Jacobian_approach(analytical)_old

January 12, 2024

1 Determine Jacobinas(DelI for Del TMP) Analytically and Plot Them

2 Values Ranges Used in Simulation (New)

Variable	Range(lower)	Range(Upper)	Point Count
Materna Sturation	0.9	1.0	5
Maternal Hb Conc	11	15	5
Fetal Saturation	0.2	0.6	5
Fetal Hb Conc	11	15	5
Maternal BVF	0.2		
Fetal BVF	0.22		

3 Values Ranges Used in Simulation (old)

Variable	Range(lower)	Range(Upper)	Point Count
Materna Sturation	0.9	1.0	5
Maternal Hb Conc	11	15	5
Fetal Saturation	0.1	0.6	5
Fetal Hb Conc	0.11	0.15	5

[ ]:
```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
from inverse_modelling_tfo.tools.name_decoder import decode_extended_filename
from inverse_modelling_tfo.tools.s_based_intensity_datagen import MU_MAP_BASE1,␣
↪MU_MAP_BASE2, get_mu_a
from tfo_sensitivity.data import load_raw
from tfo_sensitivity.jacobian import FullBloodAnalyticalJC,␣
↪FullBloodJacobianMuAEqn, PartialBloodAnalyticalJC, PartialBloodJacobianMuAEqn
from tfo_sensitivity.jacobian import calculate_jacobian
```

```python
# Plotting
FIG_WIDTH = 8
FIG_HEIGHT = 4
plt.style.use('seaborn')
# plt.rcParams['figure.dpi'] = 150    # Smaller plot
plt.rcParams['figure.dpi'] = 700    # Paper-ready plots

# Loading Files
maternal_wall_thickness, uterus_thickness, wave_int = 20, 5, 1
raw_sim_data_path = load_raw(maternal_wall_thickness, uterus_thickness,␣
 ↪wave_int)
raw_sim_data = pd.read_pickle(raw_sim_data_path)
base_mu_map = MU_MAP_BASE1 if wave_int == 1 else MU_MAP_BASE2

# Create SDD column
raw_sim_data['SDD'] = raw_sim_data['X'] - 100
all_sdd = raw_sim_data['SDD'].unique()
```

4 Defining Base Parameters

```
[ ]: # Base Parameters
MATERNAL_Hb = 2.
MATERNAL_SAT = 1.0
FETAL_SAT = 0.225
FETAL_Hb = 0.9
# FETAL_Hb = 11.0

# Sweep Parameters
all_fetal_c = np.linspace(11, 16, 6)
all_fetal_sat = np.linspace(0.1, 0.6, 6)

PLOT_NORMALIZED = True  # Plot the Jacibian divided by Current Intensity␣
↪(Similar to normalized derivative)

# Jacobian Calculator
mu_a_eqn = FullBloodJacobianMuAEqn()    # How the mu_a is calculated for Fetal/
↪Maternal variable layers
JCClass = FullBloodAnalyticalJC

# mu_a_eqn = PartialBloodJacobianMuAEqn(0.2, 0.22)    # How the mu_a is␣
↪calculated for Fetal/Maternal variable layers
# JCClass = PartialBloodAnalyticalJC

# SDD
sdd_indices = np.arange(2, 20, 2) # Which detectors to calculate (2-20, every␣
↪2, for Faster plotting)
```

5 Calculating Derivatives

```
[ ]: data_table = pd.DataFrame(columns=['Saturation', 'Derivative', 'SDD', 'Type']) ␣
↪# Types = 1, 2, 3, 4

# Comment on Types: 1 & 2 : delI/delFS, 3 & 4 : delI/delFC
# Types 1 & 3: Fetal Sat varies, Types 2 & 4: Fetal Conc varies

for sdd_index in sdd_indices:
    SDD = all_sdd[sdd_index]
    filtered_photon_data  = (raw_sim_data[raw_sim_data["SDD"] == SDD]).copy()

    # Round 1 - Plots for Varying Fetal Saturation (type 1 & 3)
    for fs in all_fetal_sat:
        fs = round(fs, 2)       # np.range sometimes creates weird numbers...␣
↪round to 2 decimal places
        AnalyticalJC = JCClass(filtered_photon_data, sdd_index, base_mu_map,␣
↪'FS', MATERNAL_Hb, MATERNAL_SAT, FETAL_Hb, fs, wave_int, mu_a_eqn,␣
↪PLOT_NORMALIZED)
```

```
        analytical_term1 = AnalyticalJC.calculate_jacobian()

        AnalyticalJC = JCClass(filtered_photon_data, sdd_index, base_mu_map,␣
↪'FC', MATERNAL_Hb, MATERNAL_SAT, FETAL_Hb, fs, wave_int, mu_a_eqn,␣
↪PLOT_NORMALIZED)
        analytical_term3 = AnalyticalJC.calculate_jacobian()


        # Adding to Table
        new_row1 = {'Saturation' : fs, 'Derivative': analytical_term1, 'SDD':␣
↪all_sdd[sdd_index], 'Type': 1}
        new_row2 = {'Saturation' : fs, 'Derivative': analytical_term3, 'SDD':␣
↪all_sdd[sdd_index], 'Type': 3}
        data_table.loc[len(data_table)] = new_row1
        data_table.loc[len(data_table)] = new_row2

    # Round 2 - Plots for Varying Fetal Concentration (type 2 & 4)
    for fc in all_fetal_c:
        fc = round(fc, 2)        # np.range sometimes creates weird numbers...␣
↪round to 2 decimal places
        AnalyticalJC = JCClass(filtered_photon_data, sdd_index, base_mu_map,␣
↪'FS', MATERNAL_Hb, MATERNAL_SAT, fc, FETAL_SAT, wave_int, mu_a_eqn,␣
↪PLOT_NORMALIZED)
        analytical_term2 = AnalyticalJC.calculate_jacobian()

        AnalyticalJC = JCClass(filtered_photon_data, sdd_index, base_mu_map,␣
↪'FC', MATERNAL_Hb, MATERNAL_SAT, fc, FETAL_SAT, wave_int, mu_a_eqn,␣
↪PLOT_NORMALIZED)
        analytical_term4 = AnalyticalJC.calculate_jacobian()

        # Adding to Table
        new_row1 = {'Saturation' : fc, 'Derivative': analytical_term2, 'SDD':␣
↪all_sdd[sdd_index], 'Type': 2}
        new_row2 = {'Saturation' : fc, 'Derivative': analytical_term4, 'SDD':␣
↪all_sdd[sdd_index], 'Type': 4}
        data_table.loc[len(data_table)] = new_row1
        data_table.loc[len(data_table)] = new_row2
```

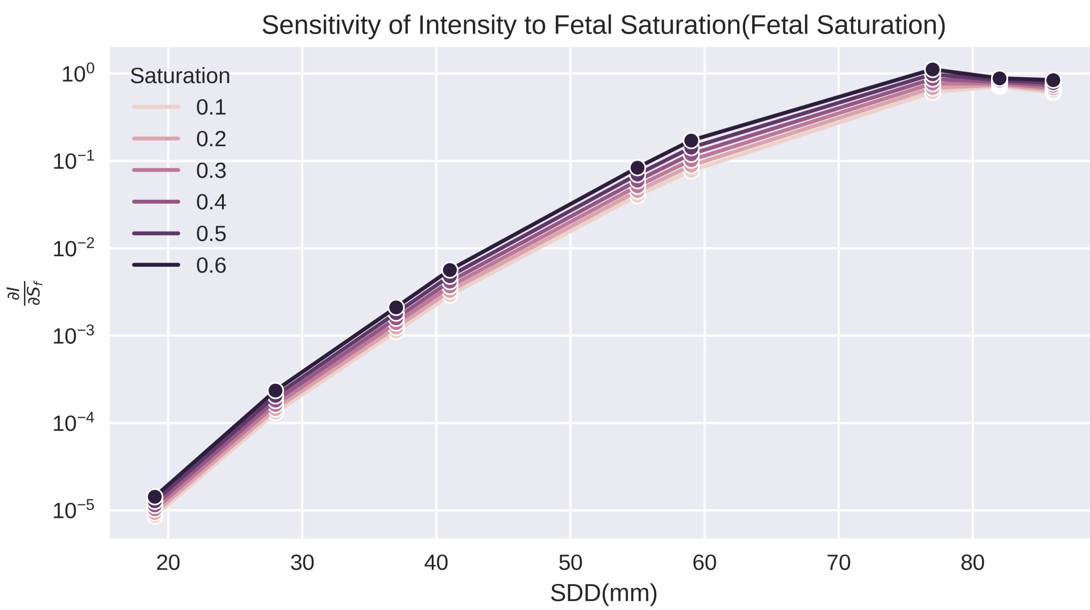
6 Plotting Data

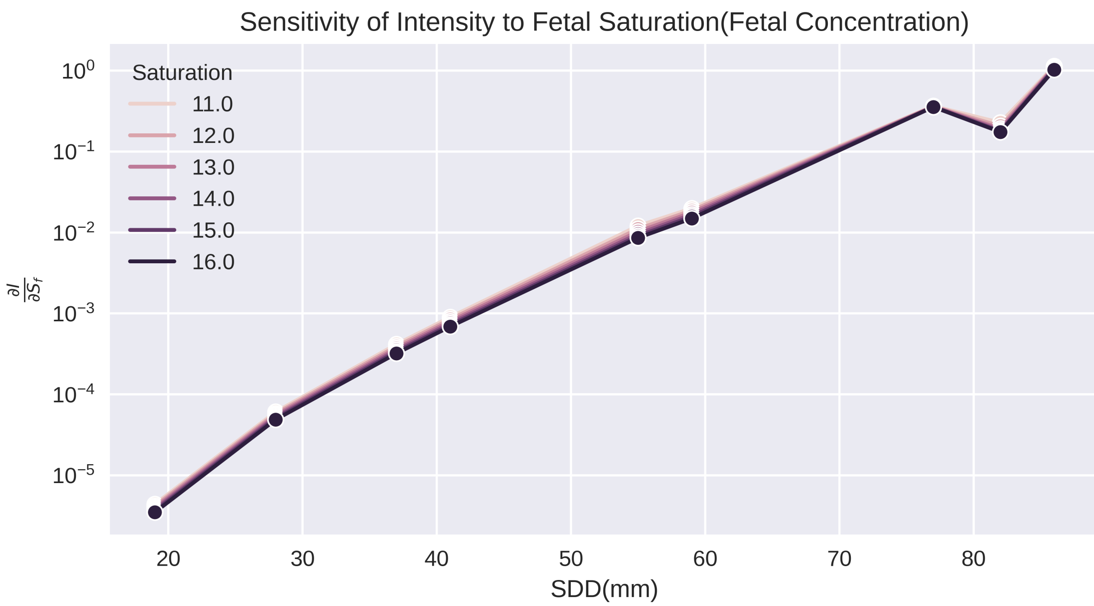
[ ]:
```
# Mandatory - Make all the derivatives positive
data_table['Derivative'] = data_table['Derivative'].abs()

partial_derivative_variable = ['Fetal Saturation', 'Fetal Saturation', 'Fetal␣
↪Concentration', 'Fetal Concentration']
```

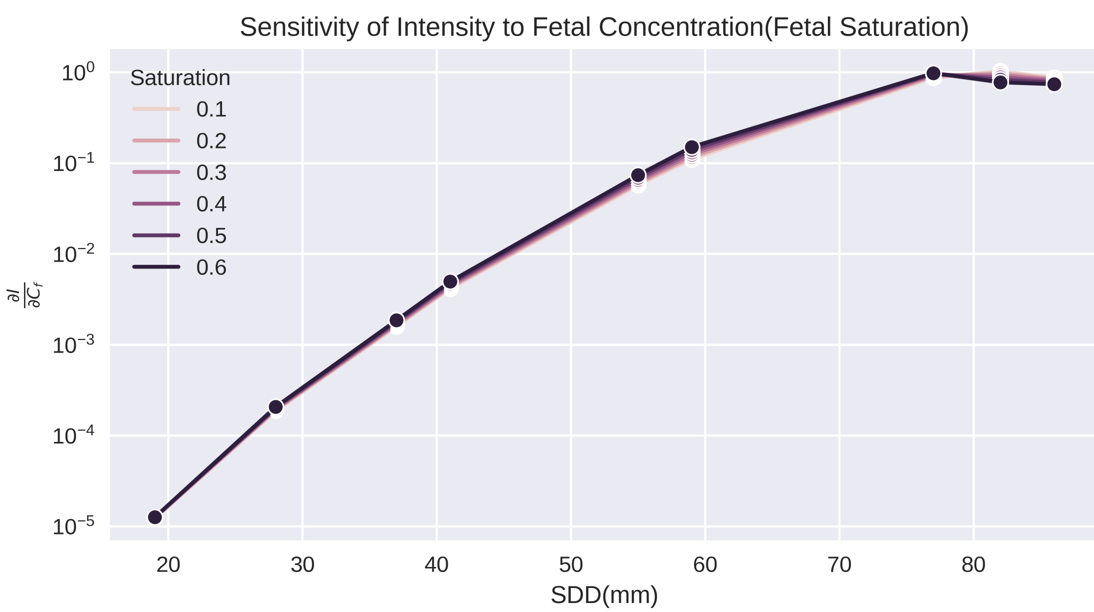
```python
variable_tmp = ['Fetal Saturation', 'Fetal Concentration', 'Fetal Saturation', 'Fetal Concentration']
y_lablels = [r'$\frac{\partial I}{\partial S_f} $', r'$\frac{\partial I}{\partial S_f} $', r'$\frac{\partial I}{\partial C_f} $', r'$\frac{\partial I}{\partial C_f} $']
plot_tiltes = [f'Sensitivity of Intensity to {derivative}({variable})' for derivative, variable in zip(partial_derivative_variable, variable_tmp)]

for i in range(len(plot_tiltes)):
    plt.figure(figsize=(FIG_WIDTH, FIG_HEIGHT))
    data_table_subset = data_table[data_table['Type'] == i + 1] # I made types 1 indexed for some stupid reason ...
    plot = sns.lineplot(data=data_table_subset, x='SDD', y='Derivative', hue='Saturation', marker='o')
    plt.title(plot_tiltes[i])
    plt.yscale('log')
    plt.xlabel('SDD(mm)')
    plt.ylabel(y_lablels[i])
```

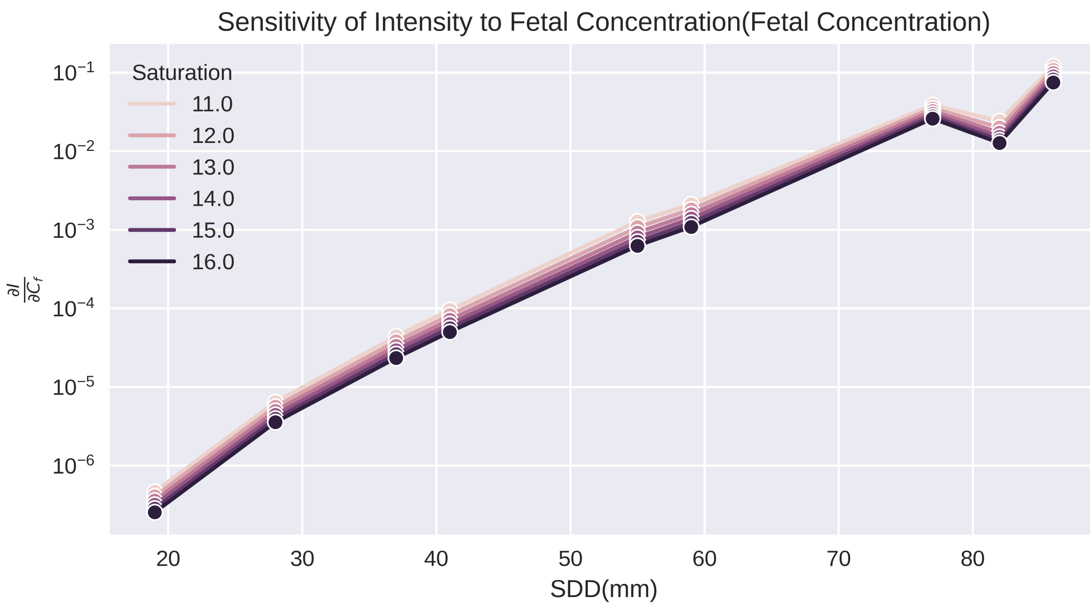




Sensitivity of Intensity to Fetal Saturation(Fetal Concentration)
Saturation
11.0
12.0
13.0
14.0
15.0
16.0
$\frac{\partial I}{\partial S_f}$
10^0
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
20
30
40
50
60
70
80
SDD(mm)



Sensitivity of Intensity to Fetal Concentration(Fetal Saturation)
Saturation
0.1
0.2
0.3
0.4
0.5
0.6
$\frac{\partial I}{\partial C_f}$
10^0
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
20
30
40
50
60
70
80
SDD(mm)


Sensitivity of Intensity to Fetal Concentration(Fetal Concentration)
Saturation
11.0
12.0
13.0
14.0
15.0
16.0
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
10^{-6}
$\frac{\partial I}{\partial C_f}$
20
30
40
50
60
70
80
SDD(mm)