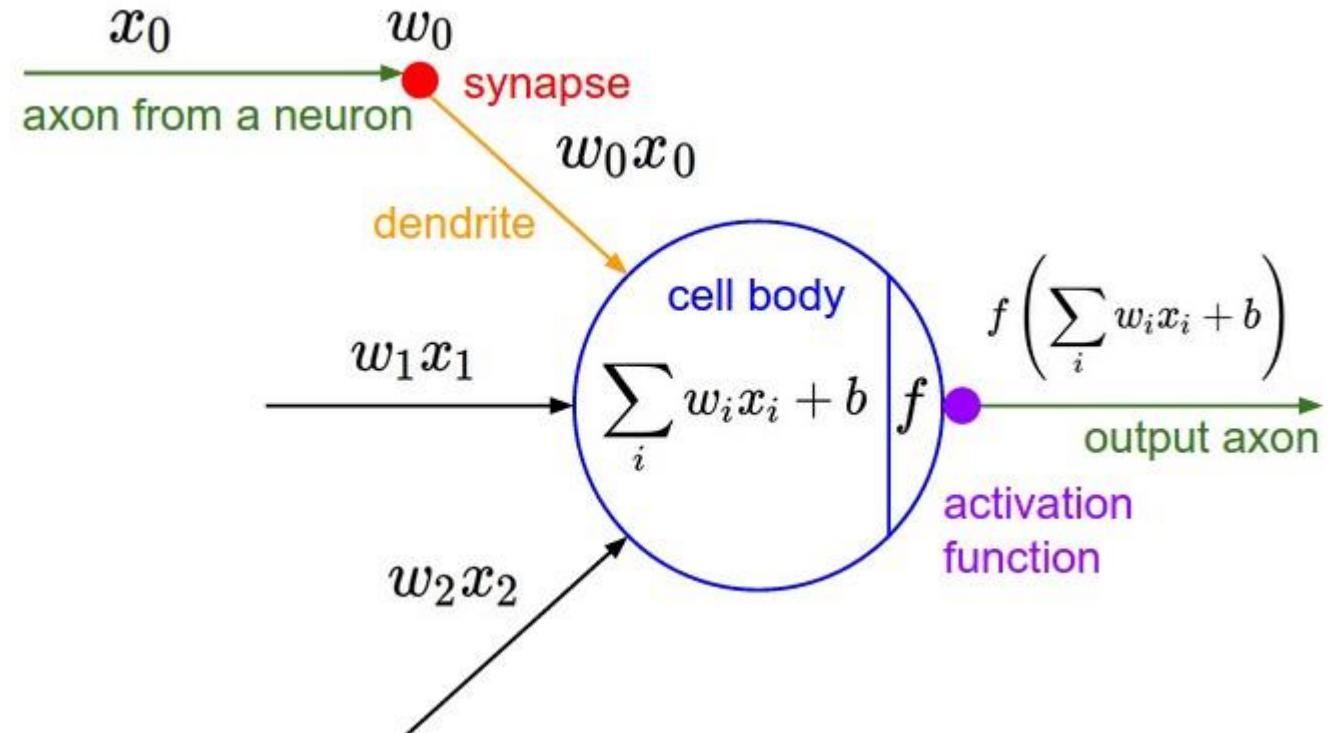
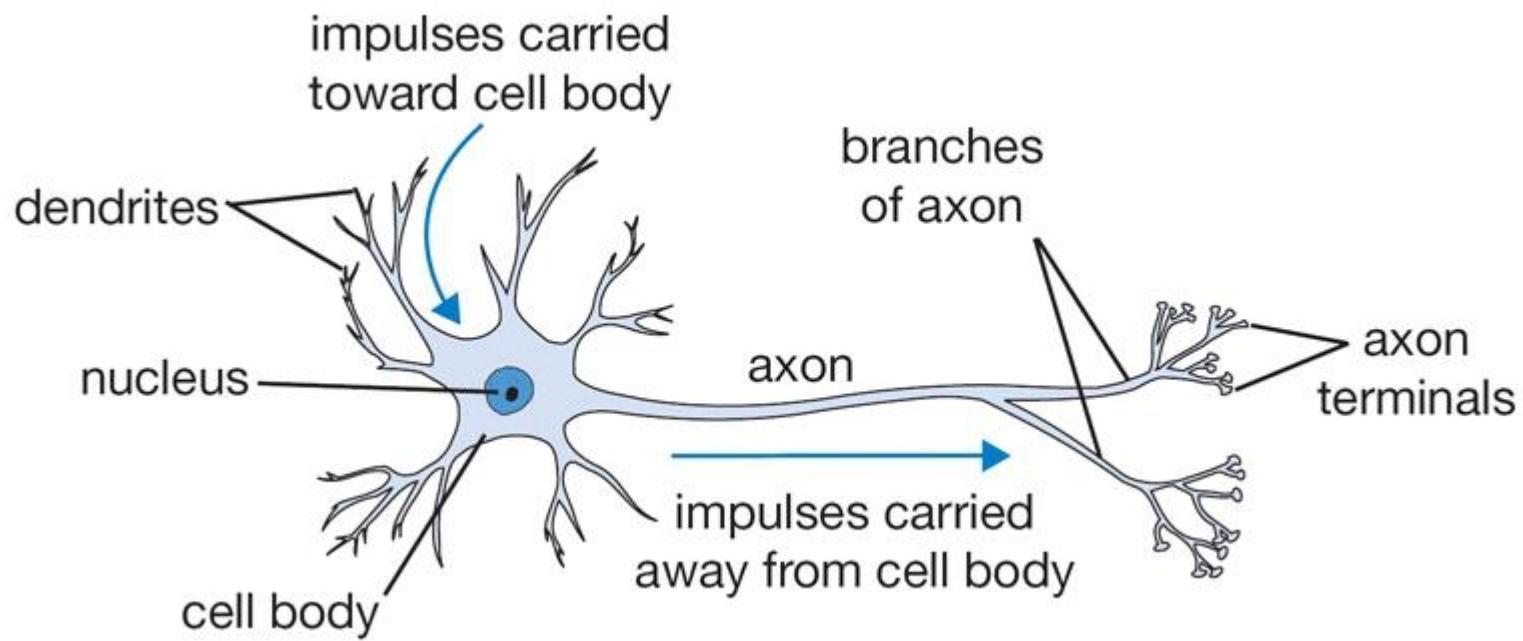


W: input weights
Activation function: Sigmoid // $\max(0, \text{value})$

Neuron (Perceptron)



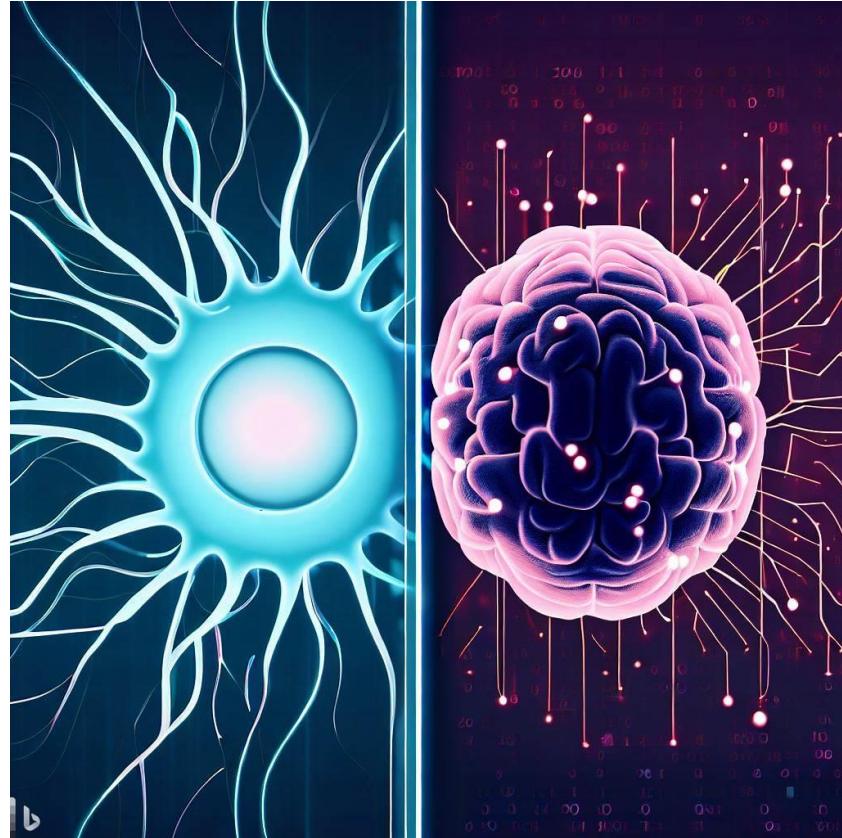
Biology-Inspired



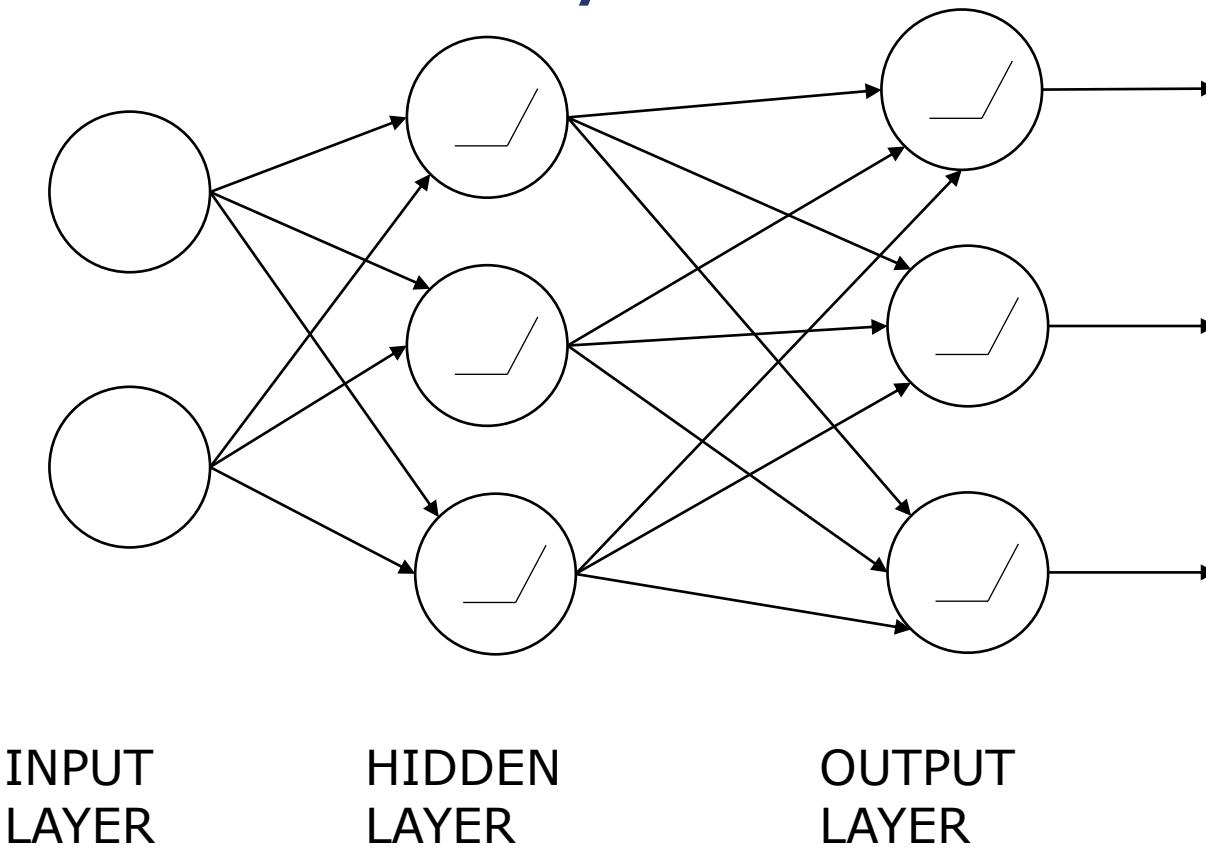
Neuron (Perceptron)

Differences from real brain neurons

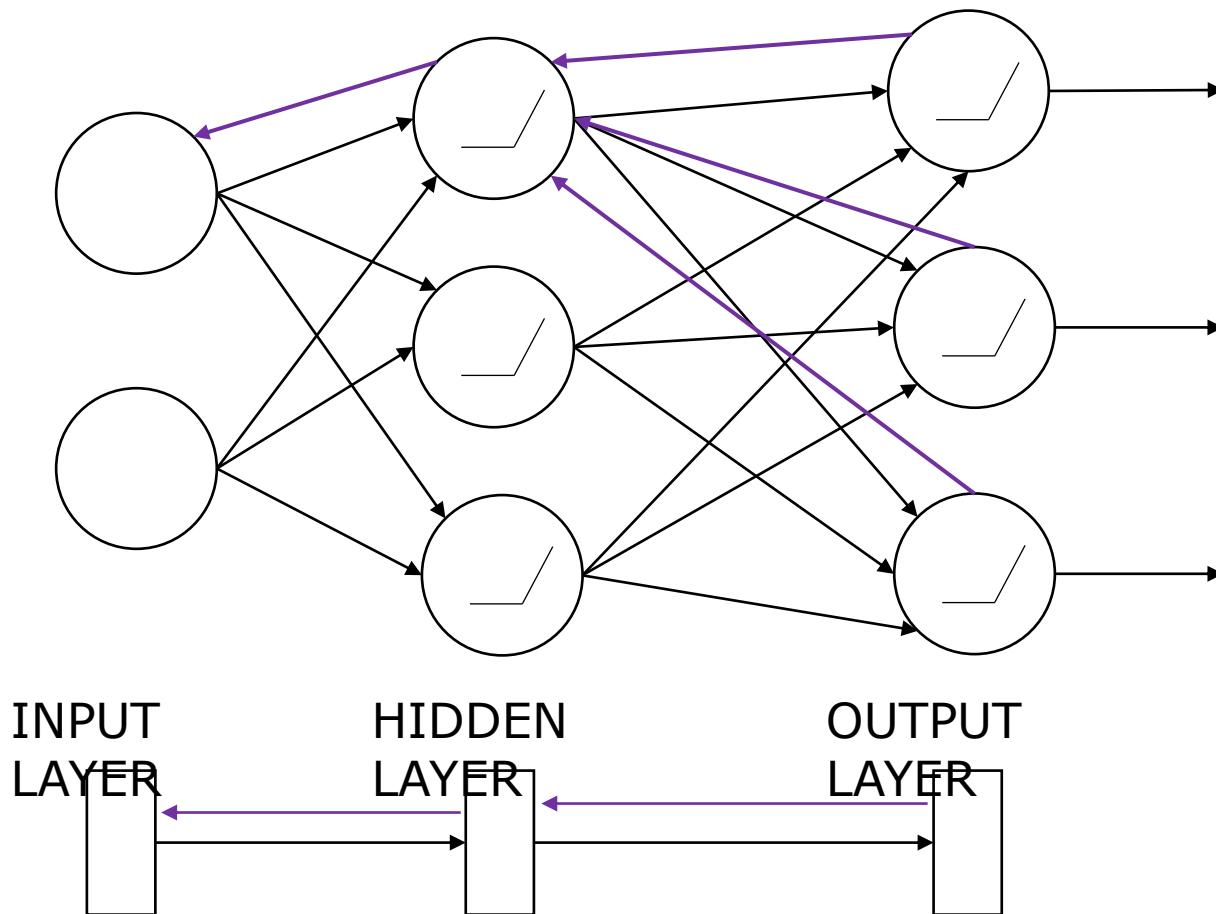
- The perceptron model is quite different from the biological neurons:
 - Those communicate by sending spike signals at various frequencies
 - The learning in brains seems also quite different
- It would be better to think of artificial neural networks as non-linear projections of data (and not as a model of brain)



Neural Network Layers



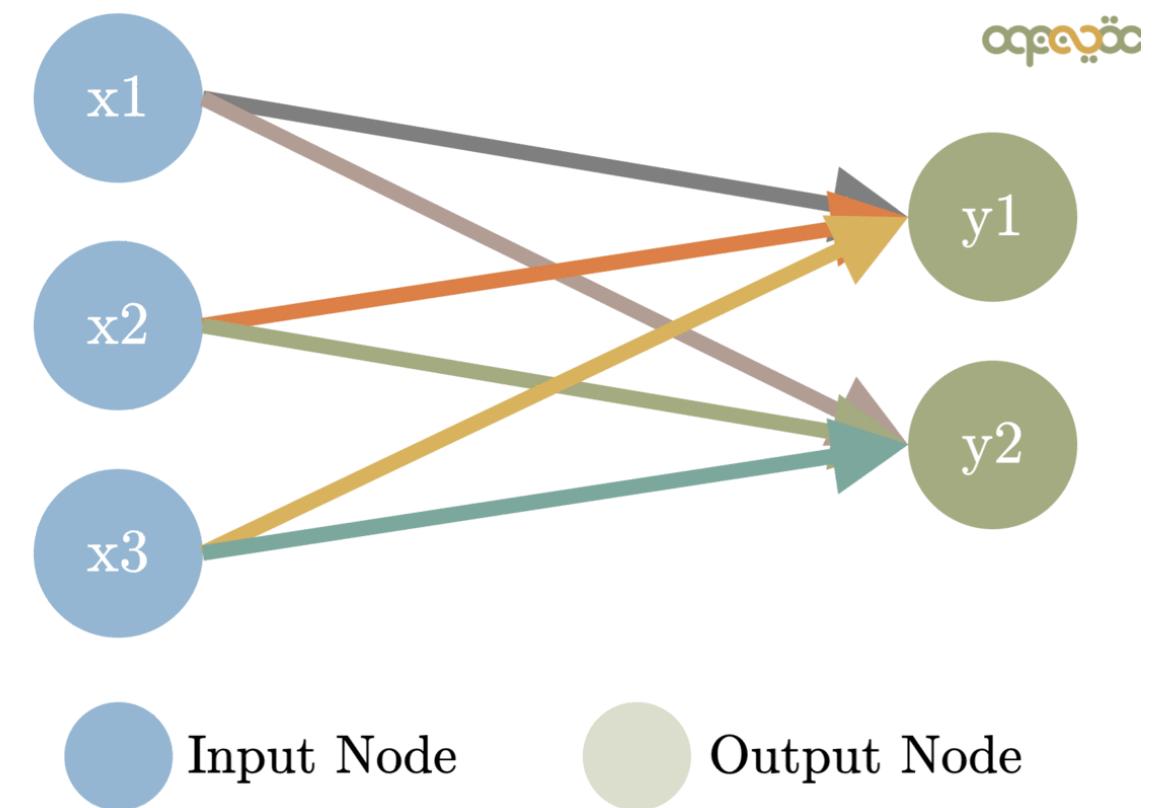
Neural Network Layers



- During the training, the network computes the values for a certain input through the network and compares the result to the given output.
- The gradient of the error is used to correct the neuron weights.

Neural Network

Simple network



Error calculation

Loss Function

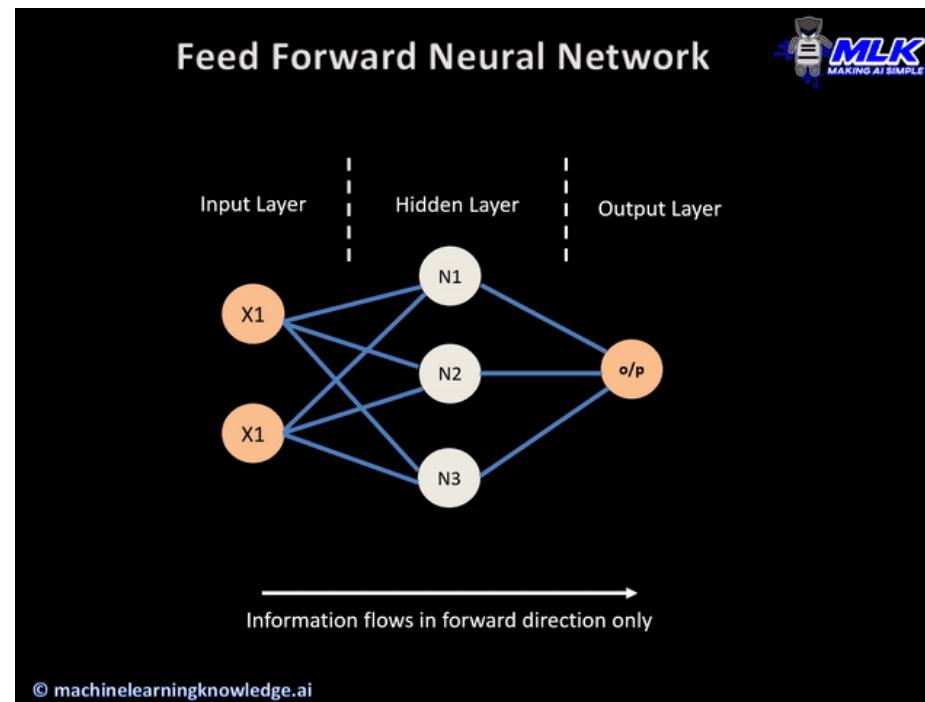
- Calculates the distance between the network output and the desired value.
- You decide which loss function to use, based on the task:
 - Mean Squared Error (MSE) – regression
 - Binary Cross Entropy – binary classification
 - Categorical Cross Entropy Loss – multiclass (one-hot-vectors)
 - Negative Log-Likelihood loss – multiclass
 - Multilabel margin loss – multilabel

And many, many more...

[torch.nn — PyTorch 2.0 documentation](#)

The Inference Part – Feed Forward

Given an input, predicting the output by calculating the values through the network



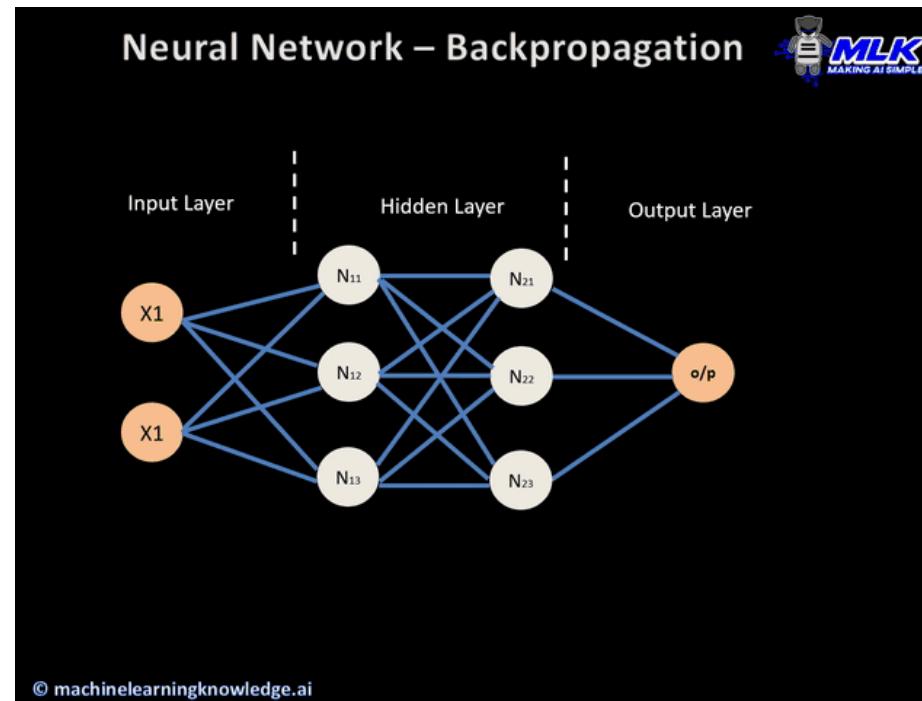
Backpropagation – Training Networks to Learn

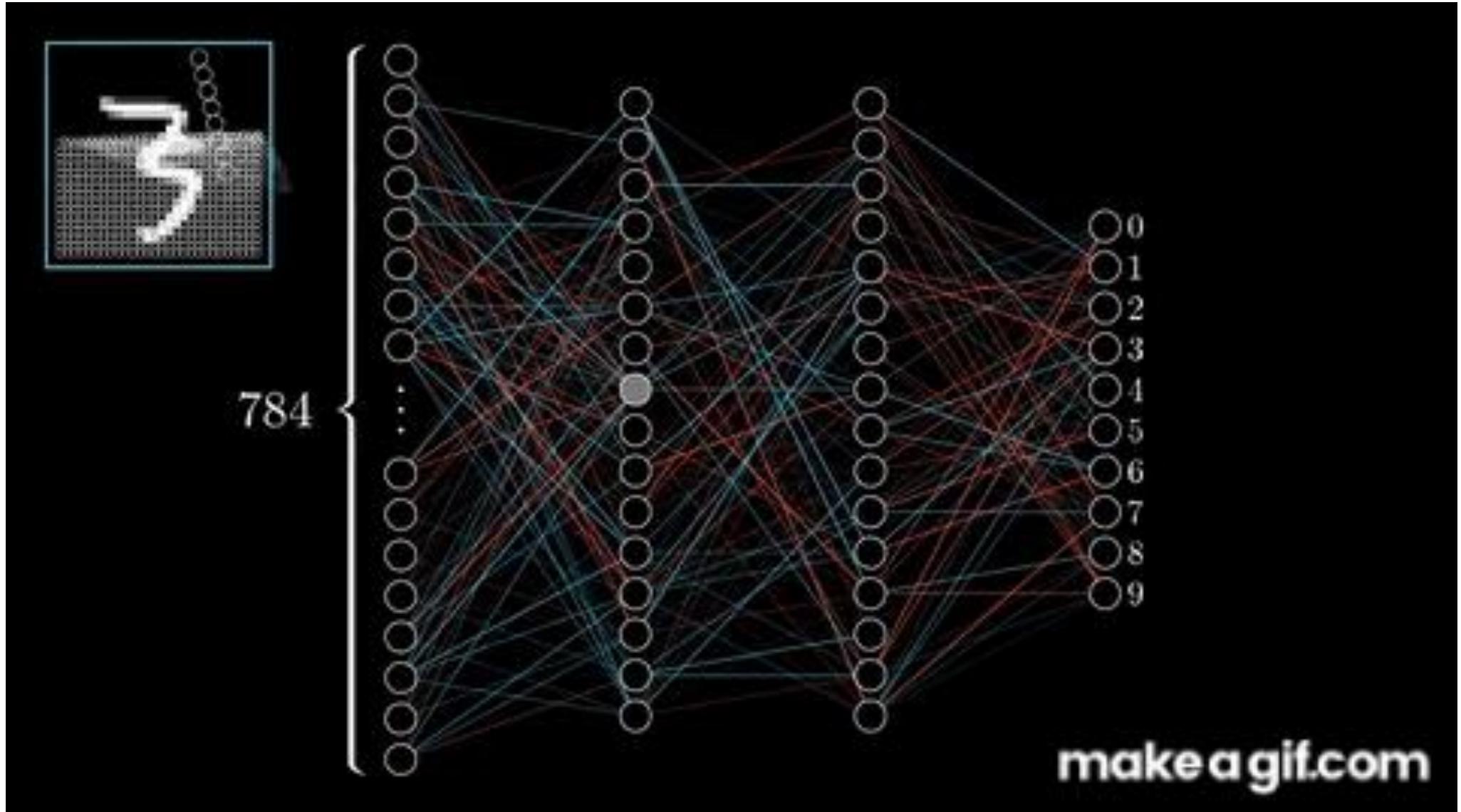
Backpropagation occurs
only during the training.

The network calculates the
error (**loss function**)

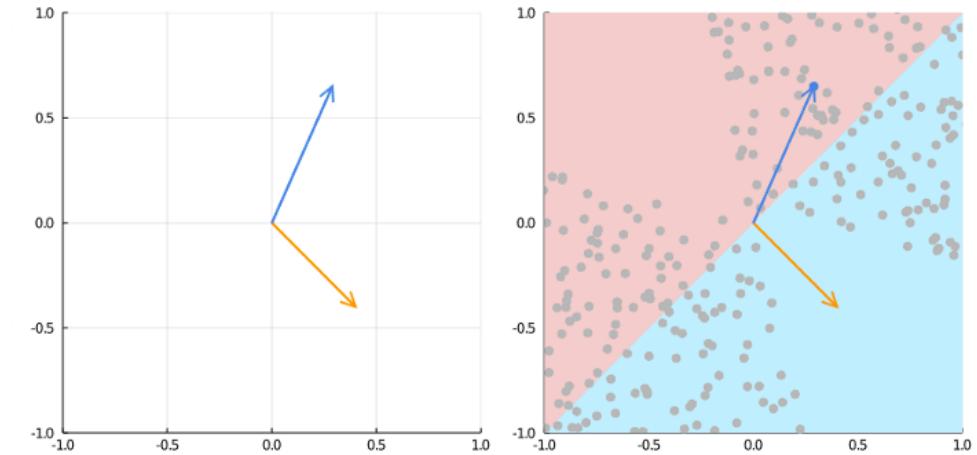
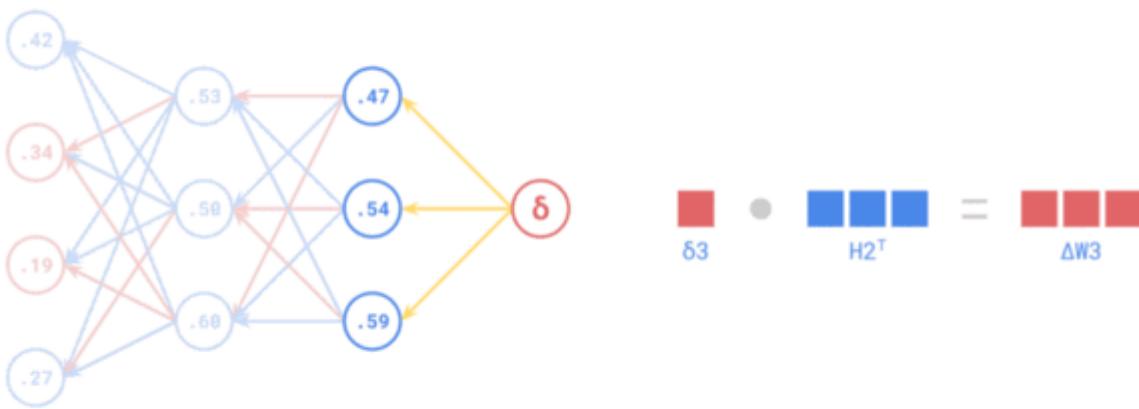
Then gently updates the
network weights

Next time, when they “see”
this sample, the prediction
is closer to the desired
result.



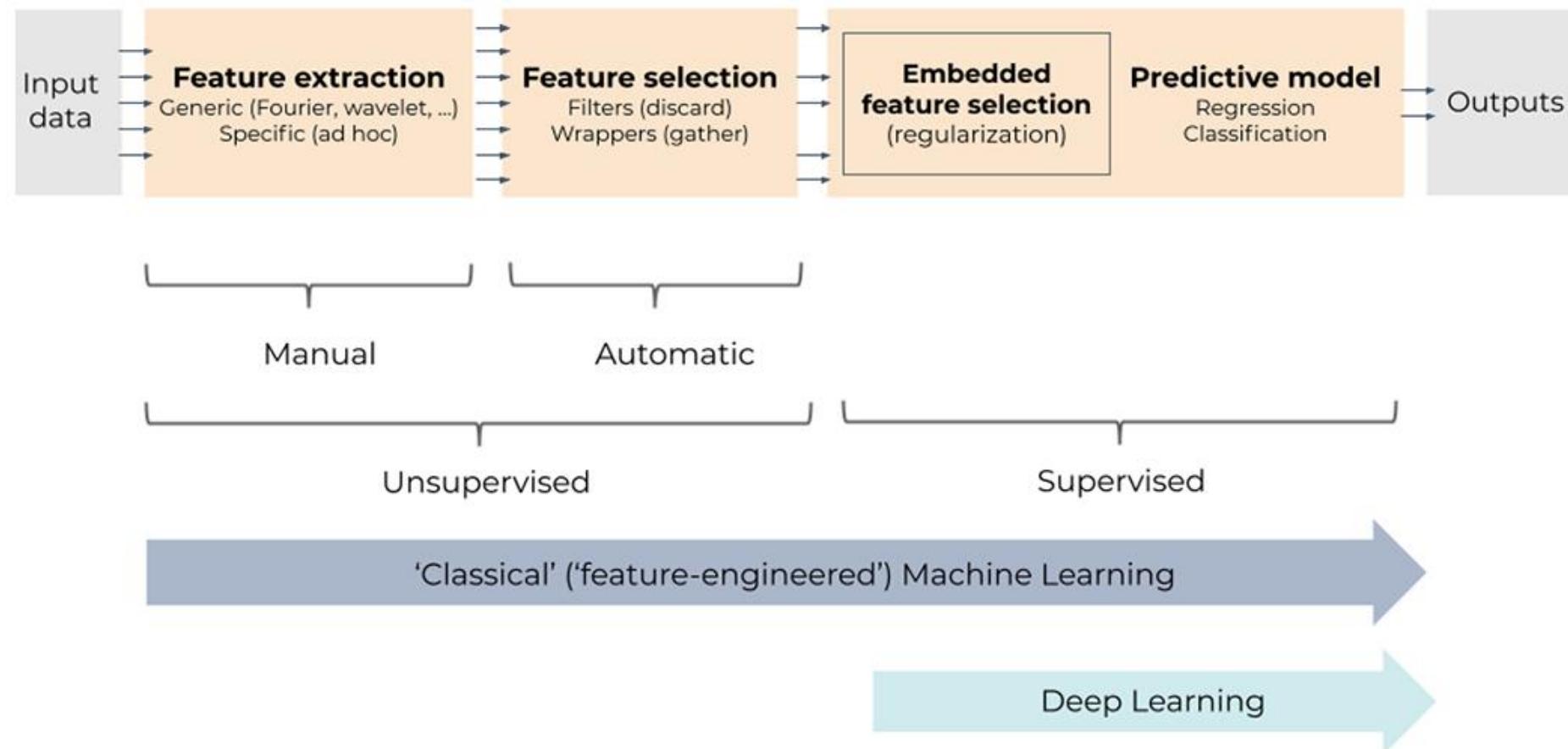


For a Deeper Dive



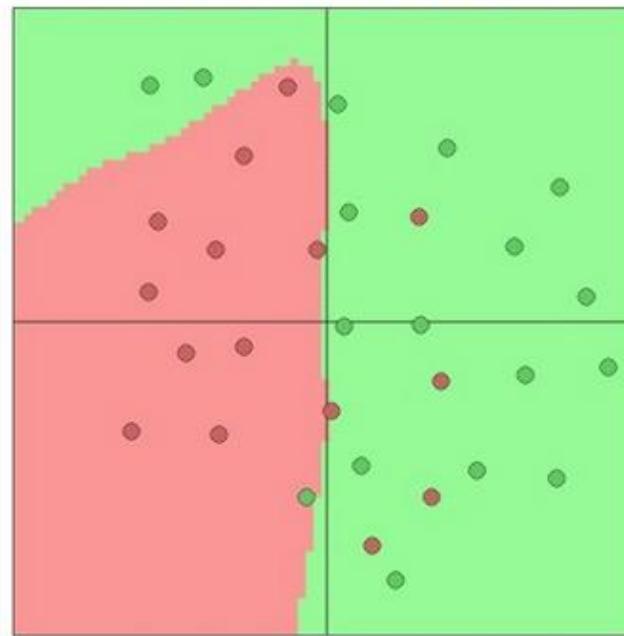
- [The Building Blocks of Deep Learning | by Tyron Jung | The Feynman Journal | Medium](#)
- [What Makes Backpropagation So Elegant? | by Tyron Jung | The Feynman Journal | Medium](#)

Manual Machine Learning vs Deep Learning

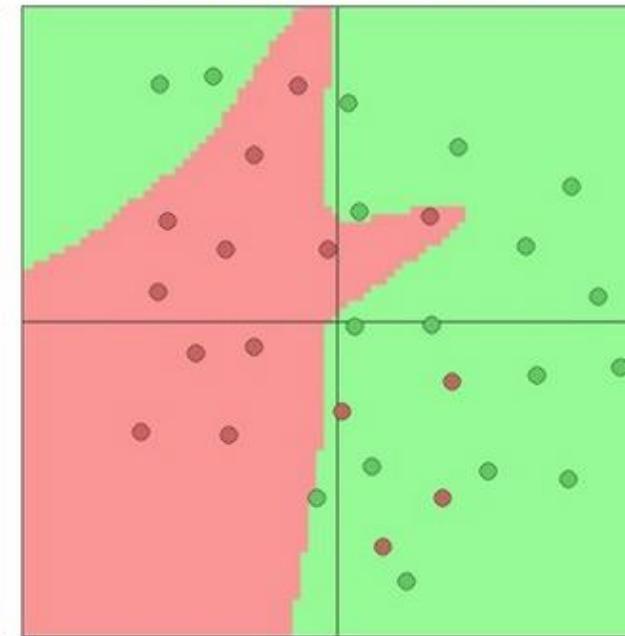


Degrees of freedom

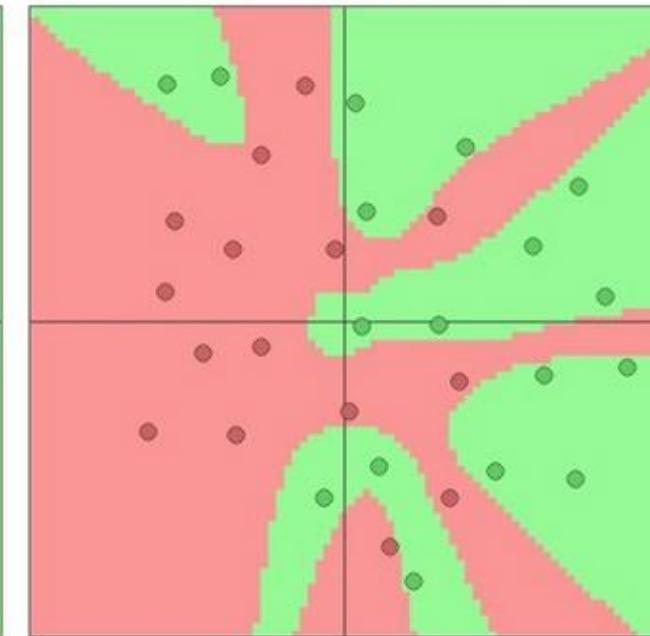
3 hidden neurons



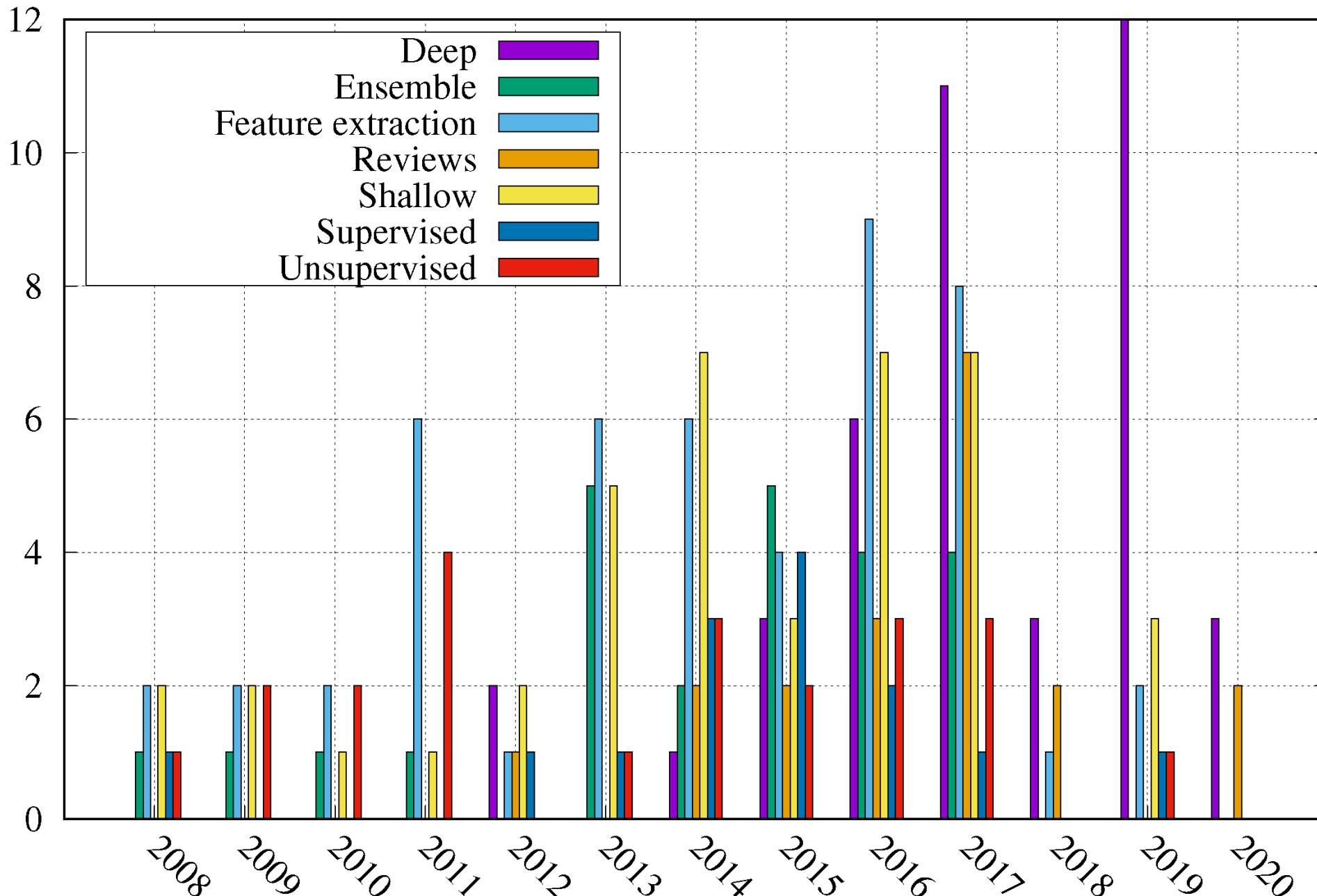
6 hidden neurons



20 hidden neurons



Articles published by year



Large-scale Medical Image Datasets

Challenges and Competitions:

- [Kaggle](#): numerous competitions
- [Grand-Challenge.org](#): numerous competitions
- MICCAI (Medical Image Computing and Computer-Assisted Intervention) conference

Collections and Directories

- NBIA/NCIA/NTIA: numerous datasets
- XNAT: numerous datasets
- ACR DS1 Dataset Directory
- [Aylward](#) open access medical image repository list

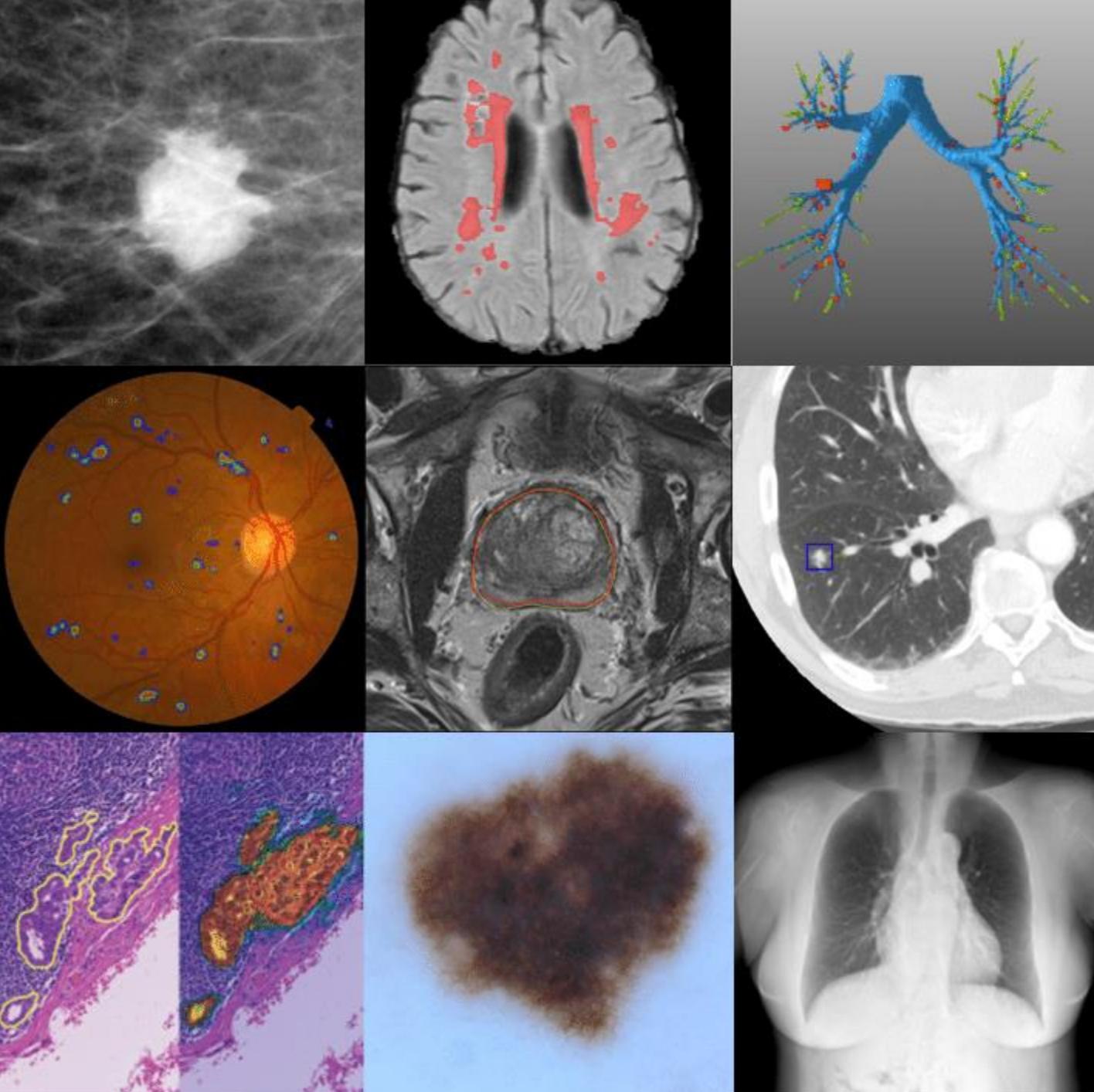
Individual Datasets

- Osteoarthritis Initiative: 431k X-ray & MR studies
- CheXpert: 224k CXR
- NIH CXR: 112k CXR
- MURA: 40k MSK X-rays
- DeepLesion: 33k bookmarked CT images
- DDSM: 2.5k mammography studies
- fastMRI: 1.5k knee MRI
- MRNet: 1.3k knee MR
- BraTs: Brain Tumor MRI

Tasks

Where DL can help

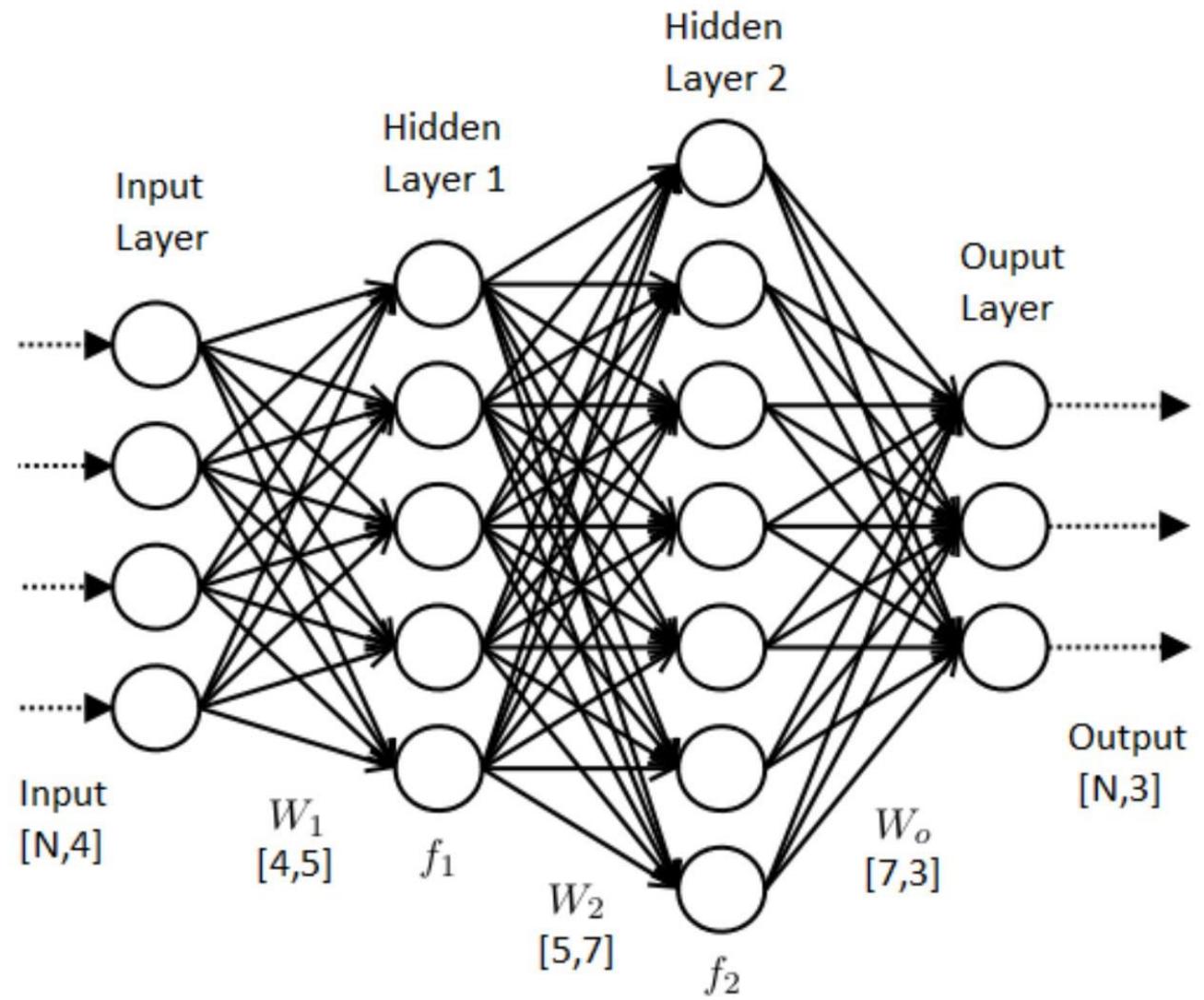
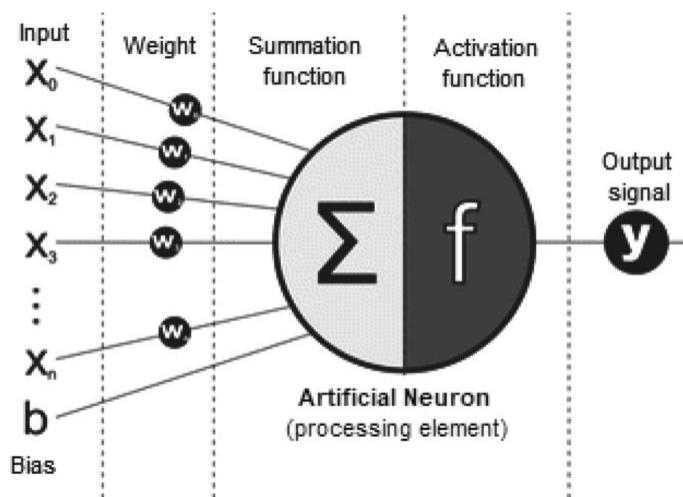
- Classification
- Detection
- Segmentation
- Visualization



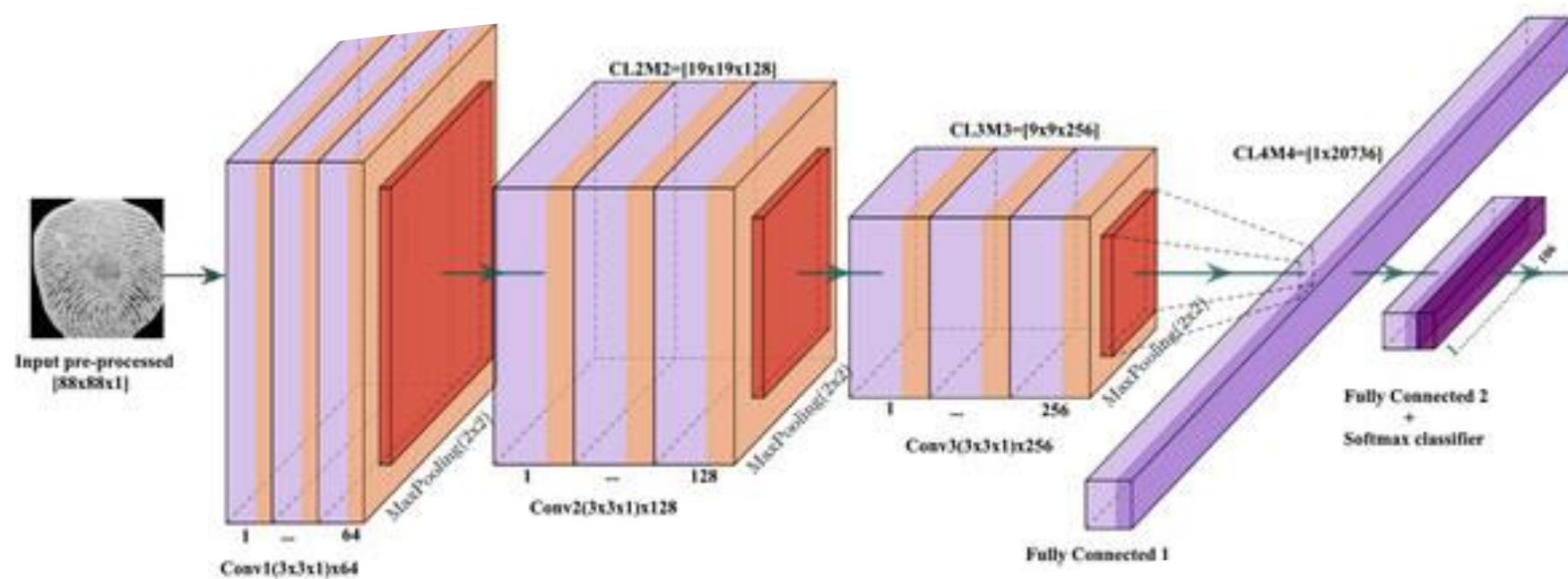
FF Neural Networks

Generic Architecture

- Vector input
- Non-linear mapping (activation) function

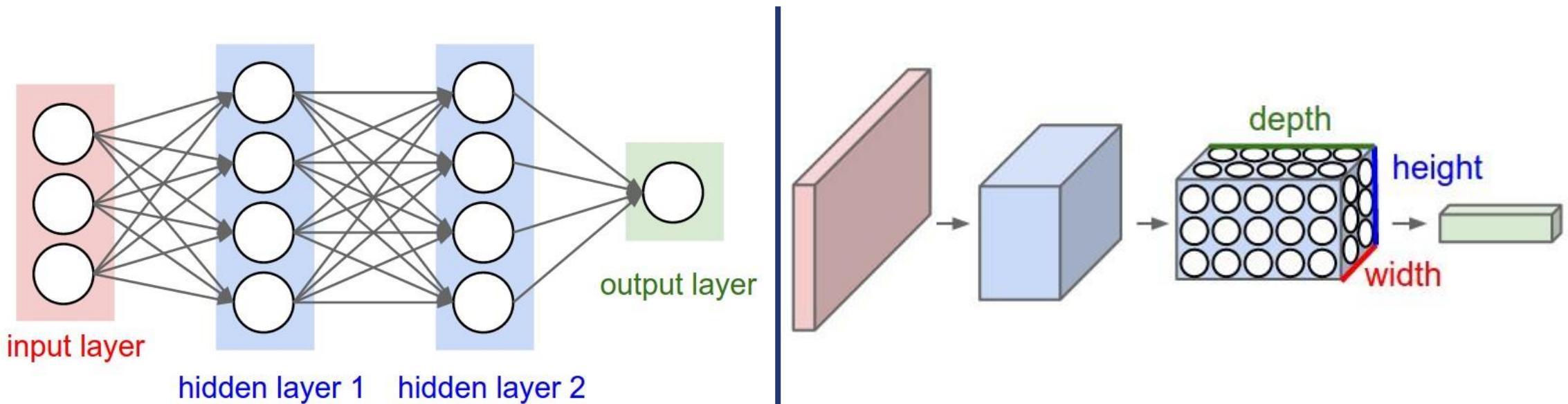


Convolutional Neural Networks (CNN)



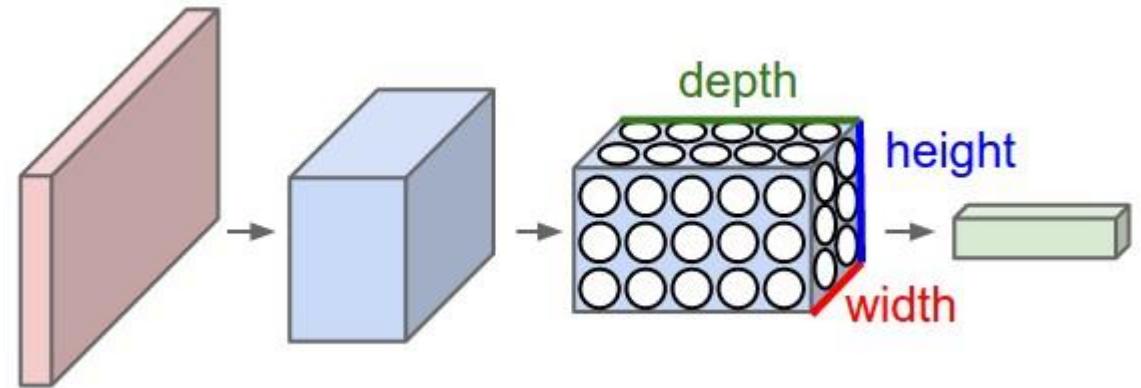
From FF to CNN

Spatial view of the input



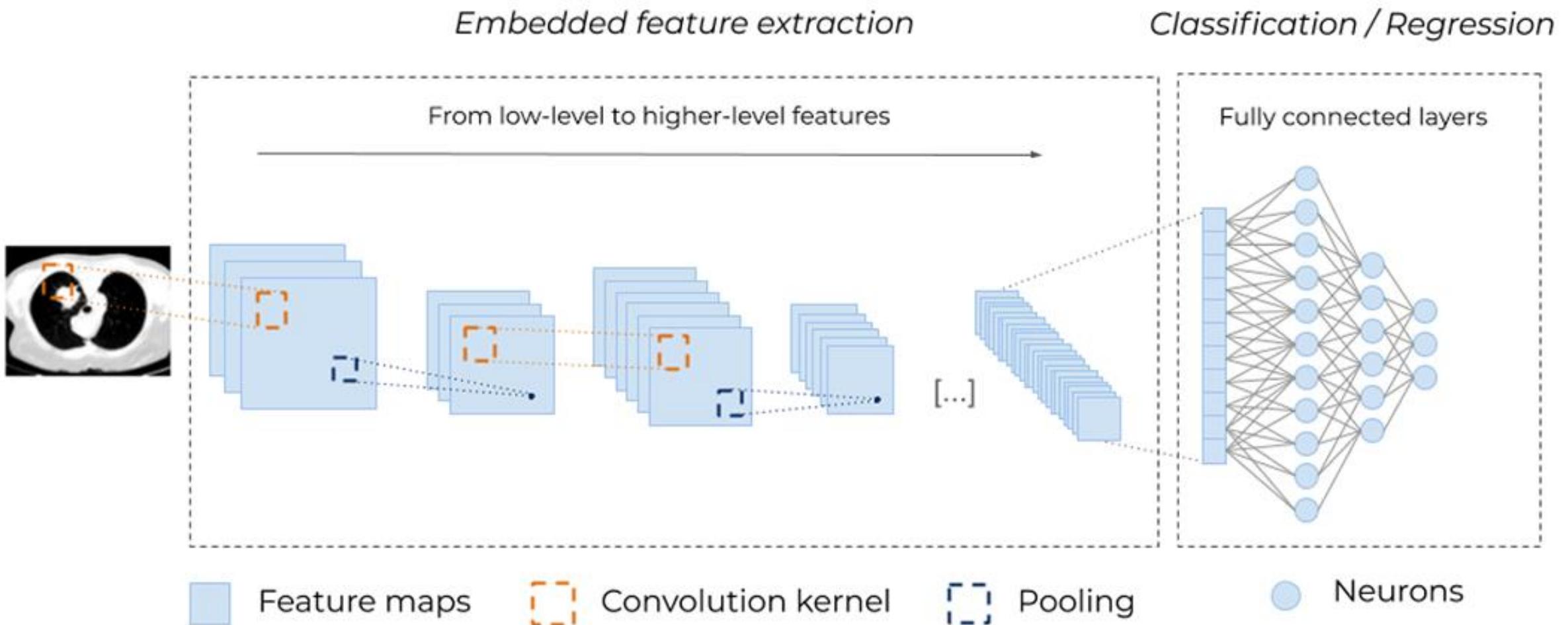
CNN

Convolutional Neural Network



- CNNs are also composed of layers, but those layers are **not** fully connected:
- CNN layers have **filters**, sets of cube-shaped weights that are applied throughout the image.
- Each 2D slice of the filters are called **kernels**.
- These filters introduce **translation invariance** and **parameter sharing**.
- How are they applied? **Convolutions!**

Convolutional Neural Network (CNN)



Key characteristics of CNNs

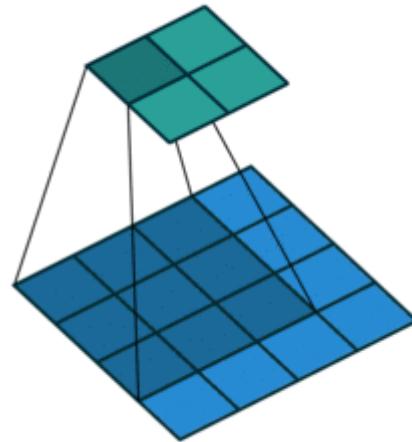
Why do they work so well on images?

- They learn a **hierarchical representation** of structures in the data
 - (i.e., more **complex** representations are expressed in terms of **simpler** representations).
- Preserve the **spatial structure** of the features extracted.

Convolutions

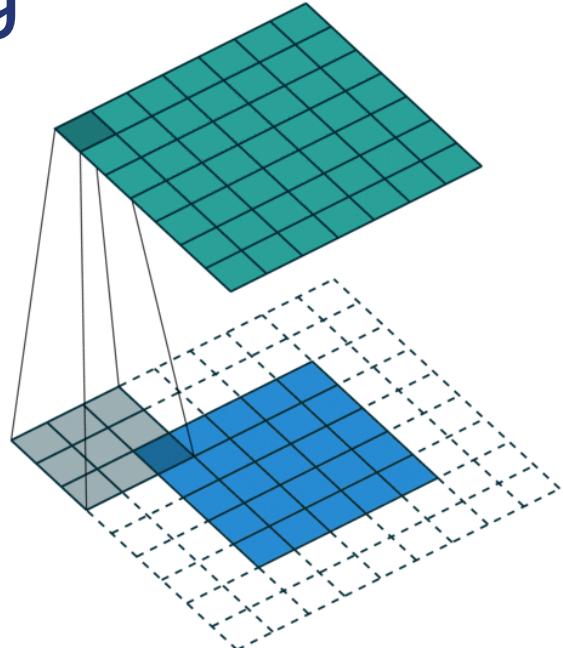
What about the edges?

- If we apply convolutions on a normal image, the result is down-sampled by an amount depending on the size of the filter:

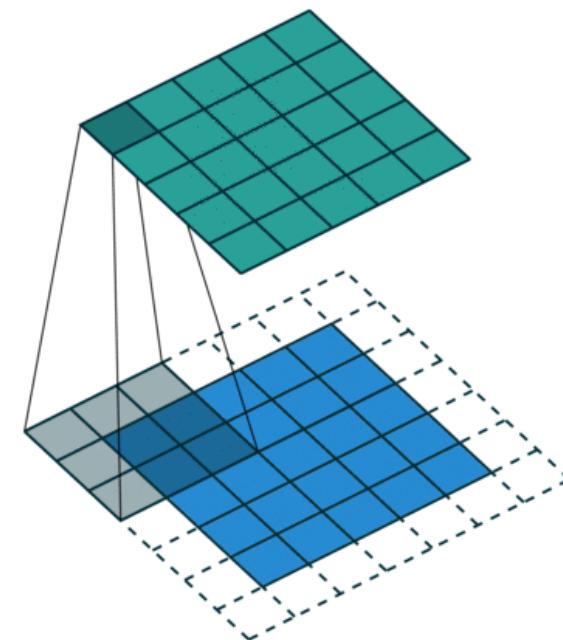


- We can avoid this by **padding** the edges in different ways.

Padding



Full padding. Adds a border of zeros such that all image pixels are visited the same number of times by the filter. Increases size of output.



Same padding. Ensures that the output has the same size as the input.

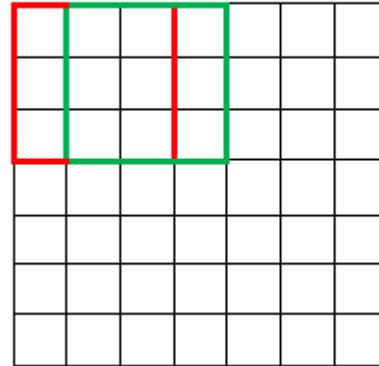
Stride

“Moving Window” Size

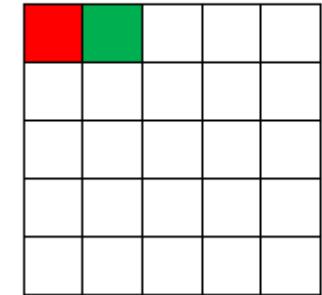
- **Stride** controls how the filter convolves around the input volume.
- Calculating the output size:
- Where n_{out} is output dim,
 n_{in} is the input dim,
 k is the filter size,
 p is padding
 s the stride

$$n_{out} = \left\lfloor \frac{n_{in} + 2p - k}{s} \right\rfloor + 1$$

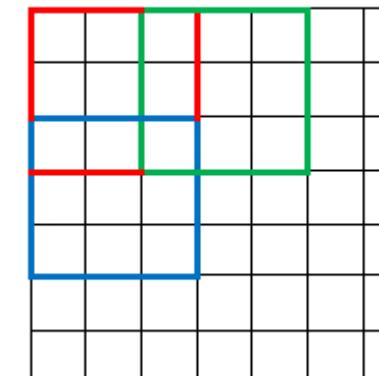
7 x 7 Input Volume



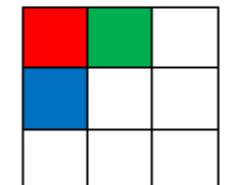
5 x 5 Output Volume



7 x 7 Input Volume

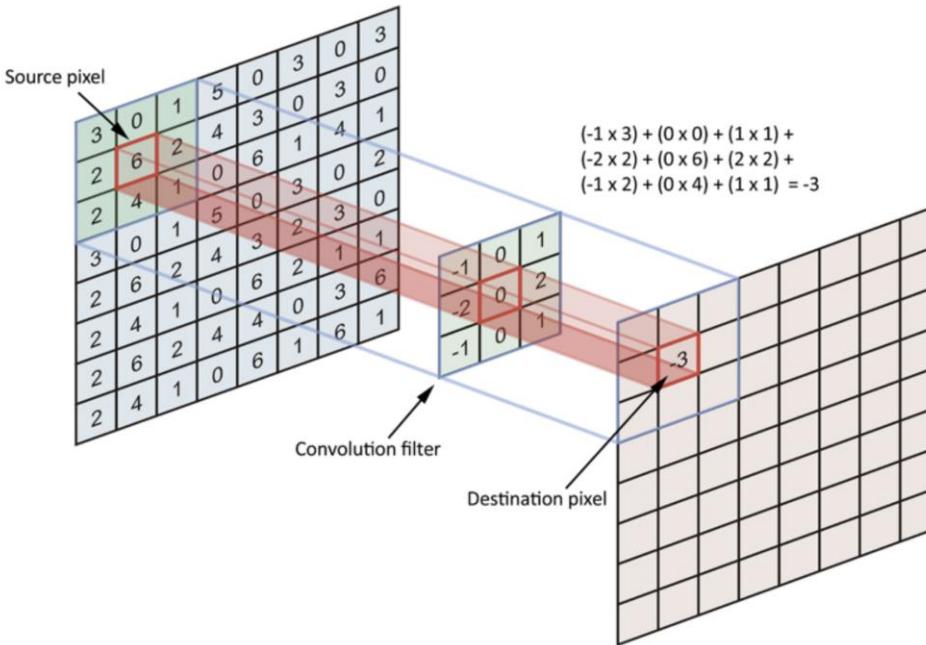


3 x 3 Output Volume



Convolutional Neural Networks

Convolution Filter

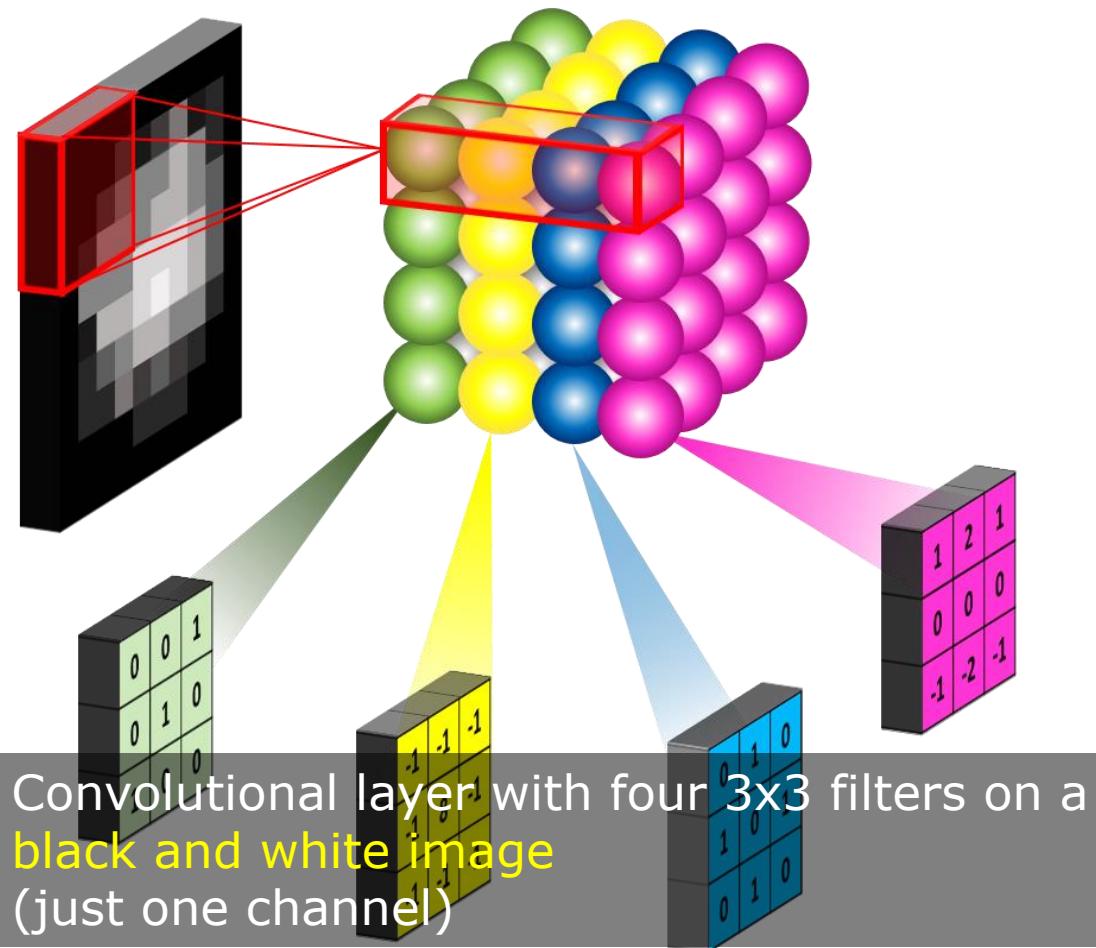


| Input Volume (+pad 1) (7x7x3) | Filter W0 (3x3x3) | Filter W1 (3x3x3) | Output Volume (3x3x2) |
|---|---|--|--|
| $x[:, :, 0]$ | $w0[:, :, 0]$ | $w1[:, :, 0]$ | $o[:, :, 0]$ |
| 0 0 0 0 0 0 0 0 1 1 2 1 2 0 0 0 2 0 0 0 0 0 1 1 1 2 2 0 0 1 2 0 0 1 0 0 0 1 0 1 1 0 0 0 0 0 0 0 0 | 1 -1 1 0 0 1 -1 0 0 0 0 -1 0 0 -1 1 0 1 0 0 0 | 0 1 1 1 0 -1 -1 1 1 1 0 1 0 1 1 -1 1 -1 0 1 0 -1 -1 1 1 0 -1 | 4 -1 -1 0 1 -2 -1 0 -1 2 -1 2 14 3 10 8 1 3 |
| $x[:, :, 1]$ | $w0[:, :, 1]$ | $w1[:, :, 1]$ | $o[:, :, 1]$ |
| 0 0 0 0 0 0 0 0 1 1 1 2 1 0 0 2 2 1 1 2 0 0 2 2 2 2 2 0 0 2 0 1 0 2 0 0 1 1 1 1 1 0 0 0 0 0 0 0 0 | 1 -1 1 -1 -1 -1 -1 0 1 0 0 0 1 1 1 0 0 0 | 1 0 1 0 1 1 -1 1 -1 0 1 0 -1 -1 1 1 0 -1 | 2 -1 2 14 3 10 8 1 3 |
| $x[:, :, 2]$ | $b0[:, :, 0]$ | $b1[:, :, 0]$ | |
| 0 0 0 0 0 0 0 0 0 1 0 0 2 0 0 1 2 0 1 2 0 0 0 2 0 0 1 0 0 2 1 2 1 1 0 0 0 2 1 0 1 0 0 0 0 0 0 0 0 | 1 | 0 | |

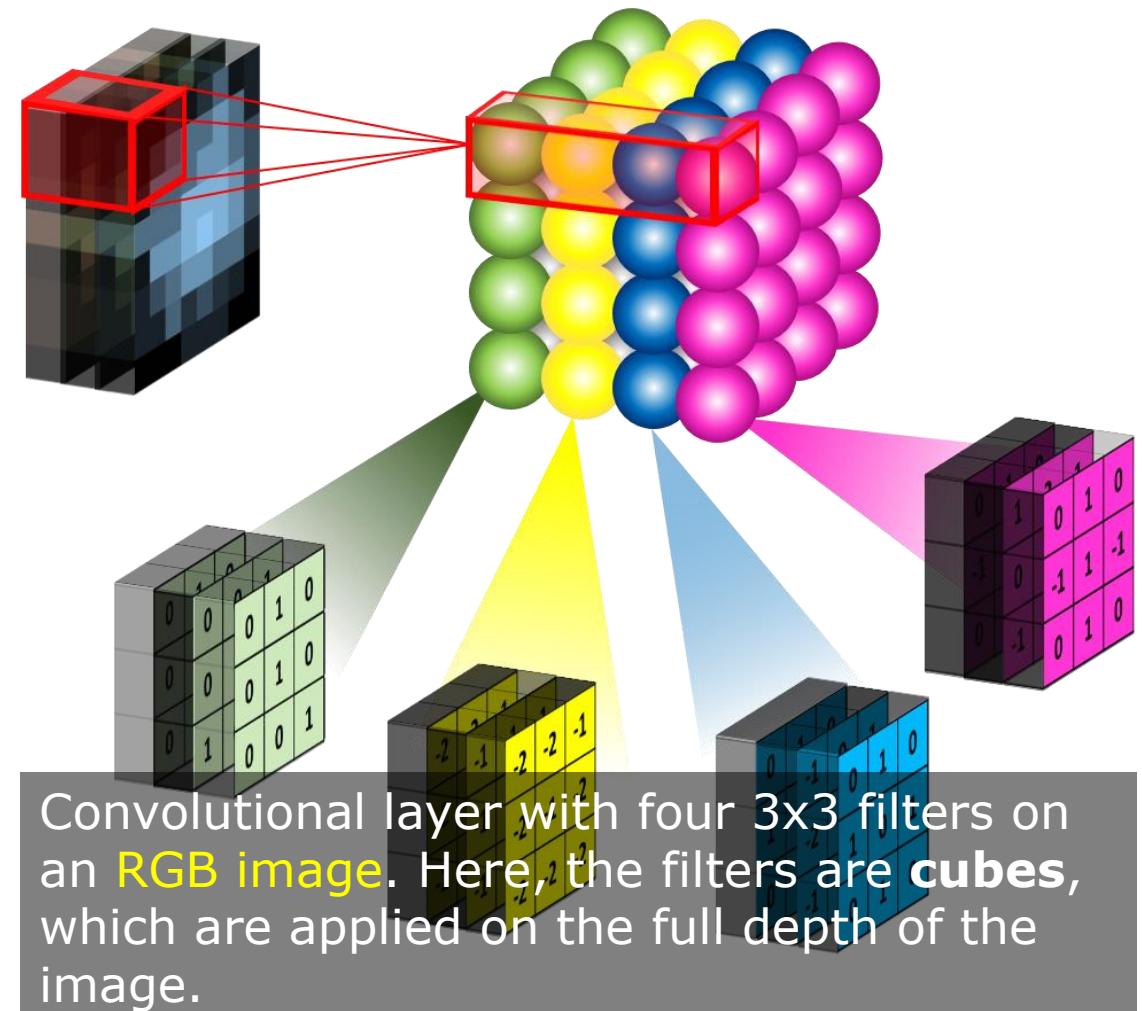
toggle movement

- Demo:
<https://cs231n.github.io/convolutional-networks/>

Convolutional Neural Network - Layers



Convolutional layer with four 3×3 filters on a black and white image (just one channel)

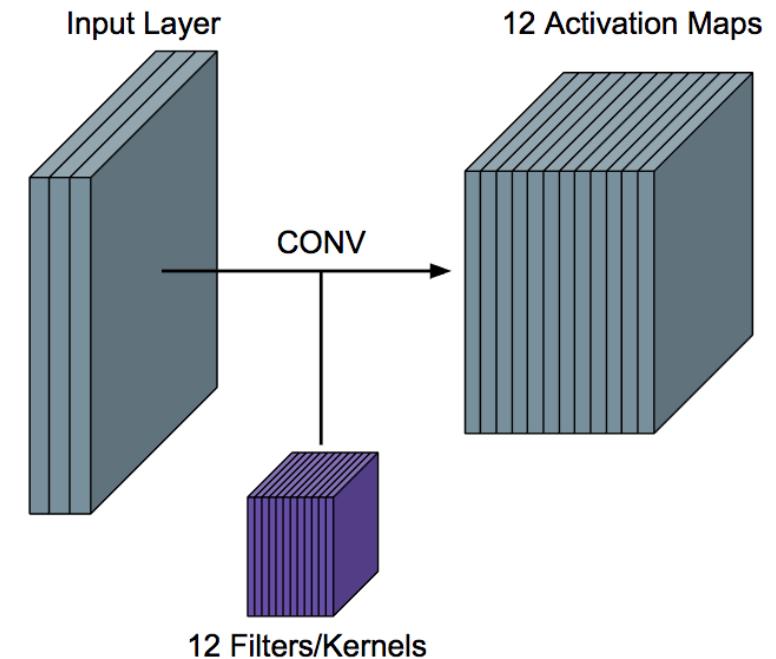


Convolutional layer with four 3×3 filters on an RGB image. Here, the filters are **cubes**, which are applied on the full depth of the image.

Convolutional Neural Network

Filter Convolution

- Filters convolve with the 3D input cube to create *2D feature maps*.
- When using multiple filters, we get a 3D output, with one *2D feature map per filter*
- The feature map dimension can vary significantly between convolutional Layers:
 - E.g., a layer input can be $32 \times 32 \times 16$ and its output $32 \times 32 \times 128$, if that layer has 128 filters.

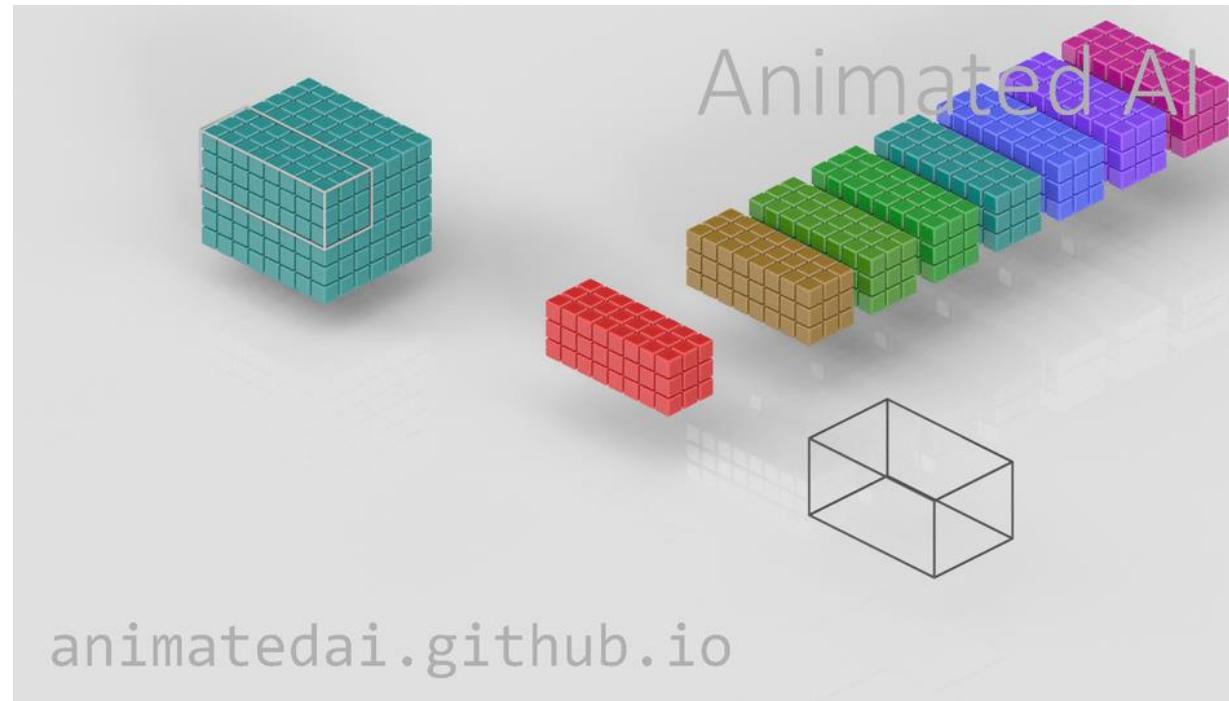




Input

Basic Convolution

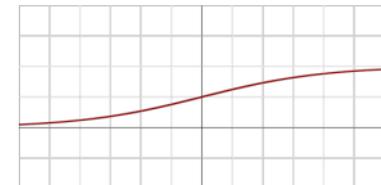
Fundamental Algorithm of Convolution in Neural Networks (youtube.com)



Activation Functions

Desired properties

- Cheap to compute
- Non-linear
- Differentiable
- Monotonic
- Bounded output



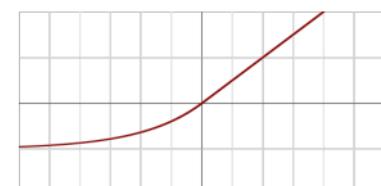
Logistic/Sigmoid

$$f(x) = \frac{1}{1 + e^{-x}}$$



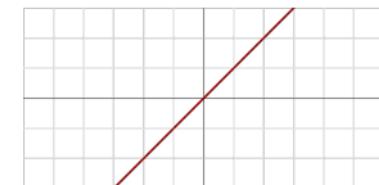
ReLU

$$f(x) = \begin{cases} x & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$



ELU

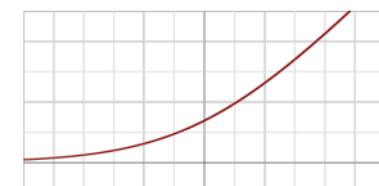
$$f(x) = \begin{cases} x & \text{if } x \geq 0 \\ \alpha(e^x - 1) & \text{if } x < 0 \end{cases}$$



Linear

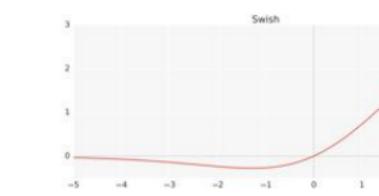
$$f(x) = x$$

Softmax $f(x) = \frac{1}{Z} e^x$



Softplus

$$f(x) = \ln(1 + e^x)$$



Swish

$$f(x) = \frac{x}{1 + e^{-x}}$$

Activation Functions

Rectified Non-Linear unit (ReLU)



ReLU

$$f(x) = \begin{cases} x & \text{if } x \geq 0 \\ 0 & \text{if } x < 0 \end{cases}$$

- Solves the vanishing gradient problem that occurs with *sigmoid*
- Easy to compute:
$$\text{Output} = \max(0, \text{input})$$
- Generates sparsity (not always beneficial)

Convolutional Layers - Recap

- A convolutional layer convolves each of its filters with the input.
- Input -
 - a **3D tensor**: Width \times Height \times Channels (or Feature Maps)
- Output -
 - a **3D tensor**: Width \times Height \times Feature Maps (one for each filter)
- Applies non-linear activation function (usually ReLU) over each value of the output.
- Multiple (hyper)parameters to be defined:
 - # of filters
 - Filters size
 - Stride
 - Padding
 - Activation function
 - Regularization.

Pooling

- Invariant to small, “local transitions”
- Reduces input size to final fully connected layers
- No learnable parameters

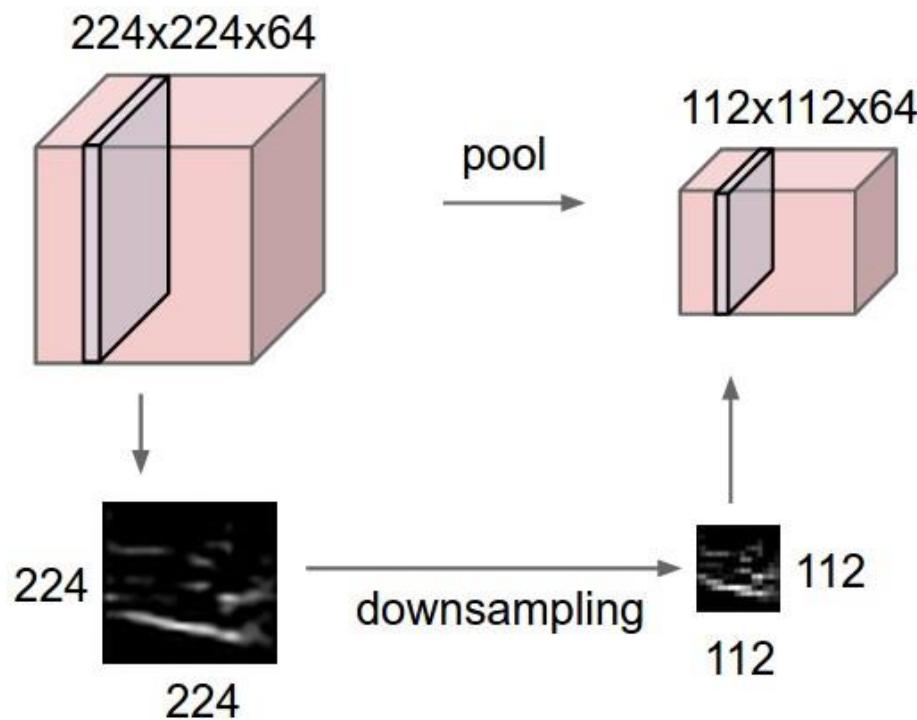
| | | | |
|---|---|---|---|
| 1 | 1 | 2 | 5 |
| 5 | 7 | 7 | 8 |
| 3 | 1 | 1 | 0 |
| 1 | 2 | 3 | 4 |

max pool with 2x2 window
and stride 1

| | | |
|---|---|---|
| 7 | 7 | 8 |
| | | |
| | | |

Pooling Layer

Max or Average → down sample layers



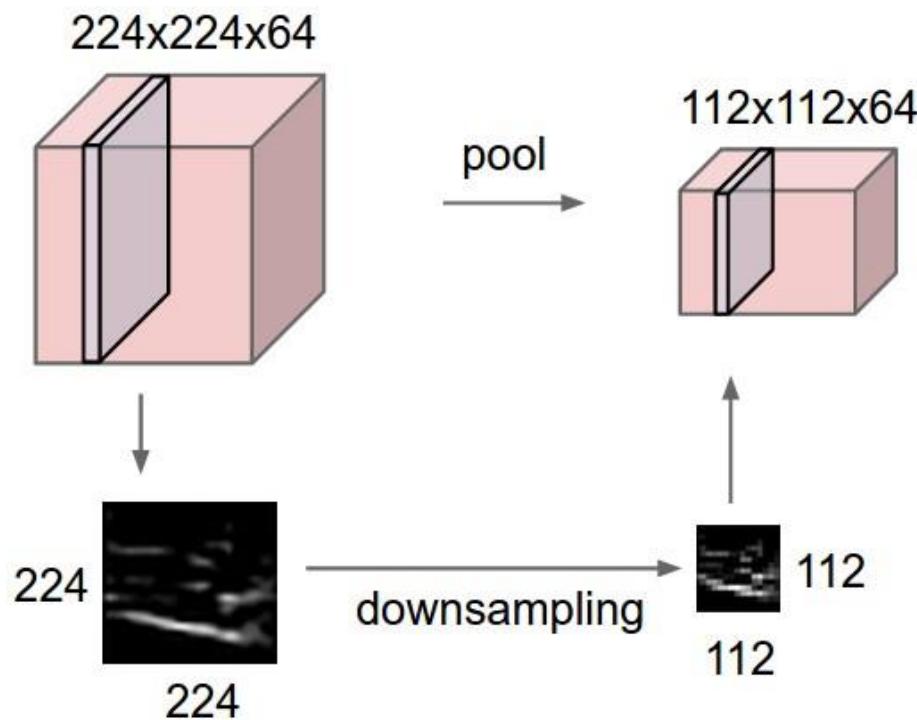
| | | | |
|---|---|---|---|
| 1 | 1 | 2 | 5 |
| 5 | 7 | 7 | 8 |
| 3 | 1 | 1 | 0 |
| 1 | 2 | 3 | 4 |

max pool with 2x2
window and stride 2

| | |
|---|---|
| 7 | 8 |
| 3 | 4 |

Pooling Layer

Max or Average → down sample layers

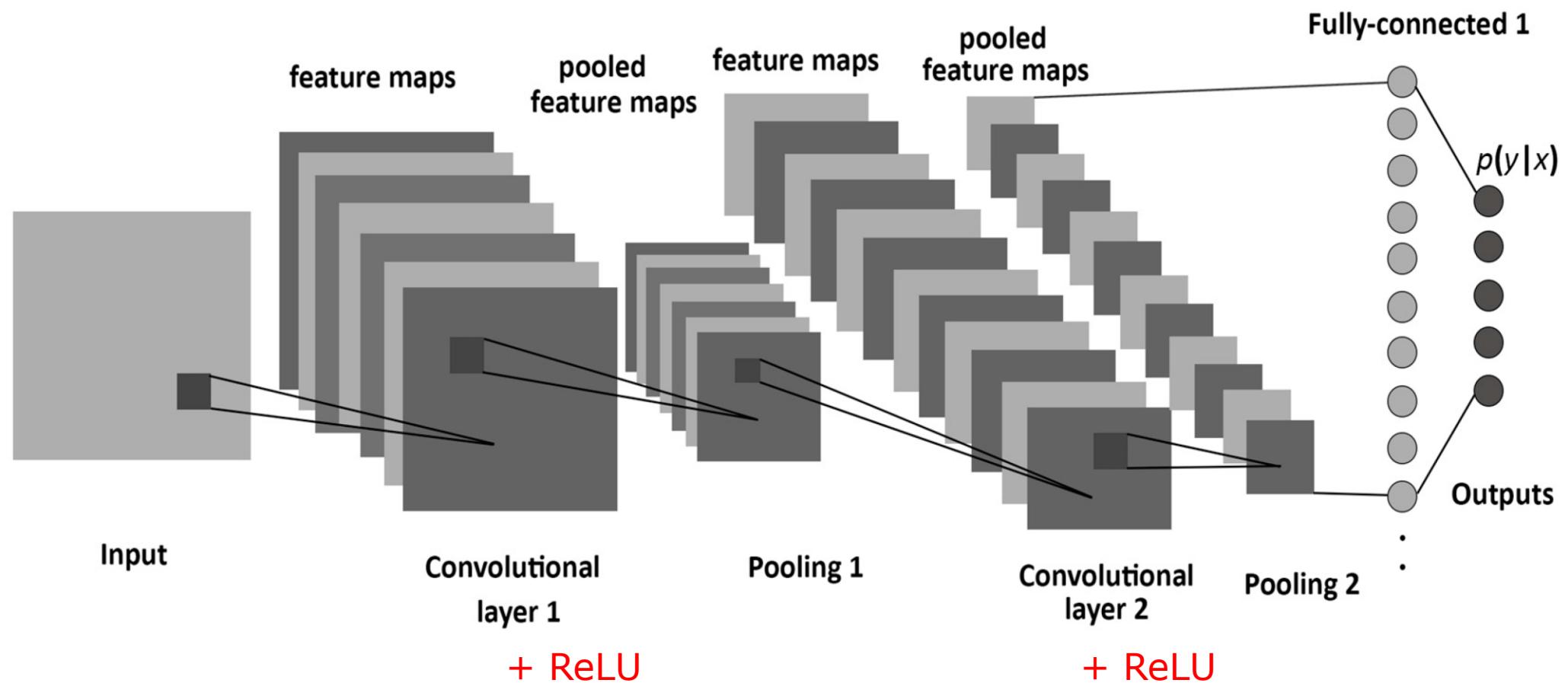


| | | | |
|---|---|---|---|
| 1 | 1 | 2 | 5 |
| 5 | 7 | 7 | 8 |
| 3 | 1 | 1 | 0 |
| 1 | 2 | 3 | 4 |

mean pool with 2x2
window and stride 2

| | |
|---|---|
| 4 | 6 |
| 2 | 2 |

A Convolutional Network



CNN Building Blocks

CNN is built by stacking layers, typically of 3 types

Convolutional
Layers

Pooling
Layers

Fully
Connected
Layers

Convolutional Layers

Action

- Apply filters to extract features
- Filters are composed of small kernels, learned.
- One bias per filter.
- Apply activation function on every value of feature map

Parameters

- Number of kernels
- Size of kernels (W and H only, D is defined by input cube)
- Activation function
- Stride
- Padding
- Regularization type and value

I/O

- Input:
3D cube -
previous set of feature maps
- Output:
3D cube -
one 2D map per filter

CNN Building Blocks

CNN is built by stacking layers, typically of 3 types

Convolutional
Layers

Pooling
Layers

Fully
Connected
Layers

Pooling Layers

Action

- Reduce dimensionality
- Extract maximum of average of a region
- Sliding window approach

Parameters

- Stride
- Size of window

I/O

- Input:
3D cube, previous set of feature maps
- Output:
3D cube,
one 2D map per filter,
reduced spatial dimensions

CNN Building Blocks

CNN is built by stacking layers, typically of 3 types

Convolutional
Layers

Pooling
Layers

Fully
Connected
Layers

Fully Connected Layers

Action

- Aggregate information from final feature maps
- Generate final classification

Parameters

- Number of nodes
- Activation function: changes depending on role of layer.
 - If aggregating info, use ReLU.
 - If producing final classification, use Softmax.

I/O

- Input: FLATTENED 3D cube, previous set of feature maps
- Output: 3D cube, one 2D map per filter

CNN Building Blocks

CNN is built by stacking layers, typically of 3 types

Convolutional
Layers

Pooling
Layers

Fully
Connected
Layers

Live example: <http://cs231n.stanford.edu/>



What Do CNN Layers Learn?

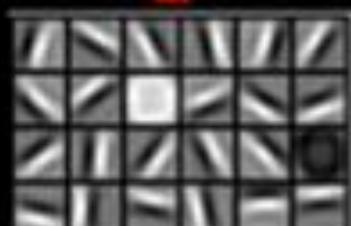
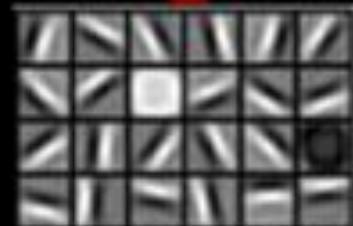
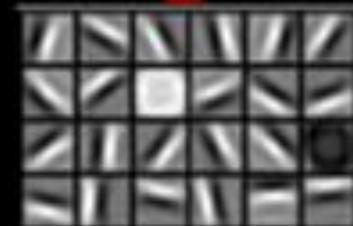
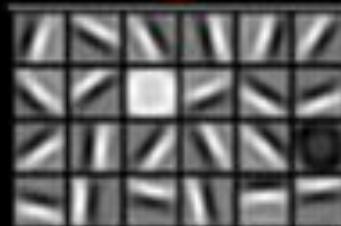
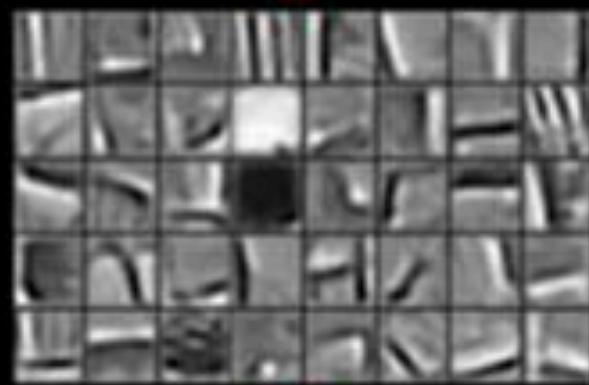
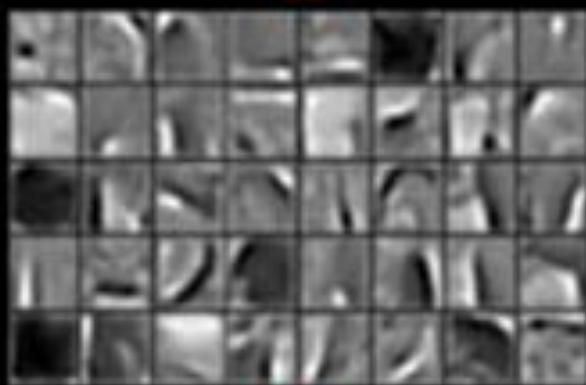
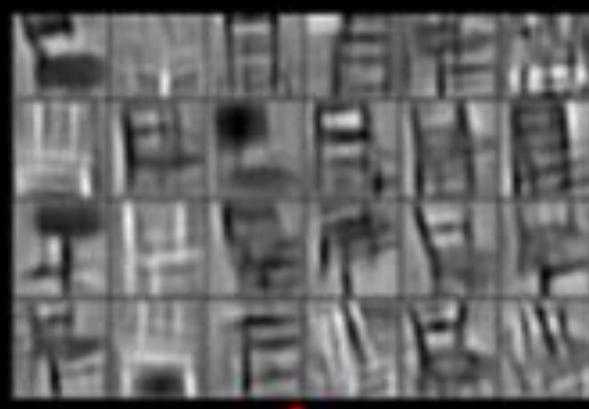
- Each CNN layer learns filters of increasing complexity.
- The first layers learn **basic feature detection filters**:
 - edges, corners, etc.
- The middle layers learn filters that detect complex textures and **parts of objects**.
 - E.g., for faces, they might learn to respond to eyes, noses, etc.
- The last layers have higher representations:
 - they learn to **recognize full objects**, in different shapes and positions.

Faces

Cars

Elephants

Chairs



Simple CNN in PyTorch

Training a Classifier — PyTorch Tutorials

```
import torch.nn as nn
import torch.nn.functional as F

class Net(nn.Module):
    def __init__(self):
        super().__init__()
        self.conv1 = nn.Conv2d(3, 6, 5)
        self.pool = nn.MaxPool2d(2, 2)
        self.conv2 = nn.Conv2d(6, 16, 5)
        self.fc1 = nn.Linear(16 * 5 * 5, 120)
        self.fc2 = nn.Linear(120, 84)
        self.fc3 = nn.Linear(84, 10)

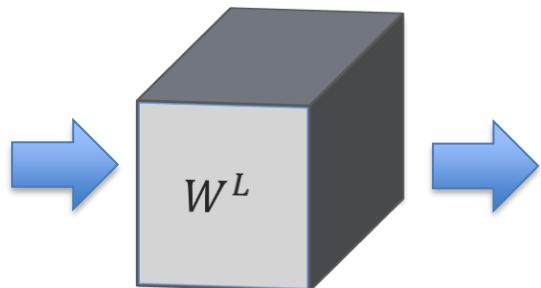
    def forward(self, x):
        x = self.pool(F.relu(self.conv1(x)))
        x = self.pool(F.relu(self.conv2(x)))
        x = torch.flatten(x, 1) # flatten all dimensions except batch
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x

net = Net()
```

Backward propagation of Maximum Pooling Layer

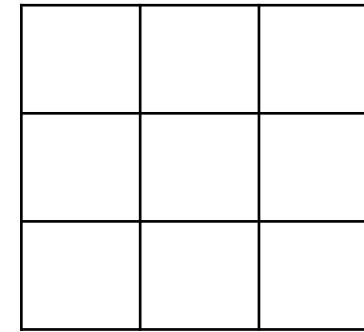
Forward mode, 3x3 stride 1

rest of the network



Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |

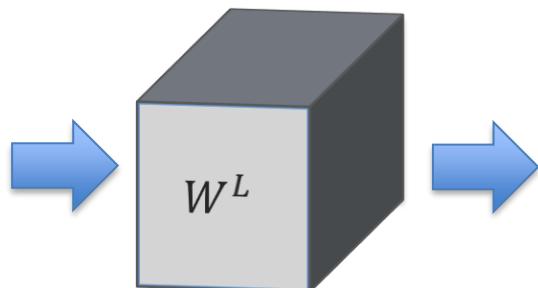


rest of the network

Backward propagation of Maximum Pooling Layer

Forward mode, 3x3 stride 1

rest of the network



Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | |
|---|--|--|
| 9 | | |
| | | |
| | | |

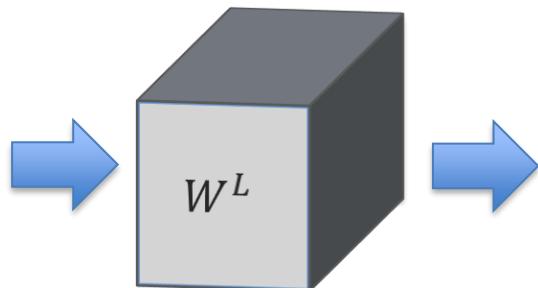


rest of the network

Backward propagation of Maximum Pooling Layer

Forward mode, 3x3 stride 1

rest of the network



Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | |
|---|---|--|
| 9 | 8 | |
| | | |
| | | |

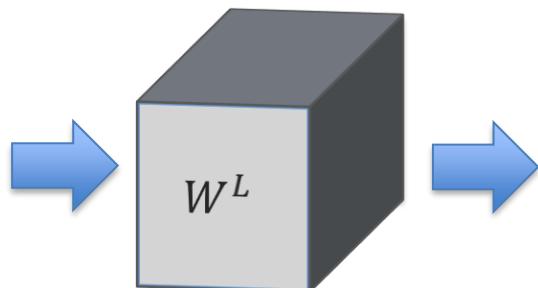


rest of the network

Backward propagation of Maximum Pooling Layer

Forward mode, 3x3 stride 1

rest of the network



Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | |
|---|---|---|
| 9 | 8 | 8 |
| | | |
| | | |

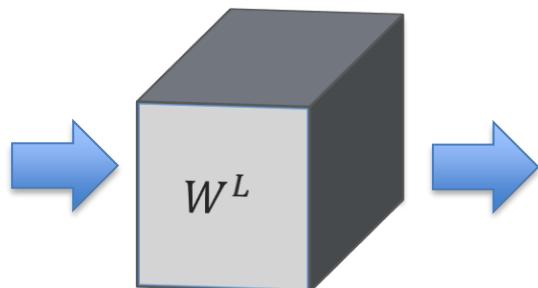


rest of the network

Backward propagation of Maximum Pooling Layer

Forward mode, 3x3 stride 1

rest of the network



Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | |
|---|---|---|
| 9 | 8 | 8 |
| 9 | 6 | 6 |
| 7 | 7 | 7 |



rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

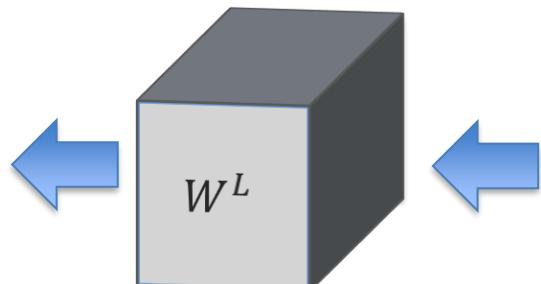
Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network

Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | |
|---|---|---|
| 1 | 3 | 1 |
| 9 | 8 | 8 |
| 1 | 4 | 2 |



rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

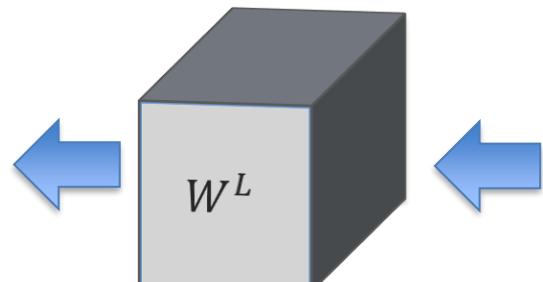
Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network

Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |



rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

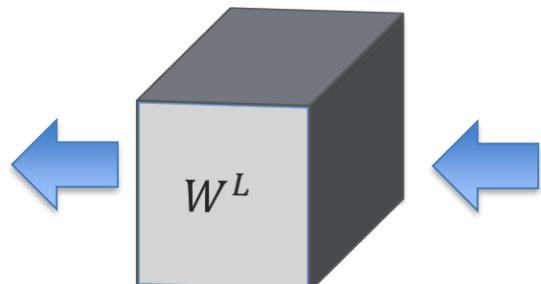
Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network

Activation of layer L

| | | | | |
|---|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |

rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

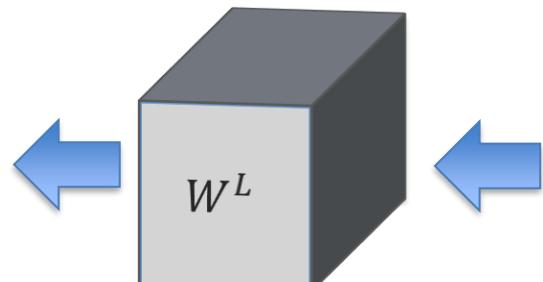
Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network

Activation of layer L

| | | | | |
|----|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| +1 | 9 | 3 | 4 | 2 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | | | |
|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 |
| 1 | 9 | 4 | 6 | 2 |
| 6 | 7 | 2 | 7 | 1 |



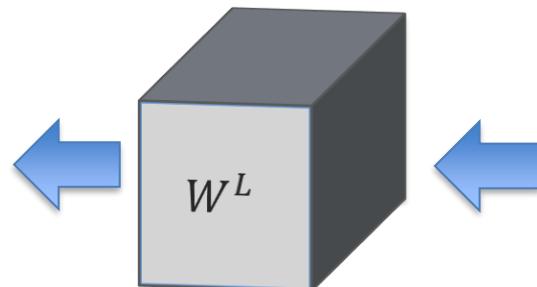
rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network



Activation of layer L

| | | | | |
|----|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| +1 | 9 | 3 | 4 | 2 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |



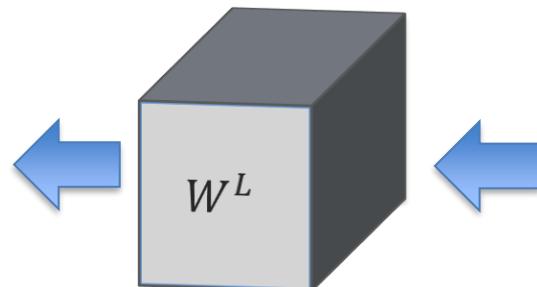
rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network



Activation of layer L

| | | | | |
|----|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| +1 | 9 | 3 | 4 | 2 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |

| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |

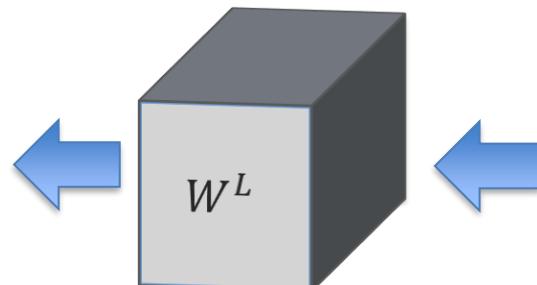
rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network



Activation of layer L

| | | | | | |
|----|---|----|---|---|---|
| 2 | 4 | +3 | 8 | 3 | 6 |
| +1 | 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 | |
| 2 | 3 | 1 | 3 | 4 | |
| 2 | 7 | 4 | 5 | 7 | |



| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |



rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

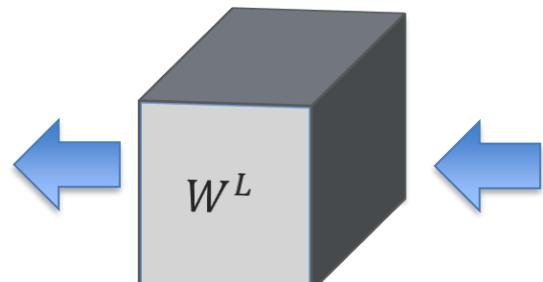
Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network

Activation of layer L

| | | | | | |
|----|---|----|---|---|---|
| 2 | 4 | +3 | 8 | 3 | 6 |
| +1 | 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 | |
| 2 | 3 | 1 | 3 | 4 | |
| 2 | 7 | 4 | 5 | 7 | |



| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |



rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

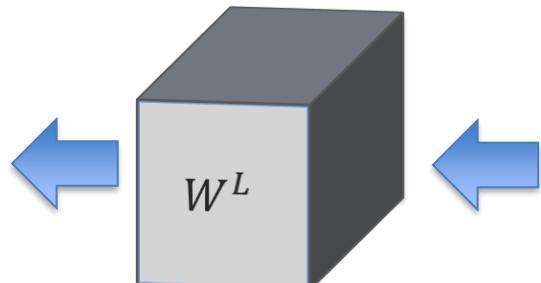
Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network

Activation of layer L

| | | | | |
|----|---|---|---|---|
| 2 | 4 | 8 | 3 | 6 |
| +1 | 9 | 3 | 4 | 2 |
| 5 | 4 | 6 | 3 | 1 |
| 2 | 3 | 1 | 3 | 4 |
| 2 | 7 | 4 | 5 | 7 |



| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |



rest of the network

Blue: the current layer's derivatives (max-pool)
Red: the corresponding value of the previous layer.

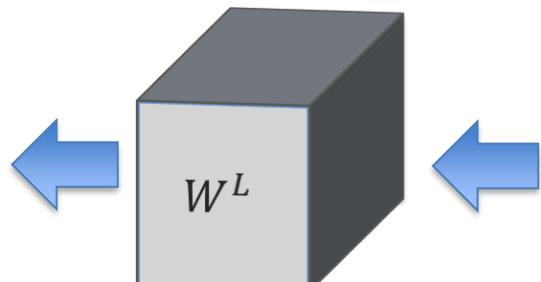
Backward propagation of Maximum Pooling Layer

Backward mode.

rest of the network

Activation of layer L

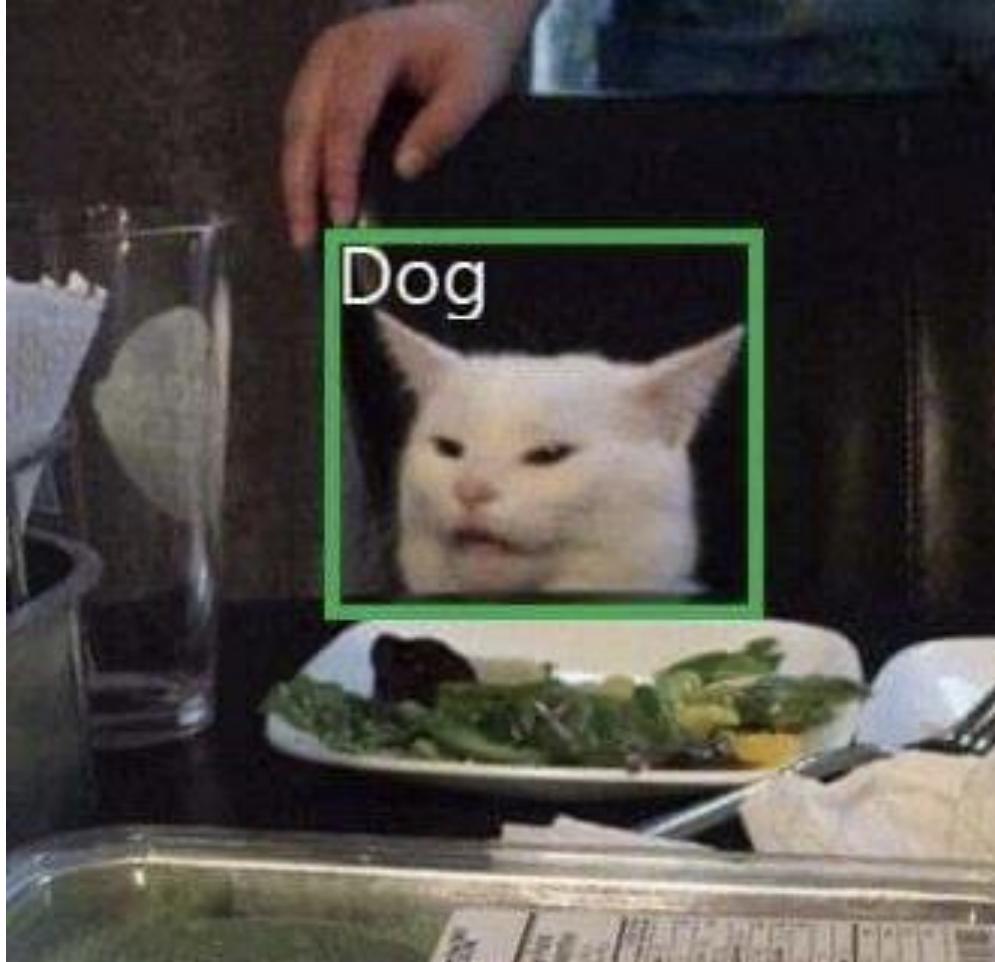
| | | | | | |
|----|---|----|---|---|---|
| 2 | 4 | +4 | 8 | 3 | 6 |
| +1 | 9 | 3 | 4 | 2 | 5 |
| 5 | 4 | 6 | 3 | 1 | |
| 2 | 3 | 1 | 3 | 4 | |
| 2 | 7 | 4 | 5 | 7 | |



| | | | | | |
|---|---|---|---|---|---|
| 1 | 9 | 3 | 8 | 1 | 8 |
| 1 | 9 | 4 | 6 | 2 | 6 |
| 6 | 7 | 2 | 7 | 1 | 7 |



rest of the network

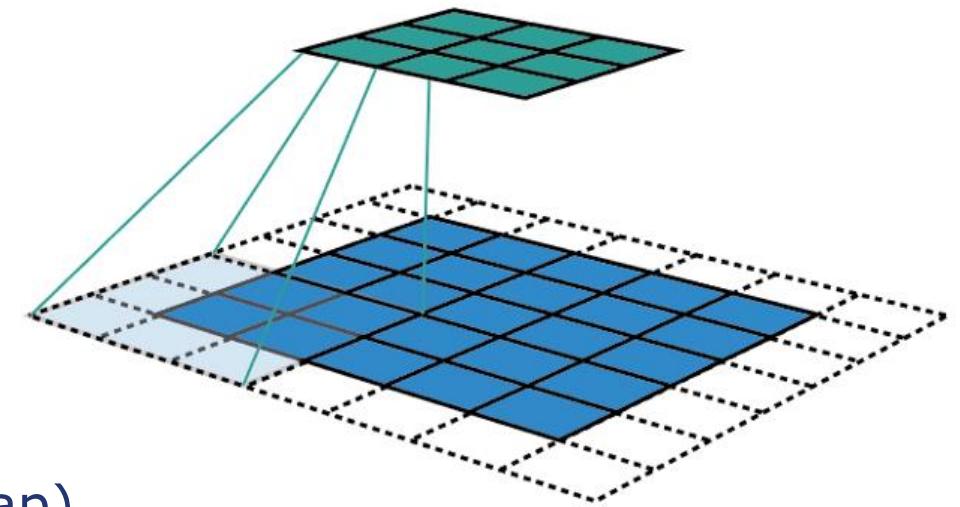


Layer's Receptive Field

- The **receptive field** is the region in the input space that a particular CNN's feature is looking at (i.e. is affected by).
- Apply a convolution C with **kernel size $k = 3 \times 3$,** **padding size $p = 1 \times 1$,** **stride $s = 2 \times 2$** on an input map **5×5** , we will get an output feature map **3×3** (green map).

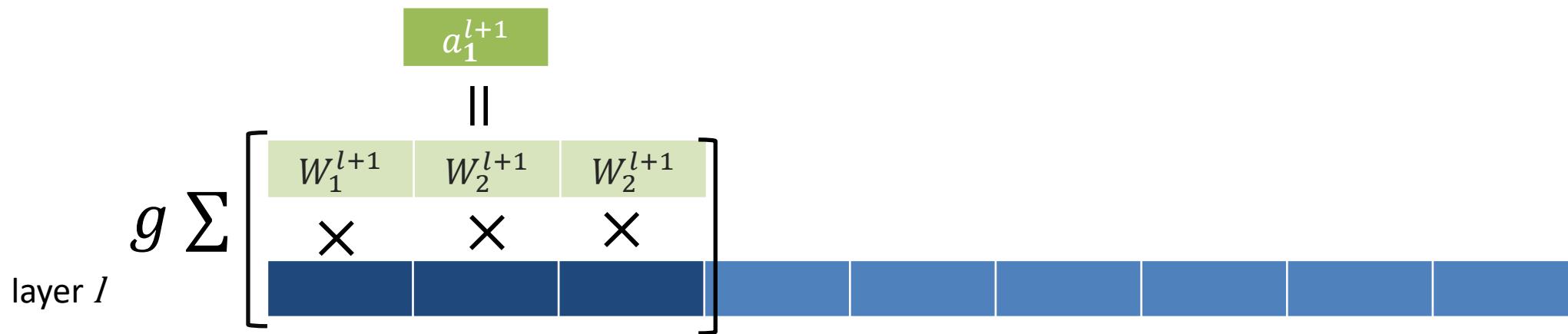
$$n_{out} = \left\lceil \frac{n_{in} + 2p - k}{s} \right\rceil + 1$$

n_{in} : # of input features
 n_{out} : # of output features
 k : convolution **kernel** size
 p : convolution **padding** size
 s : convolution **stride** size



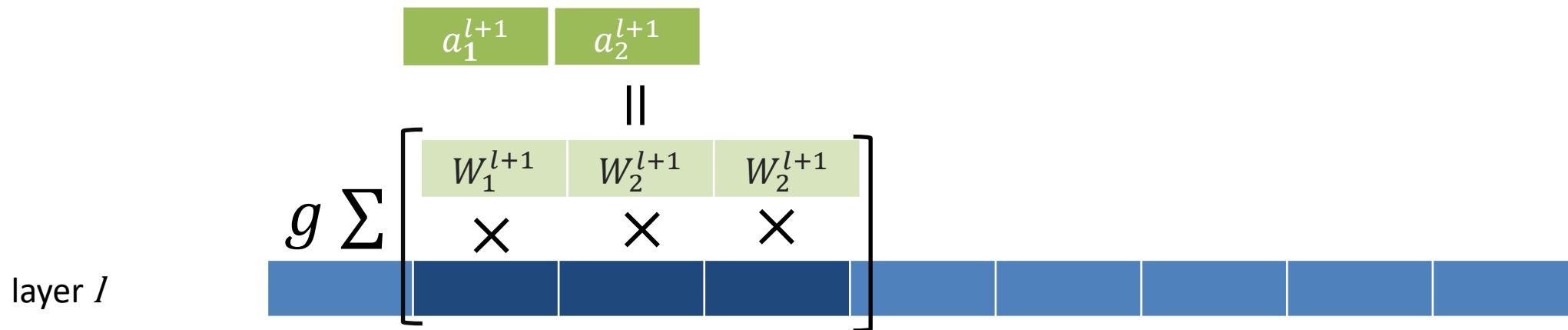
Layer's Receptive Field

Receptive field in 1D: no padding, stride 1 and kernel 3x1



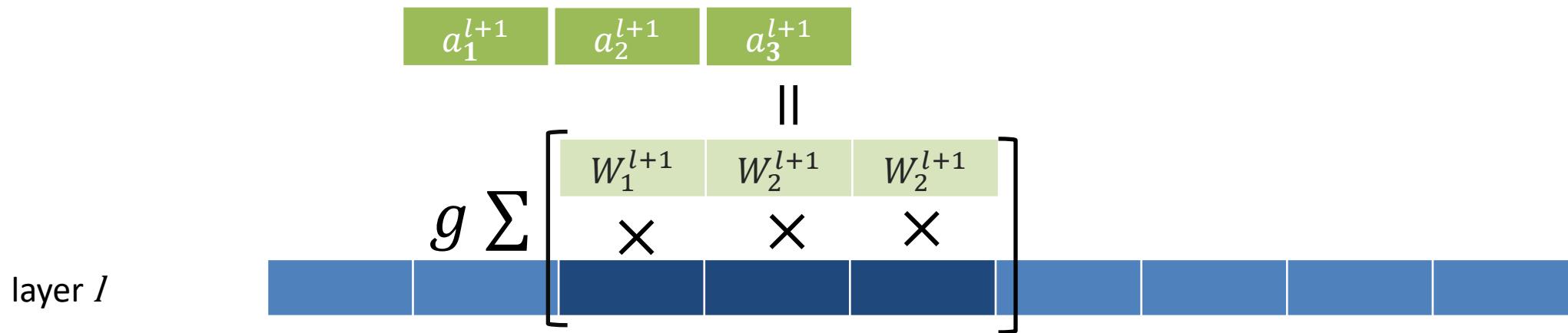
Layer's Receptive Field

Receptive field in 1D: no padding, stride 1 and kernel 3x1



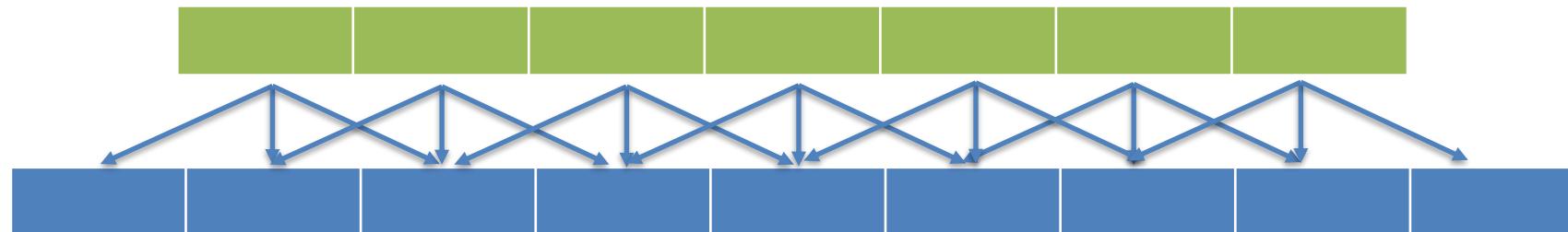
Layer's Receptive Field

Receptive field in 1D: no padding, stride 1 and kernel 3x1



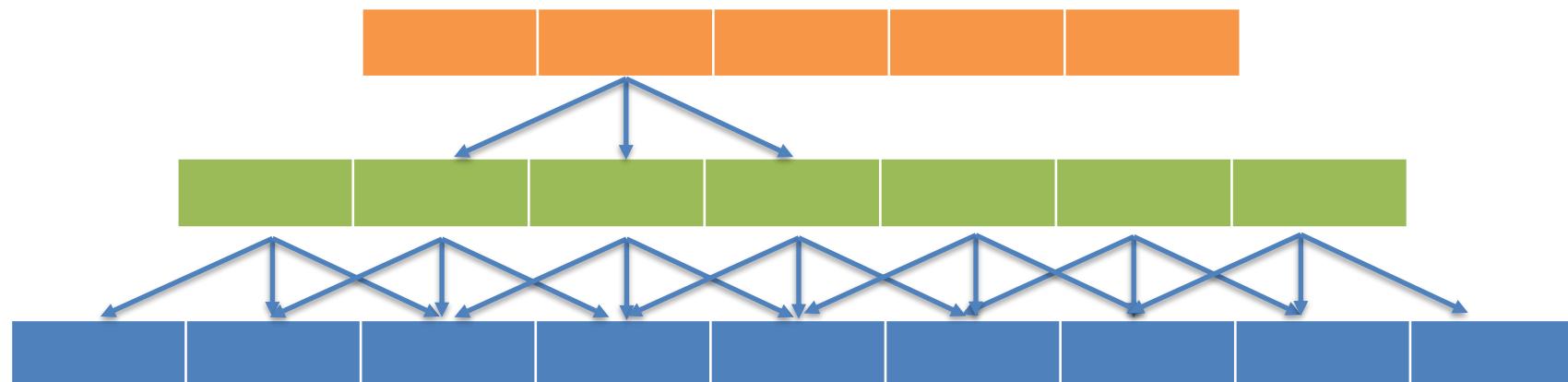
Layer's Receptive Field

Receptive field in 1D: no padding, stride 1 and kernel 3x1



Layer's Receptive Field

Receptive field in 1D: no padding, stride 1 and kernel 3x1



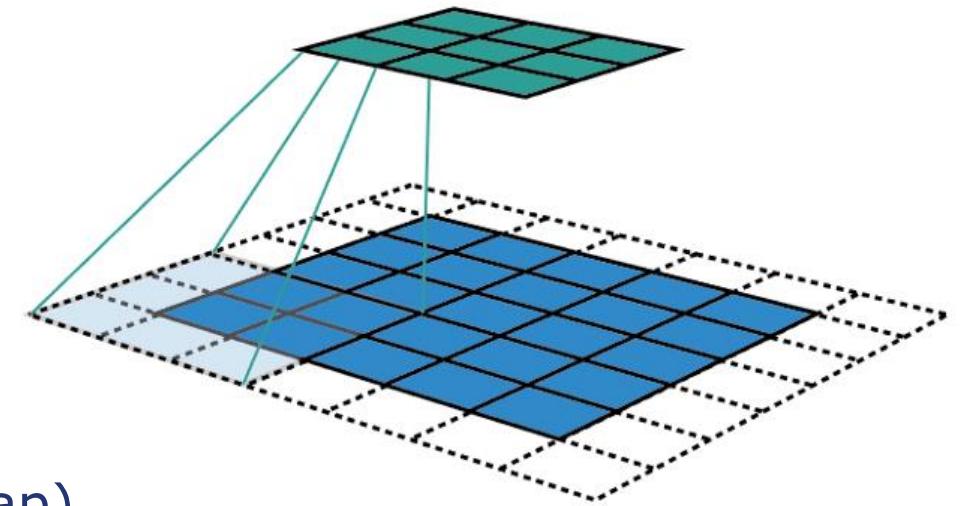
Layer's Receptive Field

Receptive field in 1D: no padding, stride 1 and kernel 3x1



Layer's Receptive Field

- The **receptive field** is the region in the input space that a particular CNN's feature is looking at (i.e. is affected by).
- Apply a convolution C with **kernel size $k = 3 \times 3$,** **padding size $p = 1 \times 1$,** **stride $s = 2 \times 2$** on an input map **5×5** , we will get an output feature map **3×3** (green map).



$$n_{out} = \left\lceil \frac{n_{in} + 2p - k}{s} \right\rceil + 1$$

n_{in} : # of input features

n_{out} : # of output features

k : convolution **kernel** size

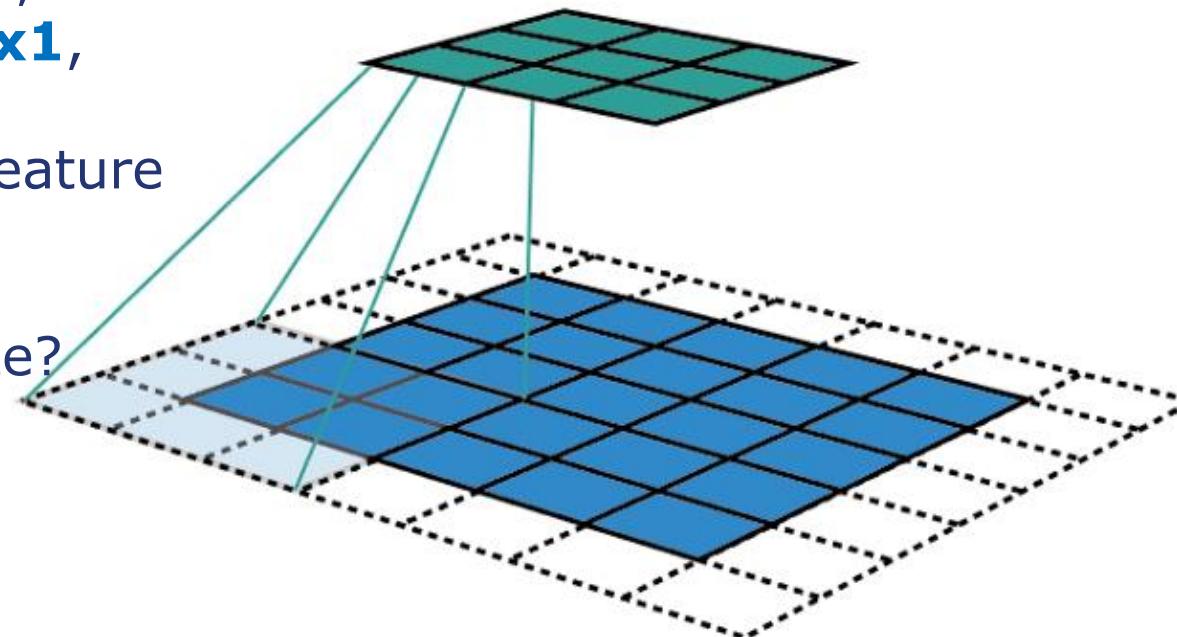
p : convolution **padding** size

s : convolution **stride** size

Layer's Receptive Field

We apply the convolution C with
kernel size $k = 3 \times 3$,
padding size $p = 1 \times 1$,
stride $s = 2 \times 2$
on the 3×3 green feature
map.

What is the new size?



$$n_{out} = \left\lceil \frac{n_{in} + 2p - k}{s} \right\rceil + 1$$

n_{in} : # of input features

n_{out} : # of output features

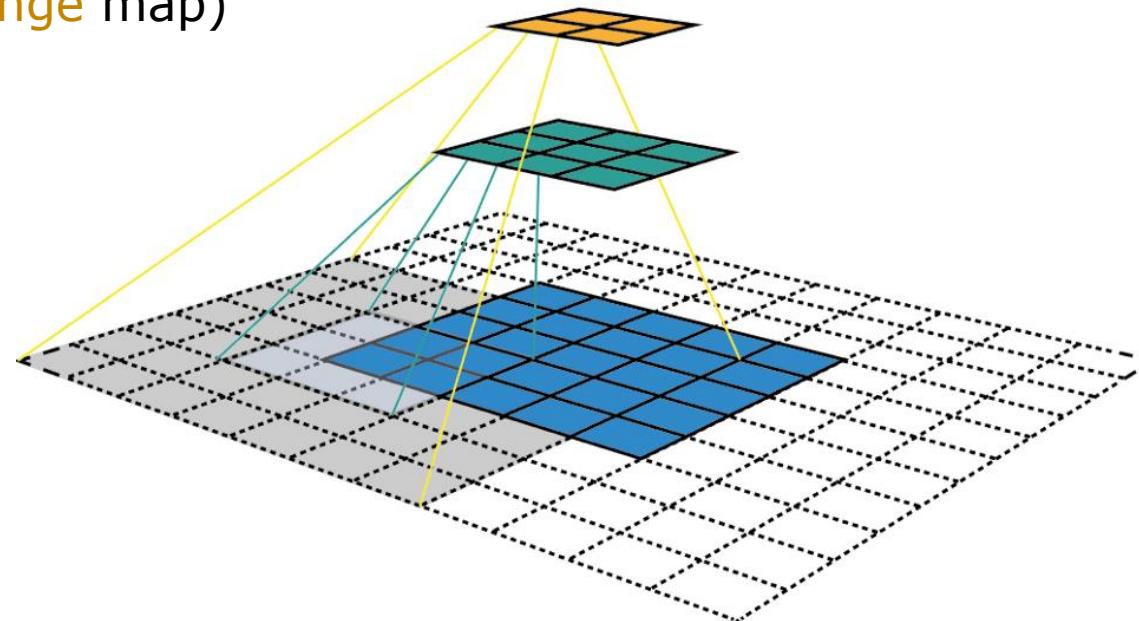
k : convolution **kernel** size

p : convolution **padding** size

s : convolution **stride** size

Layer's Receptive Field

After applying the same convolution on top of the 3x3 feature map, we will get a **2x2** feature map (orange map)



$$n_{out} = \left\lceil \frac{n_{in} + 2p - k}{s} \right\rceil + 1$$

n_{in} : # of input features

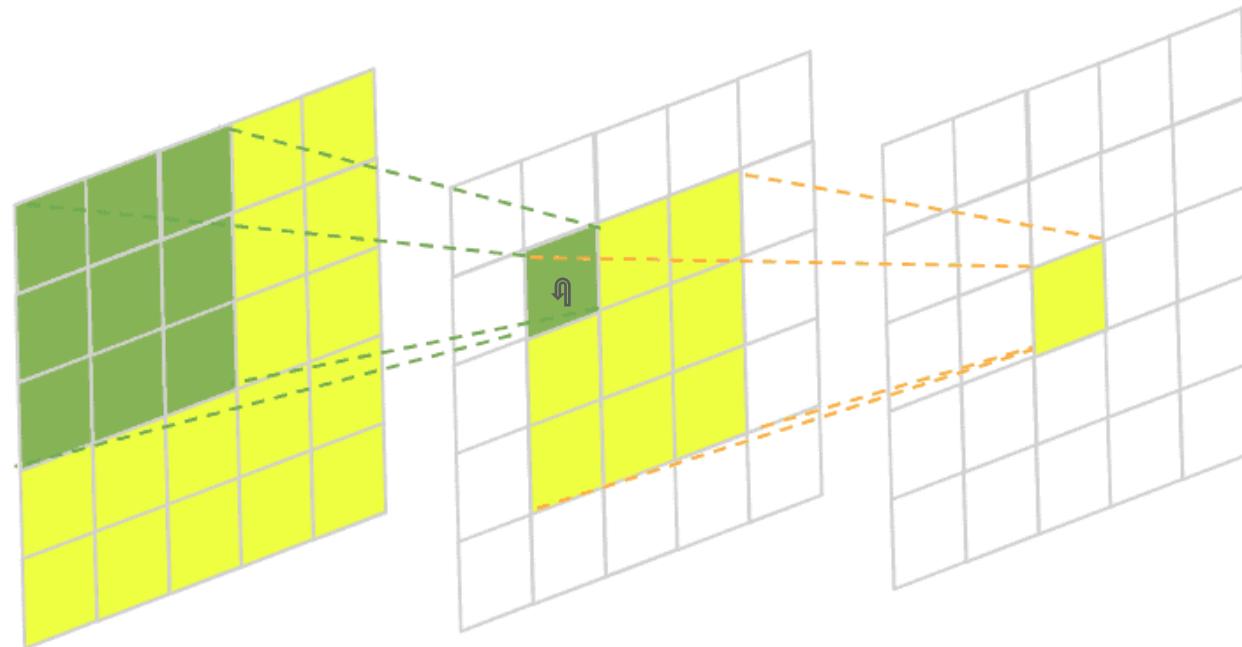
n_{out} : # of output features

k : convolution **kernel** size

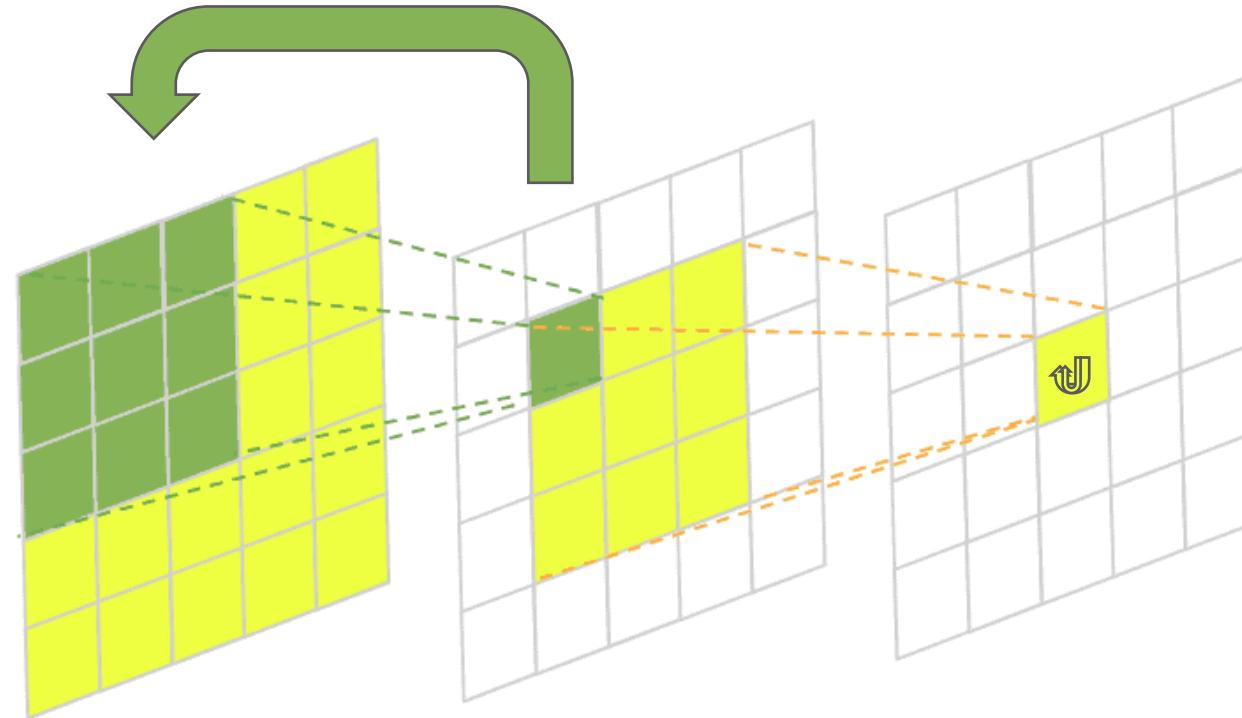
p : convolution **padding** size

s : convolution **stride** size

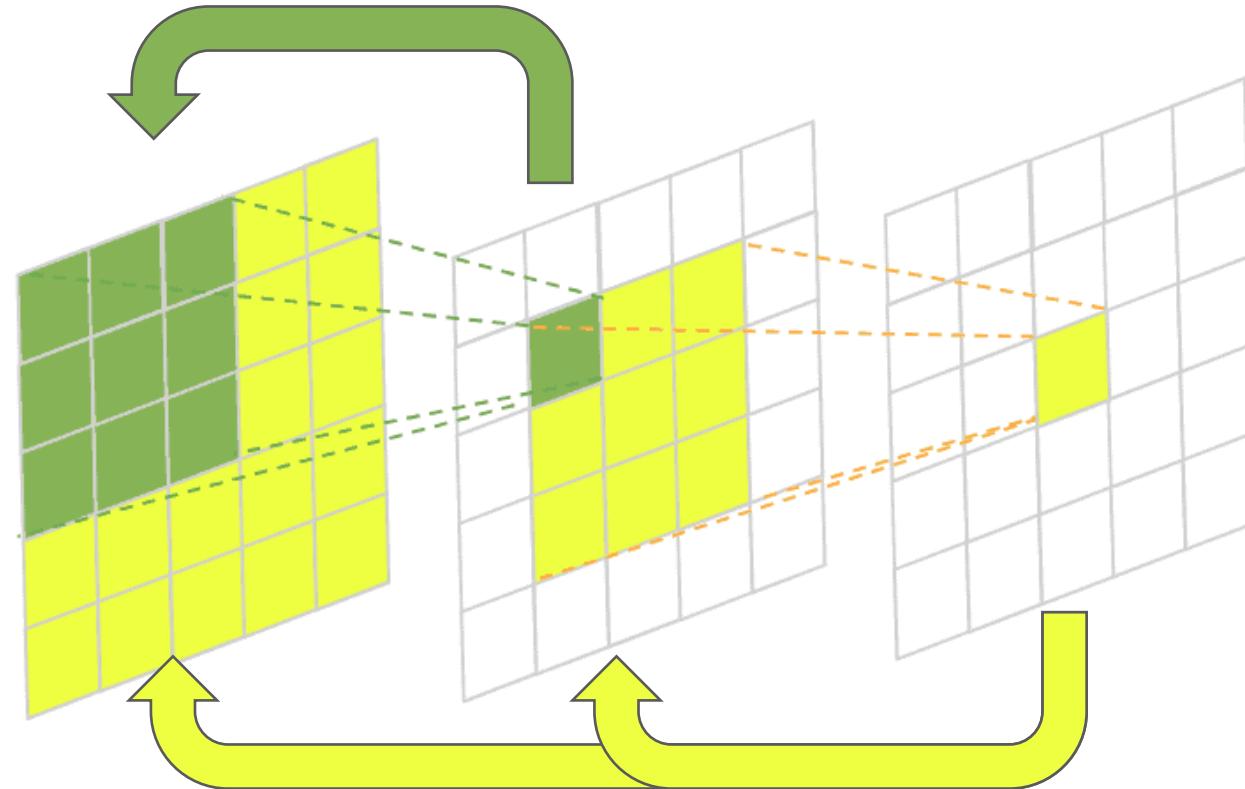
Summary: Receptive Field



Summary: Receptive Field



Summary: Receptive Field



Layer's Receptive Field

Receptive field in 1D: no padding, stride 1 and kernel 3x1



Layer's Receptive Field

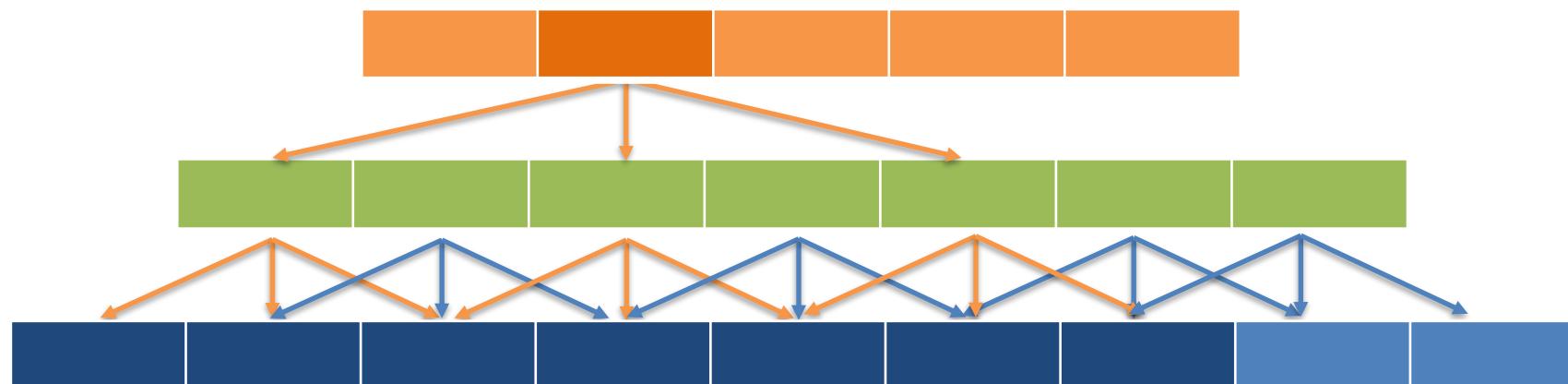
Receptive field in 1D: no padding, stride 1 and kernel 3x1



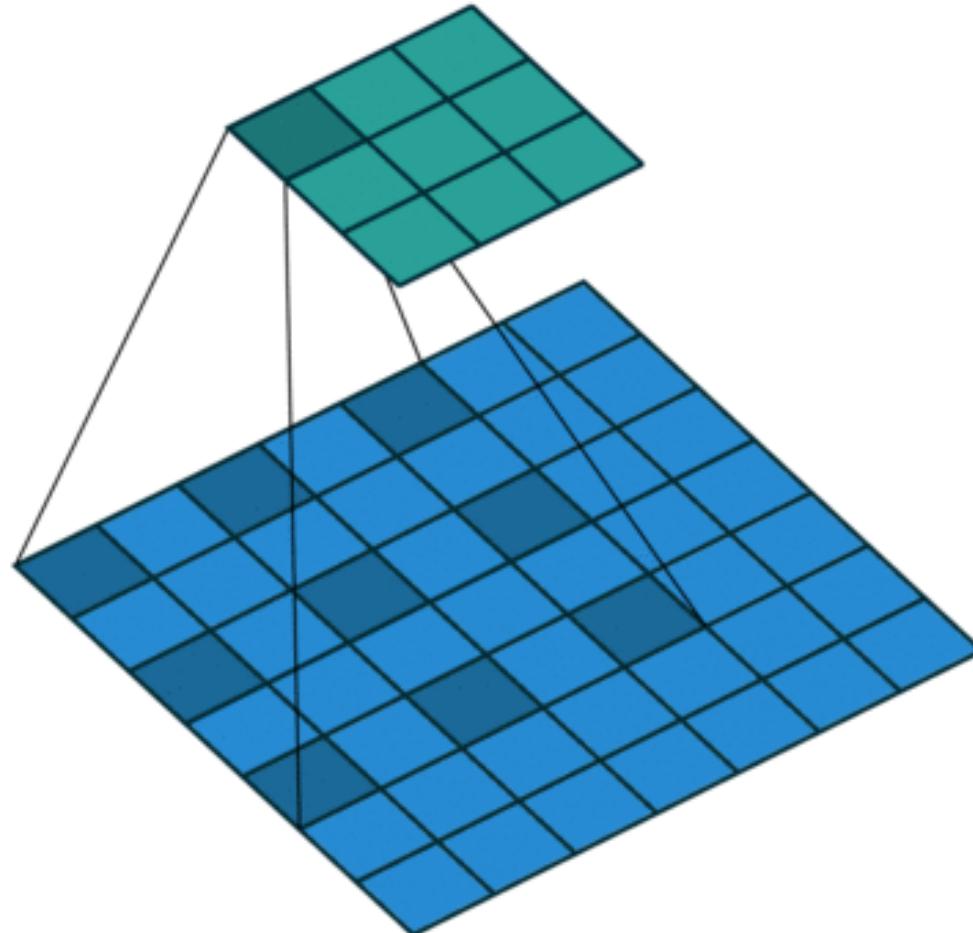
Dilated CNN

Receptive field in 1D: no padding, stride 1 and kernel 3x1

And skip some of the connections:



Dilated CNN



[Understanding the receptive field of deep convolutional networks | AI Summer \(theaisummer.com\)](https://theaisummer.com/receptive-fields/)

Loss / Cost calculation

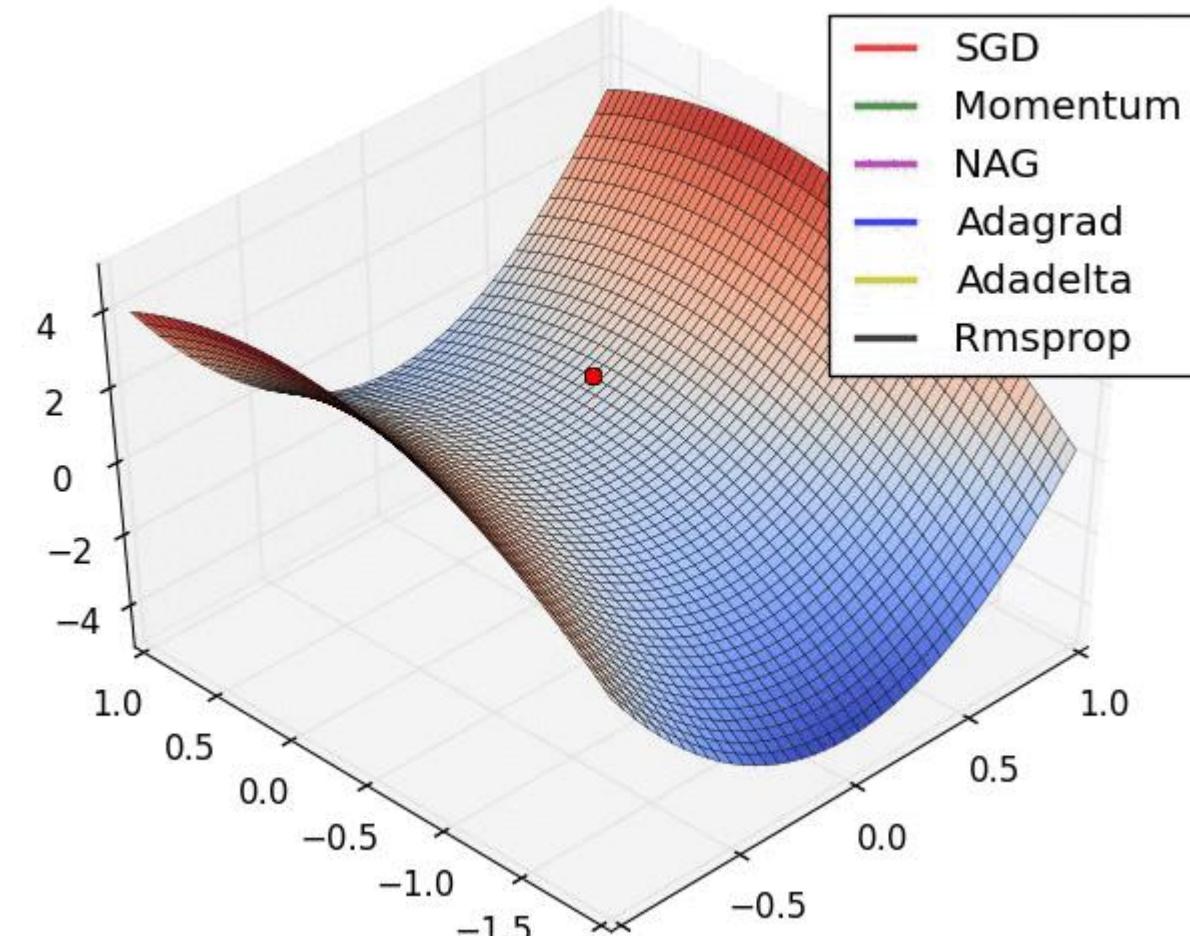
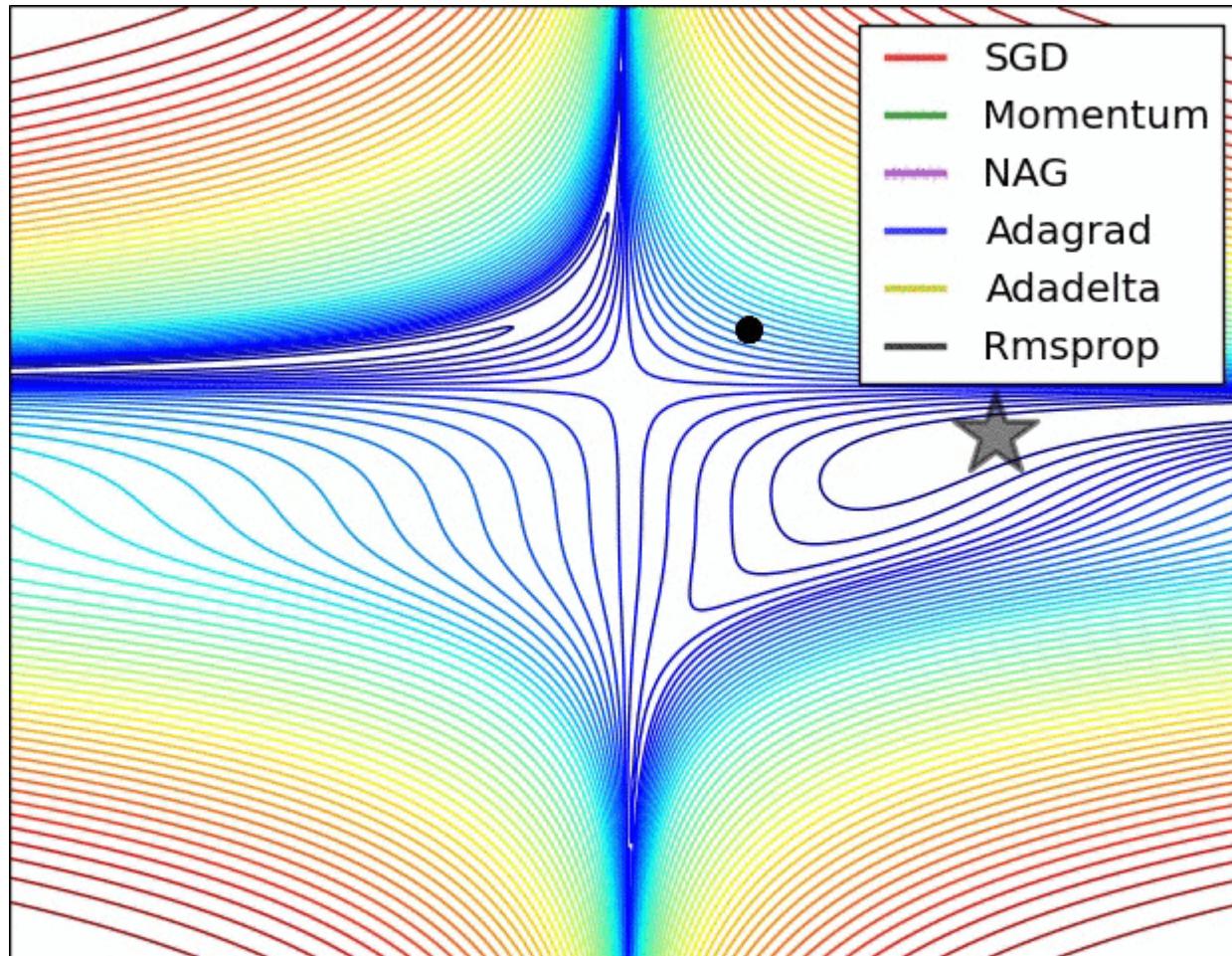
L1 Distance

- $d_1(I_1, I_2) = \sum_P |I_1^P - I_2^P|$ Where the sum is taken over all pixels:

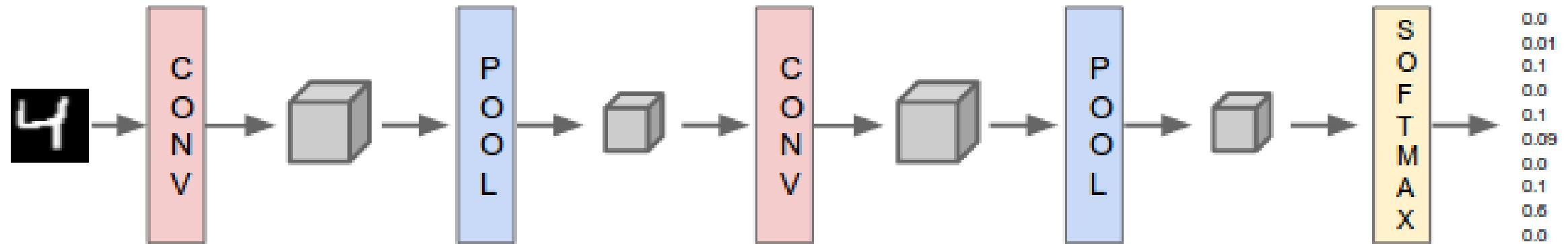
| test image | | | | - | training image | | | | = | pixel-wise absolute value differences | | | |
|------------|----|-----|-----|---|----------------|----|-----|-----|---|---------------------------------------|----|----|-----|
| 56 | 32 | 10 | 18 | | 10 | 20 | 24 | 17 | | 46 | 12 | 14 | 1 |
| 90 | 23 | 128 | 133 | | 8 | 10 | 89 | 100 | | 82 | 13 | 39 | 33 |
| 24 | 26 | 178 | 200 | | 12 | 16 | 178 | 170 | | 12 | 10 | 0 | 30 |
| 2 | 0 | 255 | 220 | | 4 | 32 | 233 | 112 | | 2 | 32 | 22 | 108 |

→ 456

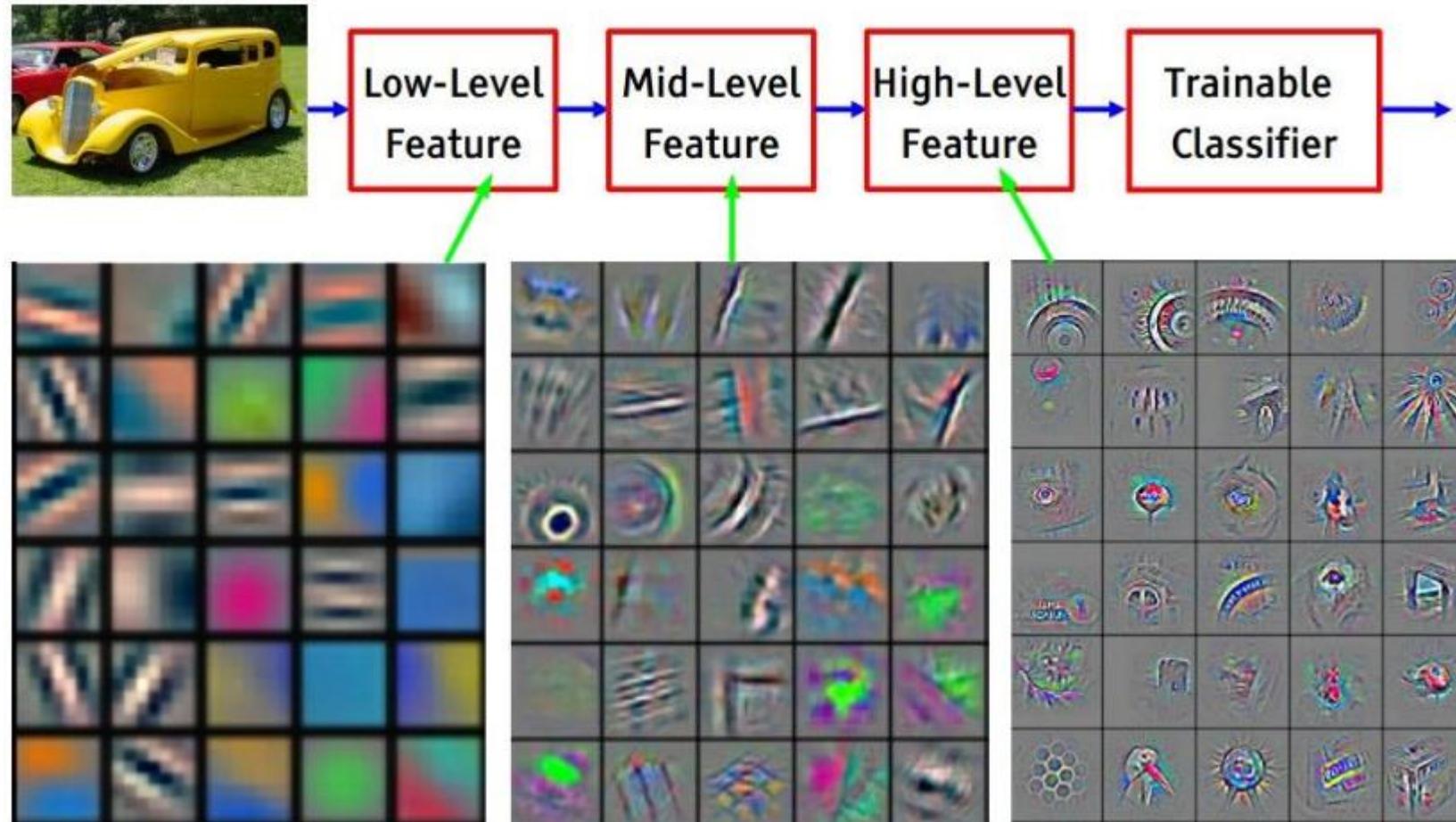
Optimization



Putting it all together



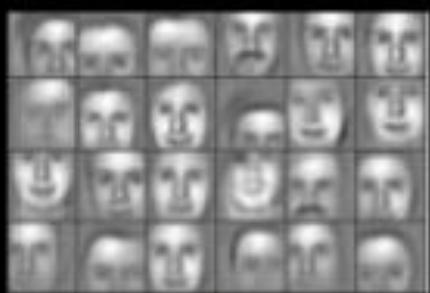
Neural Networks Extract Features



Learning of object parts

Examples of learned object parts from object categories

Faces



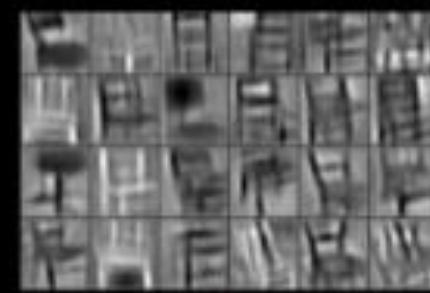
Cars



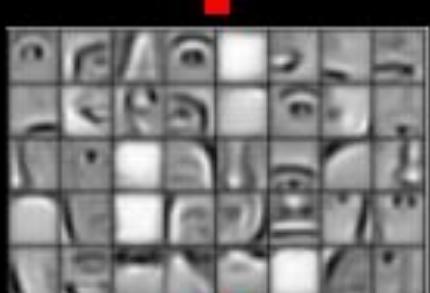
Elephants



Chairs



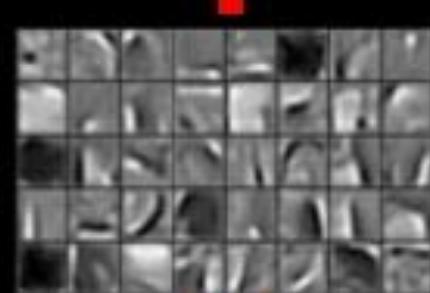
Faces



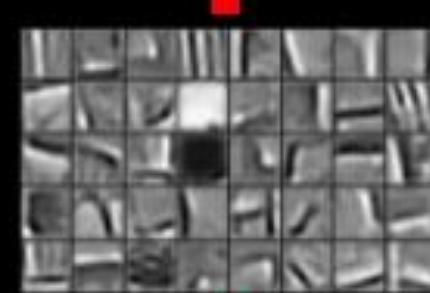
Cars



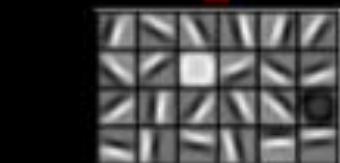
Elephants



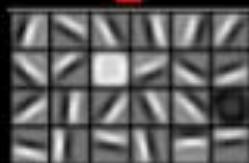
Chairs



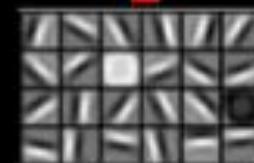
Faces



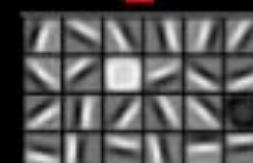
Cars



Elephants



Chairs



Demos

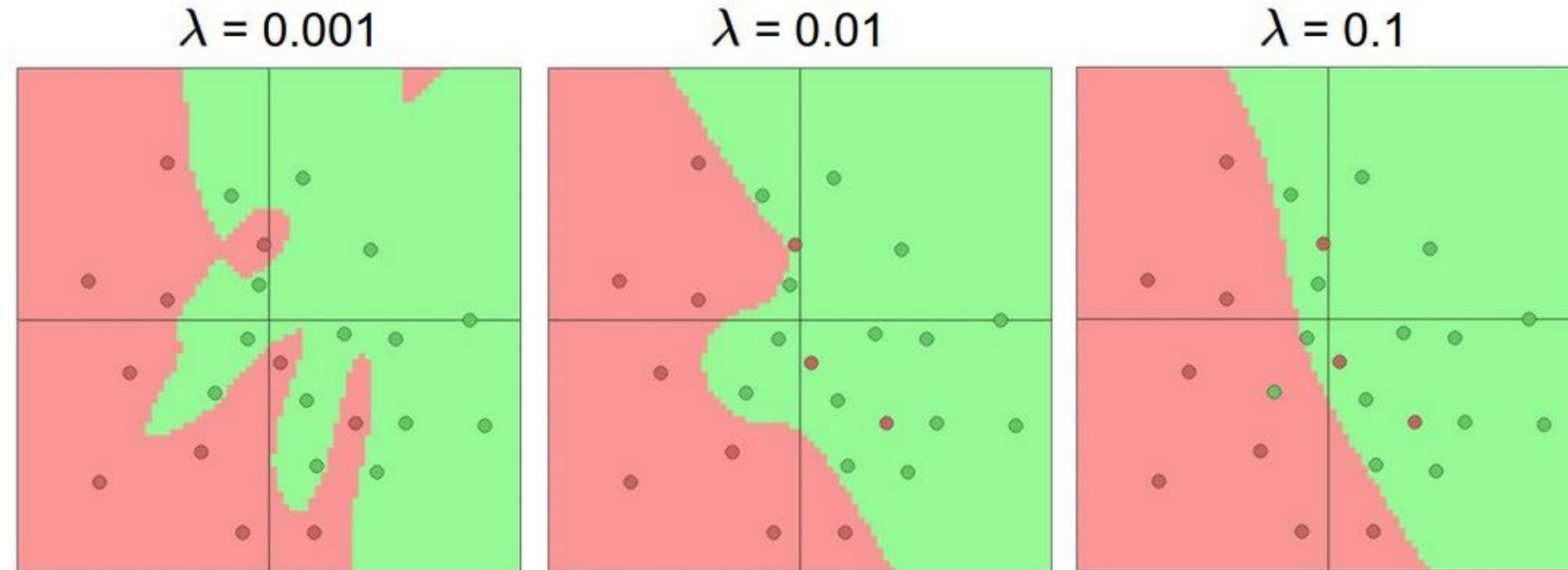
- <https://playground.tensorflow.org/>
- [ConvNetJS: Deep Learning in your browser \(stanford.edu\)](http://cs231n.stanford.edu/demos.html)

REGULARIZATION TECHNIQUES

To prevent overfitting

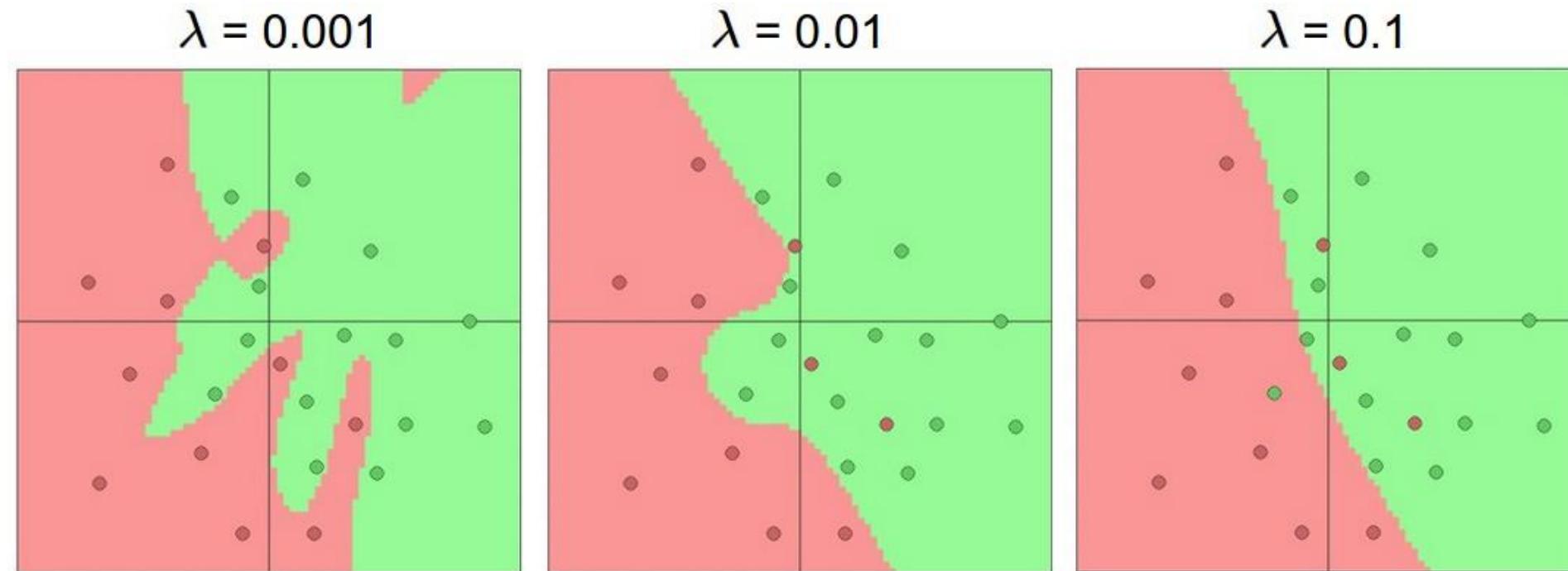
Overfitting (Recap)

$$L(w) = \sum_{i=1}^n (y^i - wx^i)^2$$



Overfitting (Recap)

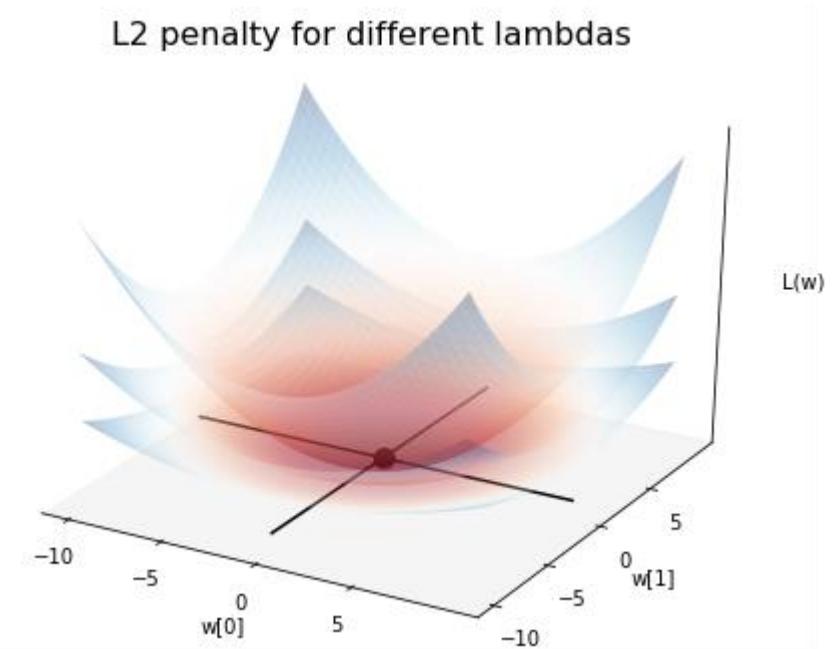
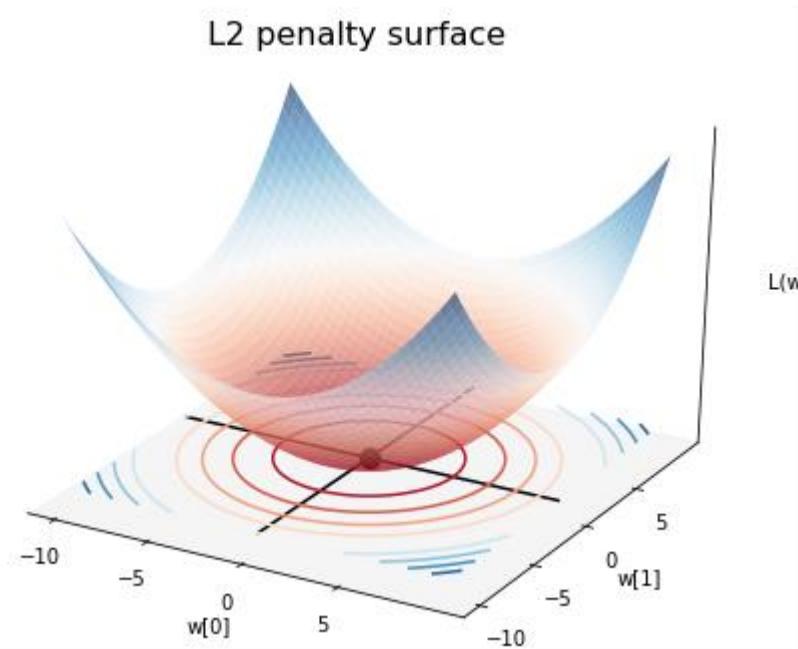
$$L(w) = \sum_{i=1}^n (y^i - w x^i)^2 + \lambda \sum_{j=0}^d w_j^2$$



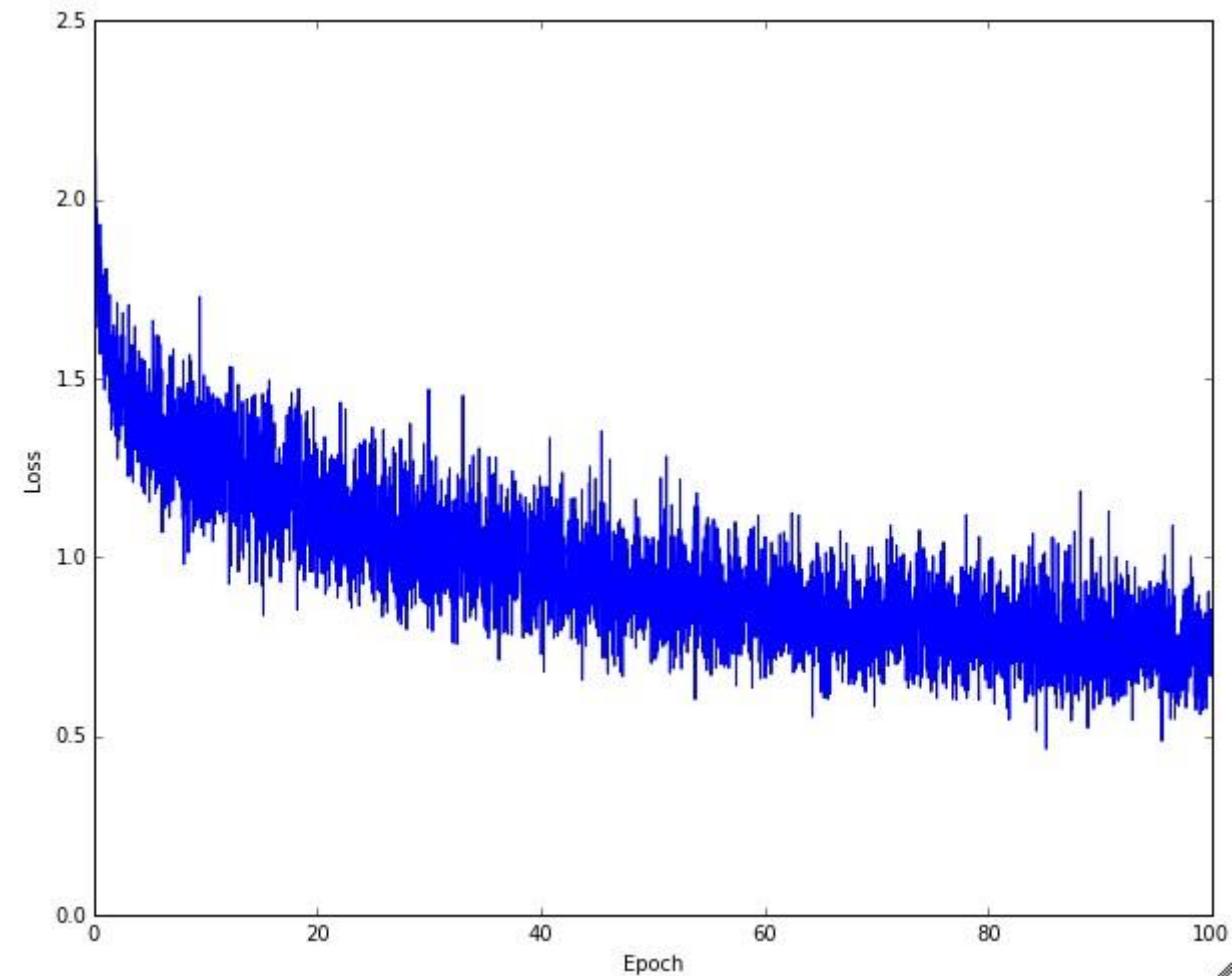
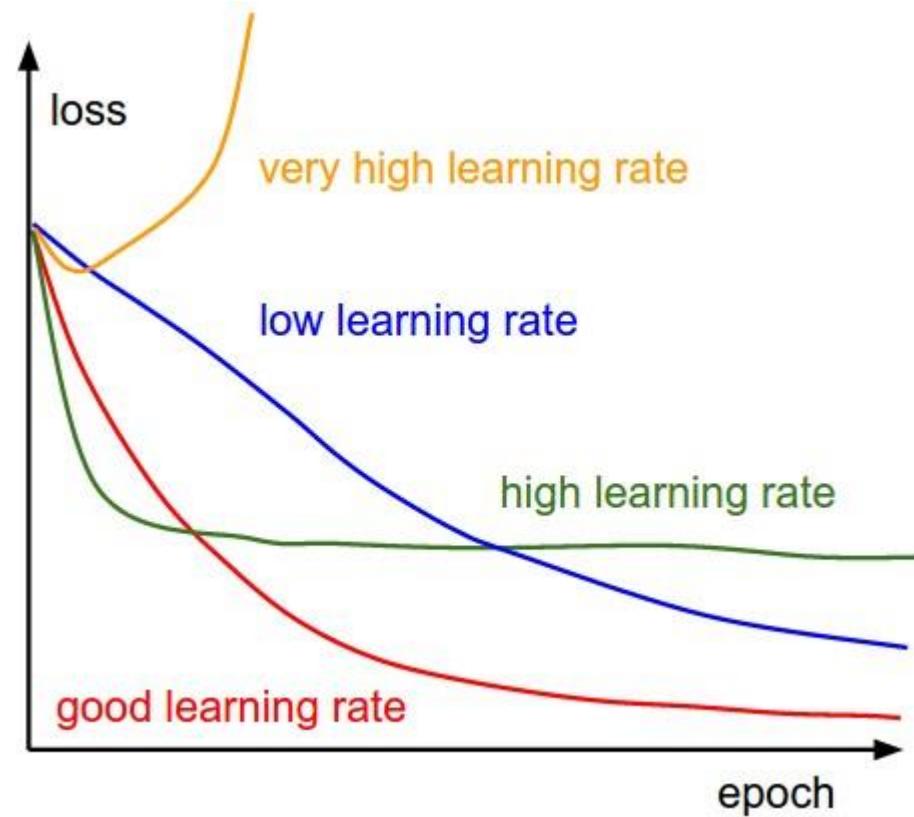
Overfitting (Recap)

$$L(w) = \sum_{i=1}^n (y^i - w x^i)^2$$

$$+ \lambda \sum_{j=0}^d w_j^2$$



Learning Rate Setting



Regularization

How to prevent overfitting?

- Choosing a proper Learning Rate
- Drop-out (elapsing neuron weights)
- Normalization (Batch Normalization, Gradient Accumulation)

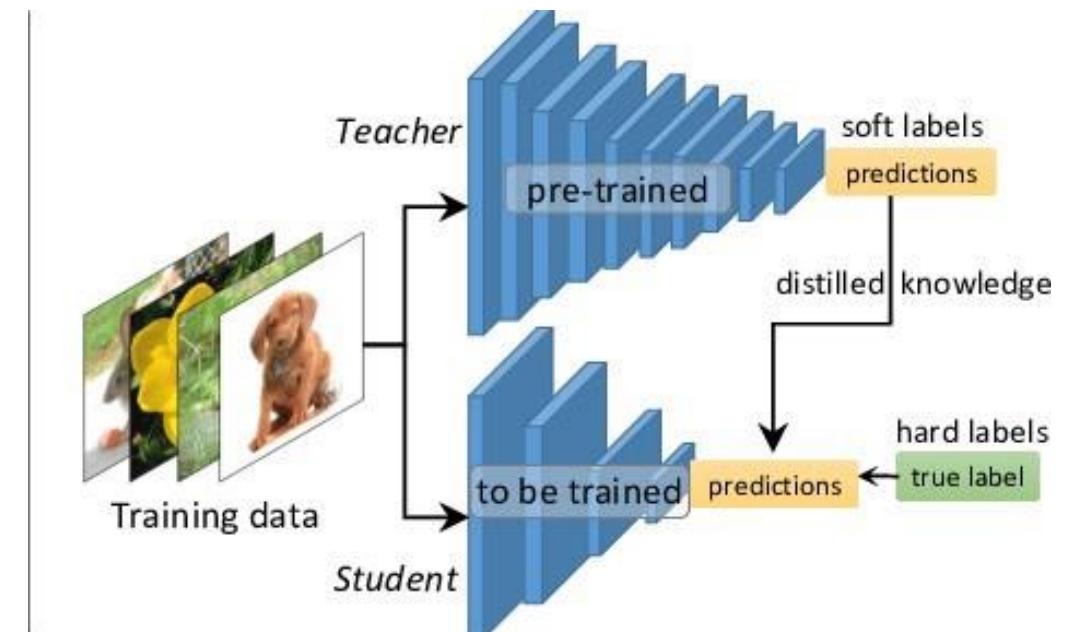
MODEL DISTILLATION

Teacher-Student

Model Distillation

Basic Idea (Example with Multi-Class Classification Network)

- Train a model with many parameters:
 - Multiple Layers
 - Multiple Neurons in each Layer
- Create a smaller Network
 - With significantly **fewer** parameters
- Train it on the outputs of the large network
 - On the float numbers, not the rounded softmax/true labels



Model Distillation

Result Network

- The new network learns with the outputs of the original, NOT with a cost function of 1s and 0s
- The network generalizes better
- Annotated Code: [Distilling the Knowledge in a Neural Network \(labml.ai\)](#)

CNN – DEEPER DIVE

CS231n Convolutional Neural Networks for Visual Recognition

MODEL INTERPRETATION

Why should we trust a model?!

Do you trust your doctor?

Imaginary Scenario

- You feel unwell
- Your doctor diagnoses you and gives you a prognosis
 - Based only on your historical medical data
 - Without meeting you in person
- Would you seek a second opinion?
- When and why would you trust your doctor?

Model Explainability / Prediction Reasoning

Tools to explain computer vision predictions

- Saliency Maps
 - Deconvolutional Network Approach (DeconvNet)
 - Gradient-Based Approach (Vanilla Gradient)
 - Guided Backpropagation Algorithm
 - Class Activation Mapping (CAM)
 - Grad-CAM
- Explanatory Tools
 - SHAP
 - LIME
- Causal Inference

Saliency Maps

What did CNN focus on?

- Given an image, visualize the excited CNN areas
- Can be applied on different layers
- Normally visualized as a heatmap layer on top of the original image
- Tools:
 - iNNvestigate neural networks' predictions!
 - DeepExplain

deconv



guided backpropagation



corresponding image crops



deconv



guided backpropagation



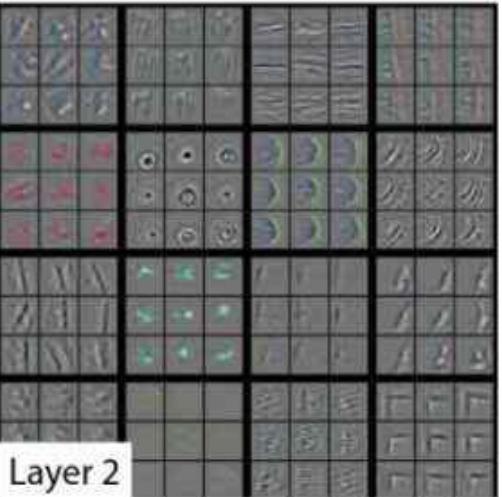
corresponding image crops



Layer 1



Layer 2



(a) Original Image



(b) Guided Backprop 'Cat'

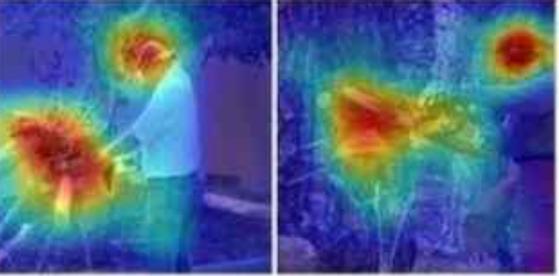
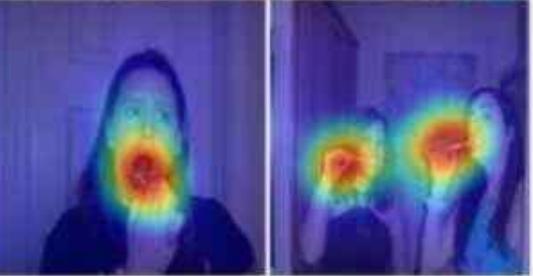


(c) Grad-CAM 'Cat'

Brushing teeth



Cutting trees

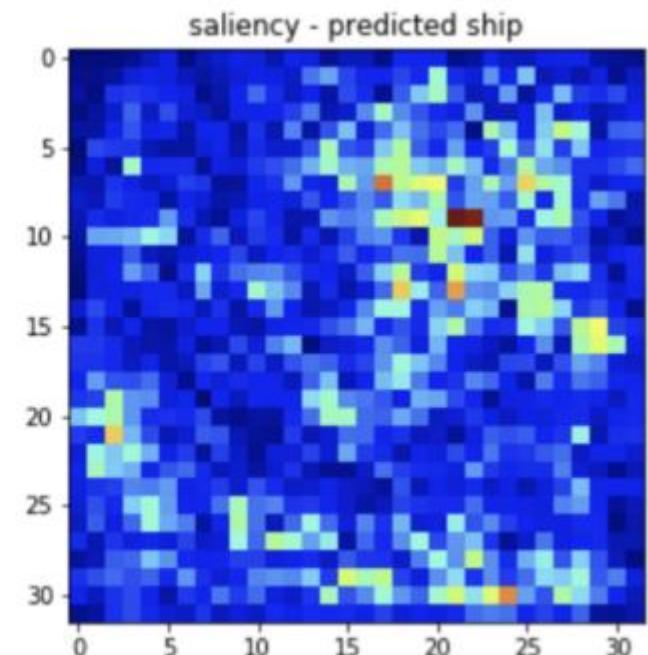
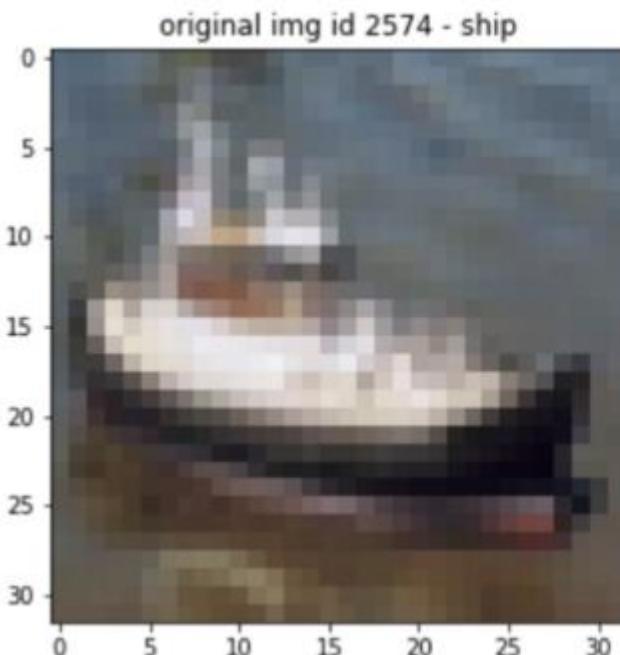


Saliency Maps

Example

The water around the ship is the reason for the prediction.

The model won't do well if the ship is in a different background.

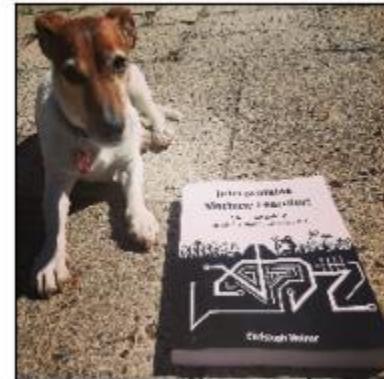


Saliency Maps

Comparison

- Relatively effective
- Fast to compute (GradCAM - only last layer)
- Gives good results
- But...
 - Hard to interpret if an interpretation is correct
 - Fragile / Sensitive
 - May be unreliable

Greyhound (vanilla)



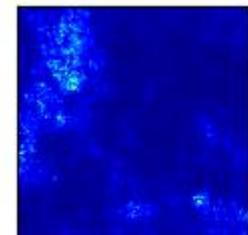
Soup Bowl (vanilla)



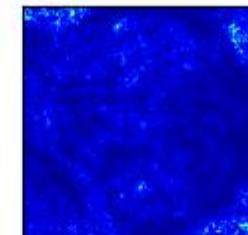
Eel (vanilla)



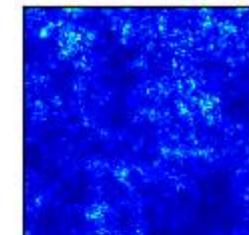
Greyhound (vanilla)



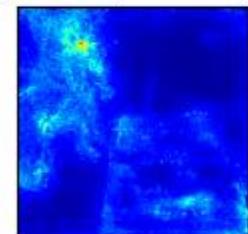
Soup Bowl (vanilla)



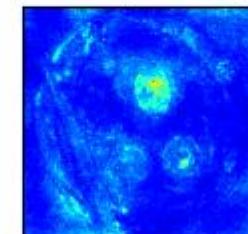
Eel (vanilla)



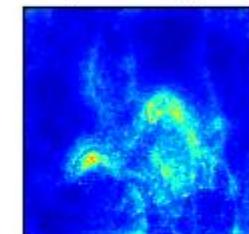
Greyhound (Smoothgrad)



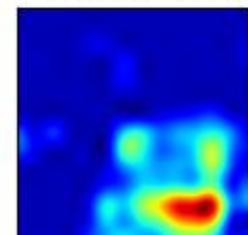
Soup Bowl (Smoothgrad)



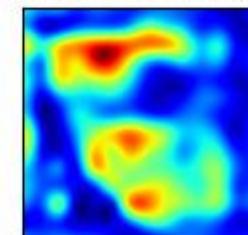
Eel (Smoothgrad)



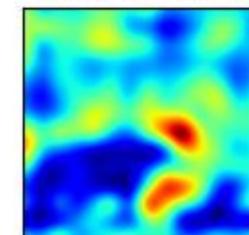
Greyhound (Grad-Cam)



Soup Bowl (Grad-Cam)

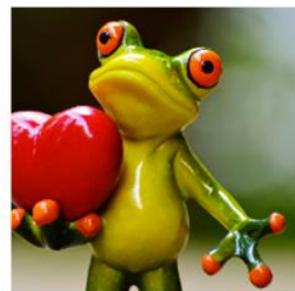


Eel (Grad-Cam)



Explanatory Tools

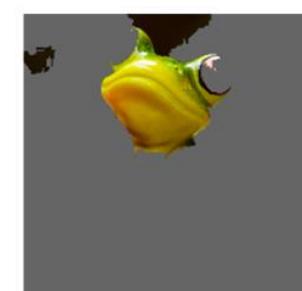
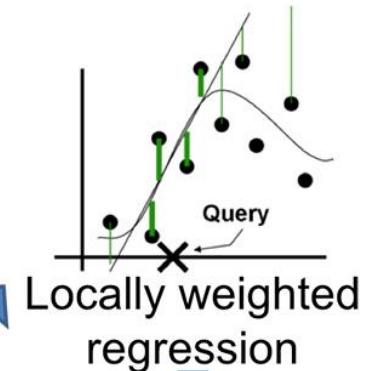
LIME - Local Surrogate



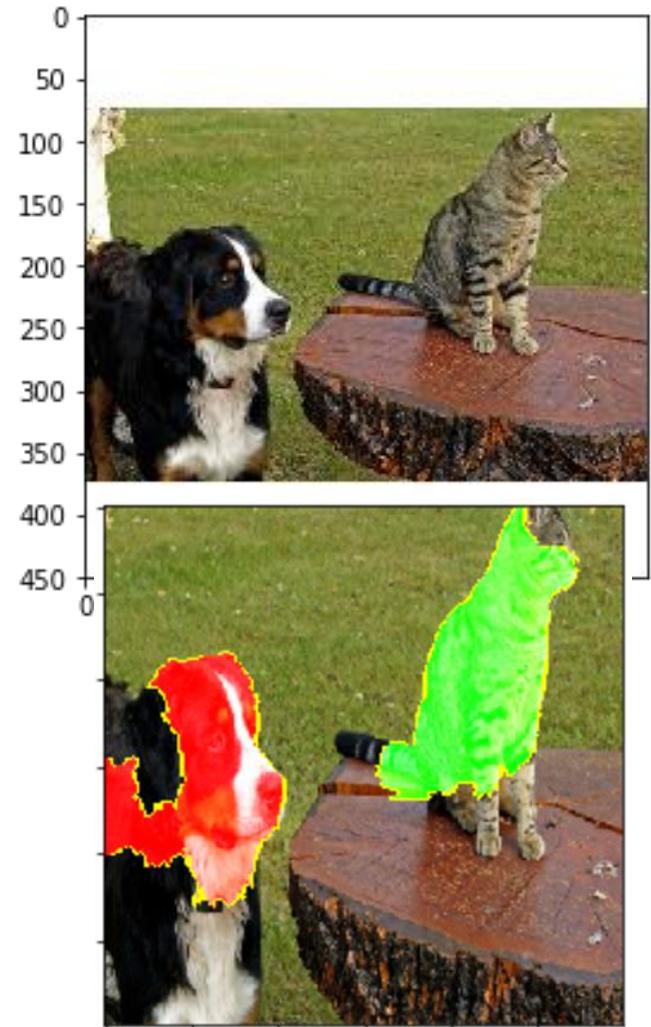
Original Image
 $P(\text{tree frog}) = 0.54$



| Perturbed Instances | $P(\text{tree frog})$ |
|---|-----------------------|
|  | 0.85 |
|  | 0.00001 |
|  | 0.52 |



Explanation



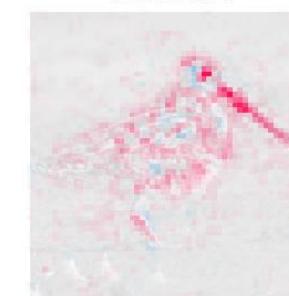
Explanatory Tools

SHAP

- Shapley values
 - Game Theory
 - How much each player (feature) in a coalition contributed to the result (prediction)
- SHAP
 - Combines LIME, Shapley Vals and others.
 - “Coalition” of super-pixels



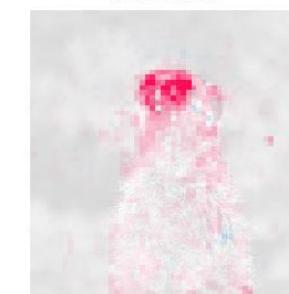
dowitcher



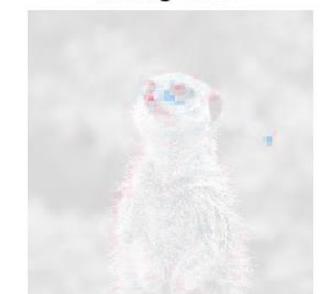
red-backed_sandpiper



meerkat



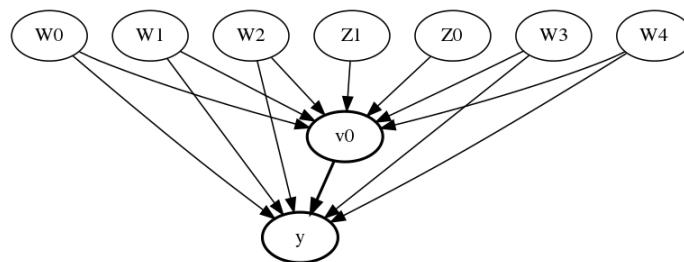
mongoose



Causal Inference

80% of the population are X... but Why?

- Statistics examine samples and deduct for whole populations
 - But lacks the (hidden) reasons why.
- A new science
 - New math:
 $P(y|x) \rightarrow P(y|do(x))$
- Applications:
 - Personalized medicine



JUDEA PEARL
WINNER OF THE TURING AWARD
AND DANA MACKENZIE

THE BOOK OF WHY



THE NEW SCIENCE
OF CAUSE AND EFFECT

TRANSFER LEARNING

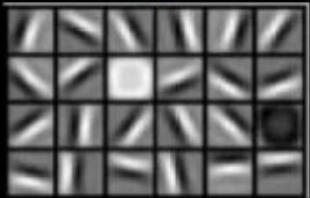
Transfer Learning

How is it done?

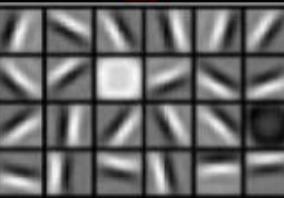
- Shared weights
 - Set a lower LR for layers
- Self-Supervised Learning
 - Training on a large amount of data
- Then, fine-tune on a down-stream task

Examples of learned object parts from object categories

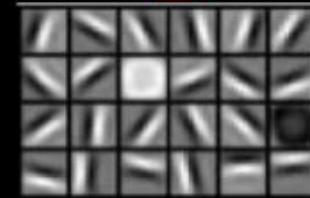
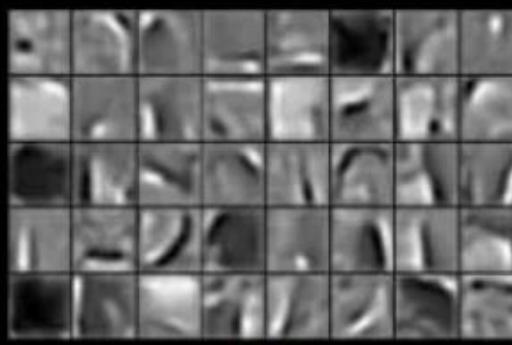
Faces



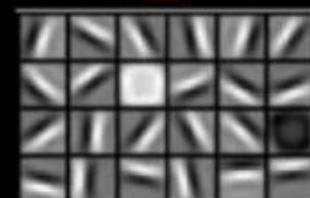
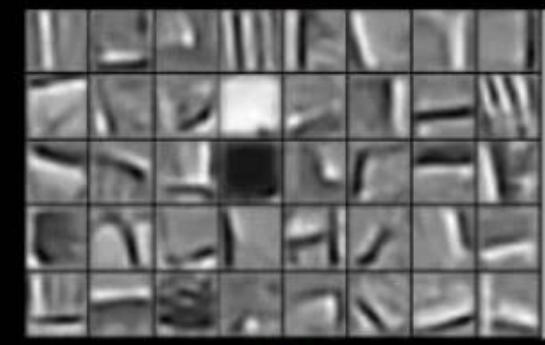
Cars



Elephants



Chairs

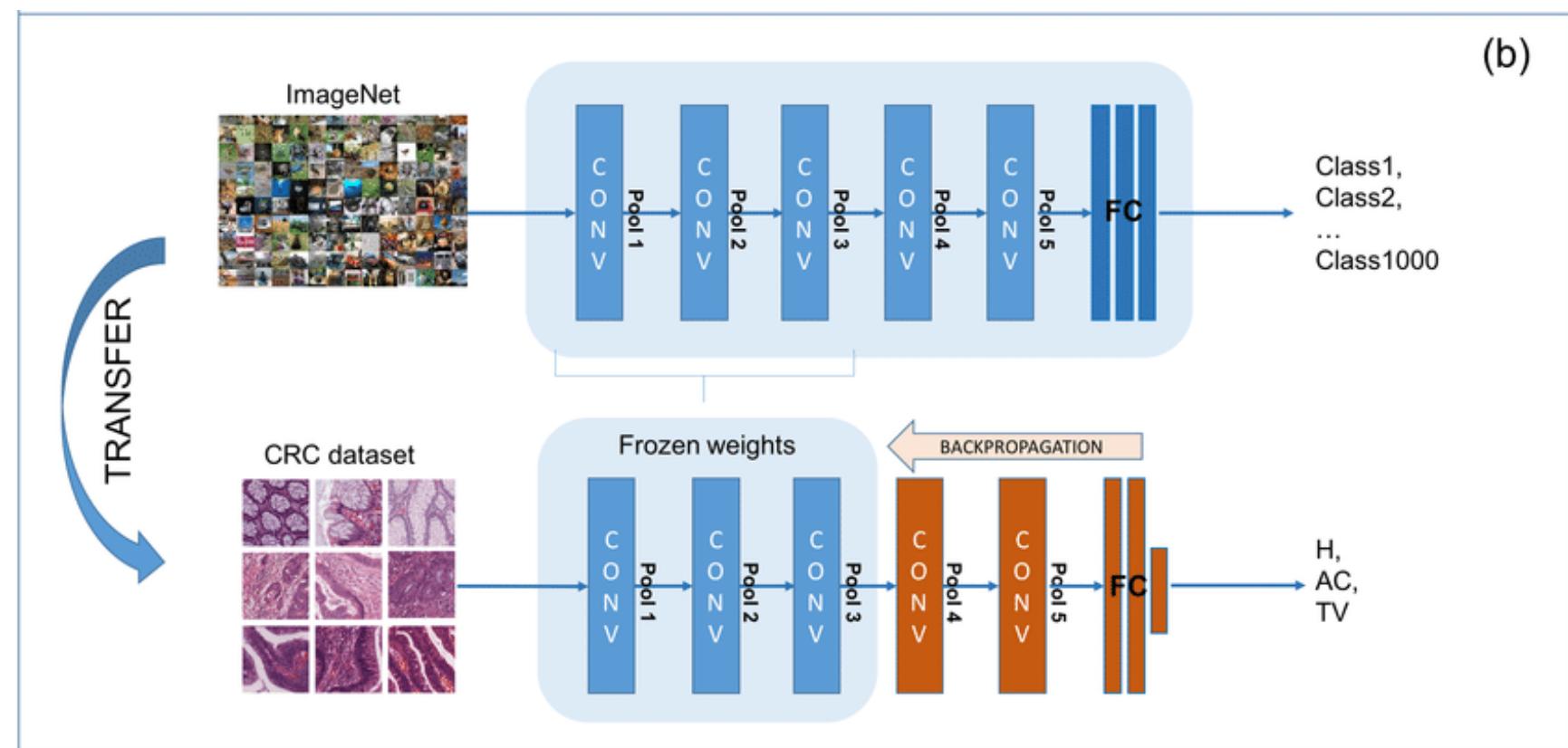


Transfer Learning

Re-using layer-weights

Setting a different LR
for each layer

More info



Transfer Learning

Training

- We often use already pre-trained networks
 - Training such models is expensive
 - Hard to find large amounts of data
- Better from the same domain
 - E.g., train on all X-Rays
 - Fine-tune on chest X-ray for specific use-case (e.g., knee)

Transfer Learning

PyTorch example

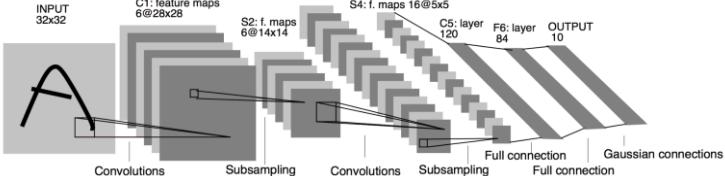
- https://pytorch.org/tutorials/beginner/transfer_learning_tutorial.html
- Learning rate:
 - Can be set to give more weight to recent layers – close to the SoftMax

CNNs in Mammography (cont'd)

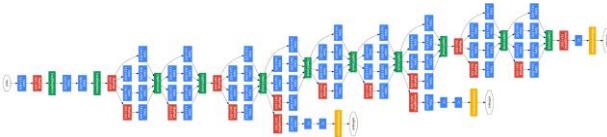
- **Best practices** to improve CNN performance:
 - Pre-processing images (especially mammograms)
 - Combination of learned and hand-crafted features
 - Data augmentation
 - Transfer learning
 - Batch normalization
 - Dropout
- Attention-based modules
- Multi-view images
- Balanced data distributions
- Context and patient information
- Multi-stage **vs** end-to-end (E2E) methods

CNN Architectures

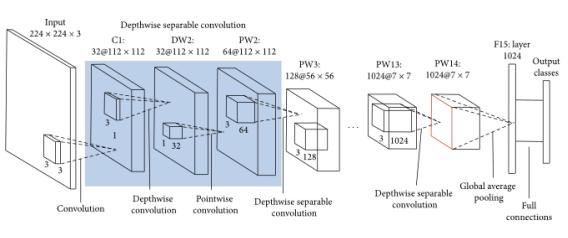
LeNet



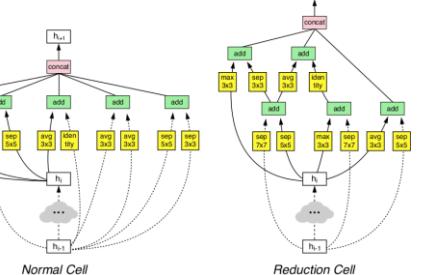
GoogLeNet



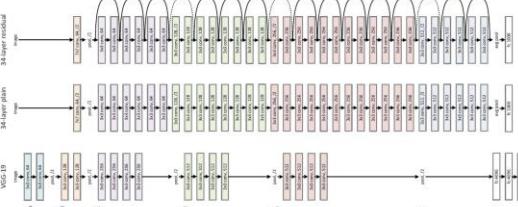
MobileNet



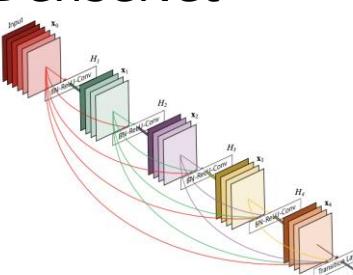
NasNet



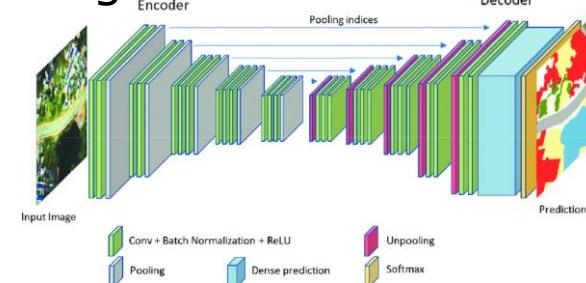
ResNet



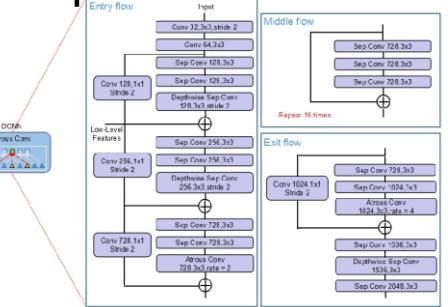
DenseNet



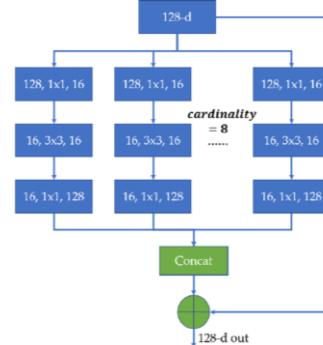
SegNet



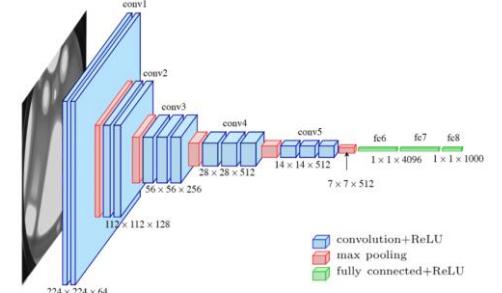
Xception



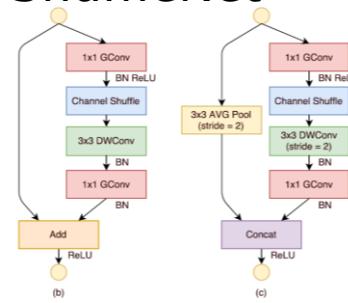
ResNext



VGG



ShuffleNet



CNN Architectures

PyTorch

- TIMM: [timm · PyPI](#)
- Now also in HuggingFace:
[GitHub - huggingface/pytorch-image-models: PyTorch image models, scripts, pretrained weights -- ResNet, ResNeXT, EfficientNet, NFNet, Vision Transformer \(ViT\), MobileNet-V3/V2, RegNet, DPN, CSPNet, Swin Transformer, MaxViT, CoAtNet, ConvNeXt, and more](#)