

## 1. COMPUTATIONAL GRAPH

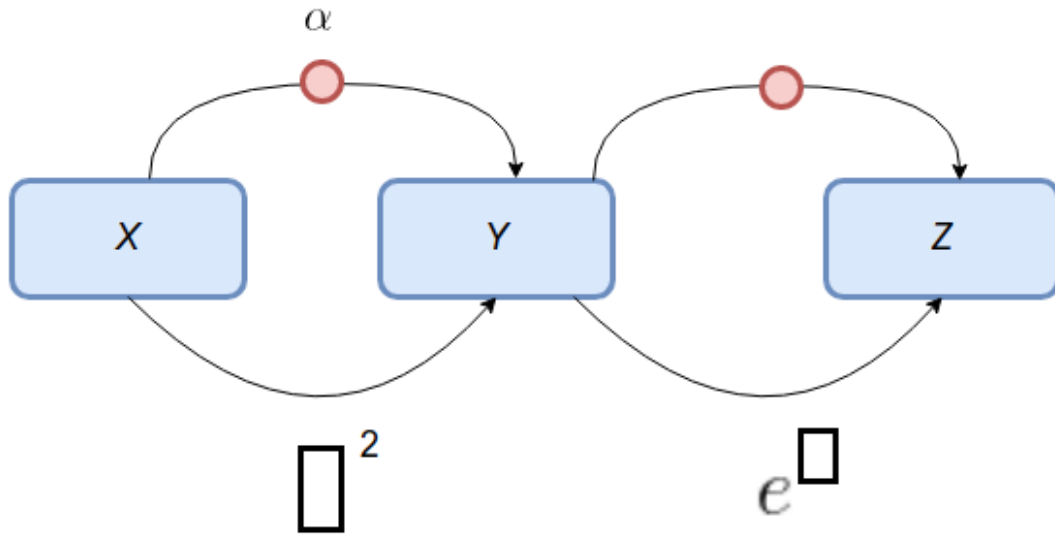


Figure 1: Example of gradient flow in a computational graph

In the shown computational graph we have two path multiplied by scalars and two paths having functional transformations. We have  $Y = \alpha X + X^2$  and  $Z = 1.Y + e^Y$  (as the scalar is not specified it is taken as 1) Forward gradients ( $\frac{\partial}{\partial X}$ ):

- $\frac{\partial X}{\partial X} = 1$
- $\frac{\partial Y}{\partial X} = 1 + 2X$
- $\frac{\partial Z}{\partial X} = \frac{\partial Z}{\partial Y} \cdot \frac{\partial Y}{\partial X} = (1 + e^Y)(1 + 2X)$

Reverse gradients ( $\frac{\partial Z}{\partial}$ ):

- $\frac{\partial Z}{\partial Z} = 1$
- $\frac{\partial Z}{\partial Y} = (1 + e^Y)$
- $\frac{\partial Z}{\partial X} = \frac{\partial Z}{\partial Y} \cdot \frac{\partial Y}{\partial X} = (1 + e^Y)(1 + 2X)$