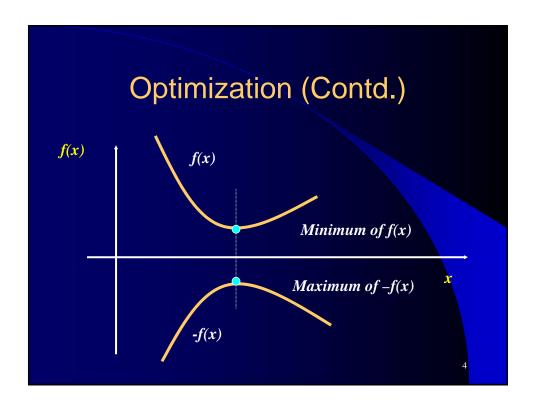


# Outline • Basic Optimization Background

### Optimization

- It is the act of obtaining the best result under given circumstances.
- Engineering problems where the emphasis is on maximizing or minimizing a certain goal.



### Optimization (contd.)

The *optimum* seeking methods are also known as mathematical programming techniques and are generally studied as a part of *operation research*.

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# Methods of Operation Research

- Mathematical Programming
- Stochastic Process Techniques
- Statistical Methods

# Mathematical Programming Techniques

- Calculus Methods
- Calculus of variations
- NonlinearProgramming
- GeometricProgramming
- QuadraticProgramming
- Linear Programming

- Dynamic Programming
- Integer Programming
- Stochastic Programming
- Separable Programming
- Multi-objective Programming
- Network Methods: CPM/PERT
- Game Theory

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# Stochastic Process Techniques

- Statistical decision theory
- Markov Processes
- Queueing Theory
- Renewal Theory
- Simulation Methods
- Reliability Theory

### Statistical Methods

- Regressional Analysis
- Cluster Analysis,
  Pattern Recognition
- Design of Experiments
- Discriminate Analysis (Factor Analysis)

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### **Engineering Applications**

- Design of Aircraft and Aerospace Structures for minimum weight
- Finding the optimal trajectories of space vehicles
- Design of Civil engineering structures frames, foundations, bridges, towers, chimneys and dams for minimum cost

# Engineering Applications (Contd.)

- Minimum weight design of structures for earthquake, wind and other types of random loading
- Design of water resources systems for maximum benefit
- Optimal plastic design of structures
- Optimum design of linkages, cams, gears machine tools and other mechanical components

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# Engineering Applications (Contd.)

- Selection of machining conditions in metal cutting processes for minimum production cost.
- Design of material handling equipment like conveyors, trucks and cranes for minimum cost.
- Design of pumps, turbines and heat transfer equipment for maximum efficiency

# Engineering Applications (Contd.)

- Optimum design of electrical machinery like motors, generators and transformers
- Optimum design of electrical networks.
- Shortest route taken by a salesmen visiting different cities during one tour
- Optimal production planning, controlling and scheduling

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# Engineering Applications (Contd.)

- Analysis of statistical data and building empirical models from experimental results to obtain the most accurate representation of the physical phenomenon.
- Optimum design of chemical processing equipment and plants
- Design of optimum pipe line networks for process industries

### **Engineering Applications** (Contd.)

- Selection of site for an industry
- Planning of maintenance and replacement of equipment
- Inventory control
- Allocation of resources or services among several activities to maximize the benefit
- Optimum design of control systems.

### Statement of an **Optimization Problem**

An Optimization or a mathematical programming problem can be stated as follows

Find 
$$X = \begin{cases} x_1 \\ \dots \\ x_n \end{cases}$$
 which minimizes  $f(X)$ 

Subject to the constraints

$$g_j(X) \le j = 1, 2, ..., m$$
 and

$$L_i(X) = 0, j = 1, 2, ..., p$$

# Statement of Optimization Problem

- Where X is an n-dimensional vector design vector
- f(X) *Objective Function*
- $\circ$   $g_i(X)$  Inequality Constraints
- $ullet L_i(X)$  Equality Constraints
- n- Number of Variables
- m- Number of inequality constraints
- p- Number equality constraints

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# Statement of Optimization Problems (Contd.)

 Earlier discussed problem is known as Constrained optimization Problem

# Definition of Terminology Design Vector Design Constraints Constraint Surface Objective Function



### **Design Vector**

- Pre-assigned Parameters
- Design or Decision variables
- Example: Gear-pair
  - Face width b
  - Number of teeth  $T_1$  and  $T_2$
  - Center distance d
  - Pressure Angle ψ
  - The tooth Profile
  - Material

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## **Design Vector**

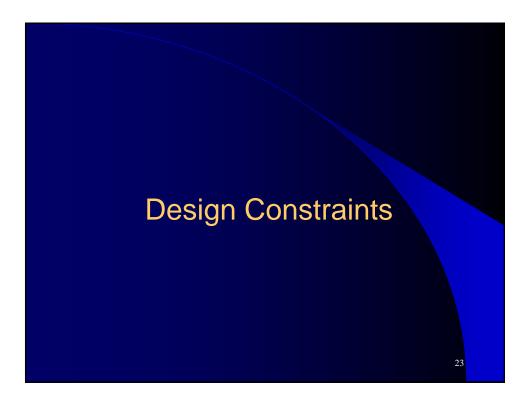
- Pre-assigned Variables
  - -Pressure Angle ψ
  - -The tooth Profile
  - -Material
- Design Vector

$$X = \{x_1 x_2 x_3\} = \{b, T_1, T_2\}$$

Design Space – N-dimensional

Design point =  $\{1.0, 20, 40\}$  – Possible Solution

Design point =  $\{1.0, -20, 40\}$  – Impossible Solution



### **Design Constraints**

- Design variables can not be chosen arbitrarily
- Design variables have to satisfy certain functional and other requirements
- Types of ConstraintsBehavior or Functional ConstraintsGeometric or Side Constraints

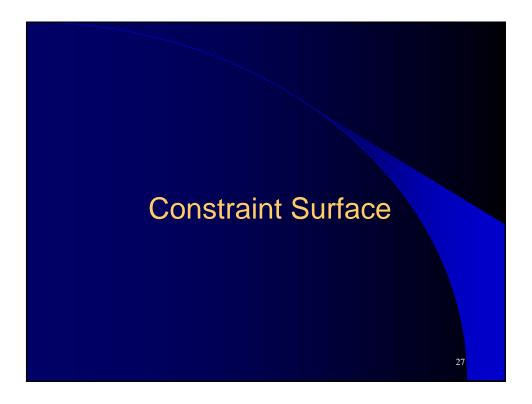
# Behavior/Functional Constraints

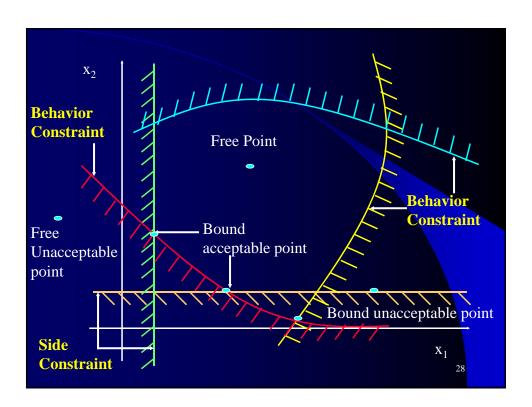
- They represent limitations on the behvaior or performance of the system
- Examples
  - Face width b can not be taken smaller than a certain value due to strength requirement
  - Ratio  $T_1/T_2$  is dictated by speeds of the input and output of shafts  $N_1$  and  $N_2$ .

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### Geometric/Side Constraints

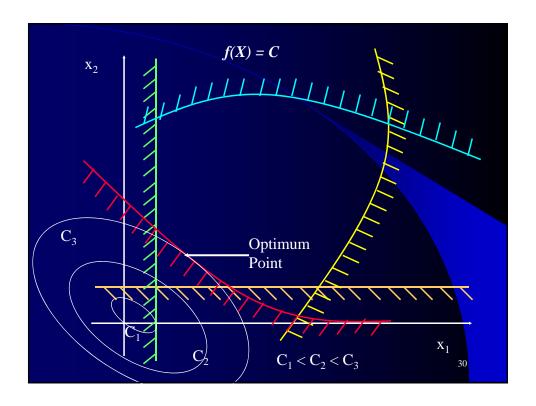
- They represent physical limitations on the design variables like availability, fabricability and transportability
- Examples
  - $T_1$  and  $T_2$  can not be real numbers
  - Upper and lower bounds on  $T_1$  and  $T_2$  due to manufacturing limitations.





## **Objective Function Surfaces**

The locus of all points satisfying f(X) = c = Constant forms a hyper-surface in the design space



### Major Hurdle

The number of design variables exceeds two or three, the constraints and objective function surfaces become complex even for visualization and the problem has to be solved purely as a mathematical problem.

