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Unit 1.3

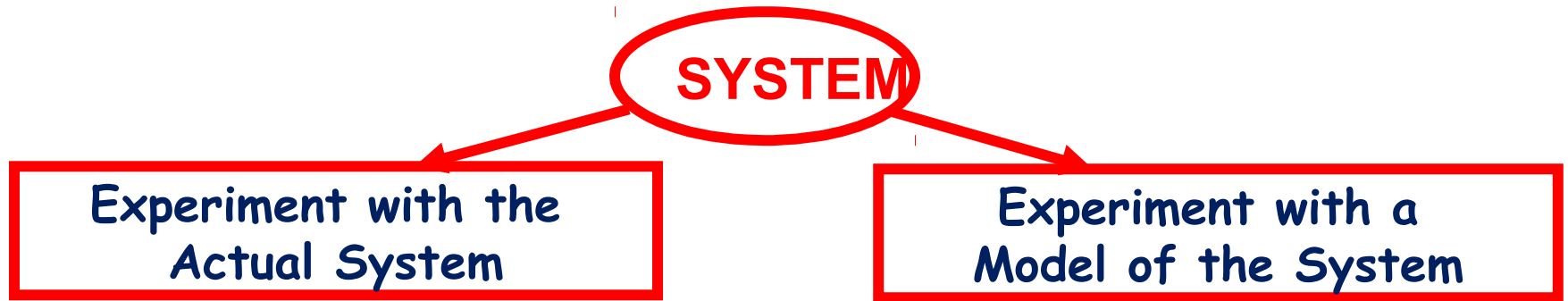
Classification or Types/Taxonomy of Models

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Unit I : Syllabus

- Introduction:
 - System
 - **Models**
 - Discrete event simulation and
 - Continuous simulation
- Discrete Event Simulation:
 - Time-Advance Mechanisms
 - Event Modeling of discrete dynamic systems
 - Single-Server Single-Queue Model
 - Event graphics
 - Monte Carlo Simulation

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Can be used as a Analysis Tool

Not appropriate for Design Tool

Costly

Disruptive

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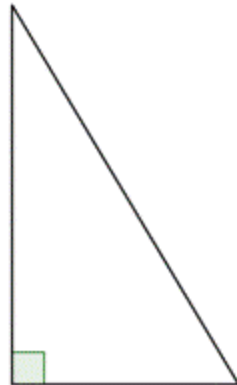
Models Taxonomy

Experiment with a model of the system



Make assumptions that take the form of mathematical or logical relationships

$$h^2 = p^2 + b^2$$



If P then Q

P

Therefore Q

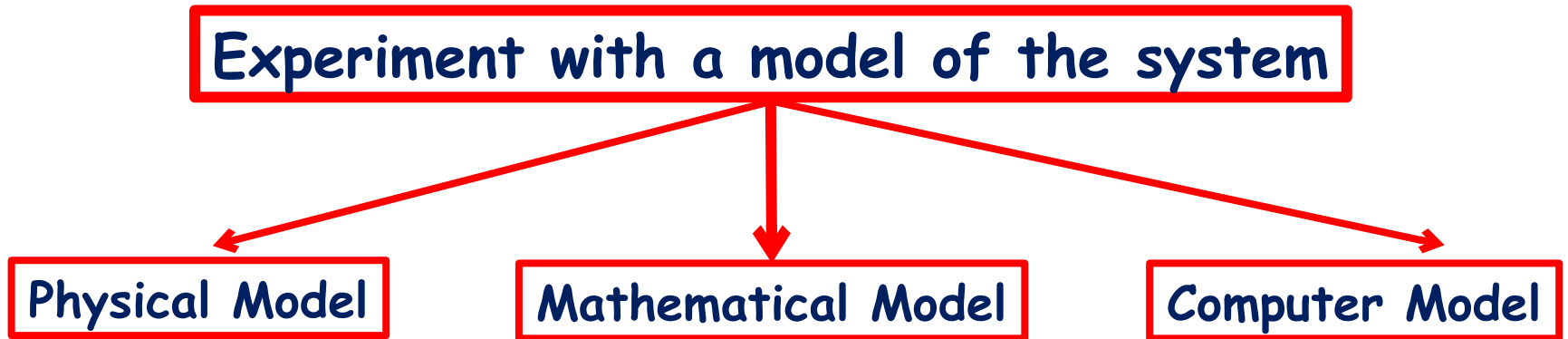
$P \rightarrow Q$

P

Q

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Models Taxonomy



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Physical Model

is a scaled down model of actual system,
which has all the properties of the system,

or

at least it is as close to
the actual system as possible.

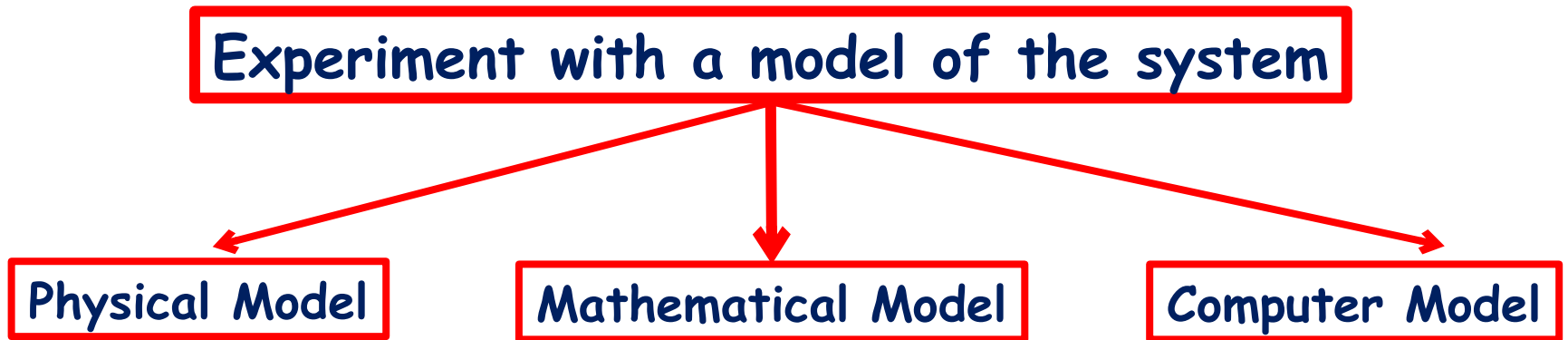
Example:

A model of a airplane,
a map,
a globe,
a model of car.



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Models Taxonomy



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Mathematical Model

Is one in which symbols

and

logic constitute the model. Therefore Q

If P then Q
P

Symbolism can be
a language

or

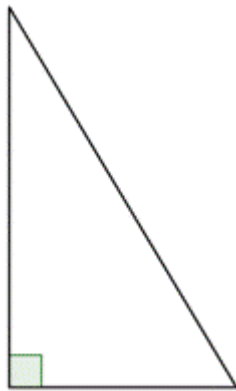
a mathematical notations.

$P \rightarrow Q$

P

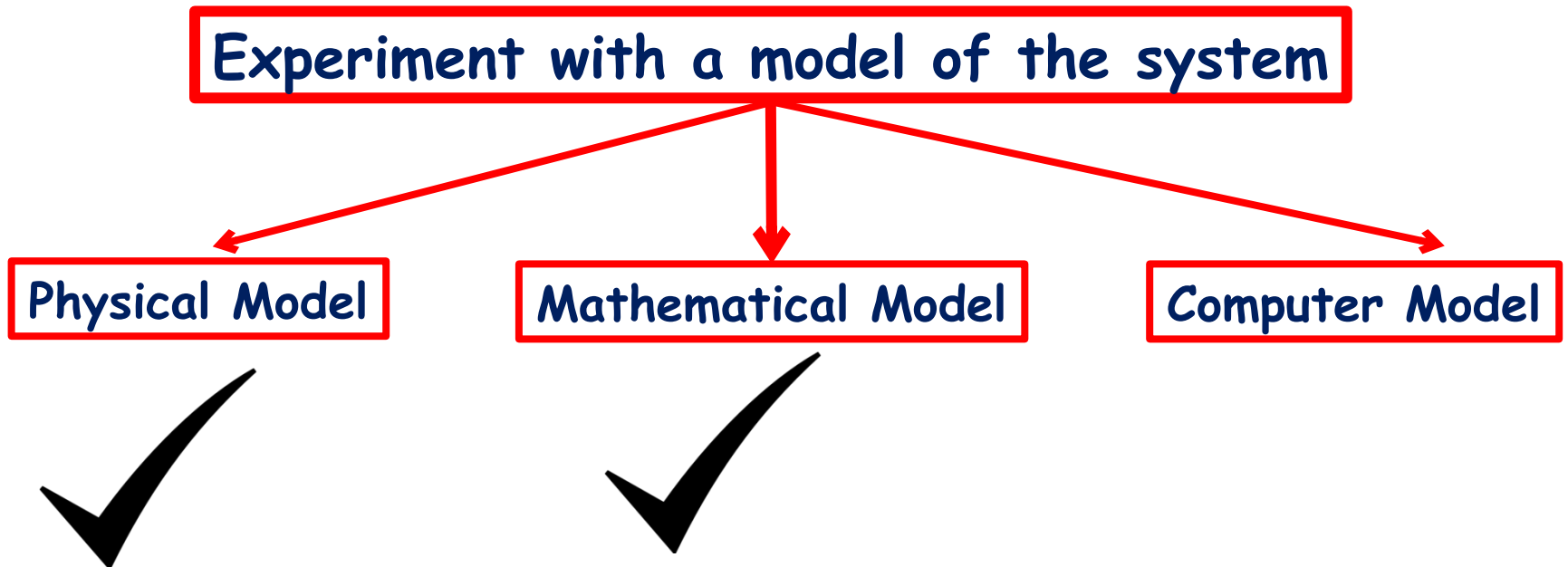
Q

$$h^2 = p^2 + b^2$$



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Models Taxonomy



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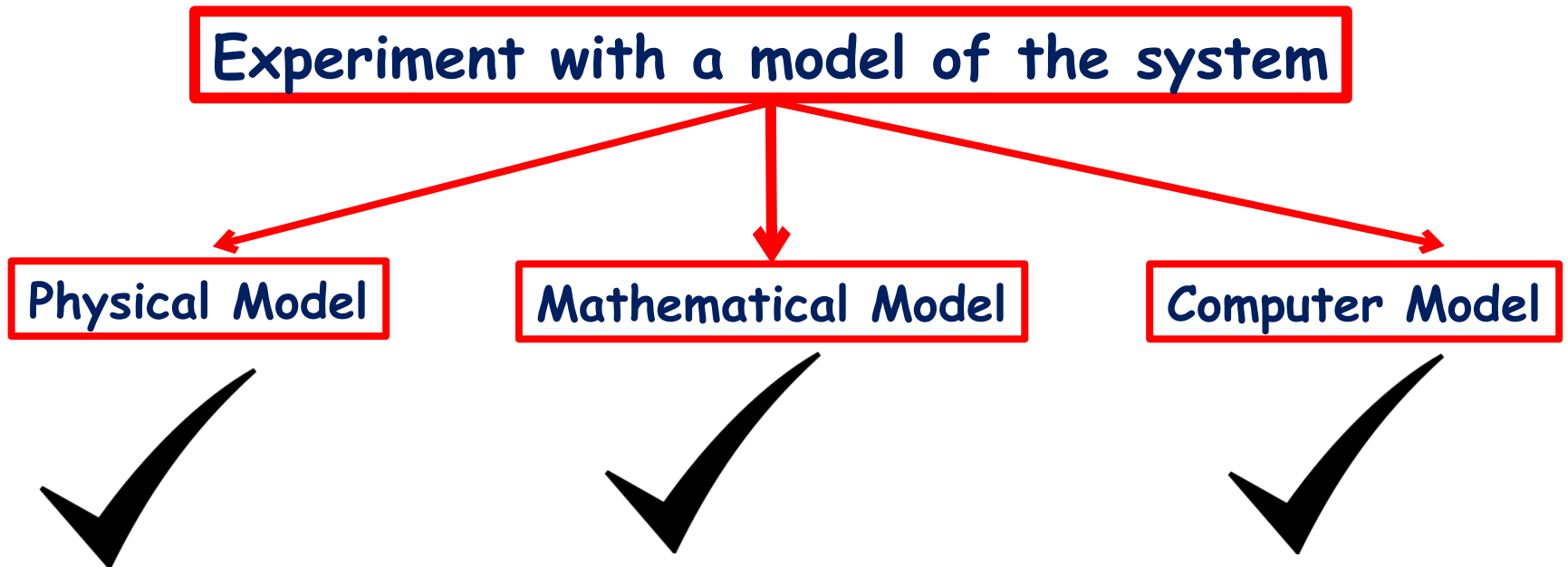
Computer Model

One can design a computer model,
with the help of graphics
as well as mathematics.

This is called Computer Models.

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Models Taxonomy



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Models Taxonomy

Experiment with a model of the system

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graph TD; A[Experiment with a model of the system] --> B[Physical Model]; A --> C[Mathematical Model]; A --> D[Computer Model]; B --> E[Static Model]; B --> F[Dynamic Model]; C --> G[Static Model]; C --> H[Dynamic Model]; D --> I[Static Model]; D --> J[Dynamic Model];
```

Physical Model

Mathematical Model

Computer Model

Static
Model

Dynamic
Model

Static
Model

Dynamic
Model

Static
Model

Dynamic
Model

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Static Vs. Dynamic Models

Static Models

State variables do not change with time.

Dynamic Models

State variables change over time

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Static Vs. Dynamic Models

Static Models

Represents the system at a particular point in time

Time plays no role

Example: **Monté Carlo Method**

Dynamic Models

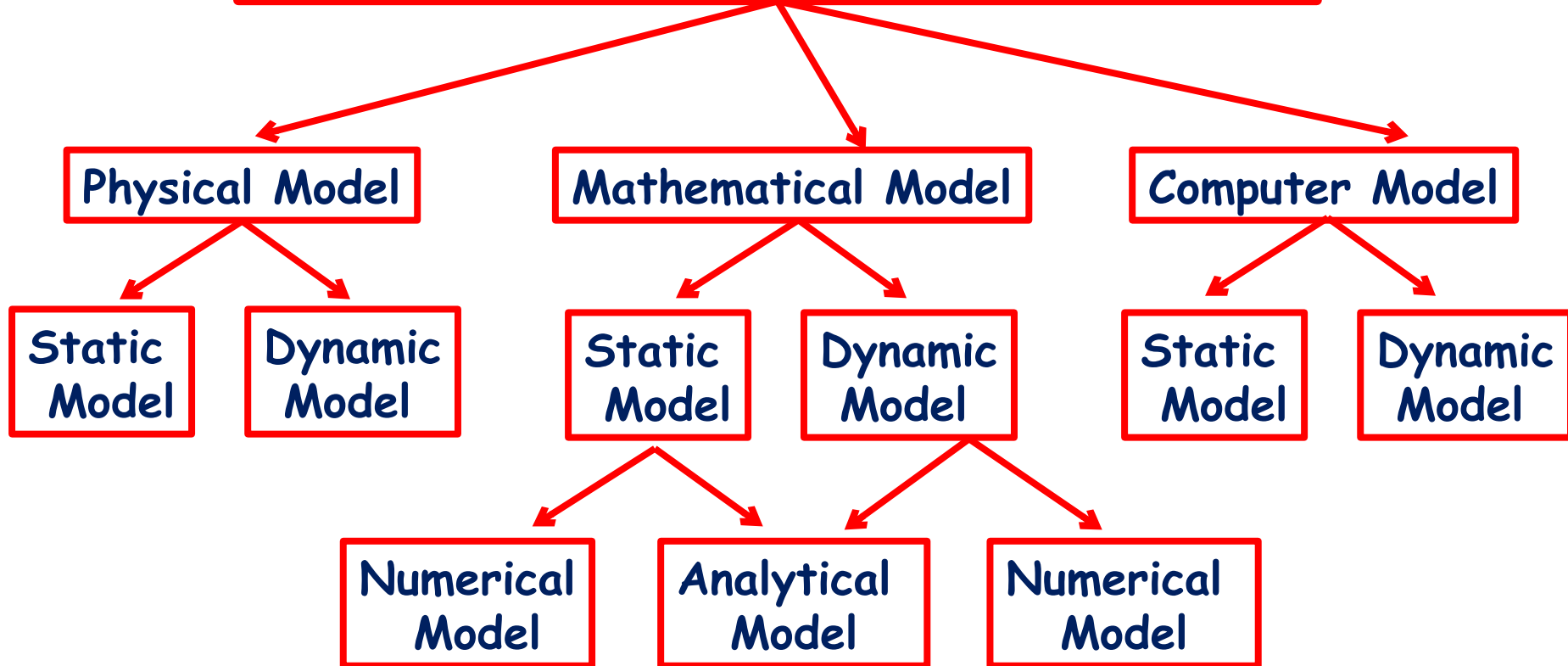
Represents a system as it evolves over time

Time plays role

Example : **Cars arriving to a parking**

Models Taxonomy

Experiment with a model of the system



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Analytical Models

Solves problems by applying
deductive mathematical theory.

If P then Q

P

Therefore Q

$P \rightarrow Q$

P

Q

If B. K. Sharma is a Teacher, then B. K. Sharma is poor.

B K. Sharma is a Teacher.

Therefore, B. K. Sharma is poor.

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Numerical Models

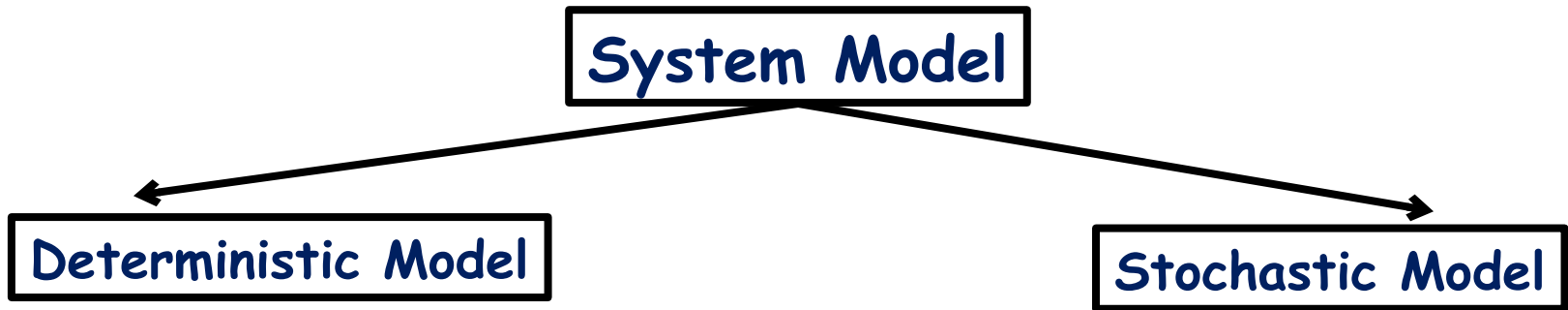
Solves problems by applying
applying computational procedures.

Finding the roots of a non-linear algebraic equations

$$ax^2 + bx + c = 0$$

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Models Taxonomy



Is everything for sure or is there uncertainty?

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Deterministic Models

The behavior is entire
predictable.

The system is perfectly understood,

then

it is possible to predict precisely what will
happen.

Stochastic model

The behavior cannot be entirely predicted.

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Deterministic Vs. Stochastic Models

Deterministic Models

No probabilistic component in the system.

Example: Worst-Case Analysis of the system

Stochastic Models

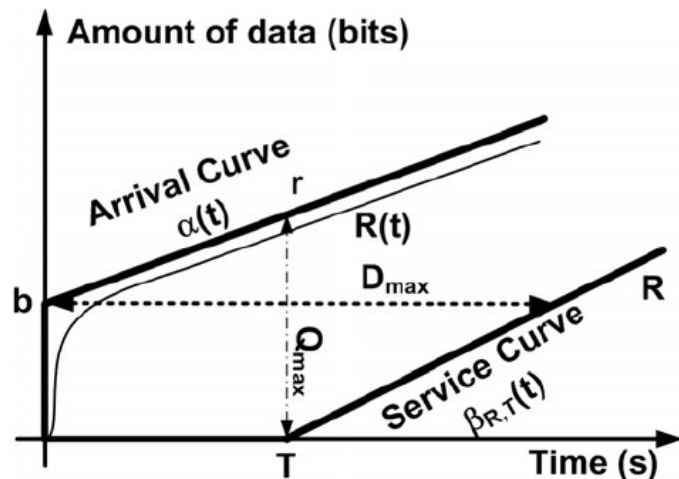
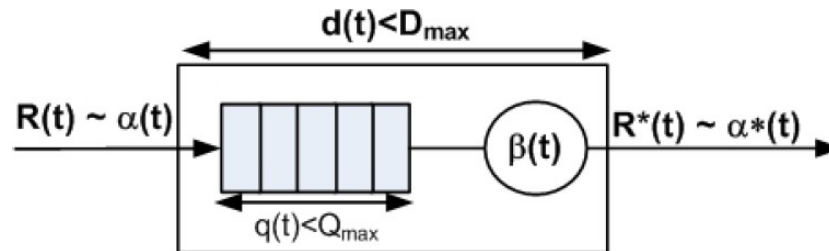
Some components of the system has a probabilistic behavior (Random variable, event probability)

Example: Queuing systems

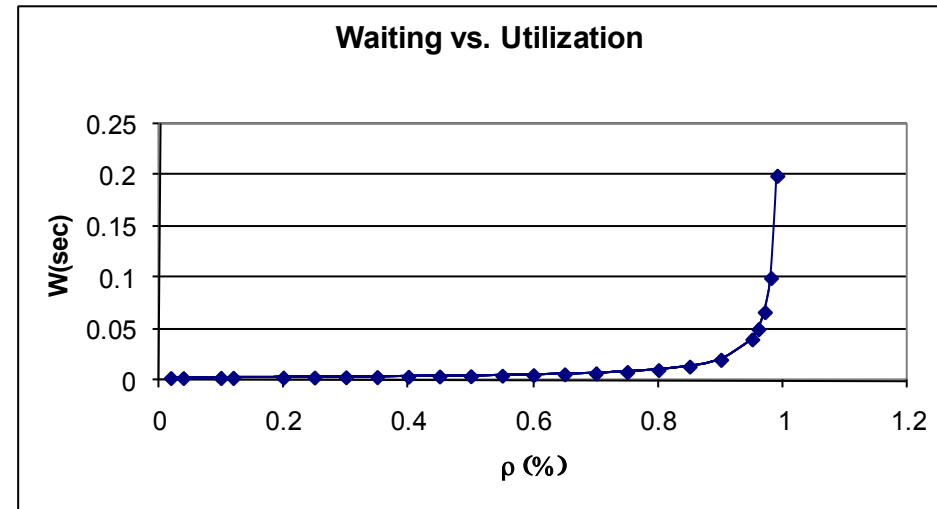
Example: Deterministic Vs. Stochastic Models

Is everything for sure or is there uncertainty?

Queueing System



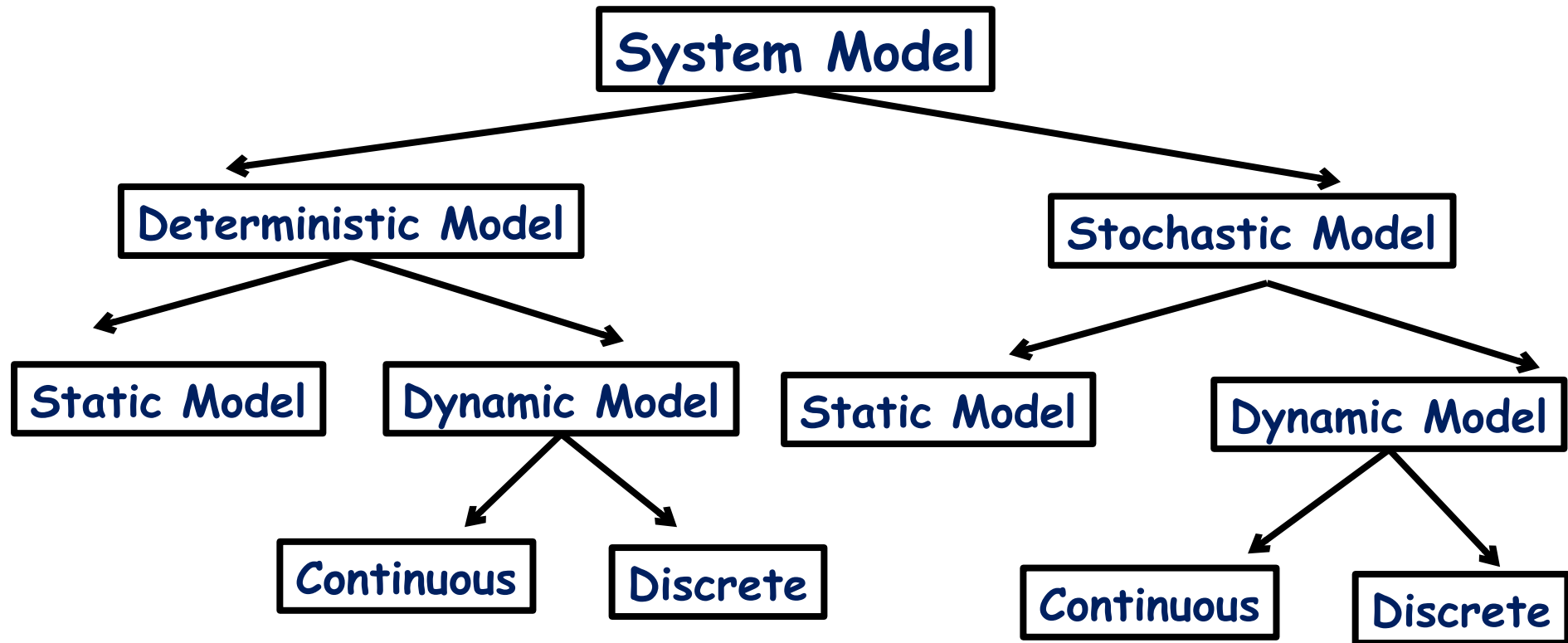
Deterministic Performance
Using Network Calculus



Stochastic Performance
Using Queueing Theory

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Models Taxonomy



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Discrete Vs. Continuous Models

Discrete Models

The state of the system changes only at discrete points in time.

The state variables change only at a countable number of time / discrete of points in time.

These points in time are the ones at which the event occurs/change in state occurs.

Firing of a gun on an enemy target.

Continuous Models

The state of the system changes continuously

The state variables change in a continuous way, and not abruptly from one state to another (infinite number of states).

Fluid flow in a pipe

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Discrete Vs. Continuous Models

Discrete Models

Model of Bank:

Number of customers waiting in line being served.

Queuing, Inventory, Machine Shop Models

Continuous Models

The head of water behind a dam

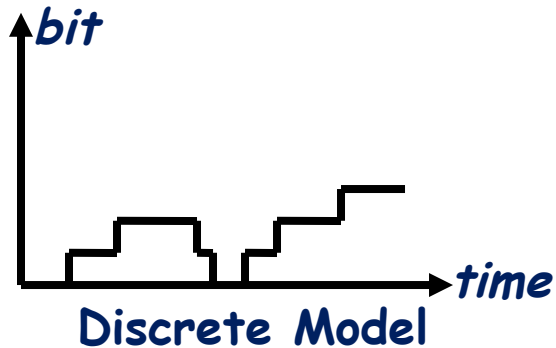
Chemical Process

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Discrete Vs. Continuous Models

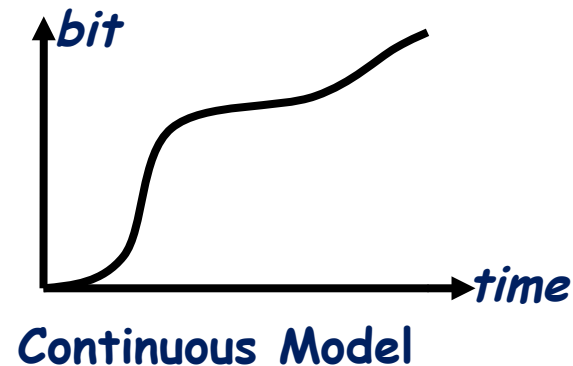
Discrete Models

of cars in a parking lot



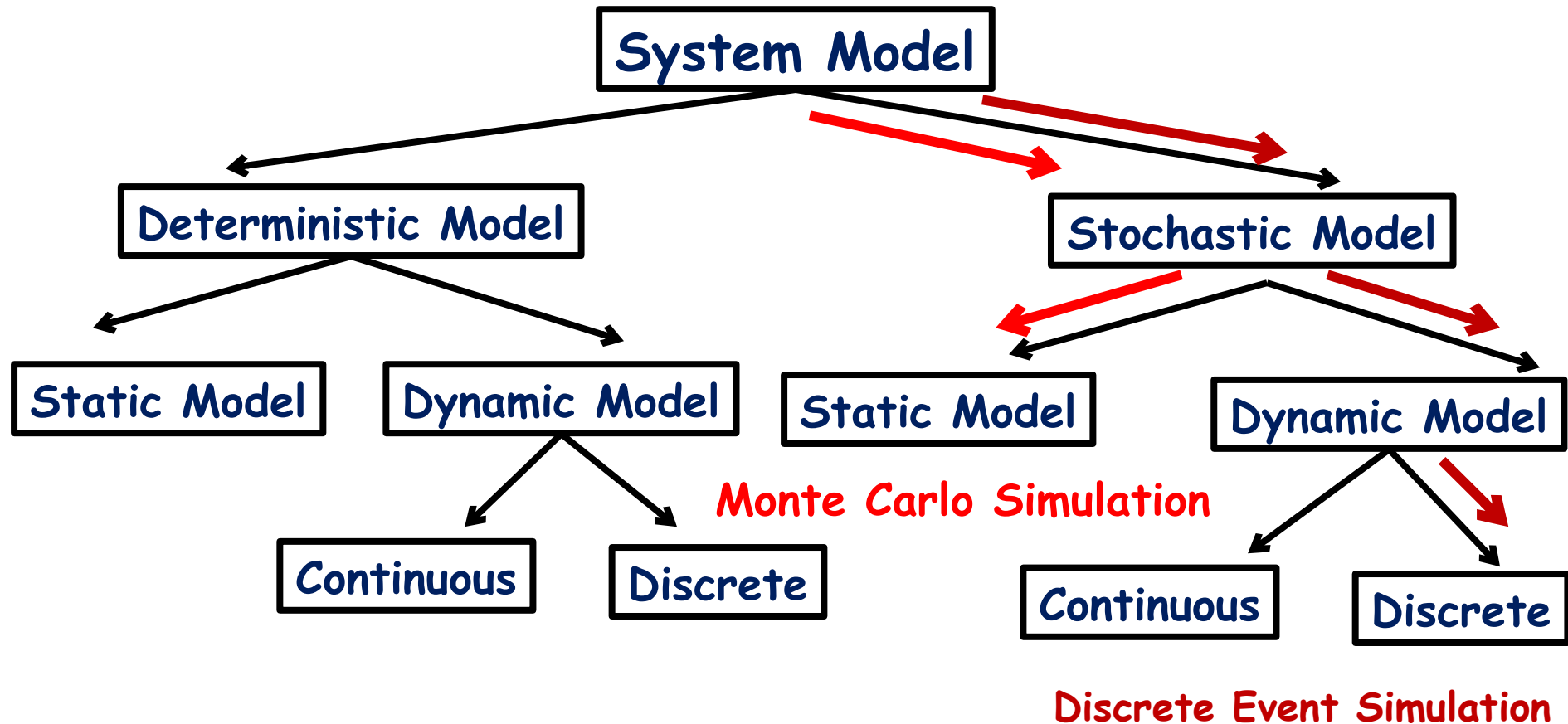
Continuous Models

Bit Arrival in a Queue



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Models Taxonomy



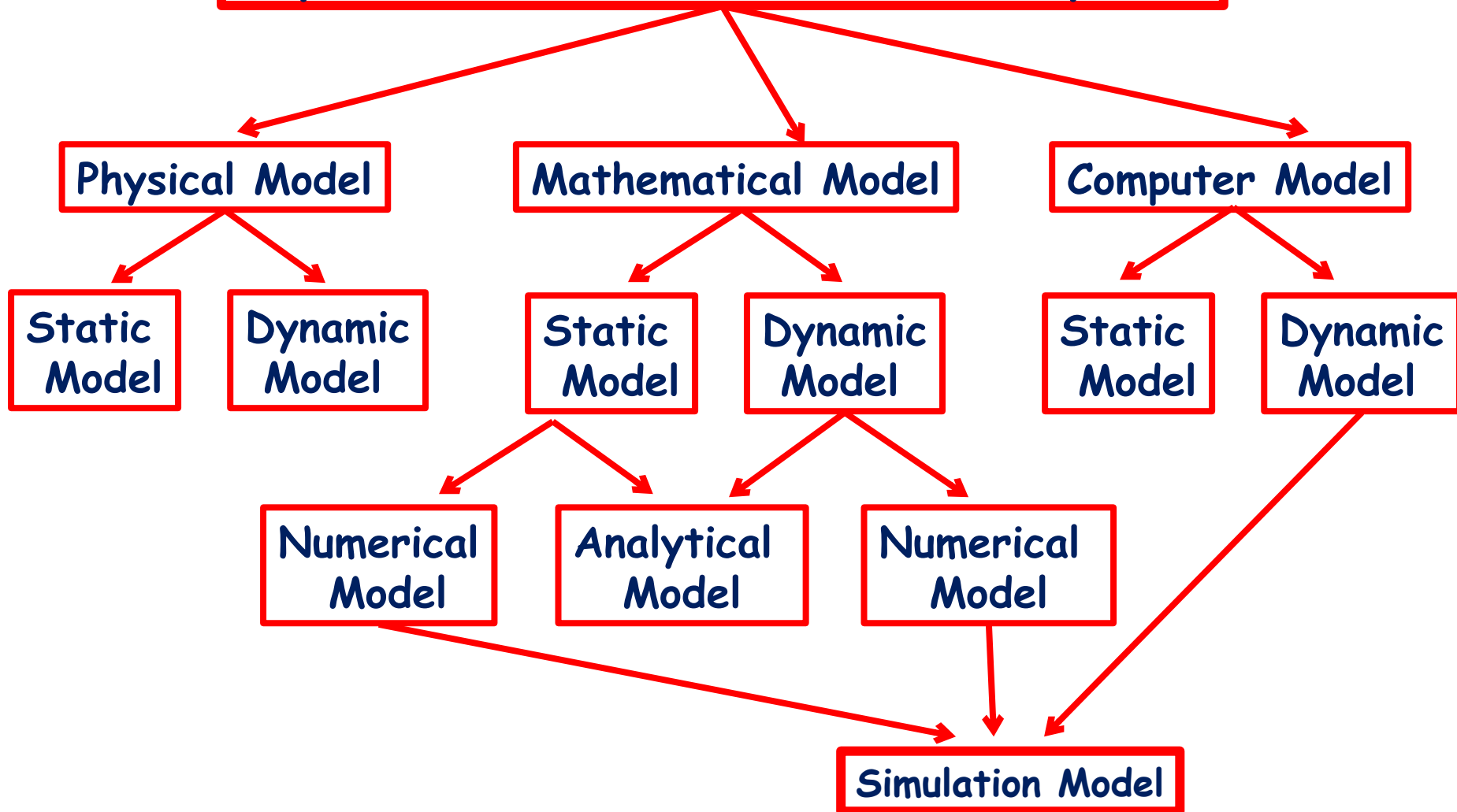
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Models Taxonomy

Experiment with a model of the system



Simulation Models

Experiment with a model of the system

Mathematical Model

Computer Model

Static
Model

Dynamic
Model

Static
Model

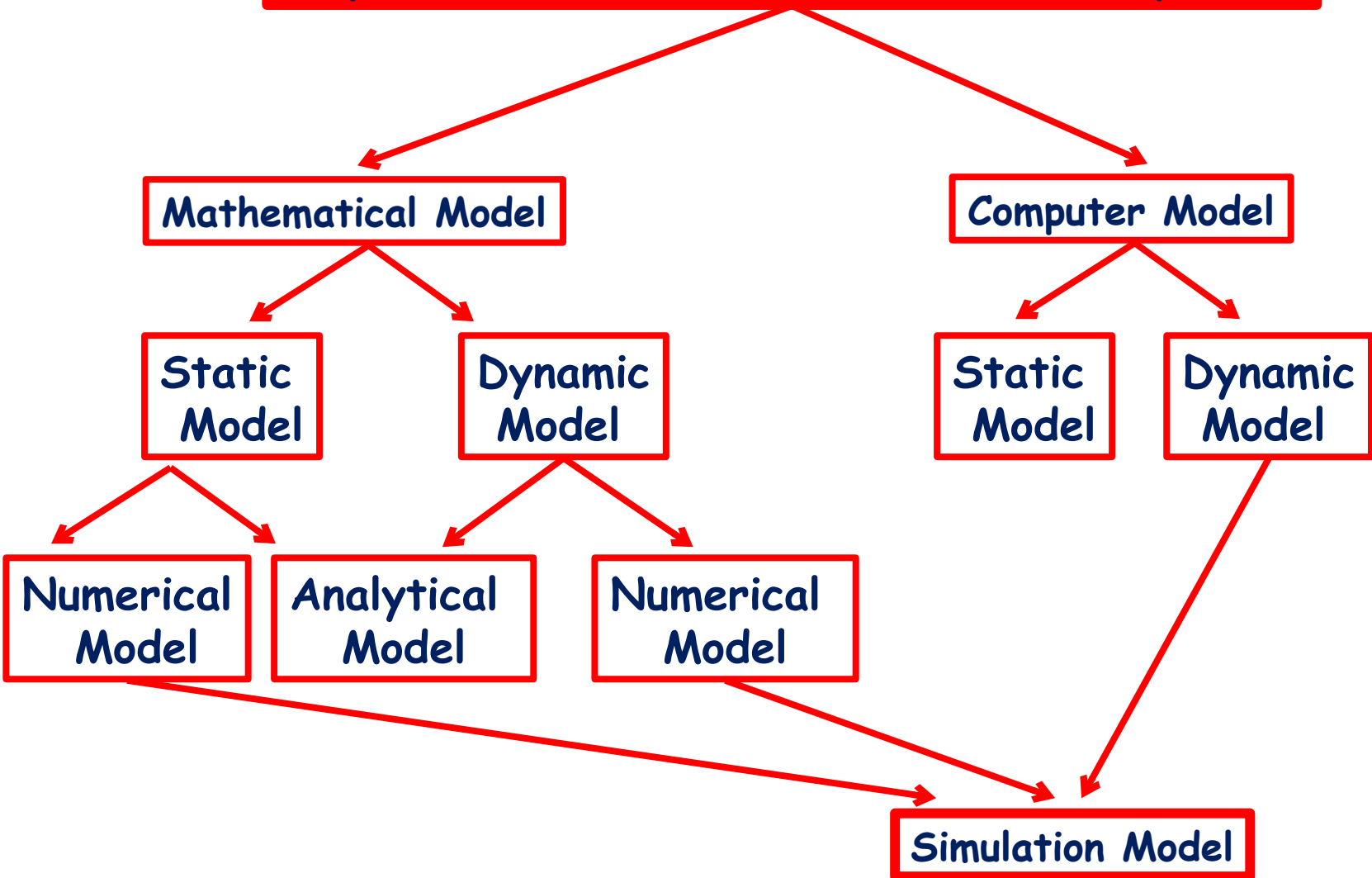
Dynamic
Model

Numerical
Model

Analytical
Model

Numerical
Model

Simulation Model



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Simulation Models

Simulation modeling

is the process of creating

and

analyzing

a digital prototype of a physical model

to predict its performance

in the real world.

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Simulation Models

Simulation modeling

is used to help
designers and engineers understand
whether,
under what conditions,
and
in which ways
a part could fail
and
what loads it can withstand.

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Simulation Models

Simulation Modeling

analyses the approximate working conditions
by applying the simulation software.

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Analytical Vs. Numerical Vs. Simulation

Analytical solutions denote **exact** solutions

that can be used to study the behavior of the system with varying properties.

Unfortunately very few practical systems lead to analytical solutions, and analytical solutions are of limited use.

That's why we use **numerical approach** to make **close answer** to practical result.

Simulation : produces a huge amount of data that can statistically be reduced to your expectations .

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Analytical Vs. Numerical Vs. Simulation

But just because this uses a lot of number crunching, it is not referred to as "numerical analysis".

Parts of it might rely on numerical methods that come from the approximation techniques of numerical analysis (as defined above), but this simulation is still not referred to as numerical analysis.

It could be called "performance prediction using modeling and simulation".

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Mathematical Modeling Vs. Simulation

Translating the actual process behavior into mathematical expressions is mathematical modeling

and

solving that model with the help of a computer numerically is simulation.

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Simulation Models Vs Analytical Models

Analytical Model is suitable when the model is simple.

For example, movement of body, we use calculus, algebra or probability theory.

Simulation model is suitable when the model is highly complex.

For example, Weather forecasting.

Simulation is **not used** when a suitable Analytical model exists.

Simulations are often **complex error-prone pieces of software**.

Simulation only produce **approximate answers**.

Simulation can take a **LONG** time to execute.

Models Taxonomy

Too costly or disruptive
Not appropriate for the
design

There is always the
question of whether it
actually reflects the
system.

SYSTEM

Experiment with the
Actual System

Experiment with a
Model of the System

Make assumptions
that take the form
of mathematical or
logical relationships

Physical Model

Mathematical Model

If the model is simple
enough.e.g., movement of
a body calculus, algebra,
probability theory

Analytical Solution

Simulation

If the model is Highly complex
systems, e.g. Weather forecasting

Types of Simulation Models

The behavior cannot
be entirely predicted

One or more
random
parameters

Stochastic

Fixed inputs
yield different
outputs

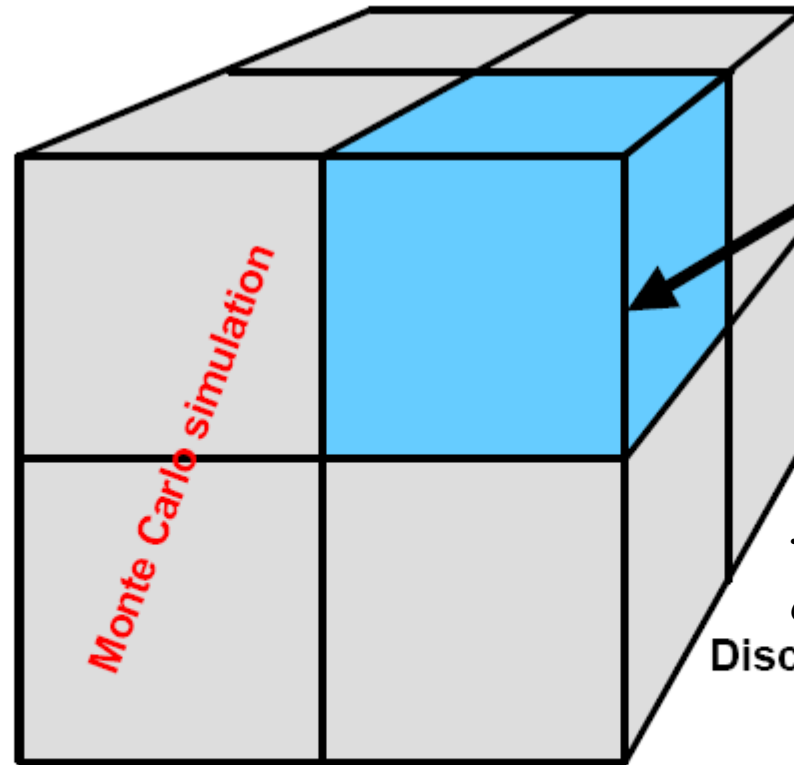
Deterministic

Fixed inputs
yield fixed
outputs

The behavior is
entirely predictable.

System description at
one point in time
**Snapshot at a single
point in time**

System description
as it changes in time
**State variables
change over time**



Focus of
this course

Model allows
system state to
change at any time

Continuous-time
The state of the system
changes continuously

Discrete-time

System state
changes at distinct
times

The state variables change
only at a countable number of
points in time.