

Correlation

Correlation

- **Correlation:**

1. How two variables move together.
 2. For example height & weight
-
1. Positive correlations mean that two variables fluctuate together (a positive change in one is a positive change to another)
 2. negative correlations mean that two variable change opposite one another (a positive change in one is a negative change in another)

Positive Correlation

- **Example Answer 1:**
 - The more hours you work, the higher your paycheck will be.
- **Example Answer 2:**
 - As a child grows, so too does their shoe size.

Negative Correlation

- **Example Answer 1:**

- The slower you drive, the longer your trip will take.

- **Example Answer 2:**

- The more you exercise, the less you'll weigh.

No correlation

- **Example Answer 1:**

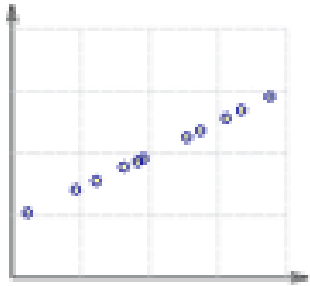
- The amount of tea someone drinks vs. how British they are.

- **Example Answer 2:**

- The price of chocolate vs. the price of cereal.

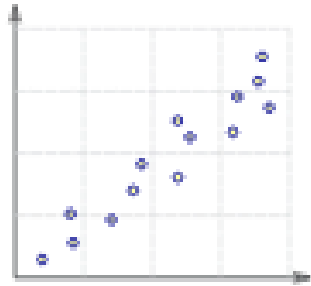
Strength

*Perfect
Positive
Correlation*



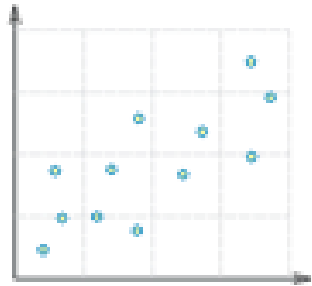
1

*High
Positive
Correlation*



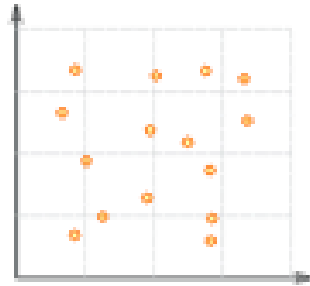
0.9

*Low
Positive
Correlation*



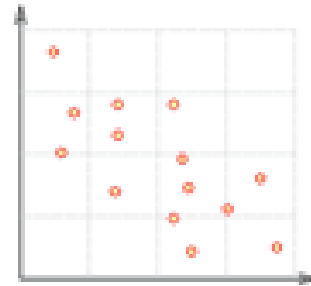
0.5

*No
Correlation*



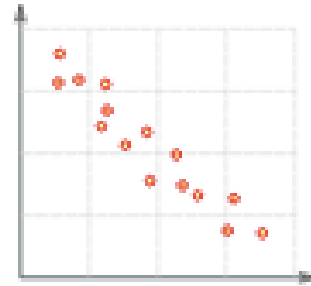
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*Low
Negative
Correlation*



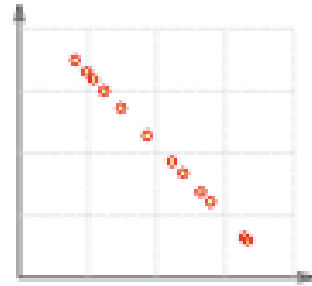
-0.5

*High
Negative
Correlation*



-0.9

*Perfect
Negative
Correlation*

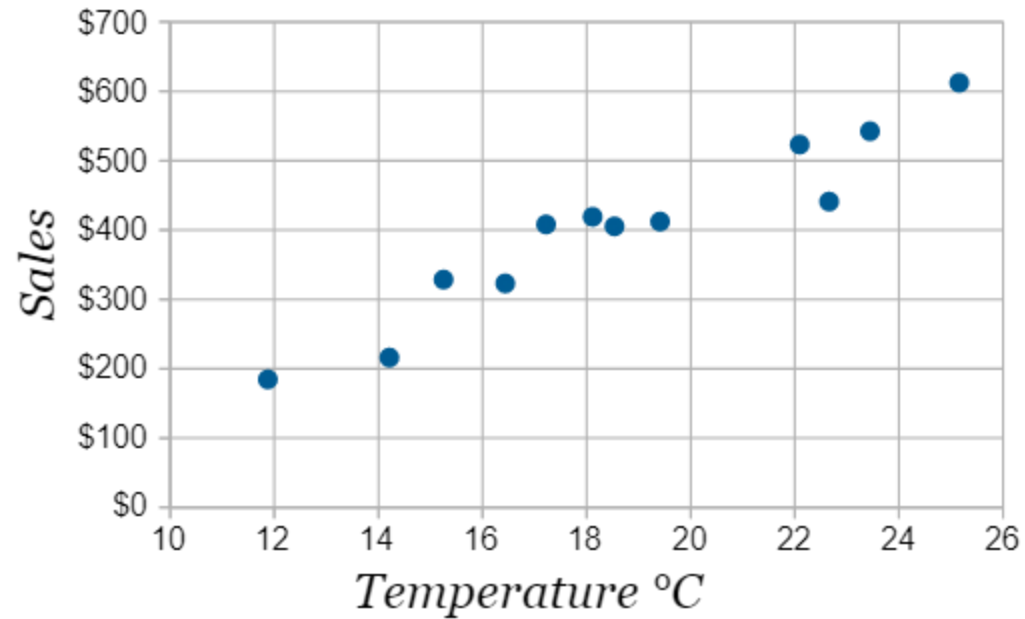


-1

The local ice cream shop keeps track of how much ice cream they sell versus the temperature on that day. Here are their figures for the last 12 days:

Ice Cream Sales vs Temperature	
Temperature °C	Ice Cream Sales
14.2°	\$215
16.4°	\$325
11.9°	\$185
15.2°	\$332
18.5°	\$406
22.1°	\$522
19.4°	\$412
25.1°	\$614
23.4°	\$544
18.1°	\$421
22.6°	\$445
17.2°	\$408

How Ice cream Sales is related to temperature



$$r_{xy} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}}$$

How to Calculate correlation coefficient

2 Subtract Mean

3 Calculate ab , a^2 and b^2

Temp °C	Sales	"a"	"b"	a×b	a ²	b ²
14.2	\$215	-4.5	-\$187	842	20.3	34,969
16.4	\$325	-2.3	-\$77	177	5.3	5,929
11.9	\$185	-6.8	-\$217	1,476	46.2	47,089
15.2	\$332	-3.5	-\$70	245	12.3	4,900
18.5	\$406	-0.2	\$4	-1	0.0	16
22.1	\$522	3.4	\$120	408	11.6	14,400
19.4	\$412	0.7	\$10	7	0.5	100
25.1	\$614	6.4	\$212	1,357	41.0	44,944
23.4	\$544	4.7	\$142	667	22.1	20,164
18.1	\$421	-0.6	\$19	-11	0.4	361
22.6	\$445	3.9	\$43	168	15.2	1,849
17.2	\$408	-1.5	\$6	-9	2.3	36
18.7	\$402			5,325	177.0	174,757

1 Calculate Means

4 Sum Up

5 $\frac{5,325}{\sqrt{177.0 \times 174,757}} = 0.9575$