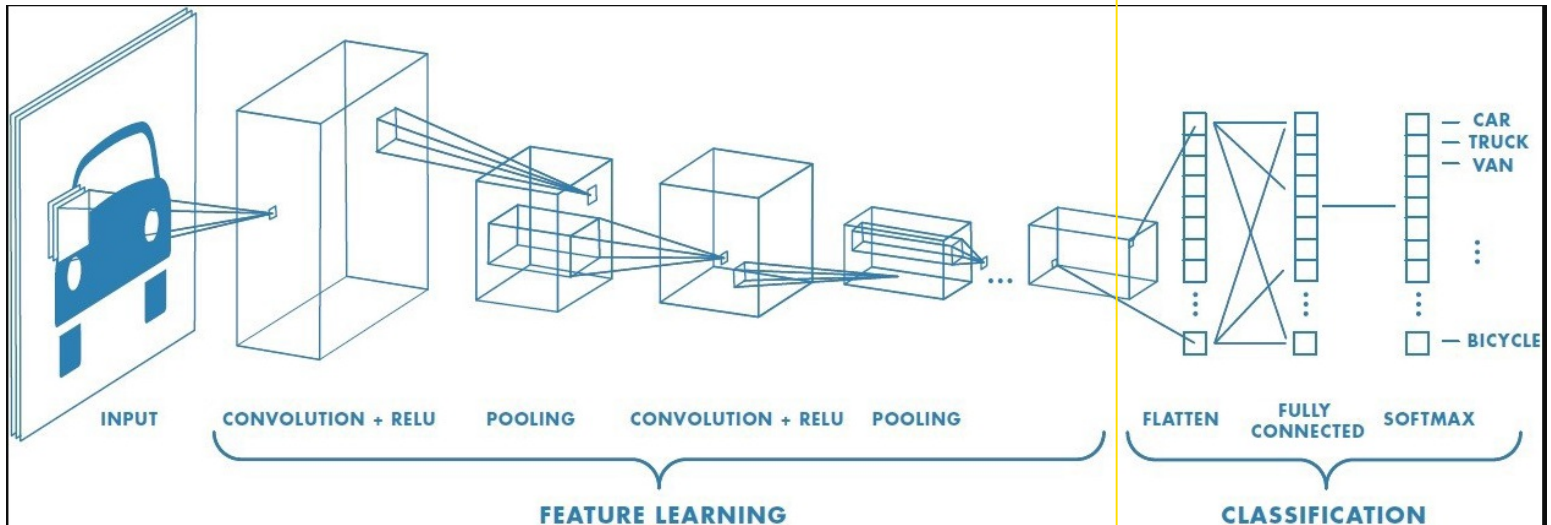


# Convolutional neural network ( CNN )

## Convolutional + neural network



Convolutional

neural network

Convolutional neural network คือ NN ที่ได้รับ input เป็น data ที่ผ่าน convolution มาแล้ว เพื่อตรวจจับ Information ที่สำคัญ (จุดที่สำคัญ หรือ feture)

## ตัวอย่าง Data ที่ผ่าน Convolutional มาแล้ว

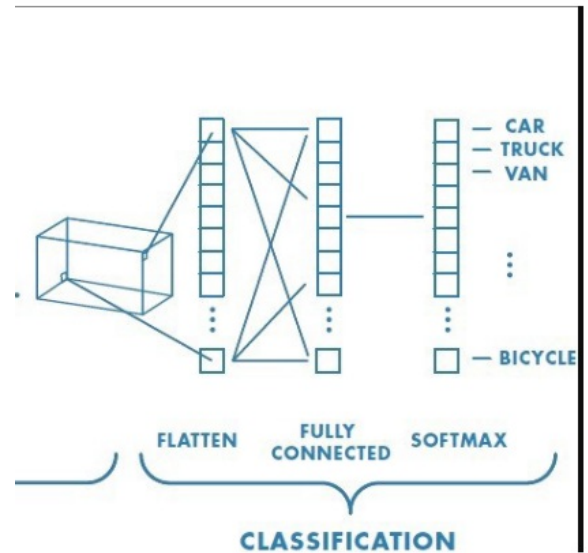
Pixel 1   Pixel 1   Pixel D

รูปที่ 1  
รูปที่ 2  
รูปที่ 3  
รูปที่ N

$$X = \begin{bmatrix} x_1^1 & x_1^2 & \cdots & x_1^D \\ x_2^1 & x_2^2 & \cdots & x_2^D \\ x_3^1 & x_3^2 & \cdots & x_3^D \\ \vdots & \vdots & \ddots & \vdots \\ x_N^1 & x_N^2 & \cdots & x_N^D \end{bmatrix}, Y = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ \vdots \\ y_N \end{bmatrix}$$

car  
Truck  
Bicycle  
N

$x_3^D$  คือ Feature ที่ D ของ Example ที่ 3



neural network

EX input >> conv >> RELU >> pooling >> FC

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0 (3x3x1)

-1	0	1
1	1	-1
1	-1	1

Filter W1 (3x3x1)

-1	1	0
1	-1	-1
-1	0	1

Bias b0 (1x1x1)

0
---

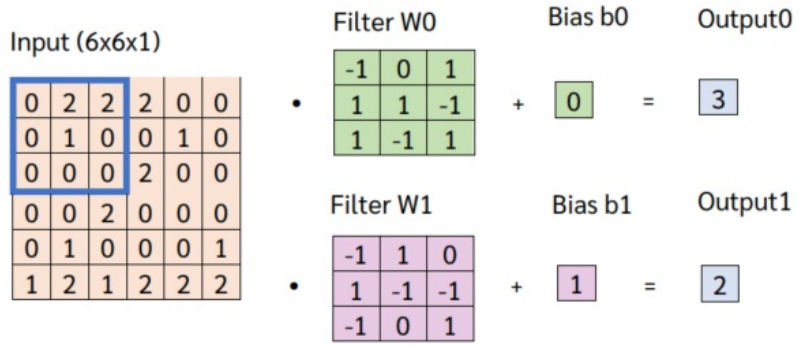
Bias b1 (1x1x1)

1
---

กำหนดให้ strid = 1 (Fiter W0)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

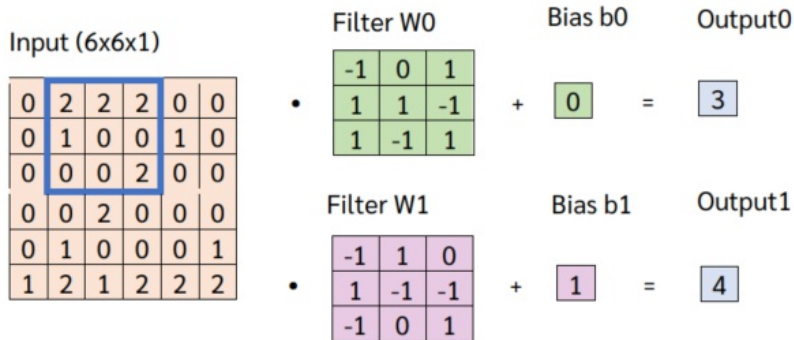
กำหนดให้  $\text{strid} = 1$  (Filter W0)



$$\begin{aligned}
 &(0)(-1) + (2)(0) + (2)(1) + \\
 &(0)(1) + (1)(1) + (0)(-1) + \\
 &(0)(1) + (0)(-1) + (0)(1) = 3 \\
 &\gg 3 + \text{bias}(0) = 3
 \end{aligned}$$


---

$$\begin{aligned}
 &(0)(-1) + (2)(1) + (2)(0) + \\
 &(0)(1) + (1)(-1) + (0)(-1) + \\
 &(0)(-1) + (0)(0) + (0)(1) = 1 \\
 &\gg 1 + \text{bias}(1) = 2
 \end{aligned}$$



$$\begin{aligned}
 &(2)(-1) + (2)(0) + (2)(1) + \\
 &(1)(1) + (0)(1) + (0)(-1) + \\
 &(0)(1) + (0)(-1) + (2)(1) = 3 \\
 &\gg 3 + \text{bias}(0) = 3
 \end{aligned}$$


---

$$\begin{aligned}
 &(2)(-1) + (2)(1) + (2)(0) + \\
 &(1)(1) + (0)(-1) + (0)(-1) + \\
 &(0)(-1) + (0)(0) + (2)(1) = 3 \\
 &\gg 3 + \text{bias}(1) = 4
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

Bias b0

0

Output0

-5

•

+

=

Filter W1

-1	1	0
1	-1	-1
-1	0	1

Bias b1

1

Output1

0

•

+

=

$$\begin{aligned}
 &(2)(-1) + (2)(0) + (0)(1) + \\
 &(0)(1) + (0)(1) + (1)(-1) + \\
 &(0)(1) + (2)(-1) + (0)(1) = -5 \\
 &>> -5 + \text{bias}(0) = -5
 \end{aligned}$$


---

$$\begin{aligned}
 &(2)(-1) + (2)(1) + (0)(0) + \\
 &(0)(1) + (0)(-1) + (1)(-1) + \\
 &(0)(-1) + (2)(0) + (0)(1) = -1 \\
 &>> -1 + \text{bias}(1) = 3
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

Bias b0

0

Output0

1

•

+

=

Filter W1

-1	1	0
1	-1	-1
-1	0	1

Bias b1

1

Output1

-4

•

+

=

$$\begin{aligned}
 &(2)(-1) + (0)(0) + (0)(1) + \\
 &(0)(1) + (1)(1) + (0)(-1) + \\
 &(2)(1) + (0)(-1) + (0)(1) = 1 \\
 &>> 1 + \text{bias}(0) = 1
 \end{aligned}$$


---

$$\begin{aligned}
 &(2)(-1) + (0)(1) + (0)(0) + \\
 &(0)(1) + (1)(-1) + (0)(-1) + \\
 &(2)(-1) + (0)(0) + (0)(1) = -5 \\
 &>> -5 + \text{bias}(1) = -4
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

•

Bias b0

+

0

=

2

Output0

Filter W1

-1	1	0
1	-1	-1
-1	0	1

•

Bias b1

+

1

=

4

Output1

$$\begin{aligned}
 &(0)(-1) + (1)(0) + (0)(1) + \\
 &(0)(1) + (0)(1) + (0)(-1) + \\
 &(0)(1) + (0)(-1) + (2)(1) = 2 \\
 &>> 2 + \text{bias}(0) = 2
 \end{aligned}$$


---

$$\begin{aligned}
 &(0)(-1) + (1)(1) + (0)(0) + \\
 &(0)(1) + (0)(-1) + (0)(-1) + \\
 &(0)(-1) + (0)(0) + (2)(1) = 3 \\
 &>> 3 + \text{bias}(1) = 4
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

•

Bias b0

+

0

=

-5

Output0

Filter W1

-1	1	0
1	-1	-1
-1	0	1

•

Bias b1

+

1

=

-2

Output1

$$\begin{aligned}
 &(1)(-1) + (0)(0) + (0)(1) + \\
 &(0)(1) + (0)(1) + (2)(-1) + \\
 &(0)(1) + (2)(-1) + (0)(1) = -5 \\
 &>> -5 + \text{bias}(0) = -5
 \end{aligned}$$


---

$$\begin{aligned}
 &(1)(-1) + (0)(1) + (0)(0) + \\
 &(0)(1) + (0)(-1) + (2)(-1) + \\
 &(0)(-1) + (2)(0) + (0)(1) = -3 \\
 &>> -3 + \text{bias}(1) = -2
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

Bias b0

0

Output0

5

Filter W1

-1	1	0
1	-1	-1
-1	0	1

Bias b1

1

Output1

-3

$$\begin{aligned}
 &(0)(-1) + (0)(0) + (1)(1) + \\
 &(0)(1) + (2)(1) + (0)(-1) + \\
 &(2)(1) + (0)(-1) + (0)(1) = -5 \\
 &>> -5 + \text{bias}(0) = -5
 \end{aligned}$$


---

$$\begin{aligned}
 &(0)(-1) + (0)(1) + (1)(0) + \\
 &(0)(1) + (2)(-1) + (0)(-1) + \\
 &(2)(-1) + (0)(0) + (0)(1) = -4 \\
 &>> -4 + \text{bias}(1) = -3
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

Bias b0

0

Output0

-3

Filter W1

-1	1	0
1	-1	-1
-1	0	1

Bias b1

1

Output1

-1

$$\begin{aligned}
 &(0)(-1) + (0)(0) + (0)(1) + \\
 &(0)(1) + (0)(1) + (2)(-1) + \\
 &(0)(1) + (1)(-1) + (0)(1) = -3 \\
 &>> -3 + \text{bias}(0) = -3
 \end{aligned}$$


---

$$\begin{aligned}
 &(0)(-1) + (0)(1) + (0)(0) + \\
 &(0)(1) + (0)(-1) + (2)(-1) + \\
 &(0)(-1) + (1)(0) + (0)(1) = -2 \\
 &>> -2 + \text{bias}(1) = -1
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

• Filter W0

-1	0	1
1	1	-1
1	-1	1

+ Bias b0

0
---

= Output0

5
---

• Filter W1

-1	1	0
1	-1	-1
-1	0	1

+ Bias b1

1
---

= Output1

-2
----

$$(0)(-1) + (0)(0) + (2)(1) + (0)(1) + (2)(1) + (0)(-1) + (1)(1) + (0)(-1) + (0)(1) = 5$$

>> 5 + bias(0) = 5

---

$$(0)(-1) + (0)(1) + (2)(0) + (0)(1) + (2)(-1) + (0)(-1) + (1)(-1) + (0)(0) + (0)(1) = -3$$

>> -3 + bias(1) = -2

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

• Filter W0

-1	0	1
1	1	-1
1	-1	1

+ Bias b0

0
---

= Output0

2
---

• Filter W1

-1	1	0
1	-1	-1
-1	0	1

+ Bias b1

1
---

= Output1

5
---

$$(0)(-1) + (2)(0) + (0)(1) + (2)(1) + (0)(1) + (0)(-1) + (0)(1) + (0)(-1) + (0)(1) = 2$$

>> 2 + bias(0) = 2

---

$$(0)(-1) + (2)(1) + (0)(0) + (2)(1) + (0)(-1) + (0)(-1) + (0)(-1) + (0)(0) + (0)(1) = 4$$

>> 4 + bias(1) = 5



Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

Bias b0

0

Output0

-1

•

+

=

Filter W1

-1	1	0
1	-1	-1
-1	0	1

Bias b1

1

Output1

0

•

+

=

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

Bias b0

0

Output0

3

•

+

=

Filter W1

-1	1	0
1	-1	-1
-1	0	1

Bias b1

1

Output1

0

•

+

=

$$\begin{aligned}
 &(2)(-1) + (0)(0) + (0)(1) + \\
 &(0)(1) + (0)(1) + (0)(-1) + \\
 &(0)(1) + (0)(-1) + (1)(1) = -1 \\
 &>> -1 + \text{bias}(0) = -1
 \end{aligned}$$


---

$$\begin{aligned}
 &(2)(-1) + (0)(1) + (0)(0) + \\
 &(0)(1) + (0)(-1) + (0)(-1) + \\
 &(0)(-1) + (0)(0) + (1)(1) = -1 \\
 &>> -1 + \text{bias}(1) = 0
 \end{aligned}$$


---

$$\begin{aligned}
 &(0)(-1) + (0)(0) + (2)(1) + \\
 &(0)(1) + (1)(1) + (0)(-1) + \\
 &(1)(1) + (2)(-1) + (1)(1) = 3 \\
 &>> 3 + \text{bias}(0) = 3
 \end{aligned}$$


---

$$\begin{aligned}
 &(0)(-1) + (0)(1) + (2)(0) + \\
 &(0)(1) + (1)(-1) + (0)(-1) + \\
 &(1)(-1) + (2)(0) + (1)(1) = -1 \\
 &>> -1 + \text{bias}(1) = 0
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

•

Bias b0

0
---

+

Output0

4
---

Filter W1

-1	1	0
1	-1	-1
-1	0	1

•

Bias b1

1
---

+

Output1

4
---

$$\begin{aligned}
 &(0)(-1) + (2)(0) + (0)(1) + \\
 &(1)(1) + (0)(1) + (0)(-1) + \\
 &(2)(1) + (1)(-1) + (2)(1) = 4 \\
 &>> 4 + \text{bias}(0) = 4
 \end{aligned}$$


---

$$\begin{aligned}
 &(0)(-1) + (2)(1) + (0)(0) + \\
 &(1)(1) + (0)(-1) + (0)(-1) + \\
 &(2)(-1) + (1)(0) + (2)(1) = 3 \\
 &>> 3 + \text{bias}(1) = 4
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

•

Bias b0

0
---

+

Output0

-1
----

Filter W1

-1	1	0
1	-1	-1
-1	0	1

•

Bias b1

1
---

+

Output1

0
---

$$\begin{aligned}
 &(2)(-1) + (0)(0) + (0)(1) + \\
 &(0)(1) + (0)(1) + (0)(-1) + \\
 &(1)(1) + (2)(-1) + (2)(1) = -1 \\
 &>> -1 + \text{bias}(0) = -1
 \end{aligned}$$


---

$$\begin{aligned}
 &(2)(-1) + (0)(1) + (0)(0) + \\
 &(0)(1) + (0)(-1) + (0)(-1) + \\
 &(1)(-1) + (2)(0) + (2)(1) = -1 \\
 &>> -1 + \text{bias}(1) = 0
 \end{aligned}$$

Input (6x6x1)

0	2	2	2	0	0
0	1	0	0	1	0
0	0	0	2	0	0
0	0	2	0	0	0
0	1	0	0	0	1
1	2	1	2	2	2

Filter W0

-1	0	1
1	1	-1
1	-1	1

•

+

Bias b0

0
---

=

Output0

1
---

Filter W1

-1	1	0
1	-1	-1
-1	0	1

•

+

Bias b1

1
---

=

Output1

0
---

$$\begin{aligned}
 &(0)(-1) + (0)(0) + (0)(1) + \\
 &(0)(1) + (0)(1) + (1)(-1) + \\
 &(2)(1) + (2)(-1) + (2)(1) = 1 \\
 &\gg 1 + \text{bias}(0) = 1
 \end{aligned}$$

$$\begin{aligned}
 &(0)(-1) + (0)(1) + (0)(0) + \\
 &(0)(1) + (0)(-1) + (1)(-1) + \\
 &(2)(-1) + (2)(0) + (2)(1) = -1 \\
 &\gg -1 + \text{bias}(1) = 0
 \end{aligned}$$

Output (4x4x2)

output0

3	3	-5	1
2	-5	5	2
-3	5	2	-1
3	4	-1	1

output1

2	4	0	-4
4	-2	-3	4
-1	-2	5	0
0	4	0	0

สูตรหา shape output

$$[(N-F)/S] + 1$$

$$[(6-3)/1] + 1 = 4$$

- N = input size

- F = filter

- S = stride

## ReLU Function

น้อยกว่า 0 ให้เท่ากับ 0

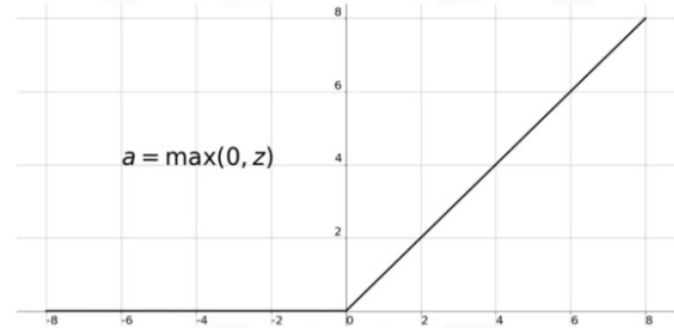
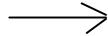
Output (4x4x2)

output0

3	3	-5	1
2	-5	5	2
-3	5	2	-1
3	4	-1	1

output1

2	4	0	-4
4	-2	-3	4
-1	-2	5	0
0	4	0	0



การคำนวณ ReLU

output0 = max(0, input0)

output1 = max(0, input1)

Output (4x4x2)

output0

3	3	0	1
2	0	5	2
0	5	2	0
3	4	0	1

output1

2	4	0	0
4	0	0	4
0	0	5	0
0	4	0	0

### ขั้นตอนที่ 3: Pooling Layer

- max pooling
- Average pooling
- min pooling

กำหนดให้เป็น Max Pooling และค่า hyperparameters เป็นดังนี้

- Filter size = 2x2
- Stride = 2
- Zero padding = 1

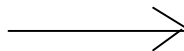
Input (4x4x2)

input0

3	3	0	1
2	0	5	2
0	5	2	0
3	4	0	1

input1

2	4	0	0
4	0	0	4
0	0	5	0
0	4	0	0



การคำนวณ Pooling Layer

input0

3	3	0	1
2	0	5	2
0	5	2	0
3	4	0	1

=>

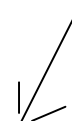
3	5
5	2

input1

2	4	0	0
4	0	0	4
0	0	5	0
0	4	0	0

=>

4	4
4	5



Output (2x2x2)

output0

3	5
5	2

output1

4	4
4	5

## Zero(0/1) Padding (เพิ่มขนาด Input)

เช่น Input เดิมเป็น 5x5

0	0	0	0	0	0	0
0	2	4	9	1	4	0
0	2	1	4	4	6	0
0	1	1	2	9	2	0
0	7	3	5	1	3	0
0	2	3	4	8	5	0
0	0	0	0	0	0	0

Image

X

1	2	3
-4	7	4
2	-5	1

Filter /  
Kernel

=

21	59	37	-19	2
30	51	66	20	43
-14	31	49	101	-19
59	15	53	-2	21
49	57	64	76	10

Feature

Padding Input กลายเป็น 7x7

สูตรหา shape output

$$[(N-F)/S] + 1$$

$$[(7-3)/1] + 1 = 5$$

- N = input size
- F = filter
- S = strid

สูตรหา shape output

$$[(N + 2P - F)/S] + 1$$

$$[(5 + (2*1) - 3)/1] + 1 = 5$$

- N = input size (เดิม)
- P =padding
- F = filter
- S = strid

```

import torch.nn as nn
import torch.nn.functional as F

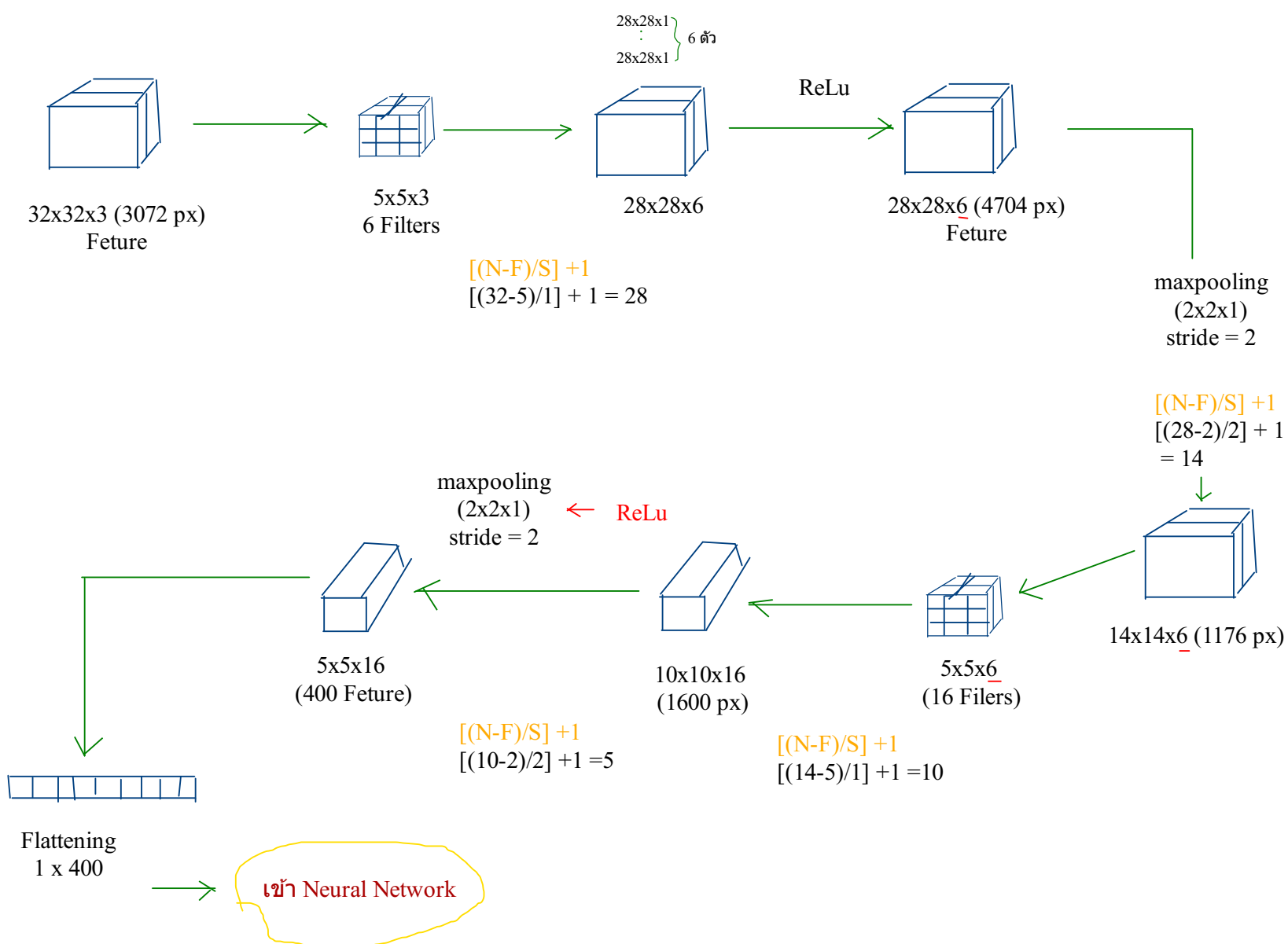
class Net(nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        self.conv1 = nn.Conv2d(3, 6, 5)
        self.pool = nn.MaxPool2d(2, 2)
        self.conv2 = nn.Conv2d(6, 16, 5)
        self.fc1 = nn.Linear(16 * 5 * 5, 120)
        self.fc2 = nn.Linear(120, 84)
        self.fc3 = nn.Linear(84, 10)

    def forward(self, x):
        x = self.pool(F.relu(self.conv1(x)))
        x = self.pool(F.relu(self.conv2(x)))
        x = x.view(-1, 16 * 5 * 5)
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x

net = Net()

device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
net.to(device)

```





## เข้า Neural Network

