

$$cost[j] = \min_{i < j+1} (c[j, i] + cost[i])$$

cost[12] = 0

multistage Graph solved example.

$$c(12) = 0$$

$$c(11) = 5 \quad d(11) = 12$$

$$c(10) = 2 \quad d(10) = 12$$

$$c(9) = 4 \quad d(9) = 12$$

$$c(8) = \min \{ 5+2, 6+5 \} = 7$$

$$d(8) = 10$$

$$c(7) = \min \{ 5+4, 3+2 \} = 5$$

$$d(7) = 10$$

$$c(6) = \min \{ 6+4, 5+2 \} = 7$$

$$d(6) = 10$$

$$c(5) = \min \{ 11+5, 8+7 \} = 15$$

$$d(5) = 8$$

$$c(4) = \min \{ 11+7 \} = 18$$

$$d(4) = 8$$

$$c(3) = \min \{ 7+5, 2+7 \} = 9$$

$$d(3) = 6$$

$$c(2) = \min \{ 4+7, 2+5, 1+7 \} = 7$$

$$d(2) = 7$$

$$c(1) = \min \{ 9+7, 8+9, 3+18, 2+15 \} = 16$$

$$d(1) = 2$$

1 - 2 - 7 - 10 - 12

minimum cost = 16

$$c(11, 12) = \min_{i \in I} \{ c(12, i) \}$$

$$\text{cost}(i, j) = \min_{\substack{l \in V, i < l < j \\ l \in E}} \{ c(i, l) + \text{cost}(l, j) \}$$

multistage Graph Exercise 1, fig 5.4

$$\text{cost}(11, 12) = \min \{ 0 +$$

$$\text{cost}(11) = \min \{ \text{cost}(11, 12) + \text{cost}(12, 12) \}$$

$$= \min \{ 5 + 0 \}$$

$$= 5$$

$$d(11) = 12$$

$$n = 9$$

$$j = n - 1 = 8, \text{cost}(1:9) = 0$$

$$\text{cost}(8) = \min \{ c(8, 9) + c(9) \}$$

$$= 3 + 0 = 3$$

$$d(8) = 9$$

$$\text{cost}(7) = c(7, 9) + c(9) = 7 + 0 = 7$$

$$d(7) = 9$$

$$\text{cost}(6) = \min \{ \text{cost}(6, 8) + \text{cost}(8), \text{cost}(6, 7) + \text{cost}(7) \}$$

$$= \min \{ 5, 13 \} = 5$$

$$d(6) = 8$$

$$\text{cost}(5) = \min \{ \text{cost}(5, 8) + \text{cost}(8), \text{cost}(5, 7) + \text{cost}(7) \}$$

$$= \min \{ 2 + 3, 6 + 7 \} = 5$$

$$d(5) = 8$$

$$\text{cost}(4) = \min \{ 7, 8 \} = 7, d(4) = 8$$

$$\text{cost}(3) = \min \{ 8 + 5, 9 + 6 \} = 10$$

$$d(3) = 11$$

$$\text{cost}(2) = \min \{ 9 + 5, 10 + 8 \} = 9$$

$$d(2) = 6$$

$$\text{cost}(1) = \min \{ 9 + 10, 8 + 8 \} = 12$$

$$d(1) = 12$$

1-3-5-8-9-12