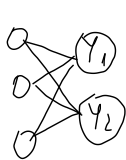
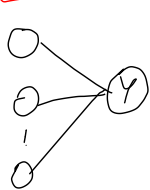


Linear ↘

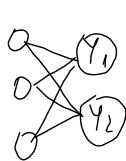
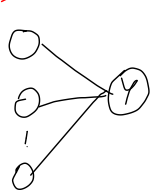


Multiple

$$\hat{y} = w_0 + w_1x_1 + \dots + w_nx_n$$

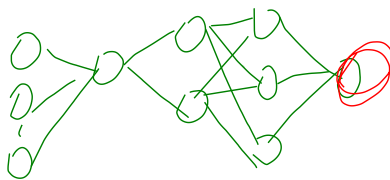
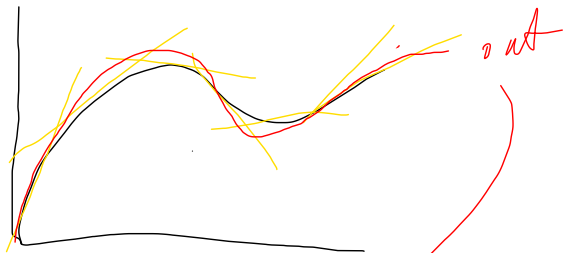
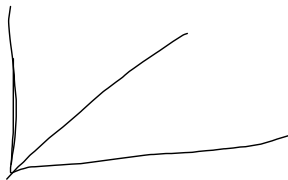


Logistic



Sigmoid (binary)

Softmax (multi-class)



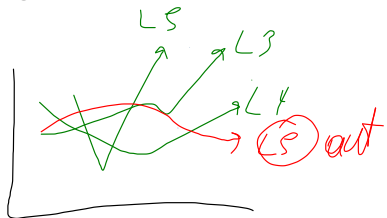
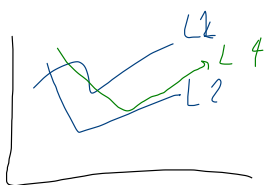
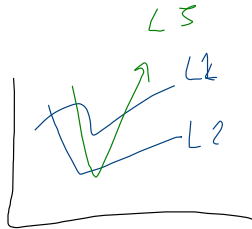
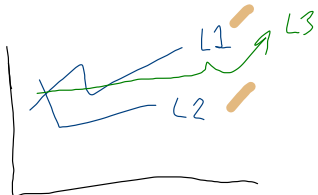
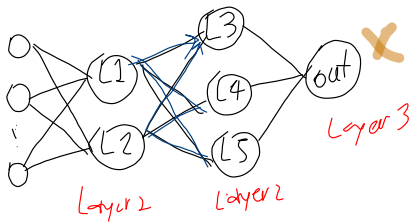
Neural Network

# Neural Network

output node

Mean Squared Error (MSE)

$$\sum_{i=1}^N \frac{(y_i - \hat{y}_i)^2}{N}$$



Activation function (Af)

- Sigmoid
- Tanh
- ReLU
- PReLU

log

Input → Af → Input (new)

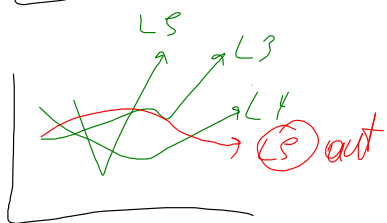
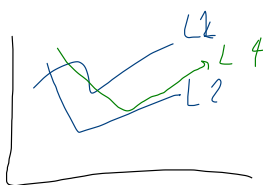
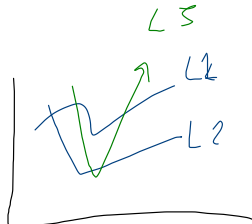
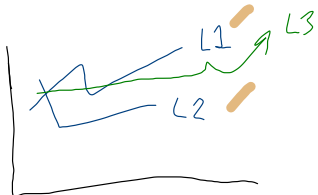
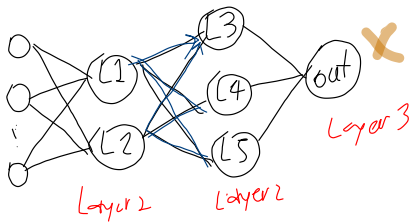
ถ้าใช้ฟังก์ชัน log คือ  
(new) MSE

# Neural Network

output node

Mean Squared Error (MSE)

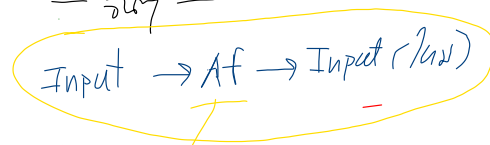
$$\sum_{i=1}^N \frac{(y_i - \hat{y}_i)^2}{N}$$



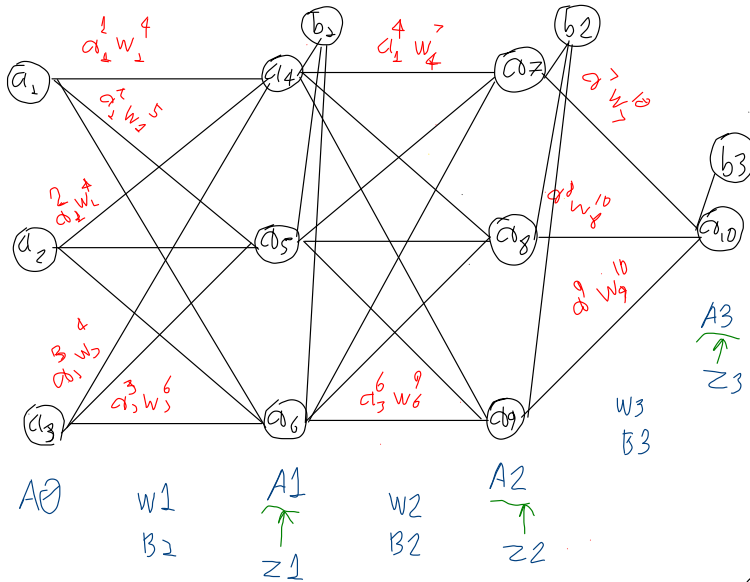
Activation function (Af)

- Sigmoid
- Tanh
- ReLU
- PReLU

log



data input output  
(new data)  
MSE



$a$  }  $a$  = Feature  $\leftarrow 1, 2, 3$   
 $a_p$  }  $p$  = Example

$x_1$	$x_2$	$x_3$
1	1	1
N	N	N

Input

Example

Hidden

$a_1, a_2, a_3$

$$A0 \rightarrow A0W1 + B1 \rightarrow Z1 \rightarrow A1 \rightarrow A1W2 + B2 \rightarrow Z2 \rightarrow A2 \rightarrow A2W3 + B3 \rightarrow Z3 \rightarrow \underline{A3}$$

$$A0 \rightarrow A0W1 + B1 \rightarrow Z1 \rightarrow A1 \rightarrow A1W2 + B2 \rightarrow Z2 \rightarrow A2 \rightarrow A2W3 + B3 \rightarrow Z3 \rightarrow \underline{\underline{A3}}$$

$$Z1 = \begin{bmatrix} z_1^4 & z_1^5 & z_1^6 \\ z_2^4 & z_2^5 & z_2^6 \\ \vdots & \vdots & \vdots \\ z_N^4 & z_N^5 & z_N^6 \end{bmatrix} = \begin{bmatrix} a_1^1 & a_1^2 & a_1^3 \\ a_2^1 & a_2^2 & a_2^3 \\ \vdots & \vdots & \vdots \\ a_N^1 & a_N^2 & a_N^3 \end{bmatrix} \times \begin{bmatrix} w_1^4 & w_1^5 & w_1^6 \\ w_2^4 & w_2^5 & w_2^6 \\ \vdots & \vdots & \vdots \\ w_N^4 & w_N^5 & w_N^6 \end{bmatrix} + [b_4 \ b_5 \ b_6] = A0W1 + B1$$

(Note:  $a_2$  is circled in red in the original image)

$$A1 = \begin{bmatrix} a_1^4 & a_1^5 & a_1^6 \\ a_2^4 & a_2^5 & a_2^6 \\ \vdots & \vdots & \vdots \\ a_N^4 & a_N^5 & a_N^6 \end{bmatrix} = \text{af} \left[ \begin{bmatrix} z_1^4 & z_1^5 & z_1^6 \\ z_2^4 & z_2^5 & z_2^6 \\ \vdots & \vdots & \vdots \\ z_N^4 & z_N^5 & z_N^6 \end{bmatrix} \right] = \text{af}(Z1)$$

af (Activation function)

$$A0 \rightarrow A0W1 + B1 \rightarrow Z1 \rightarrow A1 \rightarrow A1W2 + B2 \rightarrow Z2 \rightarrow A2 \rightarrow A2W3 + B3 \rightarrow Z3 \rightarrow \underline{\underline{A3}}$$

$$Z2 = \begin{bmatrix} z_1^7 & z_1^8 & z_1^9 \\ z_2^7 & z_2^8 & z_2^9 \\ \vdots & \vdots & \vdots \\ z_N^7 & z_N^8 & z_N^9 \end{bmatrix} = \begin{bmatrix} a_1^4 & a_1^5 & a_1^6 \\ a_2^4 & a_2^5 & a_2^6 \\ \vdots & \vdots & \vdots \\ a_N^4 & a_N^5 & a_N^6 \end{bmatrix} \times \begin{bmatrix} w_1^7 & w_1^8 & w_1^9 \\ w_2^7 & w_2^8 & w_2^9 \\ \vdots & \vdots & \vdots \\ w_N^7 & w_N^8 & w_N^9 \end{bmatrix} + \begin{bmatrix} b^7 & b^8 & b^9 \end{bmatrix} = A1W2 + B2$$

(Note:  $a_1^5$  is circled in red in the original image)

af (Activation function)

$$A2 = \begin{bmatrix} a_1^7 & a_1^8 & a_1^9 \\ a_2^7 & a_2^8 & a_2^9 \\ \vdots & \vdots & \vdots \\ a_N^7 & a_N^8 & a_N^9 \end{bmatrix} = af \left[ \begin{bmatrix} z_1^7 & z_1^8 & z_1^9 \\ z_2^7 & z_2^8 & z_2^9 \\ \vdots & \vdots & \vdots \\ z_N^7 & z_N^8 & z_N^9 \end{bmatrix} \right] = af(A2)$$

$$A0 \rightarrow A0W1 + B1 \rightarrow Z1 \rightarrow A1 \rightarrow A1W2 + B2 \rightarrow Z2 \rightarrow A2 \rightarrow A2W3 + B3 \rightarrow Z3 \rightarrow \underline{\underline{A3}}$$

$$Z2 = \begin{bmatrix} z_1^7 & z_1^8 & z_1^9 \\ z_2^7 & z_2^8 & z_2^9 \\ \vdots & \vdots & \vdots \\ z_N^7 & z_N^8 & z_N^9 \end{bmatrix} = \begin{bmatrix} a_1^4 & a_1^5 & a_1^6 \\ a_2^4 & a_2^5 & a_2^6 \\ \vdots & \vdots & \vdots \\ a_N^4 & a_N^5 & a_N^6 \end{bmatrix} \times \begin{bmatrix} w_1^7 & w_1^8 & w_1^9 \\ w_2^7 & w_2^8 & w_2^9 \\ \vdots & \vdots & \vdots \\ w_N^7 & w_N^8 & w_N^9 \end{bmatrix} + \begin{bmatrix} b^7 & b^8 & b^9 \end{bmatrix} = A1W2 + B2$$

(Note:  $a_1^5$  is circled in red in the original image)

af (Activation function)

$$A2 = \begin{bmatrix} a_1^7 & a_1^8 & a_1^9 \\ a_2^7 & a_2^8 & a_2^9 \\ \vdots & \vdots & \vdots \\ a_N^7 & a_N^8 & a_N^9 \end{bmatrix} = af \left[ \begin{bmatrix} z_1^7 & z_1^8 & z_1^9 \\ z_2^7 & z_2^8 & z_2^9 \\ \vdots & \vdots & \vdots \\ z_N^7 & z_N^8 & z_N^9 \end{bmatrix} \right] = af(A2)$$

$$A0 \rightarrow A0W1 + B1 \rightarrow Z1 \rightarrow A1 \rightarrow A1W2 + B2 \rightarrow Z2 \rightarrow A2 \rightarrow A2W3 + B3 \rightarrow Z3 \rightarrow \underline{\underline{A3}}$$

$$Z3 = \begin{bmatrix} z_1^{10} \\ z_2^{10} \\ \vdots \\ z_N^{10} \end{bmatrix} = \begin{bmatrix} a_1^7 & a_1^8 & a_1^9 \\ a_2^7 & a_2^8 & a_2^9 \\ \vdots & \vdots & \vdots \\ a_N^7 & a_N^8 & a_N^9 \end{bmatrix} \begin{bmatrix} w_7^{10} \\ w_8^{10} \\ w_9^{10} \end{bmatrix} + [b_{10}]$$

af (Activation function)

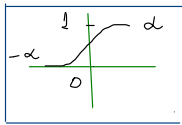
$$A3 = \begin{bmatrix} a_1^{10} \\ a_2^{10} \\ \vdots \\ a_N^{10} \end{bmatrix} = \text{af} \begin{bmatrix} z_1^{10} \\ z_2^{10} \\ \vdots \\ z_N^{10} \end{bmatrix} = \text{af}(A3)$$



## af (Activation Function)

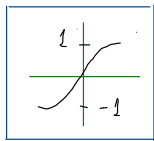
1) Sigmoid

$$af(z) = \sigma(z) = \frac{1}{1 + e^{-z}}$$



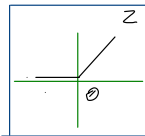
2) Tanh (Hyperbolic Tangent)

$$af(z) = \tanh(z) = \frac{(e^z - e^{-z})}{(e^z + e^{-z})}$$



3) ReLU (Rectified Linear Unit)

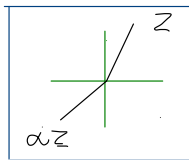
$$af(z) = \begin{cases} 0 & ; z \leq 0 \\ z & ; z > 0 \end{cases}$$



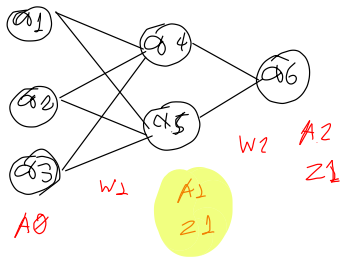
4) PReLU (Parametric Rectified Linear Unit)

$$af(z) = \begin{cases} \alpha z & ; z \leq 0 \\ z & ; z > 0 \end{cases}$$

$\alpha \neq 1$



# Activation function



$$A_1 = Z_1 = A_0 w_1 + b_1$$

$$[a_4 \ a_5] = \left[ \sum_{i=1}^3 a_i w_i^4 + b_4 \quad \sum_{i=1}^3 a_i w_i^5 + b_5 \right]$$

$$A_2 = Z_2 = A_1 w_2 + b_2$$

$$[a_6] = \left[ \sum_{i=4}^5 a_i w_i^6 + b_6 \right]$$

$$= \underline{a_4 w_4^6} + \underline{a_5 w_5^6} + b_6$$

$$\Rightarrow \left( \sum_{i=1}^3 a_i w_i^4 + b_4 \right) w_4^6 + \left( \sum_{i=1}^3 a_i w_i^5 + b_5 \right) w_5^6 + b_6$$

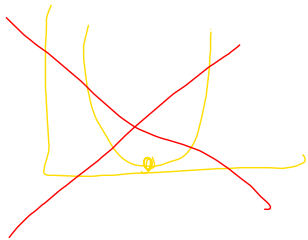
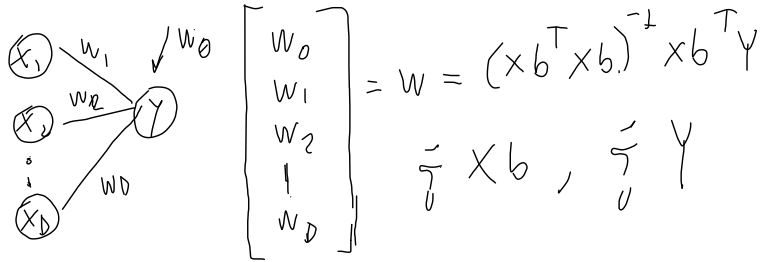
$$(a_1 w_1^4 + a_2 w_2^4 + a_3 w_3^4 + b_4) w_4^6 + (a_1 w_1^5 + a_2 w_2^5 + a_3 w_3^5 + b_5) w_5^6 + b_6$$

$$a_1 (\underline{w_1^4 w_4^6 + w_1^5 w_5^6}) + a_2 (\underline{w_2^4 w_4^6 + w_2^5 w_5^6}) + a_3 (\underline{w_3^4 w_4^6 + w_3^5 w_5^6}) + \underline{b_6}$$

$$\underline{w_1 a_1} + \underline{w_2 a_2} + \underline{w_3 a_3} + \underline{w_0} \rightarrow \underline{\text{Multiple Regression}}$$

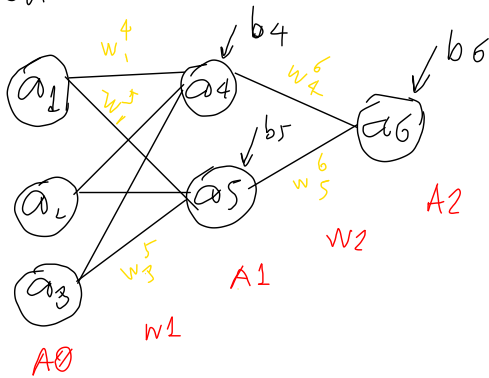
# Neural Network (unlabeled Global)

Review Multiple Regression



# Neural Network (unlabeled Global 12/15)

Review Multiple Regression



$$w_1 = (A_0 b^T A_0 b)^{-1} A_0 b^T A_1$$

$\vec{y} A_0 b, \vec{y} A_1$

$$w_2 = (A_1 b^T A_1 b)^{-1} A_1 b^T A_2$$

$\vec{y} A_1 b, \vec{y} A_2$