

Mostre também que

$$\|E_{k,l}\|^2 = (E_{k,l}, E_{k,l}) = m \cdot n$$

$$\begin{aligned} (E_{k,l}, E_{k,l}) &= \sum_{r=0}^{m-1} \sum_{s=0}^{n-1} e^{i2\pi \left(\frac{k_r}{m} + \frac{l_s}{n} \right)} \cdot \overline{e^{i2\pi \left(\frac{k_r}{m} + \frac{l_s}{n} \right)}} \\ &= \sum_{r=0}^{m-1} \sum_{s=0}^{n-1} e^{i2\pi \left(\frac{k_r^0 - k_r}{m} + \frac{l_s^0 - l_s}{n} \right)} = e^0 = 1 \\ &= \sum_{r=0}^{m-1} \sum_{s=0}^{n-1} 1 = m \cdot n \end{aligned}$$