





Radial Basis Function (RBF) Networks



Lecture 14

1



Radial Basis Function Networks

- ✦ Overview
- ✦ Regularization Network
- ✦ Generalized RBFNs
- ✦ Applications



Overview

- ✦ A Feed-Forward Neural Network
- ✦ Designed to a Curve-Fitting problem in a high dimensional space
- ✦ Strict Interpolation
- ✦ Three Layers: Input , Hidden, and Output



Comparison of RBF Networks and MLP-Similarities

- ✦ RBF Networks and MLP are examples of nonlinear layered feed-forward networks.
- ✦ Universal Approximators
- ✦ RBF networks capable of mimicking MLP or Vice versa.



Comparison of RBF Networks and MLP- Differences

✦ **Network Architecture-**

MLP – One or more hidden layers

RBF network - Single hidden layer

✦ **Computation nodes**

MLP – Hidden or Output layer – Share a common neuronal model.

RBF Network – Hidden and Output layer serve different purpose

5



Comparison of RBF Networks and MLP- Differences

✦ **Hidden and Output Layer -**

MLP – Usually hidden and output layer nonlinear

RBF network - Hidden – Nonlinear, Output – Linear

Activation Function

MLP – Hidden - Inner product of input vector and synaptic weight vector

RBF Network – Hidden Euclidean Norm (distance) between the input vector and the center of the unit

6



Comparison of RBF Networks and MLP- Differences

✦ Approximations to Nonlinear input-output mapping

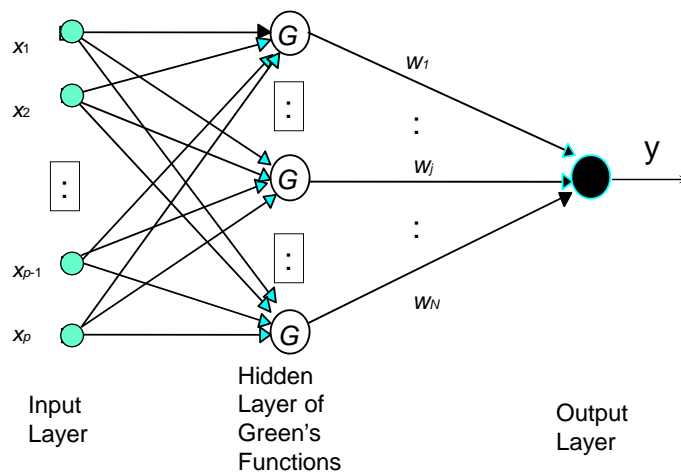
MLP – Constructs **GLOBAL** approximations

RBF network – Using exponentially decaying localized nonlinearities (e.g. Gaussian Functions) constructs **LOCAL** approximations.

7



The Regularization Network



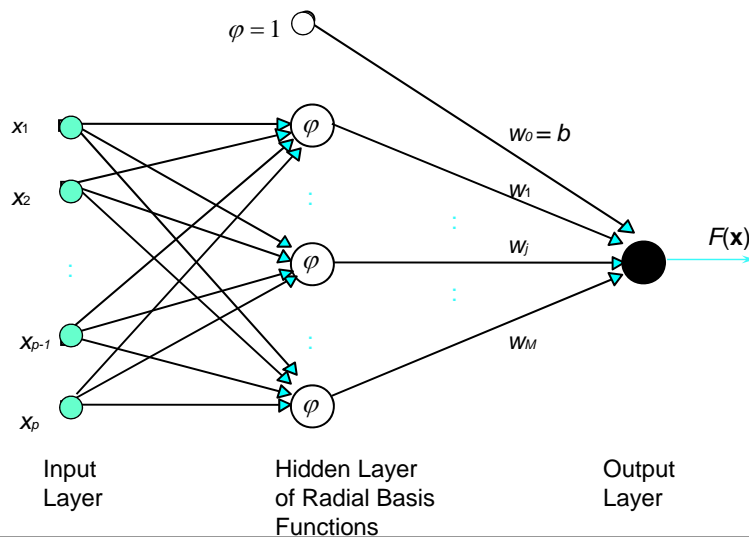


The Regularization Network

- ✦ A *universal approximator*
- ✦ Has the *best-approximation* property
- ✦ Computes the optimal solution
- ✦ One-to-one correspondence
- ✦ Computationally complex for large N

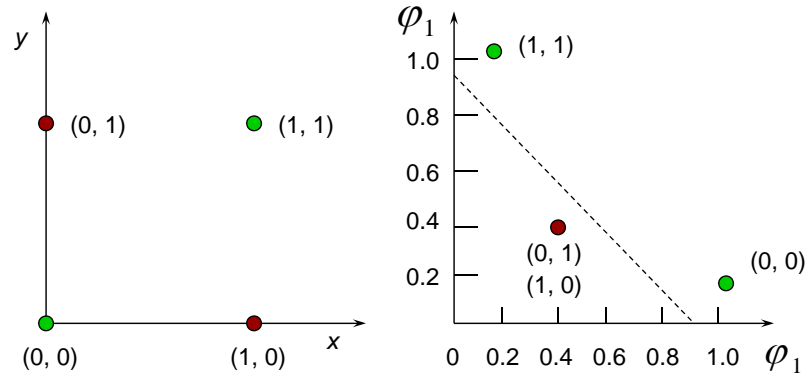


The Generalized RBFNs

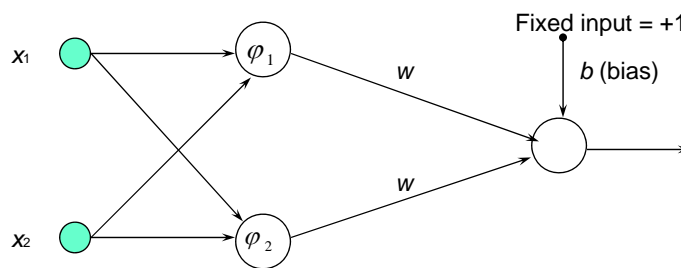




The XOR Problem



The RBFN for the XOR Problem



Data Point, j	Input Pattern, \mathbf{x}_j	Desired Output, d_j	Actual Output, y_i
1	(1, 1)	1	+0.901
2	(0, 1)	0	-0.01
3	(0, 0)	1	+0.901
4	(1, 0)	0	-0.01

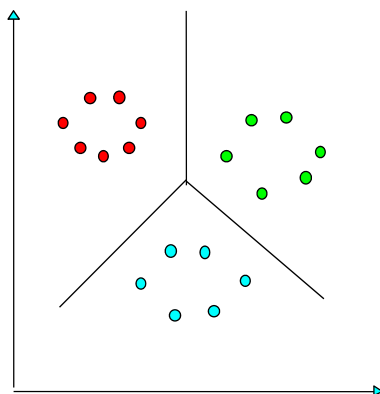


Applications

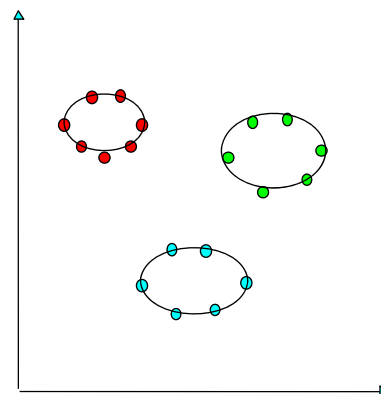
- ✦ Image Processing
- ✦ Speech Recognition
- ✦ Pattern Recognition
- ✦ Time-Series Analysis
- ✦ Radar Point Source Location
- ✦ Medical Diagnosis
- ✦ Process Faults Detection



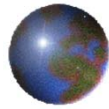
Decision Surfaces in Two Dimensions



Multi-layer Perceptron



Radial Basis Function Network

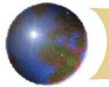


Color Image Classification Problem in an Industrial Application

FERAT SAHIN

Bradley Department of Electrical Engineering
Virginia Polytechnic Institute and State University

July 8, 1998



Overview of Presentation

- ✦ The Color Classification System
- ✦ Definitions
- ✦ RBFN Solution to the Color Image Classification Problem
- ✦ Comparisons and Discussion
- ✦ Conclusions and Future Directions



The Color Classification System

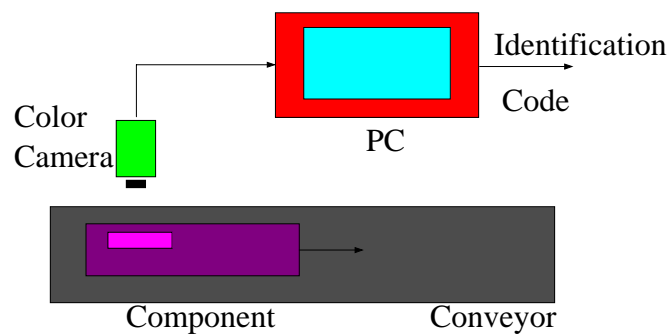
✦ Background

- Automatic Vision-based Classification System
- American Woodmark Corporation

✦ System Overview



System Overview

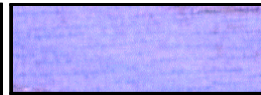




Images of Eight Different Wooden Cabinets



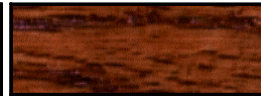
Maple/Frost



Oak/Frost



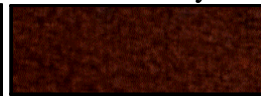
Oak/Natural



Oak/Honey



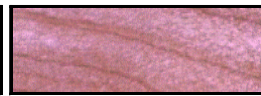
Oak/Toffee



Cherry/Toffee



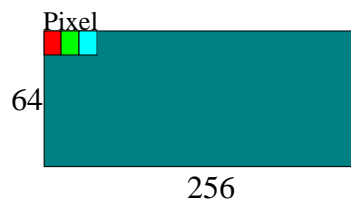
Maple/White



Maple/Natural



The Structure of the Images



The Number of Pixel an Image : $64 \times 256 = 16384$



Each pixel has 24 bits (3 bytes)

An Image is $16384 \times 24 = 49152$ bytes



The most important issues in a pattern recognition system

- ✦ Selection of a suitable color space
- ✦ Quantization of the color space(feature extraction)
- ✦ Finding an appropriate classification method
- ✦ Acquisition of a model database of images



Definitions

- ✦ Color Spaces
- ✦ Color Quantization
- ✦ Color Classification Methods

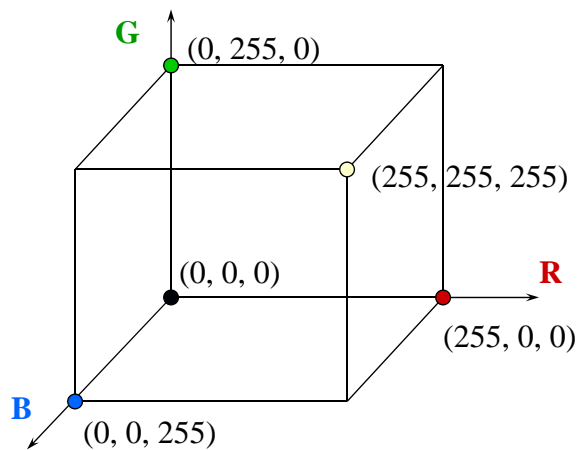


Color Spaces

- ✦ RGB Space
- ✦ Normalized RGB Space



RGB Space





Normalized RGB Space

$$N_c = \frac{C}{(R + G + B)} \quad \text{for } C \in \{R, G, B\} \text{ and } R + G + B \neq 0$$

$$N_r + N_g + N_b = 1$$

$$Y = c_1 R + c_2 G + c_3 B \quad \text{where } c_1 + c_2 + c_3 = 1$$

$$T_1 = \frac{R}{(R + G + B)}$$

$$T_2 = \frac{G}{(R + G + B)}$$

Y : Luminance

T_1, T_2 : Chromatic

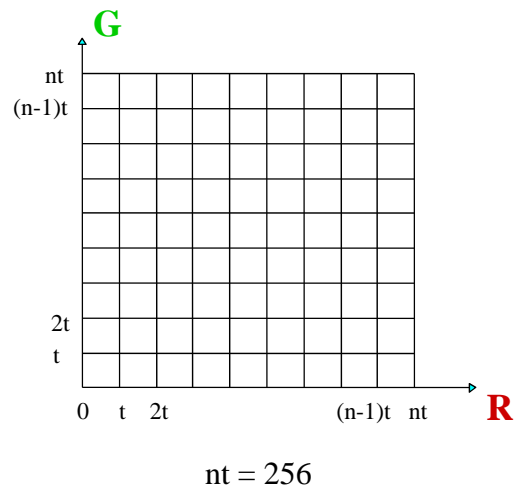


Color Quantization

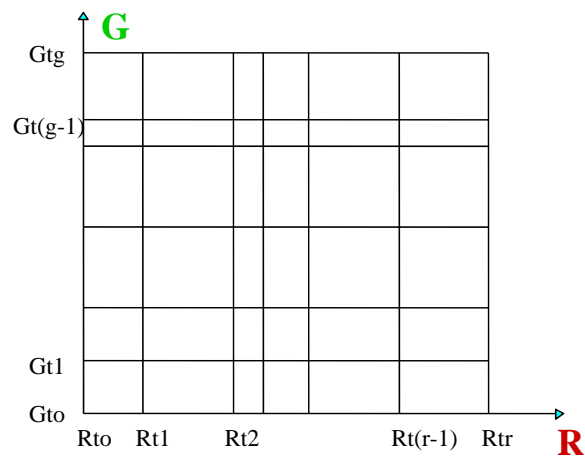
- ✦ Uniform Quantization
- ✦ Nonuniform Quantization
- ✦ Clustering and Vector Quantization



Uniform Quantization

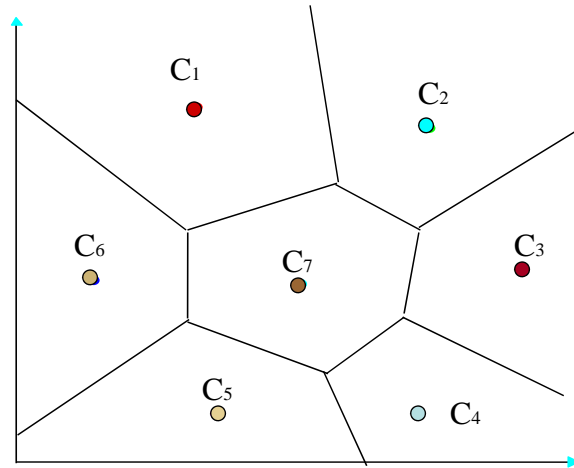


Non-uniform Quantization





Clustering or Vector Quantization



• Color Classification Methods

- ✦ Minimum Distance Classifiers
- ✦ Radial Basis Function Networks



Minimum Distance Classifiers

- Euclidean Distance

$$d_1^2(x, y) = \sum_{i=1}^k (x_i - y_i)^2$$

- City-block Metric Distance

$$d_2(x, y) = \sum_{i=1}^k |x_i - y_i|$$

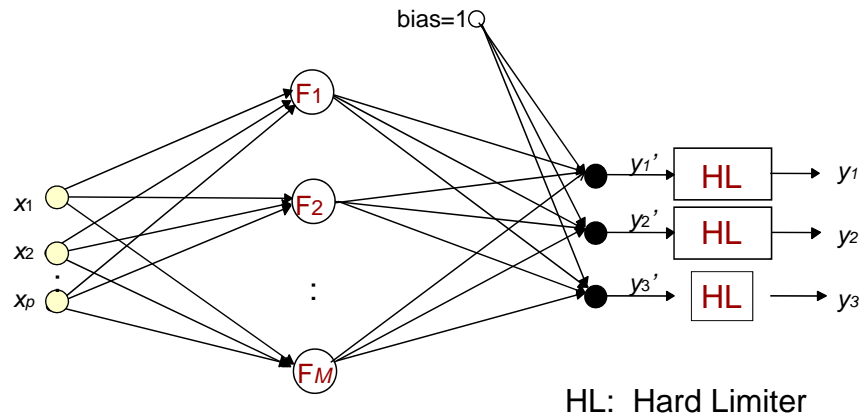


RBFN Solution to the Color Image Classification Problem

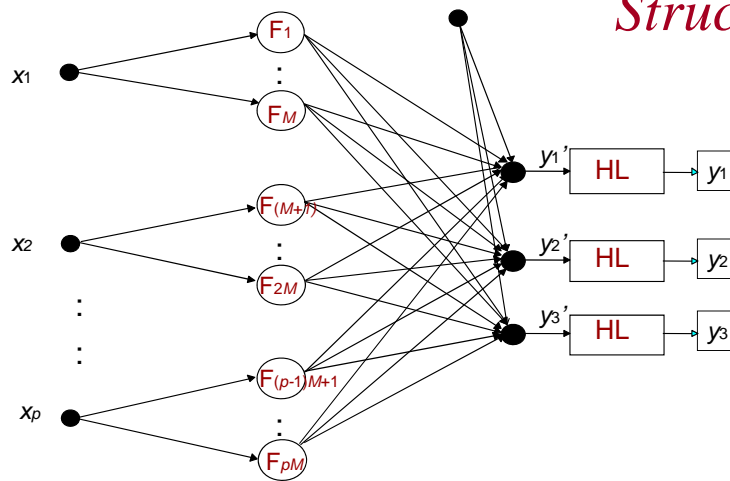
- ✦ Network Structures
 - The Generalized RBFNs
 - Proposed One-dimensional RBFNs
- ✦ Input Features
- ✦ Methods



The Generalized RBFN Structure



Proposed One-dimensional RBFN Structure





Input Features

✦ The Average Values of Colors

✦ Covariance Matrix

$$\Sigma = \begin{bmatrix} \sigma_{rr} & \sigma_{rg} & \sigma_{rb} \\ \sigma_{rg} & \sigma_{gg} & \sigma_{gb} \\ \sigma_{rb} & \sigma_{gb} & \sigma_{bb} \end{bmatrix}$$

✦ The Image Partitioning

✦ Histogram



Methods

Method Name	Input Feature Type	# of Centers and RBFs	Network Structure	% Correct Classification
Method I	Average Colors (r, g, b)	8	Traditional RBFN	55.06
Method II	Image Partitioning ($r_1, g_1, b_1, r_2, g_2, b_2, r_3, g_3, b_3$)	8	Traditional RBFN	66.75
Method III	Average Colors (r, g, b)	23	Traditional RBFN	67.79
Method IV	Average Colors (r, g, b)	8	O-RBFN	72.20
Method V	Av. Colors and STDs ($r, g, b, \sigma_r, \sigma_g, \sigma_b$)	8	O-RBFN	77.66
Method VI	Covariance Matrix (Nine input features)	8	O-RBFN	78.12
Method VII	Histogram (24 elements)	8	Traditional RBFN	77.14
Method VIII	Histogram with white noise (24 elements)	8	Traditional RBFN	78.15
Method IX	Histogram (24 elements)	30	RBFN (Fixed Dilation)	77.34
Method X	Histogram (8 elements for each color)	21, 21 19, 19 16, 16	RBFN (Fixed Dilation)	79.74 (red) 80.25 (green) 81.81 (blue)
Method XI	Histogram (Only blue 64 elements.)	80	RBFN (Fixed Dilation)	84.41 (blue)

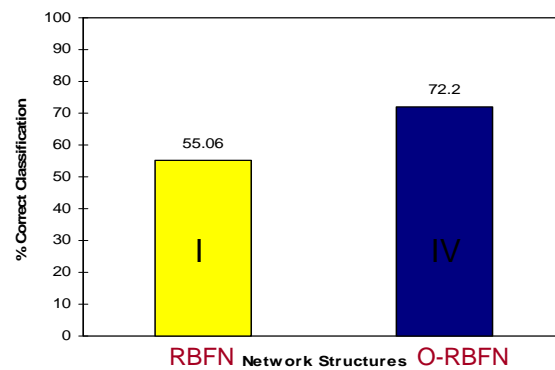


Comparisons and Discussion

- ✦ Network structure
- ✦ The number of input feature
- ✦ The number of RBFs in the Network

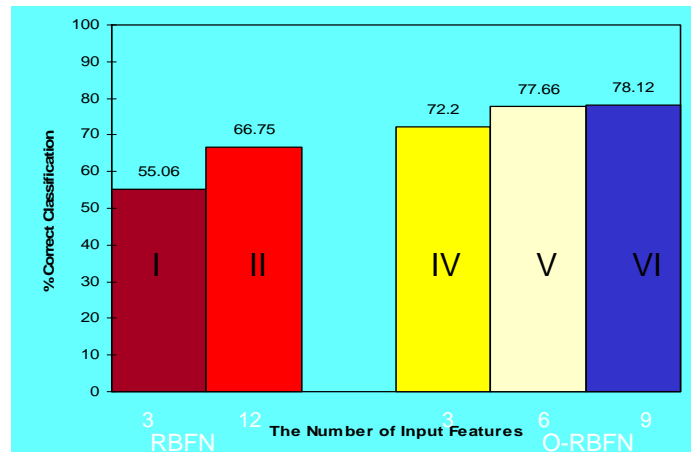


Network Structure

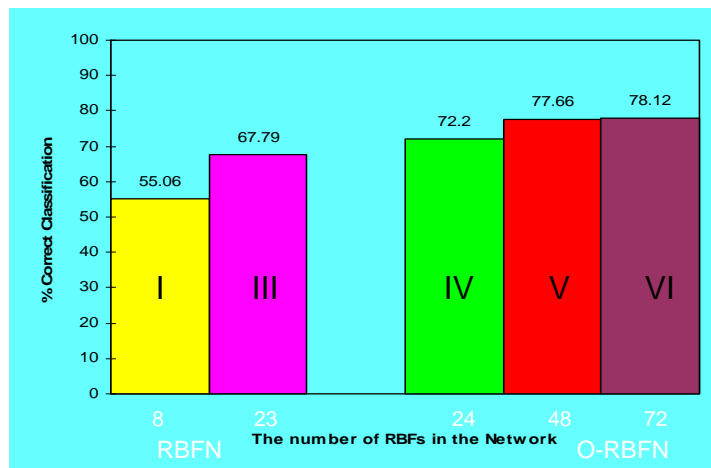




The Number of Input Features



The Number of RBFs in the Network

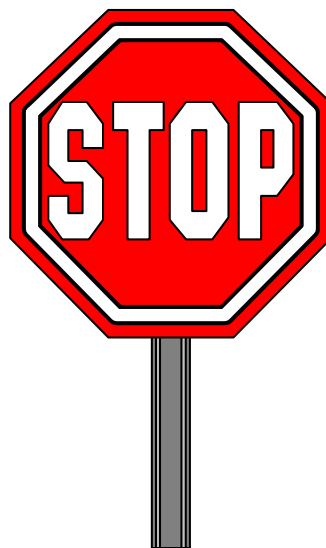




Conclusions

- ✦ RBFNs are fast and generalize the solution well.
- ✦ RBFNs are the best for the nonlinear classification
- ✦ One-dimensional RBFNs are successful
- ✦ Only one color's histogram is enough
- ✦ RBFNs gave more accurate results

41



42