

Perceptron

FEBRUARY - 2021
 M T W T F S S M T W T F S S
 1 2 3 4 5 6 7 8 9 10 11 12 13 14
 15 16 17 18 19 20 21 22 23 24 25 26 27 28

(018-347) Wk 04
 JANUARY
 MONDAY

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Over View of Perceptron

- ① Perceptron Definition
- ② Perceptron intuition with an analogy
- ③ Mathematical Representation
- ④ Perceptron Weight Update Rule

OR

Perceptron Learning Rule

⑤ → frequently Used terms for Deep Learning

Perceptron Definition

① It was invented by Frank Rosenblatt in 1957.

Published the paper. —

The perceptron: A probabilistic model for Information storage and Organization in the Brain.

It was different from first neuron.

They thought that input is nothing but it is binary.

Our greatest glory is not in never falling, but in rising every time we fell

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JANUARY

TUESDAY

JANUARY - 2021													
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11	12	13	14	15	16	17	18	19	20	21	22	23	24
25	26	27	28	29	30	31							

This perception Architecture is Also known as. —

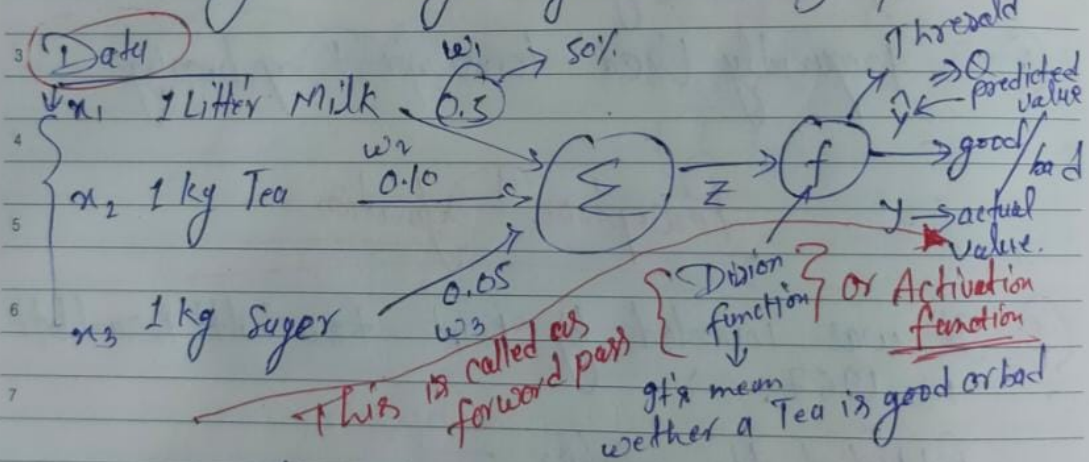
LTU \rightarrow Linear Threshold Unit
TLU \rightarrow Threshold Logic Unit.

Ex. -

Task - like

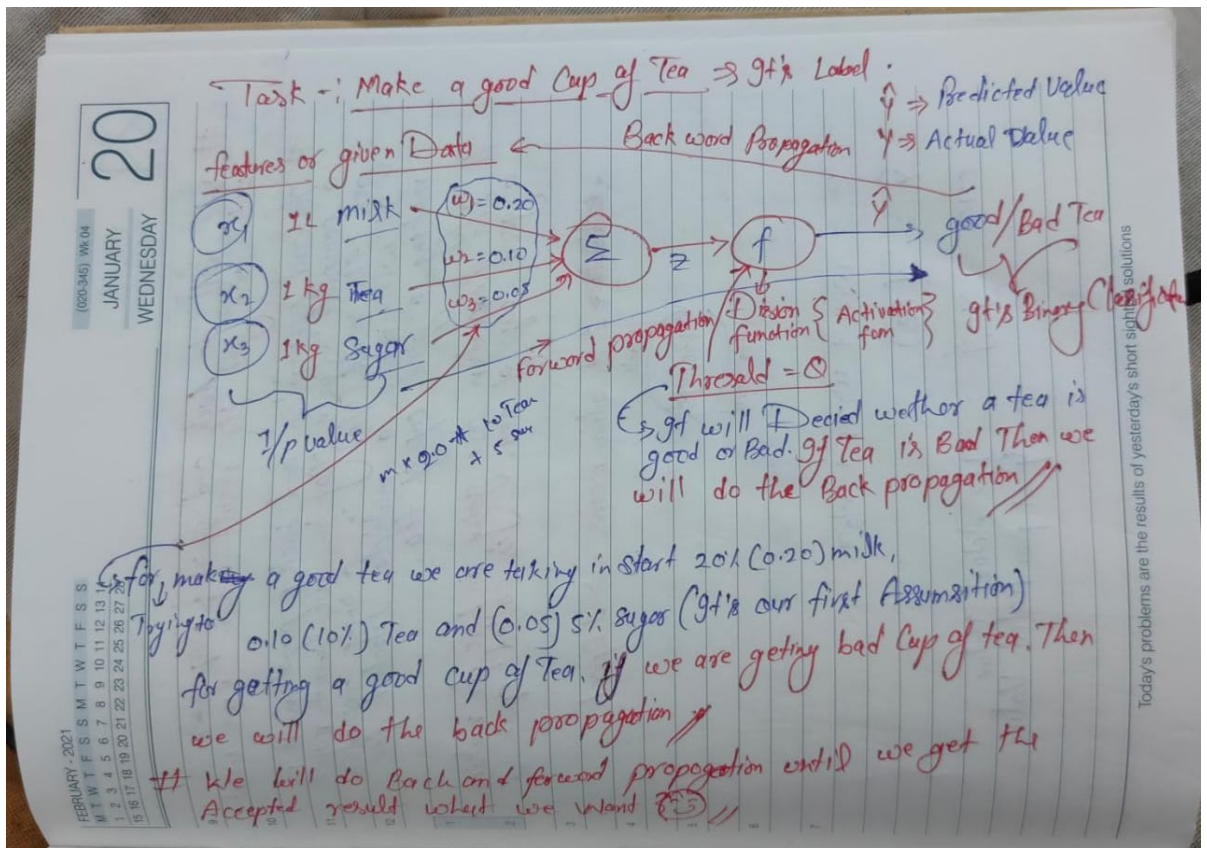
Make a good cup of tea.

Possibility \rightarrow binary classification \rightarrow good/bad.



Threshold will decide that whether a tea is good or bad.

Worry is the interest paid on trouble before it falls due



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25	26	27	28	29	30	31							

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 THURSDAY

(021-344) Wk 04

We will do back and forward propagation until we get the result what we want

Forward propagation and back propagation. It is a complete cycle. May be we ~~can't~~ can't get the result (O/p) in a single repetition. It will make a multiple iteration for making a good cup of tea.

The Repeation are going on here for making a good cup of tea. It's called epoch

~~1 iteration~~ 1 iteration means \rightarrow 1 Epoch

$$z = w_1x_1 + w_2x_2 + w_3x_3$$

$$\hat{y} = f(z)$$

$$\text{error} = y - \hat{y}$$

$y \Rightarrow$ Actual Value
 $\hat{y} \Rightarrow$ predicted Value.

Life is great; make the most out of it. Be an Optimist

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Based on this error \Rightarrow we will be back propagating and we will be updating the weights for this we have a \rightarrow Perceptron Weight Update Rule.

Perceptron Weight Update Rule is \rightarrow

$$w_{\text{new}} = w_{\text{old}} + \underbrace{\eta}_{\text{learning rate}} \underbrace{\text{error} \times x}_{\text{input}} \rightarrow \Delta w$$

$\eta \rightarrow$ learning rate

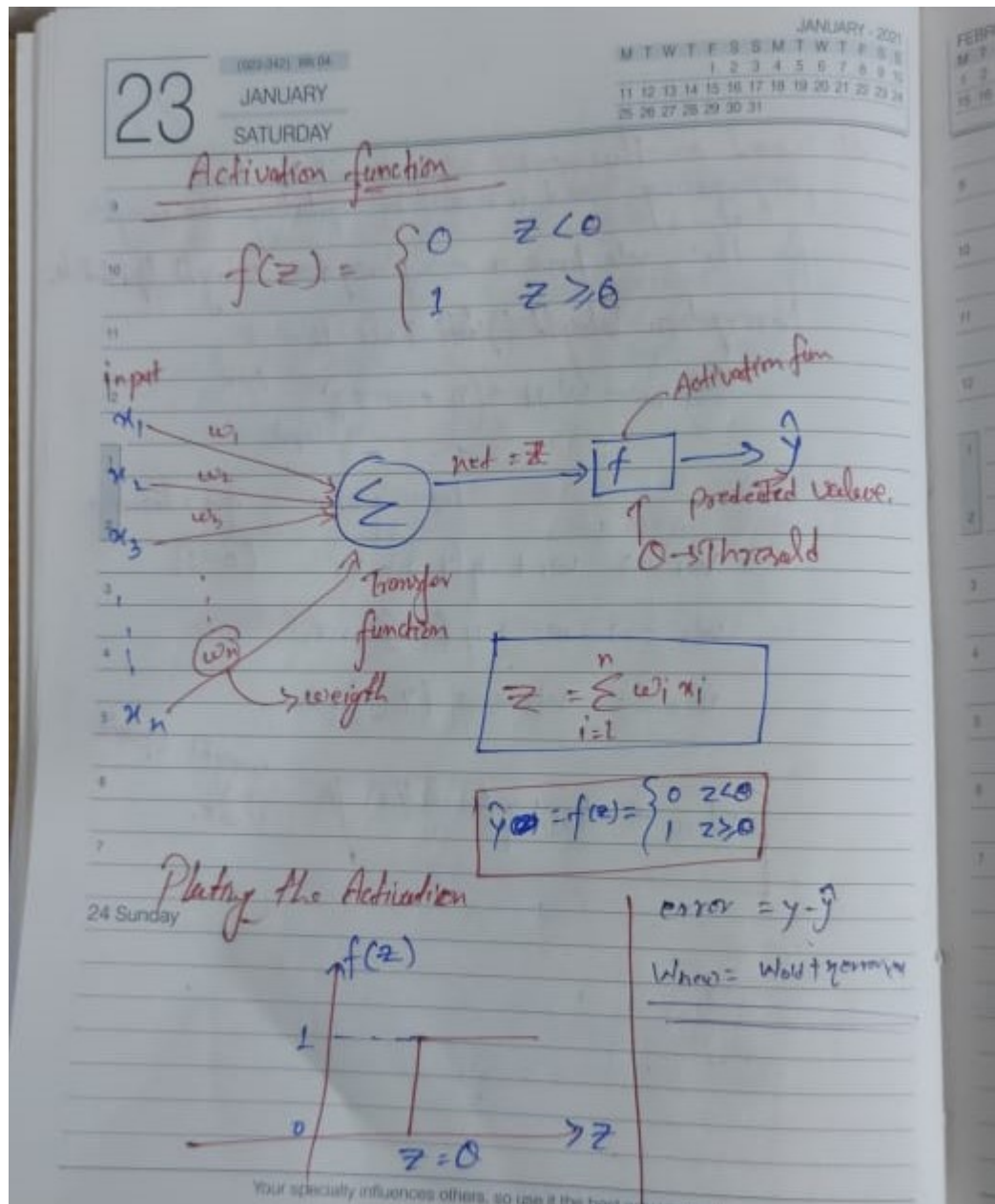
$$w_1 \Rightarrow w_1 + \eta (y - \hat{y}) \cdot x_1 \quad (0-1)$$

$$w_2 \Rightarrow w_2 + \eta (y - \hat{y}) \cdot x_2$$

$$w_3 \Rightarrow w_3 + \eta (y - \hat{y}) \cdot x_3$$

$w_{\text{new}} = w_{\text{old}} + \eta (\text{error} \times x)$

\rightarrow Weight Update Rule.



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Let's Learn More About Perceptron

$$z = w_1 x_1 + w_2 x_2 \quad \text{--- (1)}$$

$$\hat{y} = f(z) = \begin{cases} 1 & z \geq 0 \\ 0 & z < 0 \end{cases}$$

$$= \begin{cases} 1 & w_1 x_1 + w_2 x_2 \geq 0 \\ 0 & w_1 x_1 + w_2 x_2 < 0 \end{cases}$$

$$= \begin{cases} 1 & w_1 x_1 + w_2 x_2 - 0 \geq 0 \\ 0 & w_1 x_1 + w_2 x_2 - 0 < 0 \end{cases}$$

$w_1 x_1 + w_2 x_2 - 0$

Let's take Assumption —

$$w_0 = 0, x = -1$$

$$w_0 x_0 = 0 \times -1 = -0 \quad \text{--- (2)}$$

(Republic Day) TUESDAY 26

Those who deny freedom to others deserve it not for themselves.

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(027-338) Wk 05
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WEDNESDAY

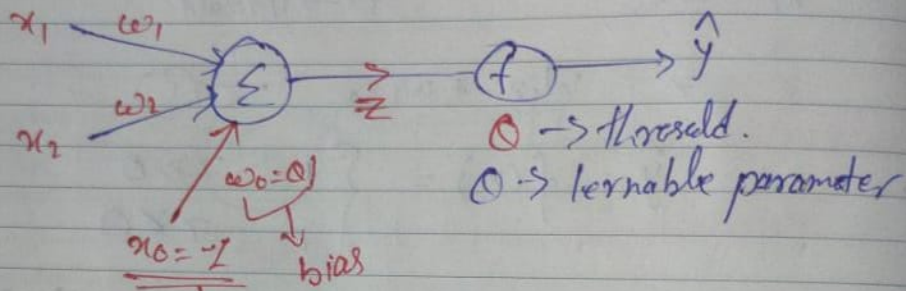
JANUARY - 2021

M	T	W	T	F	S	S	M	T	W	T	F	S	S
		1	2	3	4	5	6	7	8	9	10		
11	12	13	14	15	16	17	18	19	20	21	22	23	24
25	26	27	28	29	30	31							

$$w_1 x_1 + w_2 x_2 - 0$$

In Equation (2) \rightarrow we get $-0 = w_0 x_0$

$$w_1 x_1 + w_2 x_2 + w_0 x_0$$

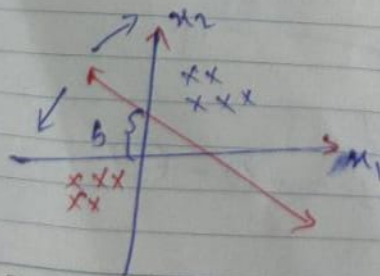


Assumption \rightarrow Constant (Noise)

$$w_1 x_1 + w_2 x_2 - 0 = 0$$

$$x_2 \Rightarrow \frac{-w_1 x_1}{w_2} + \frac{0}{w_2}$$

$$x_2 \Rightarrow -m x_1 + b$$



$m \Rightarrow$ rotation factor

$b \Rightarrow$ shifting factor/translation factor

Blessed are those who can give without remembering and take without forgetting.

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 15 16 17 18 19 20 21 22 23 24 25 26 27 28

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To create a model more generic, Here they are trying to introduce Neuron and provide a weight called bias.

Perceptron Draw Back

It is only work for linear ~~separated~~ separated data

Example for XOR

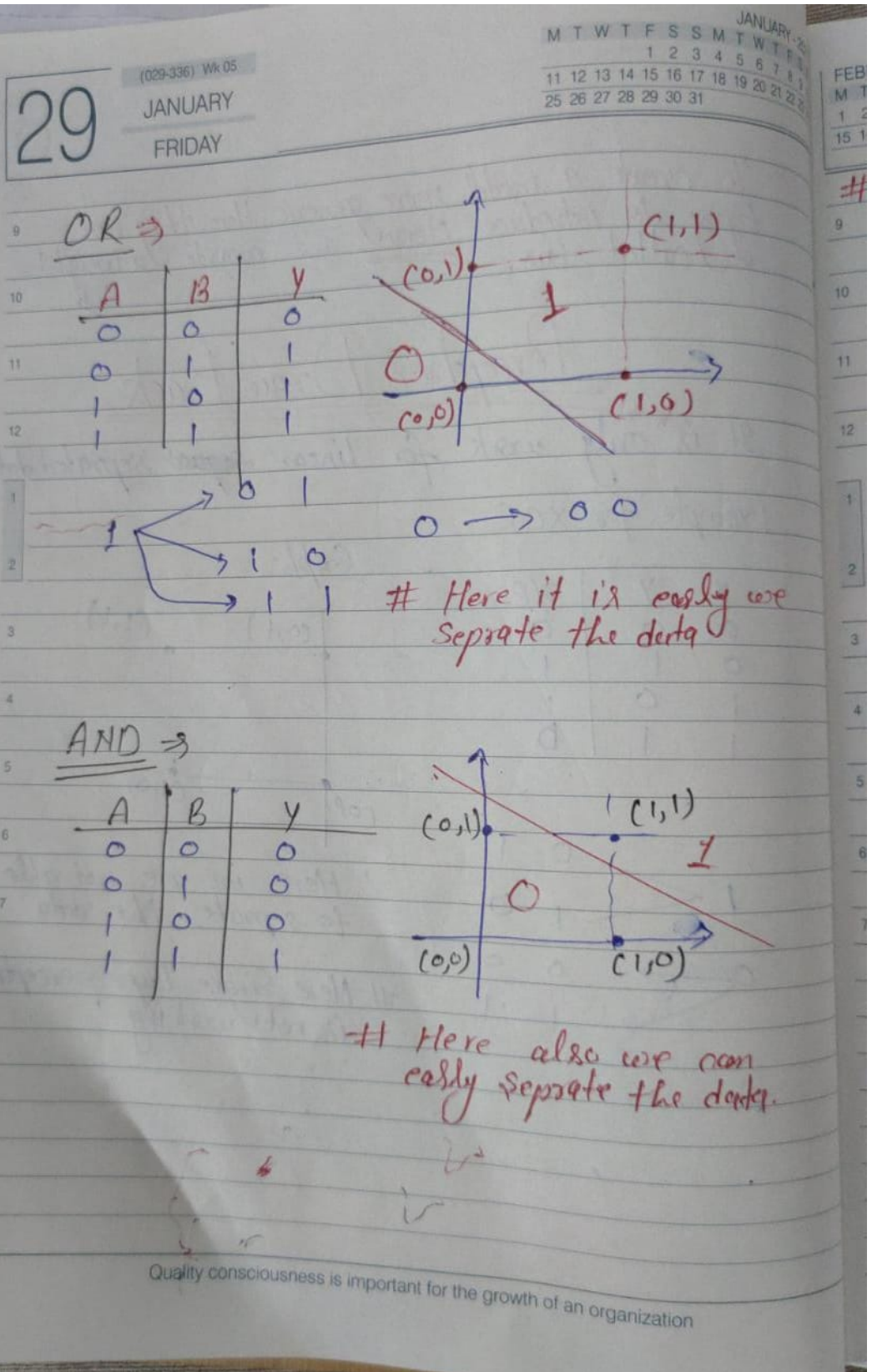
x	y	O/p
0	0	0
0	1	1
1	0	1
1	1	0

Graph:

∴ Here we are not able to separate the data

Here Single layer perceptron is not working

Loneliness comes when one forget that God is the supreme companion



FEBRUARY - 2021
 W T F S S M T W T F S S
 3 4 5 6 7 8 9 10 11 12 13 14
 17 18 19 20 21 22 23 24 25 26 27 28

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We can implement XOR with the help of NAND GATE

NAND GATE

x_1	x_2	y
0	0	1
0	1	1
1	0	1
1	1	0

x_1	x_2	$x_3 = x_1 \cdot x_2$	$x_4 = x_1 \cdot x_3$	$x_5 = x_2 \cdot x_3$	$y = x_4 \cdot x_5$
0	0	1	1	1	0
0	1	1	1	0	1
1	0	1	0	1	1
1	1	0	1	1	0

Sunday 31

Assume all the level of NAND GATE is Neuron
 So we have a multiple NAND so we can
 say it's multilayer Perceptron

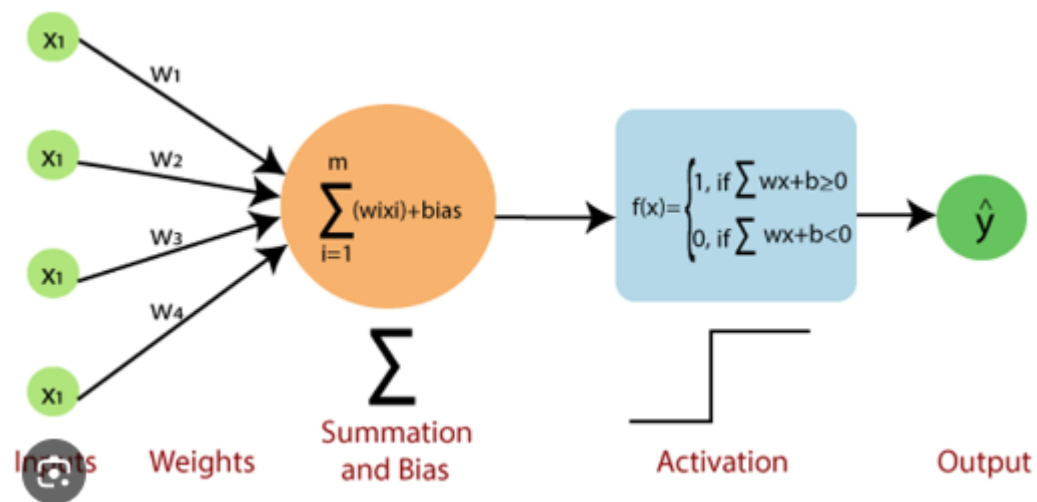
It does not cost a penny, to speak true and sweet words

Type Markdown and LaTeX: α^2

Preceptron Precatival

```
In [1]: 1 import os
2 import pandas as pd
3 import matplotlib.pyplot as plt
4 import numpy as np
5 import seaborn as sns
6 import joblib #saving the model in binary formate
7 from matplotlib.colors import ListedColormap
8
9 plt.style.use("fivethirtyeight")
```

```
In [ ]: 1
```



Perceptron skeleton :)

```
In [ ]: 1
```

```
In [ ]: 1
```

In [2]:

```
1  #the blue Print of perceptron
2
3  class Perceptron:
4      def __init__(self, eta: float=None, epochs: int=None):
5          #eta stand for Learning rate
6          #epochs =complete cycle of (forword_propogation+backward_propogati
7          try:
8              pass
9          except Exception as e:
10             raise e
11
12     def _z_outcome(self):
13         try:
14             pass
15         except Exception as e:
16             raise e
17
18     def activation_funtion(self):
19         try:
20             pass
21         except Exception as e:
22             raise e
23
24     def fit(self):
25         try:
26             pass
27         except Exception as e:
28             raise e
29
30     def predict(self):
31         try:
32             pass
33         except Exception as e:
34             raise e
35
36     def total_loss(self):
37         try:
38             pass
39         except Exception as e:
40             raise e
41
42     def _create_dir_return_path(self):
43         try:
44             pass
45         except Exception as e:
46             raise e
47
48     def save(self):
49         try:
50             pass
51         except Exception as e:
52             raise e
53
54     def load(self):
55         try:
56             pass
57         except Exception as e:
```

```
58  
59  
60
```

raise e

Let's Implement the Perceptron

In []:

```
1
```

In []:

```
1
```


In [3]:

```

1  #the blue Print of perceptron
2
3  class Perceptron:
4      def __init__(self, eta: float=None, epochs: int=None):
5          #eta stand for Learning rate
6          #epochs =complete cycle of (forward_propagation+backward_propagation)
7          try:
8              self.weights = np.random.randn(3)*1e-4 # giving small random weights
9              training = (eta is not None) and (epochs is not None)
10
11              if training:
12                  print(f"Initial weights before training :\n {self.weights}")
13                  self.eta = eta
14                  self.epochs = epochs
15
16          except Exception as e:
17              raise e
18
19      def _z_outcome(self, inputs_with_bais, weights):
20          try:
21              return np.dot(inputs_with_bais, weights)
22          except Exception as e:
23              raise e
24
25      def activation_funtion(self, z):
26          try:
27              return np.where(z > 0 ,1,0)
28          except Exception as e:
29              raise e
30
31      def fit(self, x, y):
32          try:
33              self.x = x
34              self.y = y
35
36              x_with_bais = np.c_[self.x, -np.ones((len(self.x), 1))]
37              print(f"X with bais : \n{x_with_bais}")
38
39              for epoch in range(self.epochs):
40                  print("--"*10)
41                  print(f"for epoch >> {epoch}")
42                  print("--"*10)
43
44                  z = self._z_outcome(x_with_bais, self.weights)
45                  y_hat = self.activation_funtion(z)
46                  print(f"Predicted value after forward pass : \n{y_hat}")
47
48                  self.error = self.y-y_hat
49                  print(f"error : \n{self.error}")
50
51                  self.weights = self.weights+ self.eta*np.dot(x_with_bais.T, self.y-y_hat)
52                  print(f"Updated weights after epochs : {epoch+1}/{self.epochs}")
53                  print("===="*10)
54
55          except Exception as e:
56              raise e
57

```

```
58 def predict(self,x):
59     try:
60         x_with_bais = np.c_[x,-np.ones((len(x), 1))]
61         z = self._z_outcome(x_with_bais,self.weights)
62         return self.activation_funtion(z)
63
64     except Exception as e:
65         raise e
66
67 def total_loss(self):
68     try:
69         total_loss = np.sum(self.error)
70         print(f"\n total loss : {total_loss}\n")
71         return total_loss
72
73     except Exception as e:
74         raise e
75
76 def _create_dir_return_path(self, model_dir, filename):
77     try:
78         os.makedirs(model_dir,exist_ok= True)
79         return os.path.join(model_dir,filename)
80
81     except Exception as e:
82         raise e
83
84 def save(self,filename,model_dir=None):
85     try:
86         if model_dir is not None:
87             model_file_path = self._create_dir_return_path(model_dir,
88             joblib.dump(self,model_file_path)
89
90         else:
91             model_file_path = self._create_dir_return_path('model',fil
92             joblib.dump(self,model_file_path)
93     except Exception as e:
94         raise e
95
96 def load(self,filepath):
97     try:
98         return joblib.load(filepath)
99     except Exception as e:
100         raise e
101
102
```

Let's Utilize our Perceptron class

Before that Let's create a function for Ploting


```

In [4]: 1 def save_plot(df, model, plot_dir = 'plots' ,filename='plot.png'):
2         try:
3             def _create_base_plot(df):
4                 df.plot(kind = 'scatter',x='x1',y='x2',c= 'y',s = 100,cmap='co
5                 plt.axhline(y=0,color = 'black', linestyle = '--',linewidth=1)
6                 plt.axvline(x=0,color = 'black', linestyle = '--',linewidth=1)
7
8                 figure = plt.gcf()
9                 figure.set_size_inches(10,8)
10
11             def _plot_decision_regions(X, y, classifier, resolution=0.02):
12                 colors = ('cyan', 'lightgreen')
13                 cmap = ListedColormap(colors)
14
15                 X = X.values
16                 x1 = X[:,0]
17                 x2 = X[:,1]
18
19                 x1_min,x1_max = x1.min() - 1, x1.max() + 1
20                 x2_min,x2_max = x2.min() - 1, x2.max() + 1
21
22                 xx1, xx2 = np.meshgrid(np.arange(x1_min, x1_max, resolution),
23                                         np.arange(x2_min, x2_max, resolution)
24                                         )
25
26                 y_hat = classifier.predict(np.array([xx1.ravel(), xx2.ravel()])
27                 y_hat = y_hat.reshape(xx1.shape)
28
29                 plt.contourf(xx1,xx2, y_hat, alpha = 0.3, cmap =cmap)
30                 plt.xlim(xx1.min(), xx1.max())
31                 plt.xlim(xx2.min(), xx2.max())
32
33                 plt.plot()
34                 plt.show()
35
36
37                 X,y = prepare_data(df)
38
39                 _create_base_plot(df)
40                 _plot_decision_regions(X,y,model)
41
42                 os.makedirs(plot_dir,exist_ok=True)
43                 plot_path = os.path.join(plot_dir,filename)
44
45                 plt.savefig(plot_path)
46
47             except Exception as e:
48                 raise e
49

```

```

In [ ]: 1

```

Creating a function for Cepreparing the data into X (Independent) and Y (Dependent)

```
In [5]: 1 def prepare_data(df,target_cols:str = 'y'):
2         try:
3             x = df.drop(target_cols,axis=1)
4             y=df[target_cols]
5
6             return x,y
7         except Exception as e:
8             raise e
```

AND

A	B	A AND B
0	0	0
0	1	0
1	0	0
1	1	1

```
In [6]: 1 AND = {
2         'x1': [0,0,1,1],
3         'x2': [0,1,0,1],
4         'y' : [0,0,0,1]
5     }
6
7     # dict data converting into a data frame
8
9     df_AND = pd.DataFrame(AND)
10    df_AND
```

```
Out[6]:
```

	x1	x2	y
0	0	0	0
1	0	1	0
2	1	0	0
3	1	1	1

```
In [7]: 1 x,y = prepare_data(df_AND, 'y')
        2 print(x)
        3 print('=='*10)
        4 print(y)
```

```
      x1  x2
0      0   0
1      0   1
2      1   0
3      1   1
=====
0      0
1      0
2      0
3      1
Name: y, dtype: int64
```

Here i am calling Perceptron Function for creating model

```
In [8]: 1 x,y = prepare_data(df_AND)
        2 ETA = 0.1 # eta lies between 0 to 1
        3 EPOCHS = 10
        4
        5 model_and = Perceptron(ETA,EPOCHS)
        6 model_and.fit(x,y)
        7 _ = model_and.total_loss()
```

```
Initial weights before training :
[-1.56638776e-05 -7.12828881e-05 -4.17482972e-05]
X with bias :
[[ 0.  0. -1.]
 [ 0.  1. -1.]
 [ 1.  0. -1.]
 [ 1.  1. -1.]]
-----
for epoch >> 0
-----
Predicted value after forward pass :
[1 0 1 0]
error :
0  -1
1   0
2  -1
3   1
Name: y, dtype: int64
Updated weights after epochs : 1/10 :
[-1.56638776e-05 -7.12828881e-05 -4.17482972e-05]
```

Saving the Model in the directory

```
In [9]: 1 model_and.save(filename='and.model',model_dir="Logical_model")
```


Loading the model

```
In [10]: 1 load_and = Perceptron().load(filepath='Logical_model/and.model')
          2 load_and
```

Out[10]: <__main__.Perceptron at 0x1a958c7ab20>

Doing the prediction

```
In [11]: 1 load_and.predict(x=[[0,0]])
```

Out[11]: array([0])

```
In [12]: 1 ## Let's Predict Hole data
          2 x
```

Out[12]:

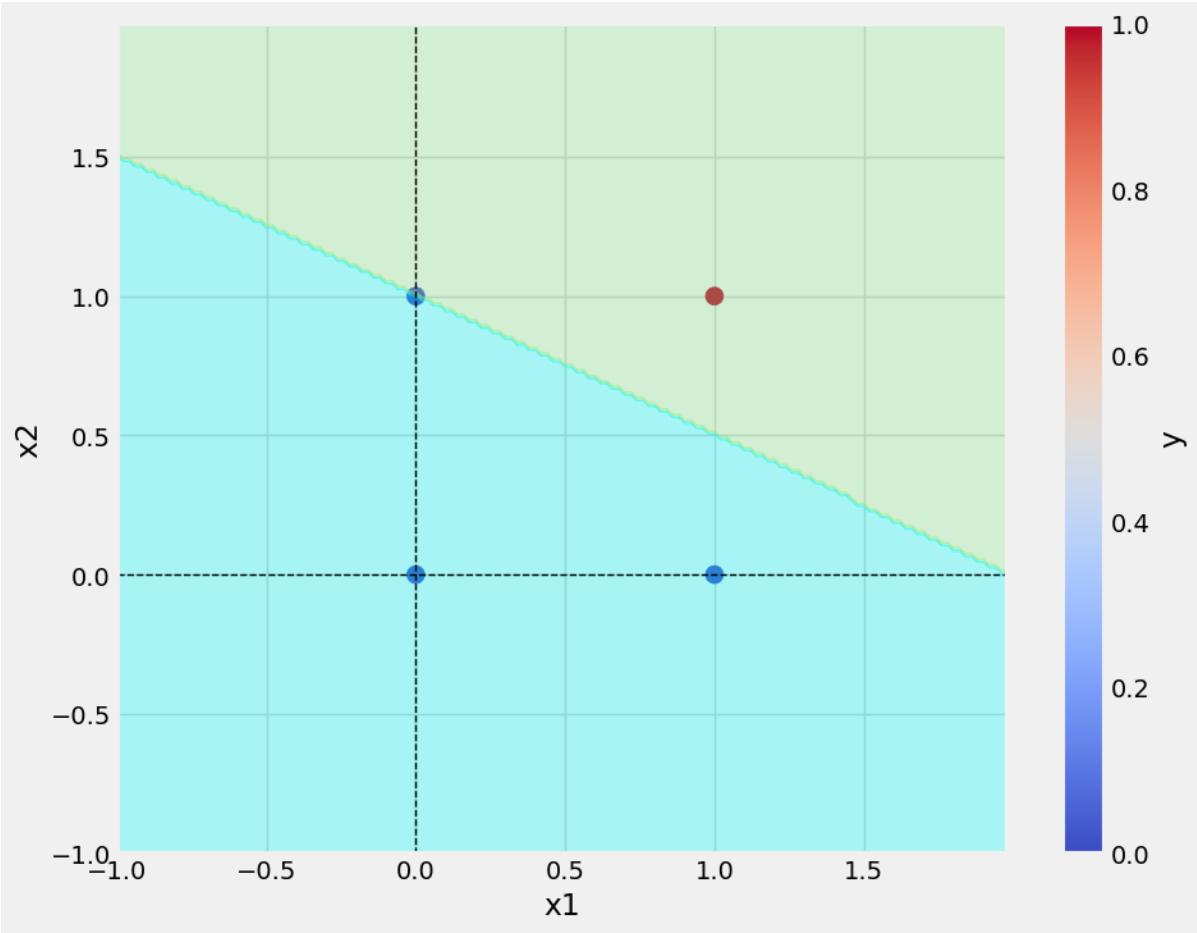
	x1	x2
0	0	0
1	0	1
2	1	0
3	1	1

```
In [13]: 1 #
          2 prediction = load_and.predict(x)
          3 print(f"Predicted values : {prediction}")
          4 print(f'Actual values :{list(y)}')
```

Predicted values : [0 0 0 1]
Actual values : [0, 0, 0, 1]

In [14]:

1 save_plot(df=df_AND,model=model_and,filename='AND.png')



<Figure size 640x480 with 0 Axes>

OR Data

Input A	Input B	OR Operator
		A B
0	0	0
0	1	1
1	0	1
1	1	1

```

In [15]: 1 OR = {
2         'x1': [0,0,1,1],
3         'x2': [0,1,0,1],
4         'y' : [0,1,1,1]
5     }
6
7     # dict data converting into a data frame
8
9     df_OR = pd.DataFrame(OR)
10    df_OR

```

```

Out[15]:
   x1  x2  y
0    0    0  0
1    0    1  1
2    1    0  1
3    1    1  1

```

```

In [16]: 1 X,y = prepare_data(df_OR)
2
3     ETA = 0.1
4     EPOCHS = 10
5
6     model_or = Perceptron(eta=ETA,epochs=EPOCHS)
7     model_or.fit(X,y)
8
9     _ = model_or.total_loss()
10

```

```

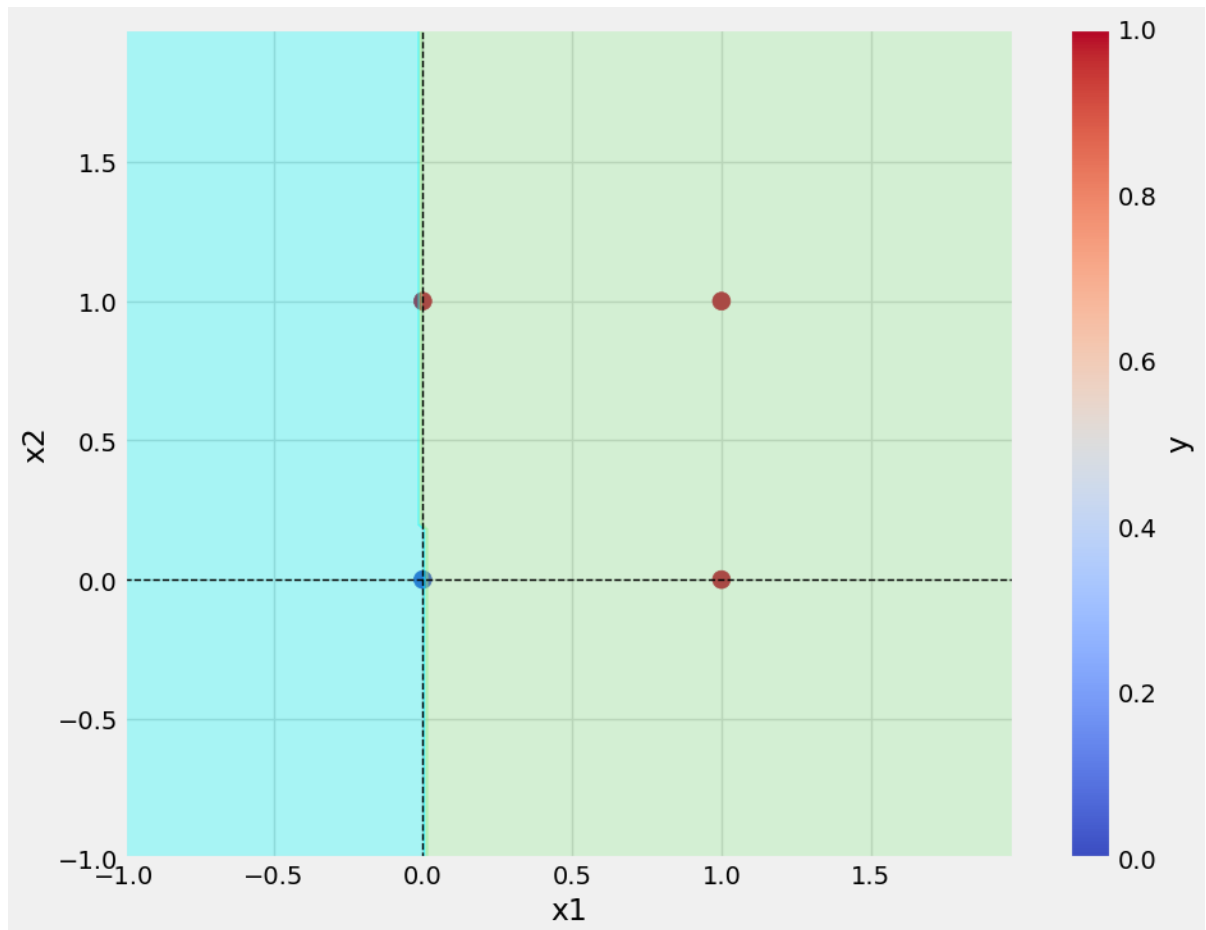
Initial weights before training :
[1.58477266e-05 1.01655688e-04 1.90209052e-05]
X with bias :
[[ 0.  0. -1.]
 [ 0.  1. -1.]
 [ 1.  0. -1.]
 [ 1.  1. -1.]]
-----
for epoch >> 0
-----
Predicted value after forward pass :
[0 1 0 1]
error :
0    0
1    0
2    1
3    0
Name: y, dtype: int64
Updated weights after epochs : 1/10 :
[ 0.0001585  0.0001016  0.0000000]

```

```
In [17]: 1 prediction_or = model_or.predict(df_OR.iloc[:, :-1])
2 print('=='*20)
3 print(f"Predicated values : {prediction_or}")
4 print('=='*20)
5 print(f"Actual values : {list(df_OR['y'])}")
```

```
=====
Predicated values : [0 1 1 1]
=====
Actual values : [0, 1, 1, 1]
```

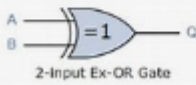
```
In [18]: 1 save_plot(df=df_OR,model=model_or,filename='OR.png')
```



<Figure size 640x480 with 0 Axes>

XOR

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

Symbol	Truth Table		
 2-Input Ex-OR Gate	A	B	Q
	0	0	0
	0	1	1
	1	0	1
	1	1	0

Boolean Expression $Q = A \text{ XOR } B$

```

In [19]: 1 XOR = {
          2     'x1': [0,0,1,1],
          3     'x2': [0,1,0,1],
          4     'y' : [0,1,1,0]
          5 }
          6
          7 # dict data converting into a data frame
          8
          9 df_XOR = pd.DataFrame(XOR)
         10 df_XOR
  
```

```

Out[19]:
   x1  x2  y
0  0  0  0
1  0  1  1
2  1  0  1
3  1  1  0
  
```



```
In [20]: 1 X,y = prepare_data(df_XOR)
          2
          3 ETA = 0.1
          4 EPOCHS = 20
          5
          6 model_xor = Perceptron(eta=ETA,epochs=EPOCHS)
          7 model_xor.fit(X,y)
          8
          9 _ = model_xor.total_loss()
         10
         11
```

```
Initial weights before training :
[-0.00019012 -0.00018722  0.00021099]
X with bias :
[[ 0.  0. -1.]
 [ 0.  1. -1.]
 [ 1.  0. -1.]
 [ 1.  1. -1.]]
-----
for epoch >> 0
-----
Predicted value after forward pass :
[0 0 0 0]
error :
0  0
1  1
2  1
3  0
Name: y, dtype: int64
Updated weights after epochs : 1/20 :
5 0.00000000 0.00000000 0.00000000
```

```
In [21]: 1 df_XOR
```

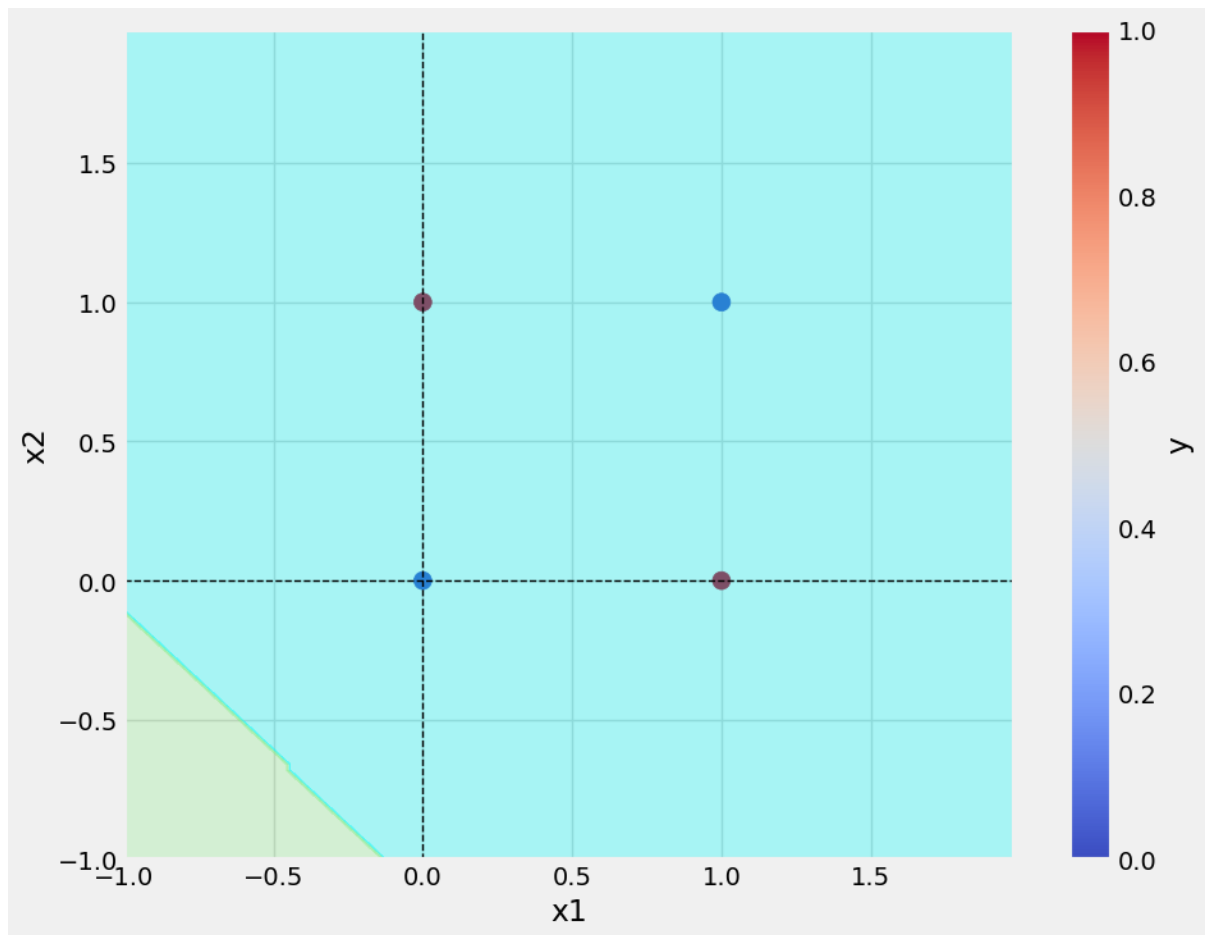
```
Out[21]:
```

	x1	x2	y
0	0	0	0
1	0	1	1
2	1	0	1
3	1	1	0

```
In [22]: 1 prediction_xor = model_xor.predict(df_XOR.iloc[:, :-1])
          2 print('=='*20)
          3 print(f"Predicted value :{prediction_xor}")
          4 print('=='*20)
          5 print(f"Actual values : {list(df_XOR['y'])}")
```

```
=====
Predicted value :[0 0 0 0]
=====
Actual values : [0, 1, 1, 0]
```

```
In [23]: 1 save_plot(df=df_XOR,model=model_xor,filename='xor.png')
```



<Figure size 640x480 with 0 Axes>

Perceptron DrawBack

Here in x-or we are not able to seprate the data ,we are not able to Draw a line So for that we need multilayer Perceptron

```
In [ ]: 1
```