

# Using TensorFlow to predict Jet numbers in CERN Proton Collisions (Evaluator-OMID-BAGHCHEH-SARAEI)

July 3, 2022

The purpose is to create a machine learning model that can predict the number of Jets in CERN's [Proton Collision Dataset](#), which is stored in `CERN_Proton_Collision.zip`. I use TensorFlow to accomplish this.

MultiJet primary dataset in AOD format from RunB of 2010. This dataset contains runs from 2010 RunB. The list of all validated runs, which must be applied to all analyses, can be found in <http://opendata.cern.ch/record/1000>. This file contains events from the MultiJet primary dataset from the CMS open data release, and computes the razor variables MR and Rsq, used in supersymmetric particle searches. More details on the razor variables can be found in Phys. Rev. D 90, 112001 (<https://journals.aps.org/prd/pdf/10.1103/PhysRevD.90.112001>)

Content:

- 1) Run: The run number of the event.
- 2) Lumi: The lumi section of the event.
- 3) Event: The event number of the event.
- 4) MR: First razor kinematic variable, the MR variable is an estimate of an overall mass scale, which in the limit of massless decay products equals the mass of the heavy parent particle.
- 5) Rsq: Second razor kinematic variable, the Rsq variable is the square of the ratio R, which quantifies the flow of energy in the plane perpendicular to the beam and the partitioning of momentum between visible and invisible particles.

6,7,8,9) E1,Px1,Py1,Pz1: The four-vector of the leading megajet (with the largest transverse momentum).

10,11,12,13) E2,Px2,Py2,Pz2: The four-vector of the subleading megajet (with the largest transverse momentum).

- 14) HT: The scalar sum of the transverse momentum of the jets.
- 15) MET: The magnitude of the vector sum of the transverse energy of the particles in the event.
- 16) nJets: The number of jets with transverse momentum above 40 GeV.
- 17) nBJets: The number of b-tagged jets with transverse momentum above 40 GeV.

Source: [Kaggle](#)

```
[ ]: #Import libraries
import numpy as np
import scipy.optimize as opt
import re, seaborn as sns
import pandas as pd
from sklearn.tree import DecisionTreeClassifier
import matplotlib.pyplot as plt
from sklearn import preprocessing
import tensorflow as tf
import cv2
from google.colab.patches import cv2_imshow
from sklearn.neighbors import KNeighborsClassifier
from sklearn import metrics
from sklearn.metrics import classification_report
from sklearn.ensemble import RandomForestClassifier
from sklearn.ensemble import GradientBoostingClassifier
from sklearn.ensemble import VotingClassifier
from sklearn.neural_network import MLPClassifier
from sklearn.naive_bayes import GaussianNB
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import MinMaxScaler
from mpl_toolkits.mplot3d import Axes3D
from matplotlib.colors import ListedColormap
%matplotlib inline
```

## 1 Read data using pandas

```
[ ]: df = pd.read_csv("CERN_Proton_Collision.zip")
df.head()
```

	Run	Lumi	Event	MR	Rsq	E1	Px1	Py1	\
0	148029	388	302318745	215.553	0.031977	136.7100	-109.893	-54.03420	
1	148029	388	302323641	155.437	0.042157	83.3865	81.150	6.88361	
2	148029	388	302336217	400.563	0.026938	253.1840	139.902	102.64000	
3	148029	388	302382289	286.245	0.094192	175.4860	-156.024	-62.95350	
4	148029	388	302403873	204.514	0.018804	833.7950	100.410	-16.65900	

	Pz1	E2	Px2	Py2	Pz2	HT	MET	nJets	\
0	-58.9032	142.1790	70.0254	41.12250	-116.5130	203.666	18.31100	2	
1	-12.9688	73.9025	-72.2472	11.88350	3.0899	154.659	14.77470	2	
2	-101.9350	535.5510	-110.3790	-89.09290	-516.1790	343.280	25.22110	3	
3	-47.7434	112.8510	89.0843	3.45025	67.9007	257.397	46.02880	2	
4	-827.4980	445.6120	-91.1991	15.55830	-390.1440	269.492	8.11345	3	

	nBJets
0	0

```
1      0
2      0
3      0
4      0
```

## 2 I need to know what type of data I am working with before I can work with dataframe, so I check it using the dtypes.

```
[ ]: df.dtypes
```

```
[ ]: Run        int64
Lumi        int64
Event       int64
MR          float64
Rsq          float64
E1          float64
Px1          float64
Py1          float64
Pz1          float64
E2          float64
Px2          float64
Py2          float64
Pz2          float64
HT          float64
MET         float64
nJets       int64
nBJets      int64
dtype: object
```

In the dataframe, there are 21726 records with 17 columns.

```
[ ]: df.shape
```

```
[ ]: (21726, 17)
```

I am going to test if there are NaN values in dataframe

```
[ ]: df.isnull().any().any()
```

```
[ ]: False
```

There are no NaN values

I want to know how many of each type of Jet are in the data frame, so I create a histogram and pie chart. Before that, I create a data frame containing a number of jets, as follows:

```
[ ]: d = {'nJets': ['2 Jets', '3 Jets', '4 Jets', '5 Jets', '6 Jets', '7 Jets'], 'Number of Jets': [14002, 6204, 1325, 169, 23, 3]}
dfC = pd.DataFrame(data=d)
```

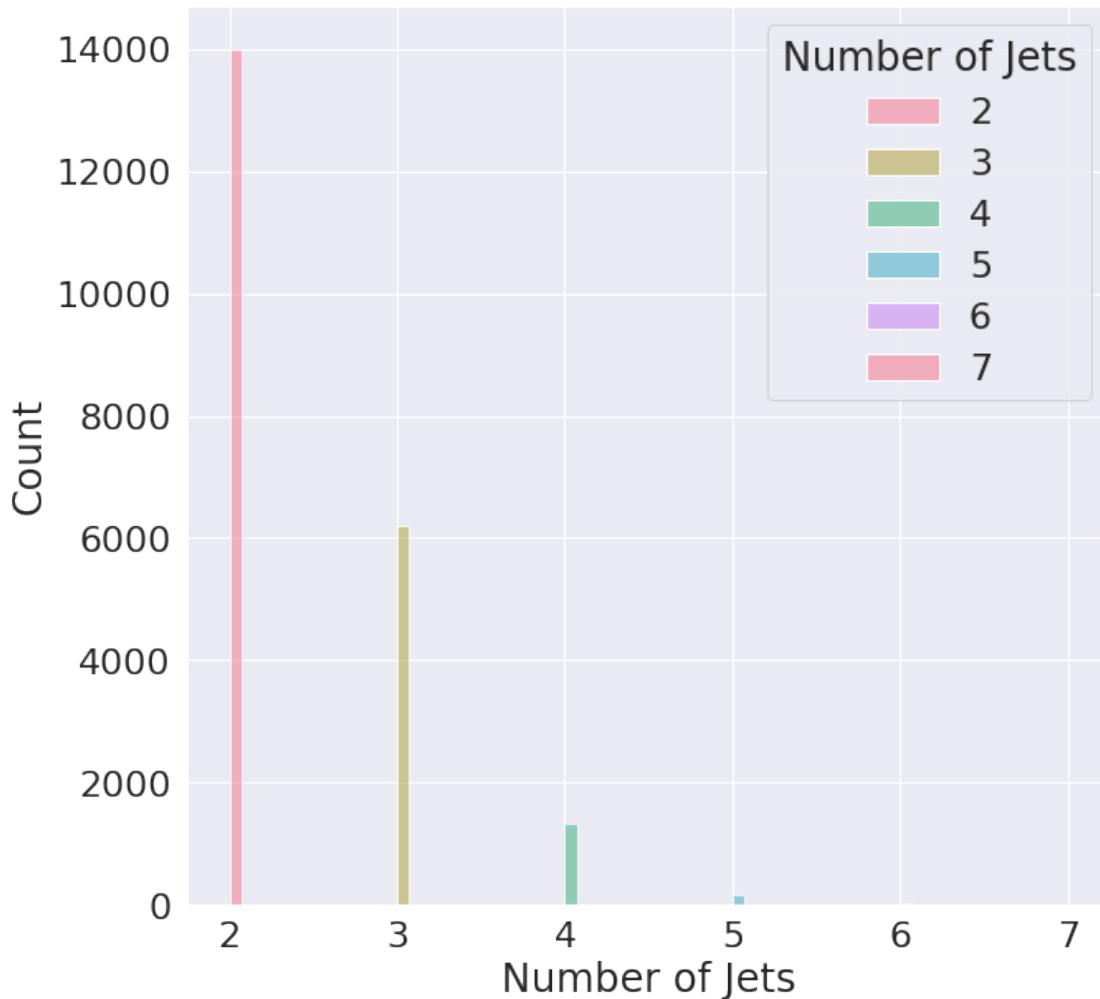
```
[ ]: nJets  Number of Jets
0 2 Jets      14002
1 3 Jets      6204
2 4 Jets      1325
3 5 Jets      169
4 6 Jets      23
5 7 Jets      3
```

### 3 Jet histogram

```
[ ]: df1 = df
df1 = df1.rename(columns={'nJets': 'Number of Jets'})
plt.figure(figsize=(10, 10))
sns.set(font_scale=2.0)
plt.title("Number of Jets histogram", y=1.04)
sns.histplot(data=df1, x="Number of Jets", hue="Number of Jets", palette="husl")
```

```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5e00e5b10>
```

Number of Jets histogram



## 4 Pie chart

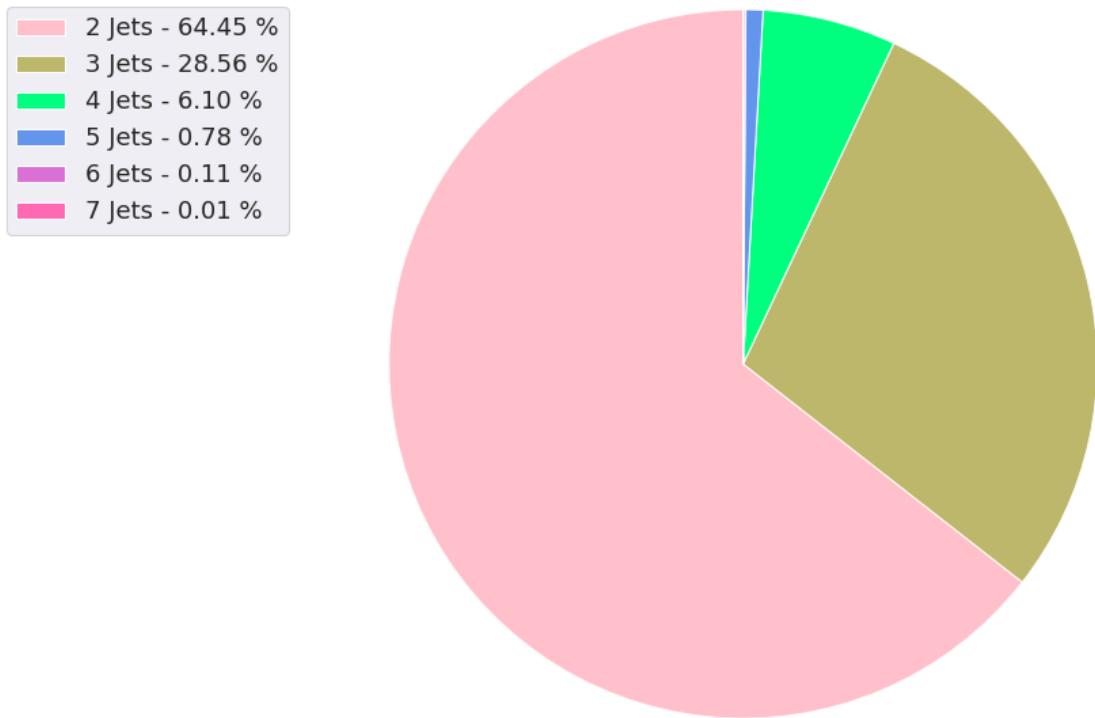
```
[ ]: plt.figure(figsize=(10, 10))
x = np.char.array(['2 Jets', '3 Jets', '4 Jets', '5 Jets', '6 Jets', '7 Jets'])
y = np.array([14002, 6204, 1325, 169, 23, 3])
colors = ['pink', 'darkkhaki', 'springgreen', 'cornflowerblue', 'orchid', 'hotpink']
percent = 100.*y/y.sum()
patches, texts = plt.pie(y, colors=colors, startangle=90, radius=1.2)
labels = ['{0} - {1:1.2f}%'.format(i,j) for i,j in zip(x, percent)]
sort_legend = True
if sort_legend:
    patches, labels, dummy = zip(*sorted(zip(patches, labels, y),
                                         key=lambda x: x[2],
```

```

        reverse=True))
plt.legend(patches, labels, loc='best', bbox_to_anchor=(-0.1, 1.),
           fontsize=18)

plt.savefig('piechart.png', bbox_inches='tight')

```



Pie chart and histograms show that 5, 6, and 7 Jets have a small percentage of the data frame.

## 5 Descriptive statistics:

```
[ ]: df.describe()
```

	Run	Lumi	Event	MR	Rsq	\
count	21726.000000	21726.000000	2.172600e+04	21726.000000	21726.000000	
mean	148666.049710	900.693501	8.635646e+08	351.981435	0.023253	
std	596.085618	496.482684	4.786516e+08	193.691363	0.023291	
min	147926.000000	388.000000	3.023155e+08	29.999900	0.000009	
25%	148029.000000	463.000000	4.976106e+08	229.790750	0.007907	
50%	149181.000000	986.000000	9.709389e+08	292.911000	0.016817	
75%	149181.000000	999.000000	9.844834e+08	406.883000	0.031612	
max	149181.000000	1804.000000	1.703645e+09	2433.820000	0.763695	

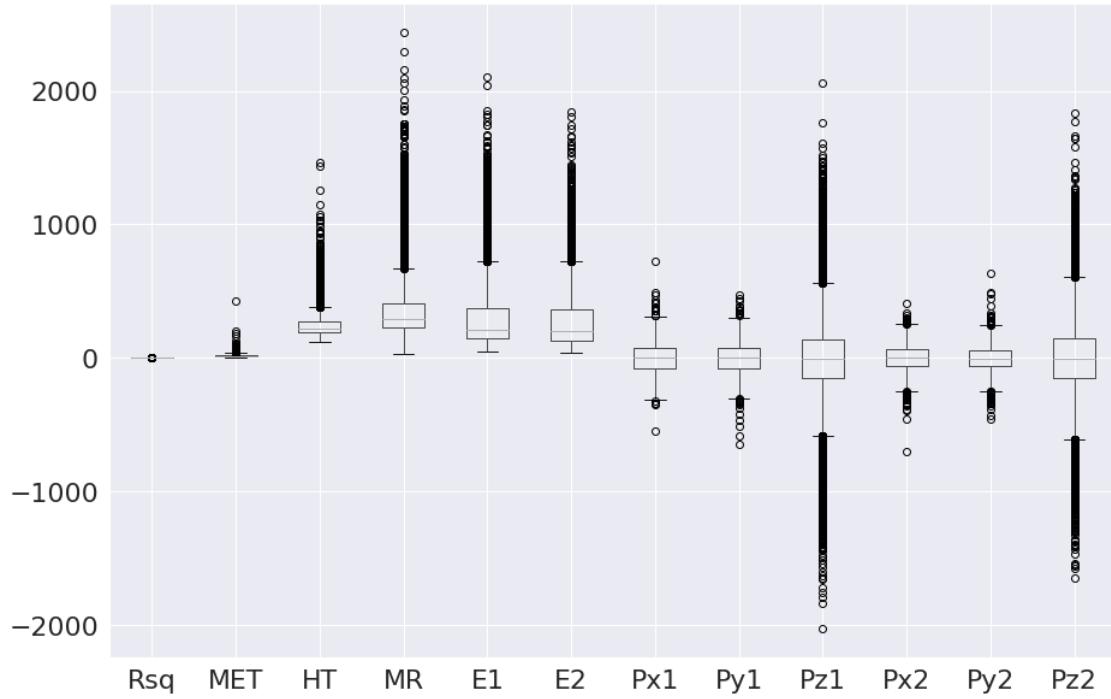
  

	E1	Px1	Py1	Pz1	E2	\
--	----	-----	-----	-----	----	---

count	21726.000000	21726.000000	21726.000000	21726.000000	21726.000000	21726.000000
mean	297.178955	0.283289	0.764211	-8.523257	277.410117	
std	224.040020	91.701247	90.770124	341.366770	206.890743	
min	44.947600	-543.821000	-648.385000	-2022.310000	42.048600	
25%	143.531000	-78.472975	-75.770000	-151.347750	126.916250	
50%	212.060500	-0.310509	1.238670	-5.478110	204.140000	
75%	374.542750	78.562475	77.738075	135.345250	366.710500	
max	2101.580000	722.291000	470.234000	2061.890000	1843.360000	
	Px2	Py2	Pz2	HT	MET	\
count	21726.000000	21726.000000	21726.000000	21726.000000	21726.000000	
mean	-0.399385	-0.909938	-1.915512	242.328342	16.005371	
std	76.720135	75.758491	321.415092	78.841528	10.797882	
min	-700.112000	-459.801000	-1647.600000	120.938000	0.100445	
25%	-63.333250	-62.706450	-154.231750	193.252000	8.626845	
50%	-0.548208	-1.900460	-1.803295	223.696000	14.035000	
75%	62.852025	61.111550	151.167750	269.241500	21.091050	
max	405.326000	635.734000	1830.370000	1462.630000	423.144000	
	nJets	nBJets				
count	21726.000000	21726.000000				
mean	2.435791	0.053668				
std	0.655750	0.236334				
min	2.000000	0.000000				
25%	2.000000	0.000000				
50%	2.000000	0.000000				
75%	3.000000	0.000000				
max	7.000000	2.000000				

## 6 Boxplots and outliers

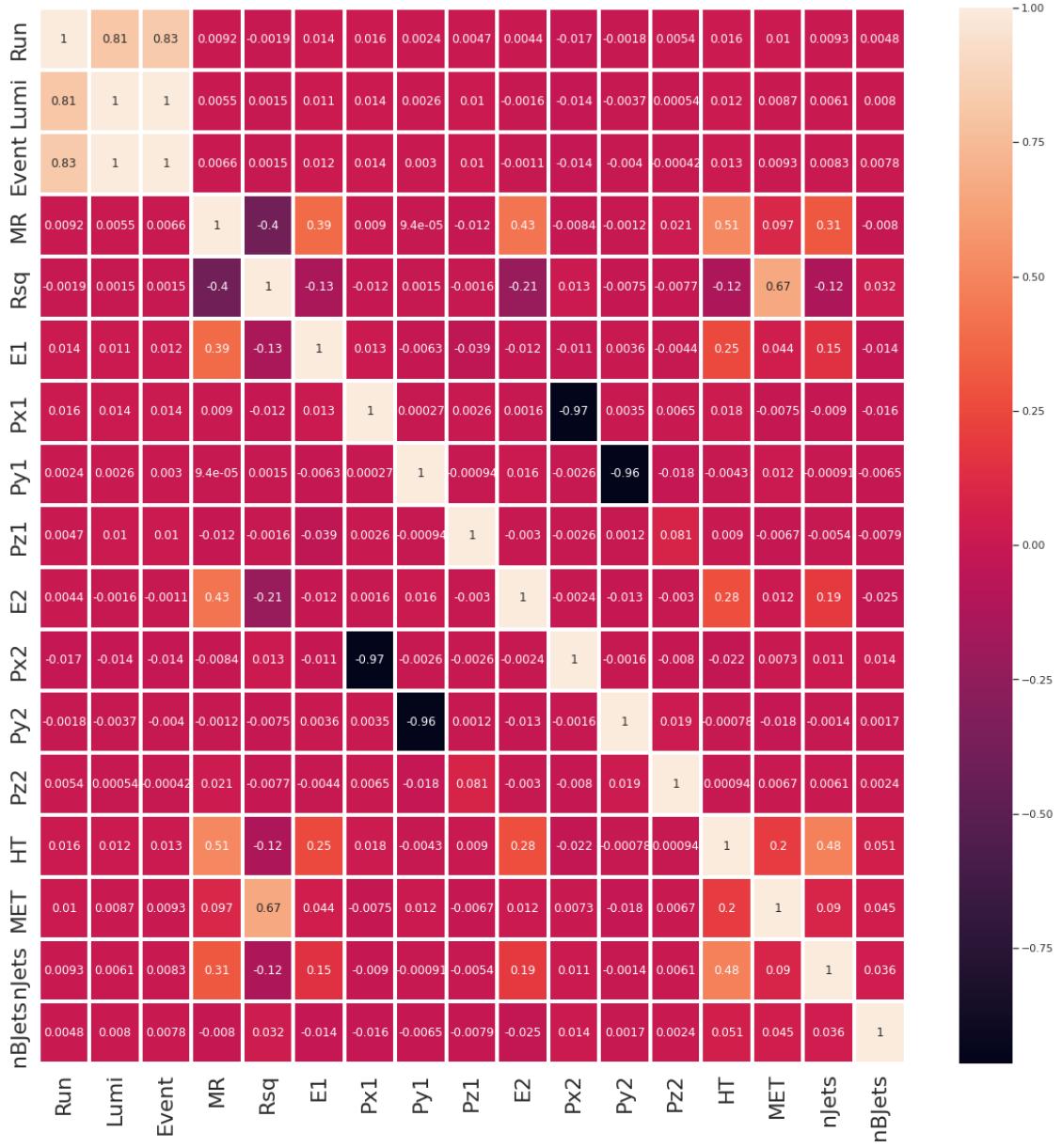
```
[ ]: plt.figure(figsize=(15, 10))
boxplot = df.boxplot(column=['Rsq', 'MET', 'HT', 'MR', 'E1', 'E2', 'Px1', □
→ 'Py1', 'Pz1', 'Px2', 'Py2', 'Pz2'])
```



I use the Seaborn `heatmap()` function to determine which features have the most impact on `nJets`.

```
[ ]: fig, ax = plt.subplots(figsize=(20,20))
sns.set(font_scale=1.0)
sns.heatmap(df.corr() , annot= True, linewidths=3, ax=ax)
```

```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5dfa71890>
```



## 7 Number of Jets is greatly influenced by:

```
[ ]: d = {'Number of Jets is greatly influenced by': ['HT', 'MR', 'E2', 'E1'],
      'correlation coefficient': [0.48, 0.31, 0.19, 0.15]}
dfC = pd.DataFrame(data=d)
```

```
[ ]: Number of Jets is greatly influenced by: correlation coefficient
          HT           0.48
          0
```

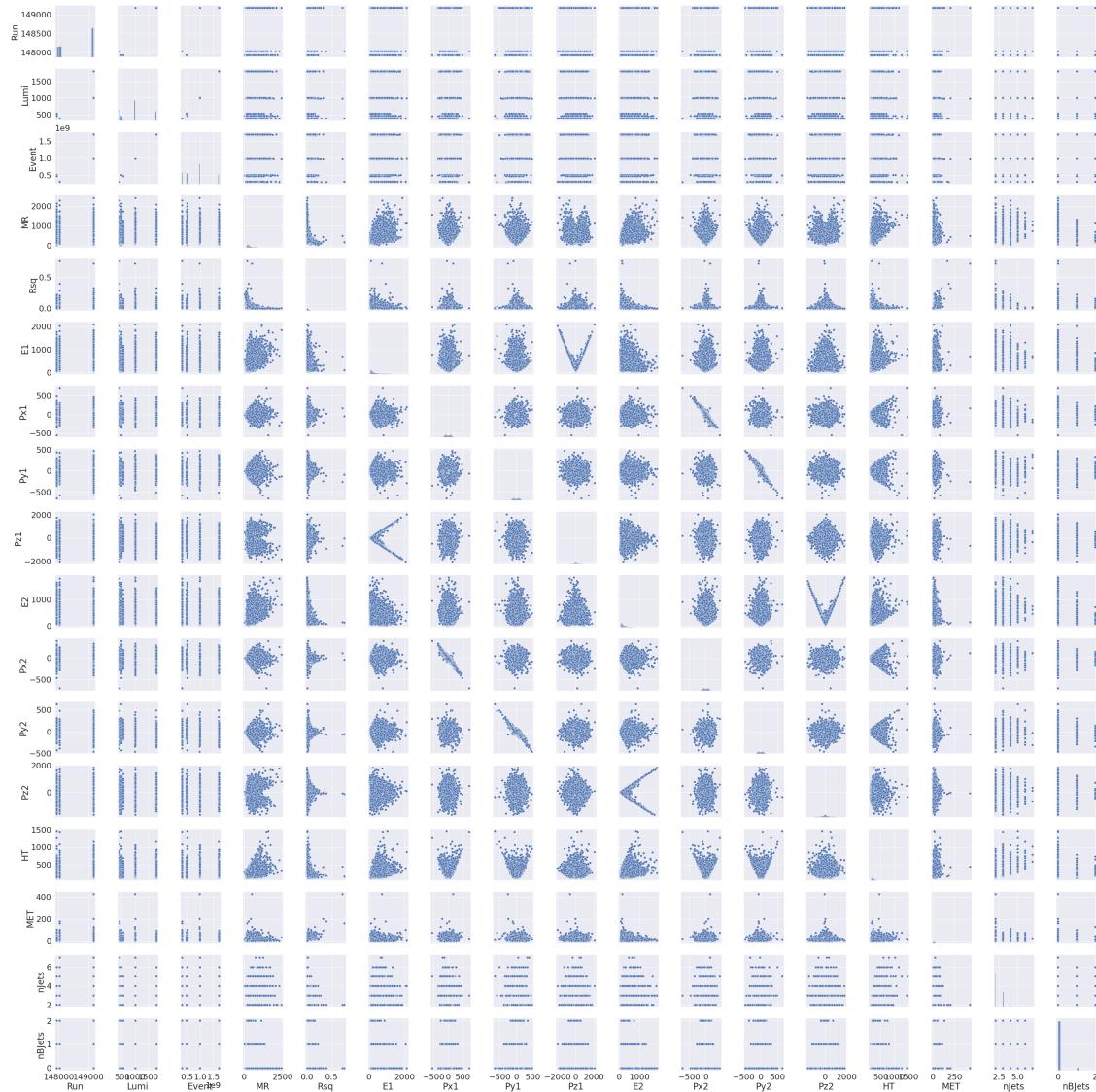
1	MR	0.31
2	E2	0.19
3	E1	0.15

## 8 Data Visualization and Analysis:

```
[ ]: plt.figure(figsize=(10, 8))
sns.set(font_scale=2.0)
sns.pairplot(df)
```

```
[ ]: <seaborn.axisgrid.PairGrid at 0x7fc5dfccde90>
```

<Figure size 720x576 with 0 Axes>



**I would like to plot more details on some of these graphs in 2D and 3D.**

# Scatter plots in 2D

July 3, 2022

## 1 Scatter plots in 2D

### 1.1 1. E1 vs Px1

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='Px1', y='E1', hue='Number of Jets', palette="husl")
```

[ ]: <matplotlib.axes.\_subplots.AxesSubplot at 0x7fc5d398b3d0>



### 1.2 2. MR vs Px1

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='Px1', y='MR', hue='Number of Jets', palette="husl")
```

```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d3fa5cd0>
```

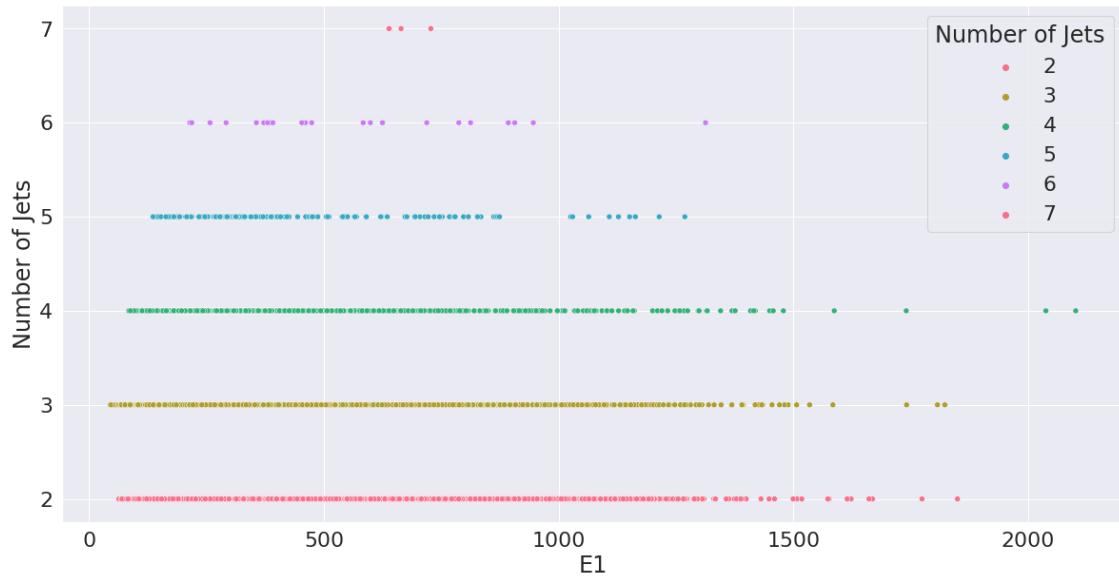


### 1.3 3. Number of Jets vs E1

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='E1', y='Number of Jets', hue='Number of Jets',
                 palette="husl")
```

```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d375d310>
```

simple 2D scatter plot



- The seven-jet phenomenon can only be spotted in  $500 < E_1 < 1000$
- The four-jet phenomenon is only a phenomenon that can be spotted in  $E_1 > 2000$

#### 1.4 4. HT vs MR

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='MR', y='HT', hue='Number of Jets', palette="husl")
```

```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d3639d10>
```

simple 2D scatter plot



## 1.5 4. Py1 vs Px1

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='Px1', y='Py1', hue='Number of Jets', palette="husl")
```

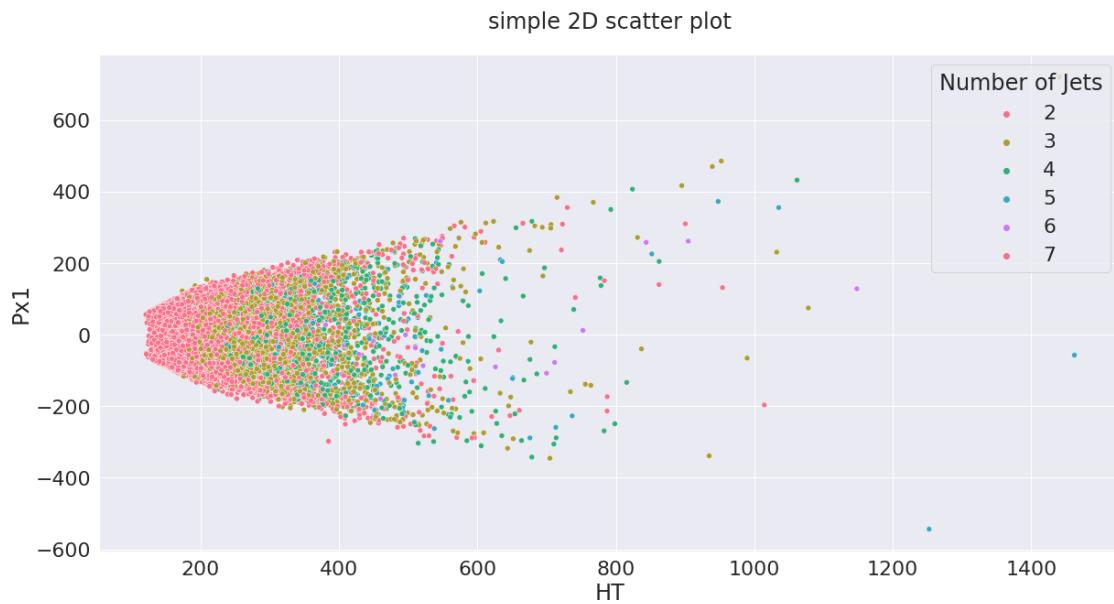
```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d33d3050>
```



## 1.6 5. Px1 vs HT

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='HT', y='Px1', hue='Number of Jets', palette="husl")
```

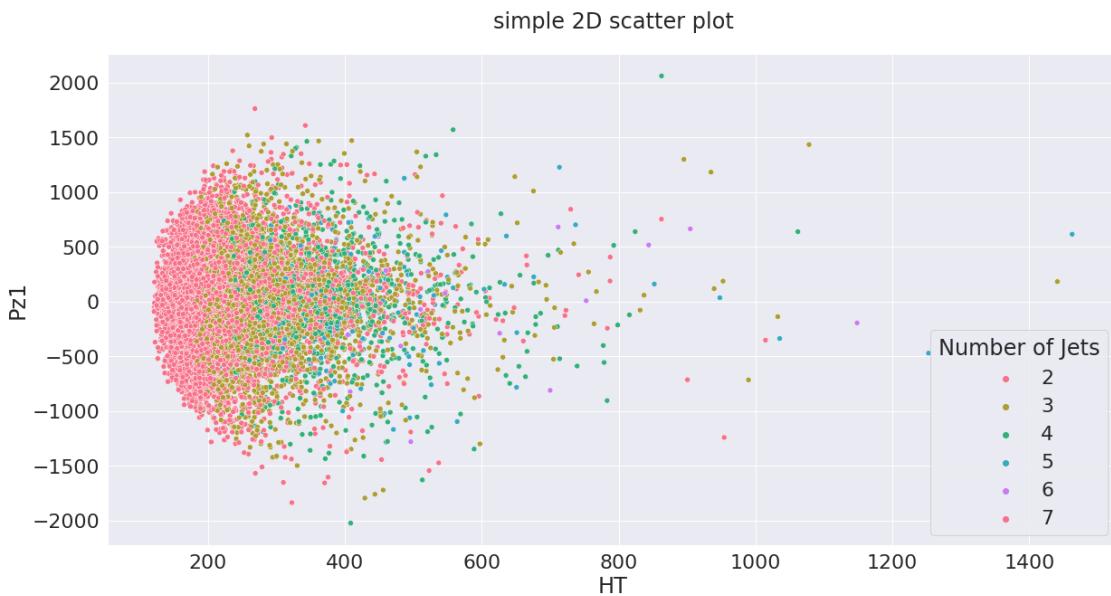
```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d367b990>
```



## 1.7 6. Pz1 vs HT

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='HT', y='Pz1', hue='Number of Jets', palette="husl")
```

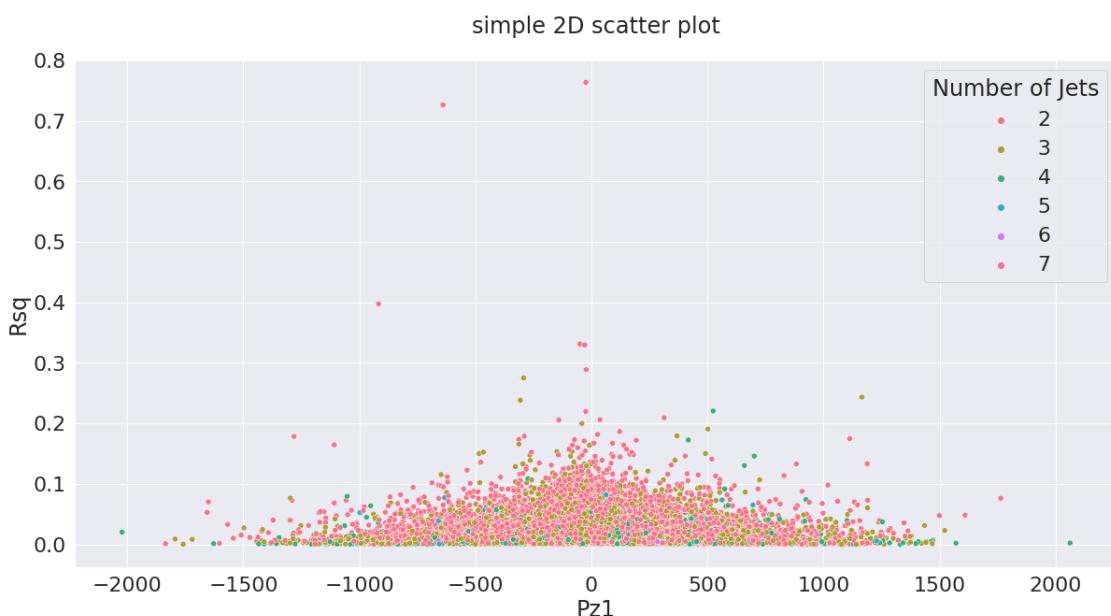
```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d30e9950>
```



## 1.8 7. Rsq vs Pz1

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='Pz1', y='Rsq', hue='Number of Jets', palette="husl")
```

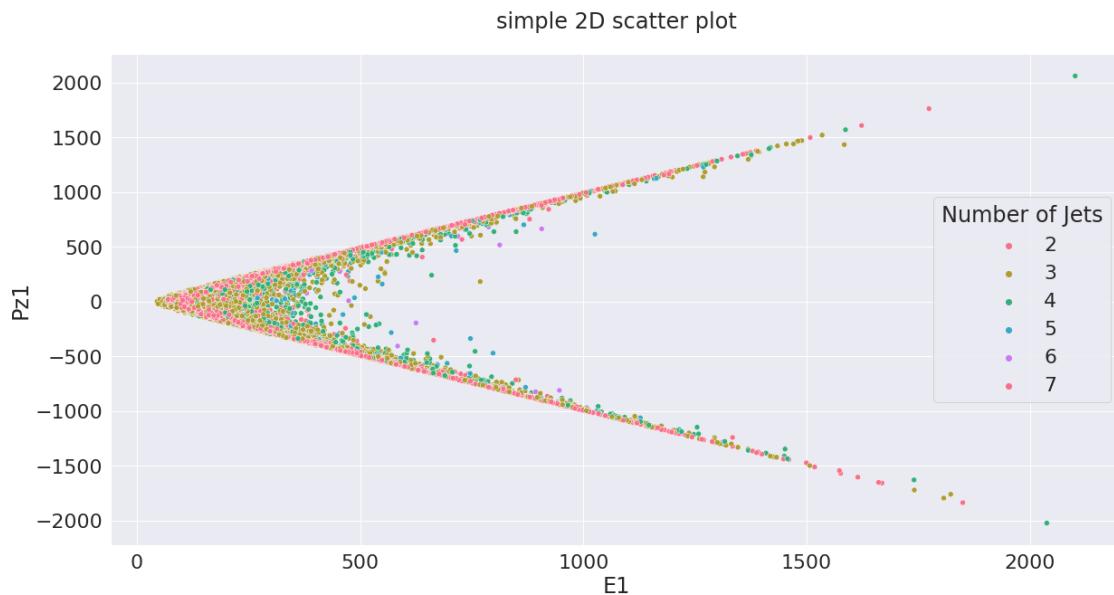
```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d365d110>
```



## 1.9 8. Pz1 vs E1

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='E1', y='Pz1', hue='Number of Jets', palette="husl")
```

```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d330ae90>
```

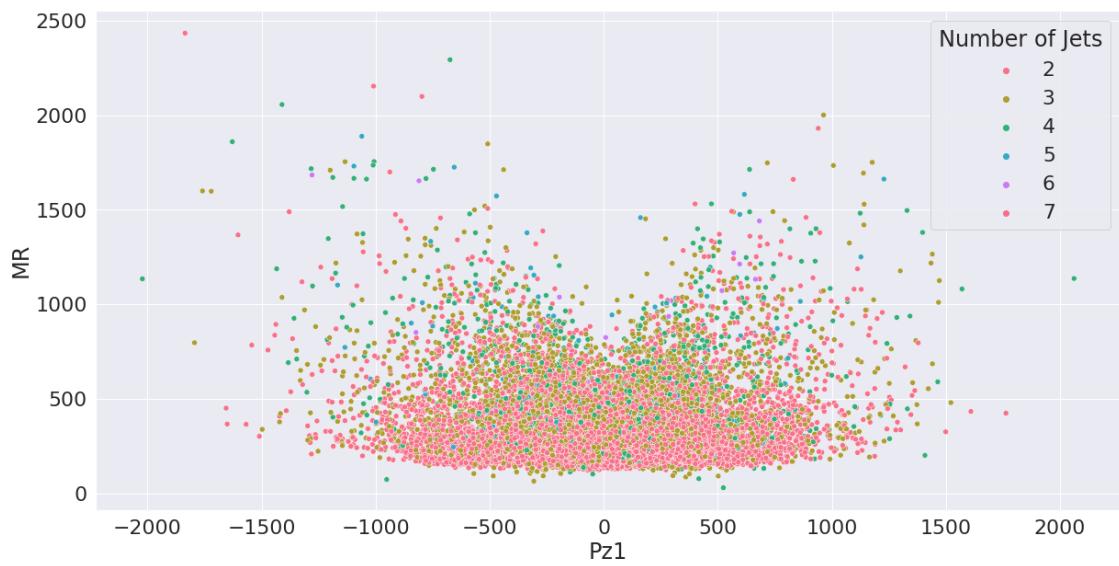


## 1.10 9. MR vs Pz1

```
[ ]: plt.figure(figsize=(20, 10))
sns.set(font_scale=2.0)
plt.title("simple 2D scatter plot", y=1.04)
sns.scatterplot(data=df1, x='Pz1', y='MR', hue='Number of Jets', palette="husl")
```

```
[ ]: <matplotlib.axes._subplots.AxesSubplot at 0x7fc5d2f298d0>
```

simple 2D scatter plot



# 3D scatter plots

July 3, 2022

## 0.1 1. E1 vs Px1 vs Py1

```
[ ]: # generate data
x = df['Px1']
y = df['Py1']
z = df['E1']

# axes instance
fig = plt.figure(figsize=(20,10))
ax = Axes3D(fig)
fig.add_axes(ax)

# get colormap from seaborn
cmap = ListedColormap(sns.color_palette("husl", 256).as_hex())

# plot
sc = ax.scatter(x, y, z, s=40, c=df['nJets'], marker='o', cmap=cmap, alpha=1)

plt.title("simple 3D scatter plot", y=1.04)

ax.set_xlabel('Px1')
ax.set_xlabel('Px1', labelpad=30)

ax.set_ylabel('Py1')
ax.set_ylabel('Py1', labelpad=30)

ax.set_zlabel('E1')
ax.set_zlabel('E1', labelpad=30)

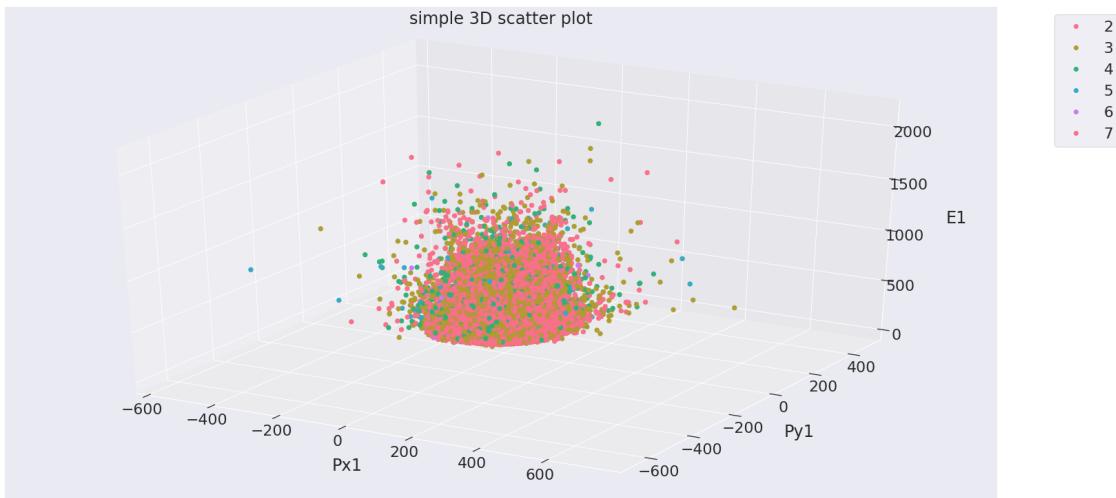
# legend
plt.legend(*sc.legend_elements(), bbox_to_anchor=(1.05, 1), loc=2)

# save
plt.savefig("scatter_hue", bbox_inches='tight')
```

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:9:  
MatplotlibDeprecationWarning: Adding an axes using the same arguments as a

previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

```
if __name__ == '__main__':
```



## 0.2 2. MR vs Px1 vs Py1

```
[]: # generate data
x = df['Px1']
y = df['Py1']
z = df['MR']

# axes instance
fig = plt.figure(figsize=(20,10))
ax = Axes3D(fig)
fig.add_axes(ax)

# get colormap from seaborn
cmap = ListedColormap(sns.color_palette("husl", 256).as_hex())

# plot
sc = ax.scatter(x, y, z, s=40, c=df['nJets'], marker='o', cmap=cmap, alpha=1)

plt.title("simple 3D scatter plot", y=1.04)

ax.set_xlabel('Px1')
ax.set_xlabel('Px1', labelpad=30)

ax.set_ylabel('Py1')
```

```

ax.set_ylabel('Py1', labelpad=30)

ax.set_zlabel('MR')
ax.set_zlabel('MR', labelpad=30)

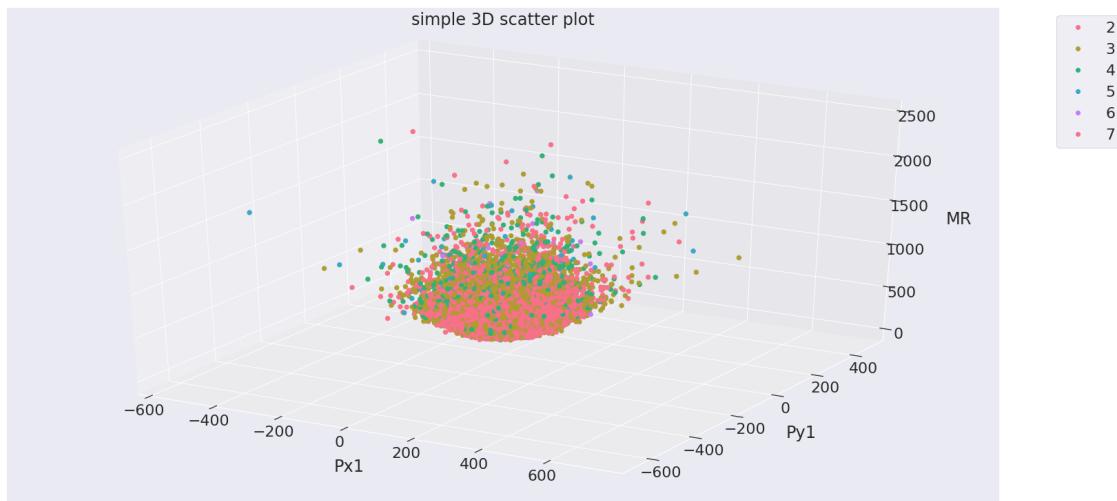
# legend
plt.legend(*sc.legend_elements(), bbox_to_anchor=(1.05, 1), loc=2)

# save
plt.savefig("scatter_hue", bbox_inches='tight')

```

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:9:  
MatplotlibDeprecationWarning: Adding an axes using the same arguments as a  
previous axes currently reuses the earlier instance. In a future version, a new  
instance will always be created and returned. Meanwhile, this warning can be  
suppressed, and the future behavior ensured, by passing a unique label to each  
axes instance.

```
if __name__ == '__main__':
```



### 0.3 3. Px1 vs Py1 vs Pz1

```
[ ]: # generate data
x = df['Px1']
y = df['Py1']
z = df['Pz1']

# axes instance
fig = plt.figure(figsize=(20,10))
ax = Axes3D(fig)
```

```

fig.add_axes(ax)

# get colormap from seaborn
cmap = ListedColormap(sns.color_palette("husl", 256).as_hex())

# plot
sc = ax.scatter(x, y, z, s=40, c=df['nJets'], marker='o', cmap=cmap, alpha=1)

plt.title("simple 3D scatter plot", y=1.04)

ax.set_xlabel('Px1')
ax.set_xlabel('Px1', labelpad=30)

ax.set_ylabel('Py1')
ax.set_ylabel('Py1', labelpad=30)

ax.set_zlabel('Pz1')
ax.set_zlabel('Pz1', labelpad=30)

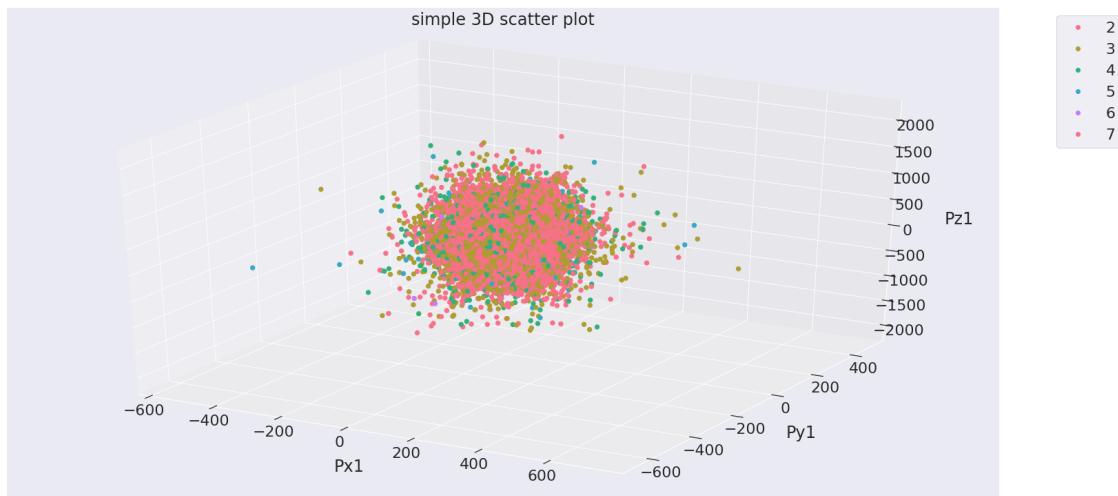
# legend
plt.legend(*sc.legend_elements(), bbox_to_anchor=(1.05, 1), loc=2)

# save
plt.savefig("scatter_hue", bbox_inches='tight')

```

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:9:  
MatplotlibDeprecationWarning: Adding an axes using the same arguments as a  
previous axes currently reuses the earlier instance. In a future version, a new  
instance will always be created and returned. Meanwhile, this warning can be  
suppressed, and the future behavior ensured, by passing a unique label to each  
axes instance.

```
if __name__ == '__main__':
```



# TensorFlow

July 3, 2022

## 1 The next step is to create a model to predict the number of Jets using TensorFlow.

### 1.1 I first split the DataFrame into X (data) and Y (labels), where:

```
[ ]: df.nJets = df.nJets.map({2: 0, 3: 1, 4: 2, 5: 3, 6: 4, 7: 5})  
X = df.drop(['nJets'], axis=1)  
y = df['nJets']
```

### 1.2 Using a train-test split, I split X and Y into train and test data.

- Train Dataset: Used to fit model.
- Test Dataset: Used to evaluate the fit model.

```
[ ]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.20,  
→random_state=42)
```

### 1.3 TensorFlow

The first thing I do is train a simple Neural Network using TensorFlow, and then plot accuracy and loss graphs on the training and validation datasets to find a balance between the model that is underfitting and one that is overfitting, resulting in a model with a good fit. I first need to convert the train and test data into a TensorFlow tensor.

#### 1.3.1 To convert DataFrame to a tensor, I use `tf.convert_to_tensor`

```
[ ]: tf.convert_to_tensor(X_train)  
[ ]: <tf.Tensor: shape=(17380, 16), dtype=float64, numpy=  
array([[1.49181000e+05, 1.78900000e+03, 1.69174702e+09, ...,  
       2.03114000e+02, 3.19493000e+01, 0.00000000e+00],  
      [1.49181000e+05, 1.78900000e+03, 1.69145596e+09, ...,  
       2.63641000e+02, 2.26033000e+01, 0.00000000e+00],  
      [1.49181000e+05, 9.98000000e+02, 9.83597837e+08, ...,  
       2.45781000e+02, 7.92845000e+00, 0.00000000e+00],  
      ...,  
      [1.47926000e+05, 4.62000000e+02, 4.98088038e+08, ...],
```

```
1.92466000e+02, 6.30772000e+00, 0.00000000e+00],  
[1.48029000e+05, 3.89000000e+02, 3.03389516e+08, ...,  
2.12675000e+02, 2.12651000e+00, 0.00000000e+00],  
[1.49181000e+05, 9.99000000e+02, 9.84587251e+08, ...,  
3.00290000e+02, 2.97415000e+01, 0.00000000e+00]])>
```

```
[ ]: tf.convert_to_tensor(X_test)
```

```
[ ]: <tf.Tensor: shape=(4346, 16), dtype=float64, numpy=  
array([[1.49181000e+05, 9.97000000e+02, 9.81749868e+08, ...,  
2.90486000e+02, 1.44300000e+01, 1.00000000e+00],  
[1.47926000e+05, 4.62000000e+02, 4.98113369e+08, ...,  
4.01390000e+02, 2.13951000e+01, 0.00000000e+00],  
[1.49181000e+05, 9.98000000e+02, 9.83048402e+08, ...,  
7.05866000e+02, 3.01095000e+01, 0.00000000e+00],  
...,  
[1.49181000e+05, 9.86000000e+02, 9.71262564e+08, ...,  
1.81506000e+02, 1.81312000e+01, 0.00000000e+00],  
[1.49181000e+05, 9.86000000e+02, 9.71122660e+08, ...,  
1.75923000e+02, 2.72315000e+01, 0.00000000e+00],  

```

### 1.3.2 Normalize X\_train, X\_test

```
[ ]: X_train_scaled = tf.keras.layers.Normalization(axis=-1)  
X_train_scaled.adapt(X_train)
```

```
[ ]: X_test_scaled = tf.keras.layers.Normalization(axis=-1)  
X_test_scaled.adapt(X_test)
```

### 1.3.3 Building a simple neural network model

The compile function takes three arguments: optimizer, loss, and metrics.

- **Optimizer:** These are certain algorithms that are used to change the attributes of the neural network to decrease the loss rate.
- **Loss:** This is used to compute the quantity that a model should seek to minimize during training.
- **Metrics:** This is used to judge the performance of the model.

## 1.4 Model 1: There are two hidden layers, each with 16 neurons and an activation function of sigmoid, epochs = 4000, and batch\_size = 400

```
[ ]: def get_basic_model():  
    model = tf.keras.Sequential([  
        X_train_scaled,
```

```

        tf.keras.layers.Dense(16, activation='sigmoid'),
        tf.keras.layers.Dense(16, activation='sigmoid'),
        tf.keras.layers.Dense(6, activation=tf.nn.softmax)
    ])

model.compile(optimizer='adam',
              loss='sparse_categorical_crossentropy',
              metrics=['accuracy'])

return model
model = get_basic_model()
history = model.fit(X_train, y_train, epochs=4000, validation_data=(X_test, y_test), batch_size=400)

```

#### 1.4.1 Evaluate the model

I create plots from the collected history data.

- A plot of accuracy on the training and validation datasets over training epochs.
- A plot of loss on the training and validation datasets over training epochs.

```

[ ]: font = {'family' : 'normal',
            'weight' : 'bold',
            'size'   : 18}

plt.rc('font', **font)

plt.figure(figsize=(15,15))

ax1 = plt.subplot(121)
ax2 = plt.subplot(122)

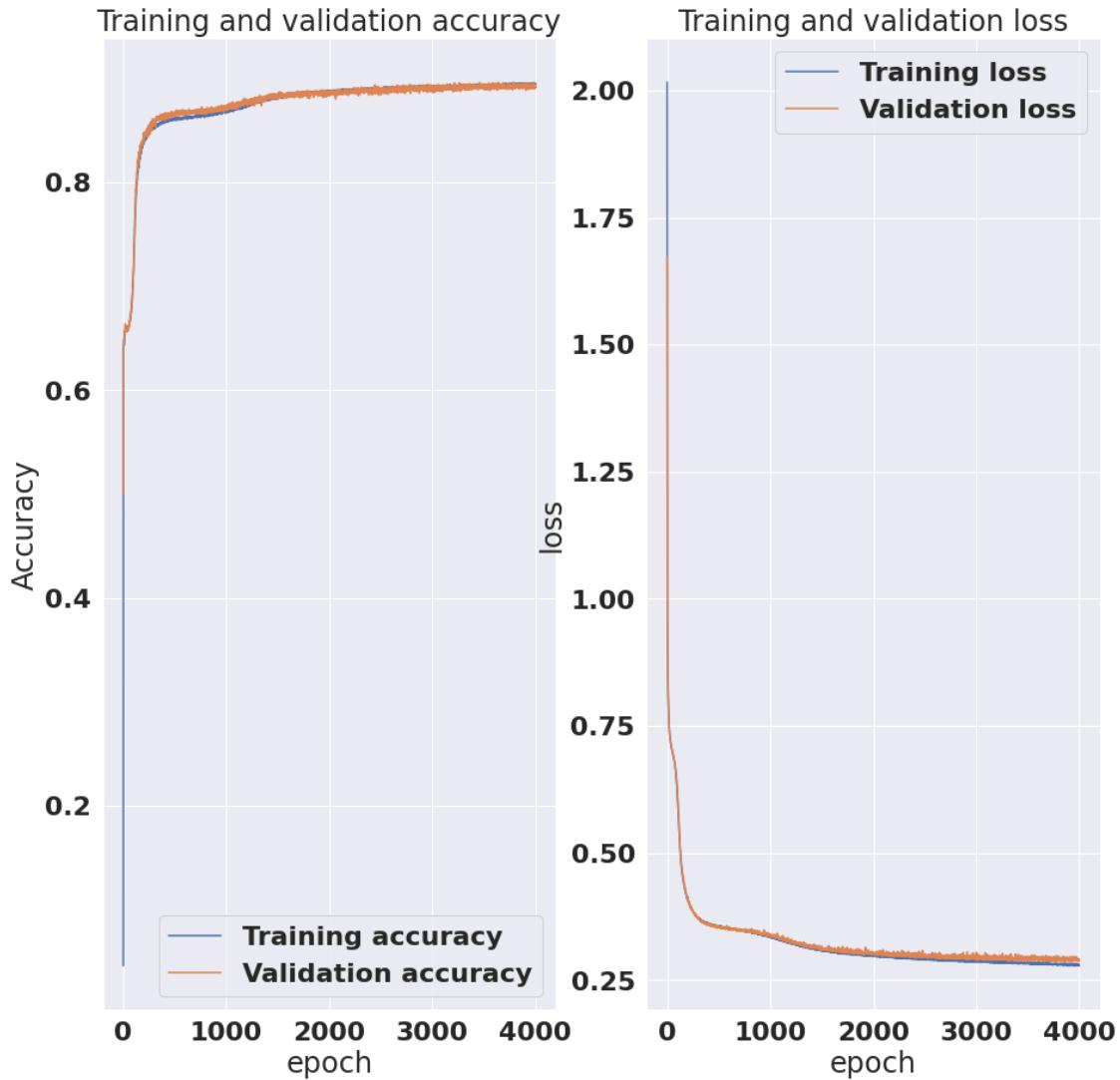
ax1.plot(history.history['accuracy'], label='Training accuracy')
ax1.plot(history.history['val_accuracy'], label = 'Validation accuracy')
ax1.set_title("Training and validation accuracy")
ax1.set(xlabel='epoch', ylabel='Accuracy')
ax1.legend(loc='lower right')

ax2.plot(history.history['loss'], label='Training loss')
ax2.plot(history.history['val_loss'], label='Validation loss')
ax2.set_title("Training and validation loss")
ax2.set(xlabel='epoch', ylabel='loss')
ax2.legend(loc='upper right')
#To check the network accuracy on test data
test_loss, test_acc = model.evaluate(X_test, y_test, verbose=2)

```

136/136 - 0s - loss: 0.2878 - accuracy: 0.8923 - 176ms/epoch - 1ms/step

```
findfont: Font family ['normal'] not found. Falling back to DejaVu Sans.  
findfont: Font family ['normal'] not found. Falling back to DejaVu Sans.
```



According to the plot of loss, validation loss is decreasing before the 2000th epoch, so the model is underfitting. However, after the 2000th epoch, Validation loss converges to 0.28, indicating that the model is balanced. After the 2000th epoch, when the model is either perfectly fitted or in a local minimum, the neural network model achieved an accuracy of 89%. The goal of Deep Learning training is to find a balance between a model that is underfitting and one that is overfitting(converging), resulting in a model with a good fit. I found an optimum where the change in the slope of loss is around the 2000th epoch, as shown above. At that point, the training process can be stopped.

## 2 Model 2: There are two hidden layers, each with 16 neurons and an activation function of sigmoid, epochs = 7000, and batch\_size = 300

```
[ ]: def get_basic_model():
    model = tf.keras.Sequential([
        X_train_scaled,
        tf.keras.layers.Dense(16, activation='sigmoid'),
        tf.keras.layers.Dense(16, activation='sigmoid'),
        tf.keras.layers.Dense(6, activation=tf.nn.softmax)
    ])

    model.compile(optimizer='adam',
                  loss='sparse_categorical_crossentropy',
                  metrics=['accuracy'])
    return model
model = get_basic_model()
history = model.fit(X_train, y_train, epochs=7000, validation_data=(X_test, y_test), batch_size=300)

[ ]: font = {'family' : 'normal',
            'weight' : 'bold',
            'size'   : 18}

plt.rc('font', **font)

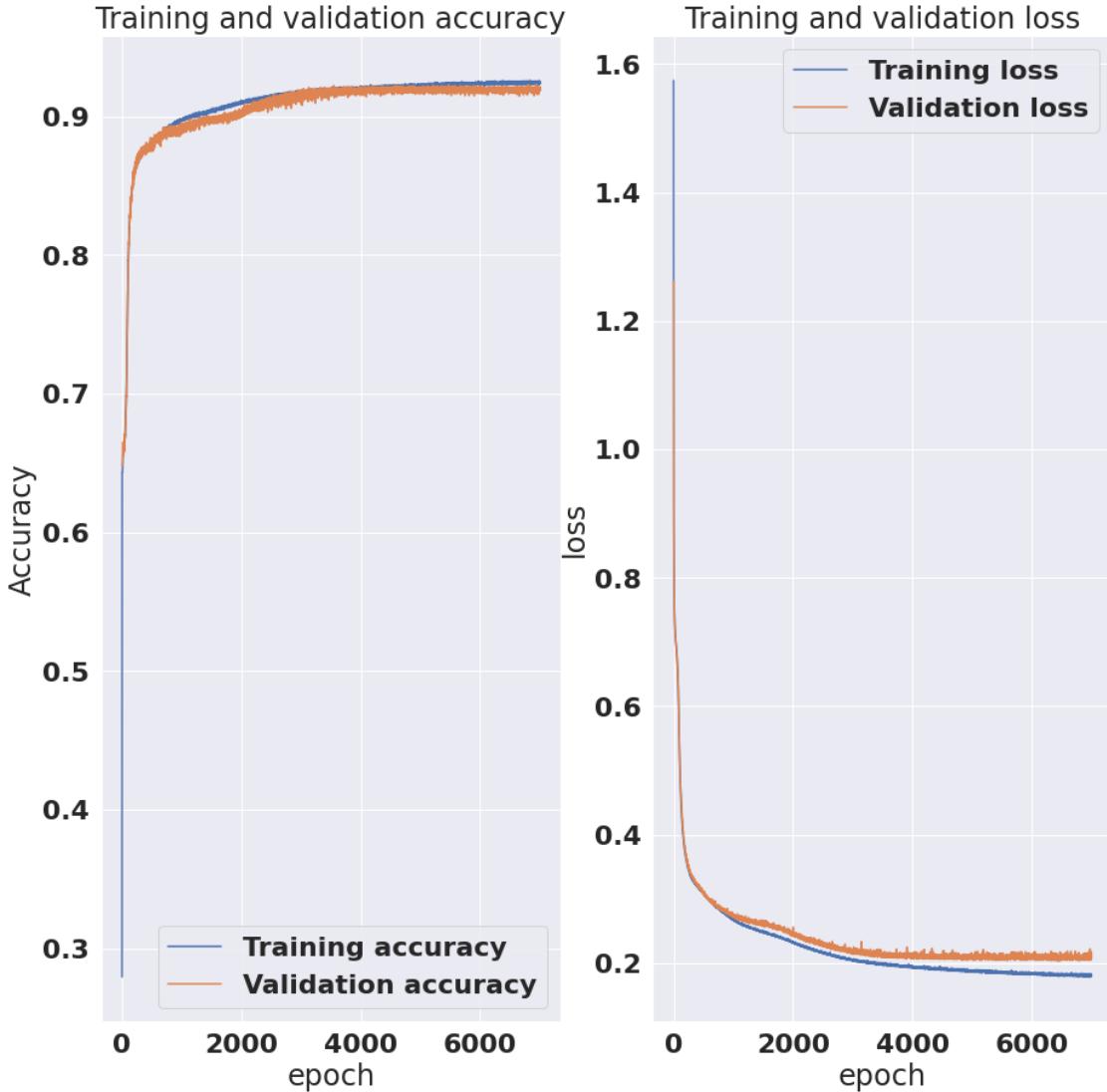
plt.figure(figsize=(15,15))

ax1 = plt.subplot(121)
ax2 = plt.subplot(122)

ax1.plot(history.history['accuracy'], label='Training accuracy')
ax1.plot(history.history['val_accuracy'], label = 'Validation accuracy')
ax1.set_title("Training and validation accuracy")
ax1.set_xlabel('epoch', ylabel='Accuracy')
ax1.legend(loc='lower right')

ax2.plot(history.history['loss'], label='Training loss')
ax2.plot(history.history['val_loss'], label='Validation loss')
ax2.set_title("Training and validation loss")
ax2.set_xlabel('epoch', ylabel='loss')
ax2.legend(loc='upper right')
#To check the network accuracy on test data
test_loss, test_acc = model.evaluate(X_test, y_test, verbose=2)
```

136/136 - 0s - loss: 0.2167 - accuracy: 0.9188 - 186ms/epoch - 1ms/step



According to the plot of loss, validation loss is decreasing before the 4000th epoch, so the model is underfitting. However, after the 4000th epoch, Validation loss converges to 0.2, indicating that the model is balanced. After the 4000th epoch, when the model is either perfectly fitted or in a local minimum, the neural network model achieved an accuracy of 92%. I found an optimum where the change in the slope of loss is around the 4000th epoch, as shown above. At that point, the training process can be stopped.

### 3 Final words

In terms of the number of hidden layers and neurons and their activation function, Model 1 and Model 2 are similar. However, by increasing the batch\_size and epochs, which give the model more time to train, the accuracy has increased by 3%. To achieve high accuracy, it is sometimes better to test different batch\_sizes for a model than to use complicated structures.