

# Direction of Innovation

Diomides Mavroyiannis

PSL/Paris Dauphine

July 10, 2019

## Introduction

- Motivation
- Literature review
- Assumptions
  - Technology
  - Sequential
  - Technology
- A priori buyout

## Bertrand

- Sequential
- Radical
- Results
- Example

## Cournot

- Sequential
- Radical
- Results
- Bertrand vs Cournot  
without buyout

## Welfare

- Policy implications

**Definition:** A buyout will be used to refer to the purchase of technological assets

Buyouts are prevalent, the basic effect of buyouts is that they decrease the price elasticity of the market.

From an economic theory point of view, buyouts are a double edged sword.

**Positive:** Increase potential payoff for entrepreneurs, more projects undertaken, more innovation

**Negative:** Increases monopoly power

Sometimes buyouts can occur without these side effects, value buyers.

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

Empirically firms which are less innovative are more likely to engage in buyouts. Higgins and Rodriguez (2006) and Zhao (2009)

Coase theorem works here because substitutability can be framed in terms of externalities. See Kuechle & Rios (2012)

Large firms avoid engaging in competition effects, Aghion (2005)

Cabal (2003) has an R&D race where two firms choose R&D technologies.

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

# Firms and cost structure

Direction of  
innovation

Diomides  
Mavroyiannis

There are two firms, an entrant( $c_e$ ) and incumbent( $c_i$ ) competition

Two potential future costs: intermediate  $c_1$  and advanced  $c_2$

Firms only use the best technology available to them. Incumbent technology is only inferior to the advanced tech.  $\pi_i(c_i, c_{e2}) > \pi_i(c_{i1}, c_{e2})$

The entrant technology is inferior to both other technologies.  $\pi_e(c_i, c_{e1}) > \pi_i(c_i, c_e)$

## Timing:

Negotiation  $\rightarrow$  Incumbent chooses  $\rightarrow$  competition(a priori) Entrant chooses  $\rightarrow$  negotiation  $\rightarrow$  competition(a posteriori)

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

# Sub-additive competitive profits

Direction of  
innovation

Diomides  
Mavroyiannis

Monopoly assumption

Pesky Entrant

$$\pi_i(c_{i2}, c_e) \geq \pi_i(c_i, c_{e2}) + \pi_e(c_i, c_{e2})$$

$$\pi_i(c_i, c_e) \geq \pi_i(c_i, c_{e1}) + \pi_e(c_i, c_{e1})$$

## Introduction

Motivation

Literature review

**Assumptions**

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

### Entrant payoff:

$$\pi_e(c_i, c_{i1})(t_2 - t_1) + \pi_e(c_i, c_{e2})(T + 1 - t_2)$$

### Incumbent payoff:

$$\pi_i(c_i, c_e)t_1 + \pi_i(c_i, c_{i1})(t_2 - t_1) + \pi_i(c_i, c_{e2})(T + 1 - t_2)$$

### Monopoly payoff:

$$\pi_i(c_i, c_e)t_2 + \pi_i(c_{i2}, c_e)(T + 1 - t_2)$$

# Sequential

Direction of  
innovation

Diomides  
Mavroyiannis

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

$$WTP = \Pi_s^m - \Pi_{is} = (\pi_i(c_i, c_e) - \pi_i(c_i, c_{i1}))(t_2 - t_1) + (\pi_i(c_{i2}, c_e) - \pi_i(c_i, c_{i1}) - \pi_e(c_i, c_{i1}))(t_2 - t_1) + (\pi_i(c_{i2}, c_e) - \pi_i(c_i, c_{e2}))$$

The sequential technology takes two periods to innovate. In the first period the entrants cost is  $c_1$  and in the second it is  $c_2$

In the radical technology, with probability  $q$ , the cost will be  $c_2$  in the first period.

If the technology fails then with probability  $q$  it will succeed in the second period.

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications



## A priori cutoff

If the buyouts are priori, the decision criteria for the radical innovation to be chosen by the incumbent is:

$$\frac{3 - \sqrt{5}}{2} < q^p$$

## Proof.

We need only set:

$$\begin{aligned} \Pi_{IR}^m &> \Pi_{IS}^m \\ \pi_i^m(1-q)(2-q) + \pi_{i2}^m q(3-q) &> \pi_i^m + \pi_{i2}^m \end{aligned}$$



## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

# Bertrand: Sequential

Direction of  
innovation

Diomides  
Mavroyannis

The market profits of the incumbent in the sequential technology case is:

$$\bar{\Pi}_{IS} = \pi_{i1} = (1 - c_{i1})(c_{i1} - c_i)$$

The market payoffs of the entrant

$$\bar{\Pi}_{ES} = \pi_{e2} = (1 - c_i)(c_i - c_{e2})$$

The monopoly profit of the incumbent with a buyout is

$$\Pi_{IS} = \pi_i + \pi_{i2}$$

Therefore the bargaining payoff if there is a buyout of the entrant is:

$$B_{ES}(\omega) = \pi_{e2}(1 - \omega) + \omega(\pi_i + \pi_{i2} - \pi_{i1})$$

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

# Model: Sequential 2

Direction of  
innovation

Diomides  
Mavroyiannis

We can also compute the difference between the entrant buyout profits to the non-buyout profits as

$$B_{ES}(\omega) - \bar{\Pi}_{ES} = \omega(\pi_i + \pi_{i2} - \pi_{i1} - \pi_{e2})$$

This is the incentive effect of buyouts

Note the effect of bargaining power.

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

# Model: Radical

Direction of  
innovation

Diomides  
Mavroyiannis

The market profits of the incumbent in the radical technology case is:

$$\bar{\Pi}_{IR} = (1 - q)(2 - q)\pi_i$$

The market payoffs of the entrant

$$\bar{\Pi}_{ER} = q2\pi_{e2} + (1 - q)q\pi_{e2} = q\pi_{e2}(3 - q)$$

The market profits of the incumbent with a buyout is

$$\Pi_{IR} = \pi_i(1 - q)(2 - q) + \pi_{i2}q(3 - q)$$

Therefore the bargaining payoff if there is a buyout of the entrant is:

$$B_{ER}(\omega) = (3 - q)q(\pi_{e2} + \omega(\pi_{i2} - \pi_{e2}))$$

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

Incentive effect of the buyout is therefore:

$$B_{ER} - \bar{\Pi}_{ER} = \omega(3 - q)q(\pi_{i2} - \pi_{e2})$$

Notice that once again this heavily depends on bargaining power\*

## Proposition 1

The entrant will choose the radical innovation over the incremental innovation if there are no buyout iff:

$$\pi_{e2}(q(3-q)-1) + k_S - k_R > 0$$

This is found simply by setting:

$$\bar{\Pi}_{ER} - k_R > \bar{\Pi}_{ES} - k_S$$

### Introduction

- Motivation
- Literature review
- Assumptions
  - Technology
  - Sequential
  - Technology
- A priori buyout

### Bertrand

- Sequential
- Radical
- Results**
- Example

### Cournot

- Sequential
- Radical
- Results**
  - Bertrand vs Cournot without buyout

### Welfare

- Policy implications

# Corollary 1

Direction of  
innovation

Diomides  
Mavroyiannis

## Cutoff probability

If costs are identical then the required  $q$  for the radical innovation to preferred is given by:

$$q > \frac{3 - \sqrt{5}}{2} = q^b$$

### Introduction

Motivation  
Literature review  
Assumptions  
Technology  
Sequential  
Technology  
A priori buyout

### Bertrand

Sequential  
Radical  
**Results**  
Example

### Cournot

Sequential  
Radical  
Results  
Bertrand vs Cournot  
without buyout

### Welfare

Policy implications

## Proposition 2

If costs are identical then a buyout will necessarily require a higher  $q^{b*}$  than  $q^b$  to incite the entrant to pursue the radical innovation.

This follows by setting

$$\begin{aligned} B_{ER}(\omega) - k_R &> B_{ES}(\omega) - k_S \\ \rightarrow (1 - \omega)\pi_{e2}(q(3 - q) - 1) + \omega\pi_{i2}(q(3 - q) - 1) \\ &\quad - \omega(\pi_i - \pi_{i1}) > 0 \end{aligned}$$

Note that the third term is negative,  $-\omega(\pi_i - \pi_{i1})$ , which implies higher  $q$

### Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

### Bertrand

Sequential

Radical

**Results**

Example

### Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

### Welfare

Policy implications



# Example

Direction of  
innovation

Diomides  
Mavroyiannis

Let  $\pi_{e2} = 40$ ,  $\pi_{i2} = 100$ ,  $\pi_{e1} = 20$ ,  $\pi_i = 80$ .  
 $\omega = .5$ ,  $q = 0.5$

**No buyouts Sequential:** Entrant earns 40. **Radical**  
entrant earns  $.5(40 + 40) + (.5)^2(40) = 50$ .  
Radical > Sequential

**Buyouts, Sequential bargaining surplus:**

$NS_S = 100 + 80 - 20 - 40 = 120$ . Therefore the payoff  
of the entrant is  $40 + \frac{1}{2}(120) = 100$ .

**Radical innovation surplus:**

$.5(200) + (.5)^2 180 + (.5)^2 160 - (.5)^2 80 - (.5)^2 - 50 = 75$ .

Therefore the payoff after bargaining is

$50 + \frac{1}{2}(75) = 87.5$

Sequential > Radical

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

The market profits of the incumbent in the sequential technology case is:

$$\bar{\Pi}_{ES} = \left( \frac{1 - 2c_{i1} + c_i}{3} \right)^2 + \left( \frac{1 - 2c_{i2} + c_i}{3} \right)^2$$

The market payoffs of the entrant

$$\bar{\Pi}_{IS} = \left( \frac{1 + c_{i1} - 2c_i}{3} \right)^2 + \left( \frac{1 + c_{i2} - 2c_i}{3} \right)^2$$

The monopoly profit is unchanged relative to Bertrand

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

The Nash surplus is given by:

$$NS_S^c = \pi^m + \pi_2^m - \pi_{i1}^c - \pi_{i2}^c - \pi_{e1}^c - \pi_{e2}^c$$

The Bargaining payoff of the entrant is:

$$B_{ES}^c = \Pi_{ES}^c + \omega NS_S^c$$

The bargaining payoff of the incumbent is:

$$B_{IS}^c = \Pi_{IS}^c + (1 - \omega) NS_S^c$$

## Introduction

- Motivation
- Literature review
- Assumptions
- Technology
- Sequential
- Technology
- A priori buyout

## Bertrand

- Sequential
- Results
- Example

## Cournot

- Sequential
- Radical
- Results
- Bertrand vs Cournot  
without buyout

## Welfare

- Policy implications

The market profits of the incumbent in the radical technology case is:

$$\bar{\Pi}_{IR} = (1 - q)(2 - q)\pi^m + q\pi_{i1}^c(3 - q)$$

The market payoffs of the entrant

$$\bar{\Pi}_{ER} = q\pi_{e2}^c(3 - q)$$

The monopoly profits are given by:

$$\Pi_R^m = \pi^m(1 - q)(2 - q) + \pi_2^m q(3 - q)$$

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

The Nash surplus is given by:

$$\begin{aligned} NS_R^c &= \pi^m(1-q)(2-q) + \pi_2^m q(3-q) - \Pi_{IR}^c - \Pi_{ER}^c \\ &= q(3-q)(\pi_2^m - \pi_{e2}^c - \pi_{i1}^c) \end{aligned}$$

The Bargaining payoff of the entrant is:

$$B_{ER}^c = \Pi_{ER}^c + \omega NS_R^c$$

The bargaining payoff of the incumbent is:

$$B_{IR}^c = \Pi_{IR}^c + (1-\omega) NS_R^c$$

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

# Cournot no buyout cutoff

Direction of  
innovation

Diomides  
Mavroyiannis

## Cournot Cutoff preferences

The cutoff point for the entrant to prefer the radical innovation without buyouts is given by:

$$\frac{3}{2} - \frac{\sqrt{5\pi_{e2}^c - 4\pi_{e1}^c}}{2\sqrt{\pi_{e2}^c}} = q^c$$

Proof:

$$\begin{aligned} \pi_{ER}^c &> \pi_{ES}^c \\ q\pi_{e2}^c(3-q) &> \pi_{e1}^c + \pi_{e2}^c \\ q &> \frac{3\pi_{e2}^c - \sqrt{\pi_{e2}^c}\sqrt{5\pi_{e2}^c - 4\pi_{e1}^c}}{2\pi_{e2}^c} \end{aligned}$$

### Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

### Bertrand

Sequential

Radical

Results

Example

### Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

### Welfare

Policy implications

# With buyout cutoff point

Direction of  
innovation

Diomides  
Mavroyiannis

## Cutoff with buyouts

With buyouts, the cutoff efficiency of the radical innovation for it to be pursued is lower in Cournot competition than in Bertrand

### Introduction

- Motivation
- Literature review
- Assumptions
- Technology
- Sequential
- Technology
- A priori buyout

### Bertrand

- Sequential
- Radical
- Results
- Example

### Cournot

- Sequential
- Radical

### Results

- Bertrand vs Cournot  
without buyout

### Welfare

- Policy implications

# Bertrand vs Cournot

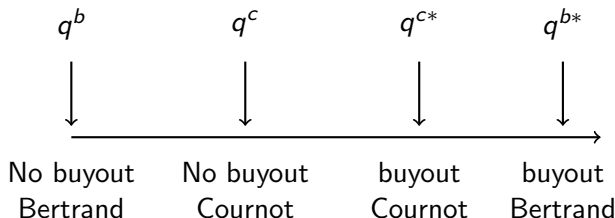
Direction of  
innovation

Diomides  
Mavroyiannis

## Cournot radical preferences entail Bertrand

Without buyouts, if the radical innovation is preferred in Cournot competition, it is also preferred in Bertrand.

We note that  $q^c$  cutoff is strictly increasing in  $\pi_{e1}^c$  and that if  $\pi_{e1}^c = 0$  we have the Bertrand payoff.



### Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

### Bertrand

Sequential

Radical

Results

Example

### Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

### Welfare

Policy implications



## Welfare proposition

The cutoff point for welfare to be maximized by radical innovation with buyouts,  $q^{w*}$  is the same as the a priori cutoff point,  $q^*$  and the posterior no buyout cutoff point,  $q^b$

This follows by setting:

$$W_R > W_S \rightarrow w_{m2}(3q - q^2 - 1) - w_{m1}(3q - q^2 - 1) > 0$$

### Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

### Bertrand

Sequential

Radical

Results

Example

### Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

### Welfare

Policy implications

# Conclusive comments

Direction of  
innovation

Diomides  
Mavroyiannis

Allowing buyouts has distortion effects on the market if the entrant has bargaining power

Therefore any cost benefit analysis that evaluates the effects of buyouts should include the costs and benefits of industry diversification

Intellectual property may cause industry convergence

Convergence effect vs a divergence effect

## Introduction

Motivation  
Literature review  
Assumptions  
Technology  
Sequential  
Technology  
A priori buyout

## Bertrand

Sequential  
Radical  
Results  
Example

## Cournot

Sequential  
Radical  
Results  
Bertrand vs Cournot  
without buyout

## Welfare

Policy implications

## Introduction

Motivation

Literature review

Assumptions

Technology

Sequential

Technology

A priori buyout

## Bertrand

Sequential

Radical

Results

Example

## Cournot

Sequential

Radical

Results

Bertrand vs Cournot  
without buyout

## Welfare

Policy implications