## Lab10

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#### Collab Link

Exercise 1: Decision Trees Construct a decision tree corresponding to each of the following Boolean functions. The examples  $x \ D$  have one attribute for each Boolean variable  $A, B, \ldots$  in the formula; the target concept c(x) is the truth value of the formula itself. Assume the set D contains examples with all possible combinations of attribute values.

Hint: It may be helpful to write out the set D, i.e., the truth table for the variables and formula, first.

- (a) A ňB
- (b) A (B C)
- (c) A XOR B
- (d) (A B) (C D)
- (e) (A B) (C XOR D)

```
[5]: from typing import List, Dict, Optional
   import pprint

[]: !!apt-get install texlive texlive-xetex texlive-latex-extra pandoc inkscape
   !pip install pypandoc
   !pip install graphviz
   !apt-get install graphviz
   !pip install gymagic
   %load_ext gymagic
```

This function generate\_tt will generate the truth table for the given variables, applying the given functions

```
[6]: def generate_tt(variables: List[str], func):
    sz = len(variables)
    table = []
    for i in range(0, 1 << (sz)):
        new_row = dict()
        for j in range(sz):
            val = False</pre>
```

```
if ((i & (1 << j)) != 0):
    val = True
    new_row[variables[j]] = val
    table.append((new_row, func(new_row)))

return table</pre>
```

These three functions are helpers to make nodes while generating a decision tree. A Node can be simply thought of as a dictionary with 'name', 'yes' branch and 'no' branch and also 'is\_leaf' to indicate if its a leaf or not. The other attributes in make\_node function is for reduction in the 2nd pass of the tree.

```
[7]: def make_node(name):
    return {'name': name, 'yes': None, 'no': None, 'yes_vals': [], 'no_vals':
    →[], 'is_leaf': False}

def make_leaf(name):
    return {'name': name, 'is_leaf': True}

def make_node_2nd_pass(name):
    return {'name': name, 'yes': None, 'no': None, 'is_leaf': False}
```

This will be generating a brute force decision tree for us, using all the possible variable.

```
[8]: def generate_decision_tree(variables: List[str], accumulated_values: Dict[str,usbool], func):
    if len(variables) == 0:
        ans = func(accumulated_values)
        return (make_leaf(str(ans)), [ans])
    else:
        nd = make_node(variables[0])
        accumulated_values[variables[0]] = True
        nd['yes'], nd['yes_vals'] = generate_decision_tree(
            variables[1:], accumulated_values, func)
        accumulated_values[variables[0]] = False
        nd['no'], nd['no_vals'] = generate_decision_tree(
            variables[1:], accumulated_values, func)
        accumulated_values.pop(variables[0])
        return (nd, nd['yes_vals'] + nd['no_vals'])
```

This is the reduction function. This will take in the decision tree, and try to reduce it as much as possible, removing the need for branches if possible. For example, in a decision tree of (A and B) ,we dont need to use B in the 'no' branch of the A variable because if A is no(i.e False), the final result is anyways going to be False.

```
[9]: def second_pass_to_remove_redundancy(node: Dict) -> Dict:
    if node['is_leaf']:
        return node
```

```
else:
             mp = make_node_2nd_pass(node['name'])
             if node['yes_vals'] == node['no_vals']:
                 return second_pass_to_remove_redundancy(node['no'])
             if all(x == node['yes_vals'][0] for x in node['yes_vals']):
                 mp['yes'] = make_leaf(str(node['yes_vals'][0]))
             else:
                 mp['yes'] = second pass to remove redundancy(node['yes'])
             if all(x == node['no_vals'][0] for x in node['no_vals']):
                 mp['no'] = make leaf(str(node['no vals'][0]))
                 mp['no'] = second_pass_to_remove_redundancy(node['no'])
             return mp
[16]: %load_ext gvmagic
     import graphviz
     def make_dot_graph(g,root,id = 0):
         g.node(str(id))
         if root['is leaf']:
             return
         else:
             g.node(str(2*id + 1),label=root['yes']['name'])
             g.node(str(2*id + 2),label=root['no']['name'])
             g.edge(str(id),str(2*id + 1), label='yes')
             g.edge(str(id),str(2*id + 2),label='no')
             make_dot_graph(g,root['yes'],2*id + 1)
             make_dot_graph(g,root['no'], 2*id + 2)
```

The gvmagic extension is already loaded. To reload it, use: %reload\_ext gvmagic

This will print the tree.

This function will show the truth table for the given expression and then goes onto print the decision tree after making it.

```
[23]: def show_decision_tree_and_truth_table(expr, variables, func):
         global graph
         print("="*80)
         print(expr)
         print("\nTRUTH TABLE FOR THE GIVEN EXPRESSION : {}".format(expr))
         print(' '.join(map(lambda x: "{:<10}".format(x), variables + ["Result"])))</pre>
         for x in generate_tt(variables, func):
             print(' '.join(map(lambda y: "{:<10}".format(</pre>
                 str(y), list(x[0].values()) + [x[1]])))
         x = generate_decision_tree(variables, dict(), func)
         x = second_pass_to_remove_redundancy(x[0])
         print tree(x)
         print("="*80)
         g = graphviz.Digraph(strict=True)
         make_dot_graph(g,x)
         graph = g.source
         %dotstr graph
         print()
```

All the inputs given for the question

#### 1.1 A and (not B)

```
[25]: show_decision_tree_and_truth_table(*(inputs[0]))
    A and (not B)
    TRUTH TABLE FOR THE GIVEN EXPRESSION : A and (not B)
               В
                           Result
    False
                False
                           False
    True
               False
                           True
    False
                True
                           False
    True
                True
                           False
     A yes
```

B yes

Leaf: False

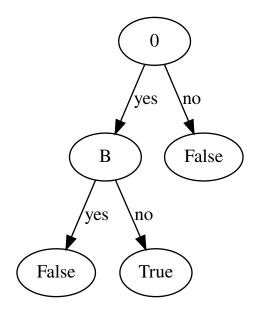
B no

Leaf: True

A no

Leaf: False

-----



## 1.2 A or (B and C)

[26]: show\_decision\_tree\_and\_truth\_table(\*(inputs[1]))

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A or (B and C)

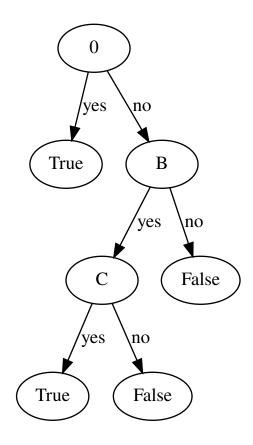
TRUTH TABLE FOR THE GIVEN EXPRESSION : A or (B and C)

Result False False False False True False False True False True False False True True False True False False True False True False True True False True True True True True True True

```
A yes
Leaf: True

A no
B yes
C yes
Leaf: True
C no
Leaf: False
B no
Leaf: False
```

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### 1.3 A xor B

[27]: show\_decision\_tree\_and\_truth\_table(\*(inputs[2]))

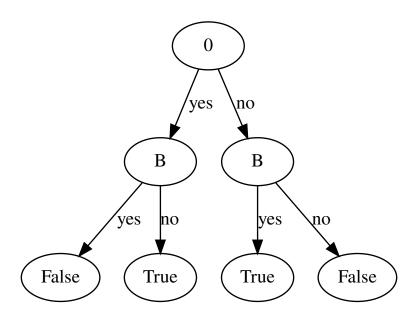
\_\_\_\_\_\_

A xor B

```
TRUTH TABLE FOR THE GIVEN EXPRESSION : A xor B
Α
                      Result
False
           False
                      False
True
           False
                      True
False
           True
                      True
True
           True
                      False
A yes
     B yes
         Leaf: False
     B no
         Leaf: True
 A no
     B yes
         Leaf: True
     B no
```

Leaf: False

\_\_\_\_\_\_

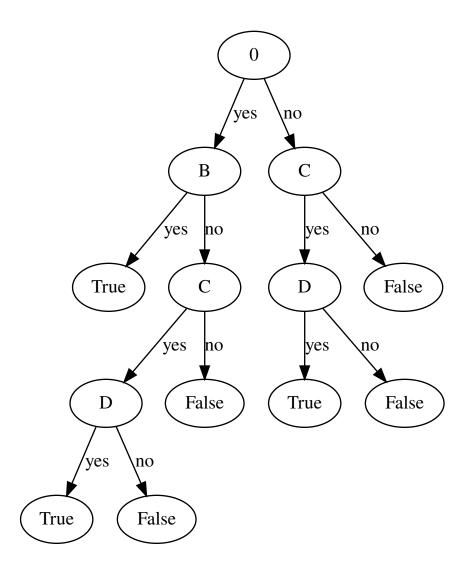


### 1.4 (A and B) or (C and D)

[28]: show\_decision\_tree\_and\_truth\_table(\*(inputs[3]))

(A and B) or (C and D)

```
TRUTH TABLE FOR THE GIVEN EXPRESSION: (A and B) or (C and D)
Α
                    C
                                         Result
False
          False
                    False
                              False
                                         False
True
          False
                    False
                              False
                                         False
False
          True
                    False
                              False
                                         False
True
          True
                    False
                              False
                                         True
False
          False
                    True
                              False
                                         False
          False
True
                    True
                              False
                                         False
False
          True
                    True
                              False
                                         False
True
          True
                    True
                              False
                                         True
False
          False
                    False
                              True
                                         False
True
          False
                    False
                              True
                                         False
          True
False
                    False
                              True
                                         False
True
          True
                    False
                              True
                                         True
False
          False
                    True
                              True
                                         True
          False
True
                    True
                              True
                                         True
False
          True
                    True
                              True
                                         True
True
          True
                    True
                              True
                                         True
A yes
    B yes
        Leaf: True
    B no
        C yes
            D yes
               Leaf: True
            D no
               Leaf: False
        C no
            Leaf: False
 A no
    C yes
        D yes
            Leaf: True
        D no
            Leaf: False
    C no
        Leaf: False
______
```



# 1.5 (A or B) and (C xor D)

[29]: show\_decision\_tree\_and\_truth\_table(\*(inputs[4]))

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( A or B ) and (C xor D)

TRUTH TABLE FOR THE GIVEN EXPRESSION : ( A or B ) and (C xor D)

A	В	C	D	Result
False	False	False	False	False
True	False	False	False	False
False	True	False	False	False
True	True	False	False	False

```
False
          False
                    True
                              False
                                        False
True
          False
                    True
                              False
                                        True
False
          True
                    True
                              False
                                        True
True
          True
                    True
                              False
                                        True
False
         False
                    False
                              True
                                        False
True
          False
                    False
                              True
                                        True
False
         True
                    False
                              True
                                        True
True
          True
                    False
                              True
                                        True
False
         False
                    True
                              True
                                        False
True
          False
                    True
                              True
                                        False
          True
False
                    True
                              True
                                        False
True
          True
                    True
                              True
                                        False
A yes
    C yes
        D yes
           Leaf: False
        D no
           Leaf: True
    C no
        D yes
           Leaf: True
        D no
           Leaf: False
 A no
    B yes
        C yes
           D yes
               Leaf: False
           D no
               Leaf: True
        C no
           D yes
               Leaf: True
           D no
               Leaf: False
    B no
        Leaf: False
______
```

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