Machine Learning November 17, 2021

## Lab

The following exercises must be submitted: 18.11.2021, 05:00PM

## Write a program in python for the scenario in the follwing scenarios

## Upload Link:

https://forms.office.com/Pages/ResponsePage.aspx? id=p1CEoozbM0yRKkQzEbIt26j5uR98u7pHk4YAJdVRMgxUM1JFWlhJR UFESlBOSzVSRVFLSkhQRUwxNy4u

For those questions where justification is asked, write in hand answers for that

## Exercise 1: Decision Trees

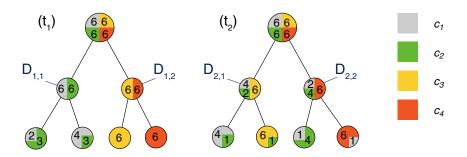
Construct a decision tree corresponding to each of the following Boolean functions. The examples  $\mathbf{x} \in D$  have one attribute for each Boolean variable  $A, B, \ldots$  in the formula; the target concept  $c(\mathbf{x})$  is the truth value of the formula itself. Assume the set D contains examples with all possible combinations of attribute values.

*Hint:* It may be helpful to write out the set D, i.e., the truth table for the variables and formula, first.

- (a)  $A \wedge \neg B$
- (b)  $A \vee (B \wedge C)$
- (c) A XOR B
- (d)  $(A \wedge B) \vee (C \wedge D)$
- (e)  $(A \lor B) \land (C XOR D)$

## Exercise 2: Impurity Functions

Let D be a set of examples over a feature space X and a set of classes  $C = \{c_1, c_2, c_3, c_4\}$ , with |D| = 24. Consider the following illustration of two possible decision trees,  $t_1$  and  $t_2$  – the colors represent the classes present in each document set associated with the nodes of the trees; the numbers denote how many examples of each class are present.



- (a) First, consider only the first split that each of the two trees makes: compute  $\Delta\iota(\{D_{1,1},D_{1,2}\})$  and  $\Delta\iota(\{D_{2,1},D_{2,2}\})$  with the misclassification rate  $\iota_{misclass}$  and the entropy criterion  $\iota_{entropy}$  as splitting criterion. Interpret the results: which of  $\{D_{1,1},D_{1,2}\}$  or  $\{D_{2,1},D_{2,2}\}$  is the better first split?
- (b) Which of  $t_1$ ,  $t_2$  is the better decision tree, and why?
- (c) Assuming the splits shown are the only possibilities, which of  $t_1$  or  $t_2$  would the ID3 algorithm construct, and why?