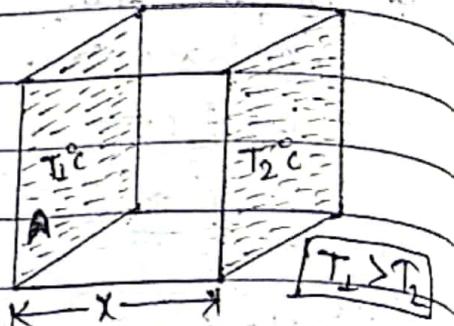


Thermal Conductivity:-

Let us Consider a Cube having side 'x' and area of each face 'A'.

Also Let, left end be at temperature  $T_1^\circ C$  and right end be at temperature  $T_2^\circ C$  such that  $T_1 > T_2$

So, flow of heat takes place from left end to right end.



Experimentally, it has been found that the amount of heat ( $Q$ ) transfer between two faces in time 't' is found to be

i) directly proportional to area of each face,

$$\text{i.e. } Q \propto A \quad \dots \text{(i)}$$

ii) directly proportional to temperature difference between two faces,

$$\text{i.e. } Q \propto (T_1 - T_2) \quad \dots \text{(ii)}$$

iii) directly proportional to time for which heat flow,

$$\text{i.e. } Q \propto t \quad \dots \text{(iii)}$$

iv) inversely proportional to distance between two faces,

$$\text{i.e. } Q \propto \frac{1}{x} \quad \dots \text{(iv)}$$

Combining all equations;

$$\Rightarrow Q \propto \frac{A(T_1 - T_2)t}{x}$$

$$\Rightarrow Q = \frac{KA(T_1 - T_2)t}{x} \quad \dots \text{(v)}$$

Where,  $K$  is proportionality constant called thermal conductivity which value depends upon nature of material.

$$\text{Also, } \frac{Q}{t} = \frac{KA(T_1 - T_2)}{x}$$

If  $A = 1 \text{ m}^2$ ,  $T_1 - T_2 = 1^\circ C/1K$  and  $x = 1 \text{ m}$ , Then,

$$\Rightarrow K = \frac{Q}{At}$$

Thus, Thermal Conductivity of material is numerically equal to the rate of flow of heat between two faces having area of each faces  $1\text{ m}^2$  separated by distance 1m and maintained at temperature difference of  $1^\circ\text{C}/1\text{K}$ .

## # Mode of transfer of heat

### [1] Conduction:-

↪ The mode of transfer of heat in which heat is transferred between two points without actual movement of particle is called Conduction.

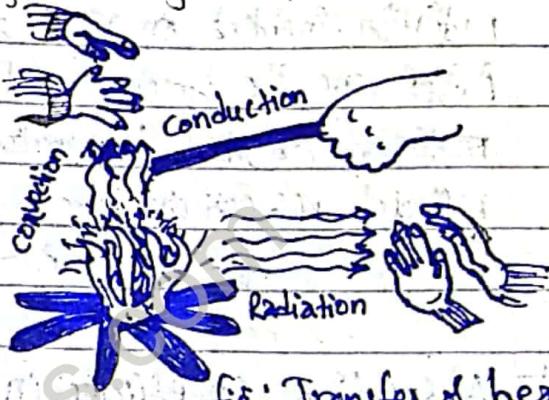


fig: Transfer of heat

In this mode heat is transferred to neighbouring particles and transfer of heat between successive particle takes place.

for e.g. heat transfer in solid.

### [2] Convection:-

↪ The mode of transfer of heat in which heat is transferred between two points by actual movement of particle is called Convection.

for e.g. heat transfer in liquid and gas.

### [3] Radiation:-

↪ The mode of transfer of heat without presence of any medium in the form of infrared wave is called radiation.

e.g. transfer of heat from Sun to earth Surface or Sun light.

## # Absorption, transmission & Reflection Co-efficient:-

↳ When heat radiation incident on a body, it is partially absorbed, partially transmitted & partially reflected.

\* Let,  $B$  be the amount of heat radiation incident on a body and  $A, T, R$  are the amount of heat ~~radiation~~ absorbed, transmitted & reflected respectively, then,

$$B = A + T + R \quad \text{--- (i)}$$

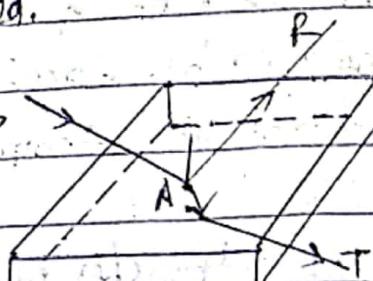


fig: reflection ( $R$ ), transmission ( $T$ ) & absorption ( $A$ ) of heat radiation

## # Absorption Co-efficient ( $a$ ):-

↳ The ratio of amount of heat radiation absorbed to the amount of heat radiation incident is called absorption Co-efficient.

$$\text{i.e., } a = \frac{A}{B}$$

$$\Rightarrow A = ab \quad \text{--- (ii)}$$

## # Transmission Co-efficient ( $t$ ):-

↳ The ratio of amount of heat <sup>radiation</sup> transmitted to the amount of heat radiation incident is called transmission Co-efficient.

$$\text{i.e., } t = \frac{T}{B}$$

$$\Rightarrow T = tb \quad \text{--- (iii)}$$

## # Reflection Co-efficient ( $r$ ):-

↳ The ratio of amount of heat radiation reflected to the amount of heat radiation incident is called reflection Co-efficient.

$$\text{i.e., } r = \frac{R}{B}$$

$$\Rightarrow R = rb \quad \text{--- (iv)}$$

Using eqn ⑪, ⑫ & ⑬ in eqn ⑩

$$\Rightarrow \alpha = 2\alpha + t\alpha + 2\alpha$$

$$\Rightarrow \alpha + t + r = 1.$$

### # Black body:-

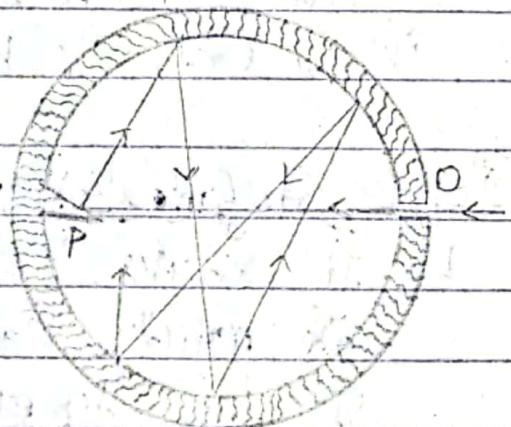
→ Which completely absorbs the heat radiations of all wave length falling on it is known as perfectly black body.

Its absorption co-efficient is unity. The Sun emits radiation of all wavelengths. So, it may be regarded as black body even though it looks white. Black body absorbs 96% to 98% of incident radiation.

### # Ferry's Black Body:-

→ Ferry's black body is made for experimental verification. This is made with closed double walled hollow sphere having a tiny hole O. and Conical projection P opposite to hole. as shown in figure below:-

There is a projection P which reflects the incident radiation passing through hole O and reflections occur in inner wall and almost all radiation is absorbed into the wall.



When the black body is heated,

absorbed radiation emerges from the hole O.

fig: Ferry's Black Body

## # Emissive power:-

↪ The emissive power of a body is defined as the amount of heat radiation emitted per second per unit area by the body of all wave length of heat radiation.

It is denoted by  $E$  & given by:

$$E = \frac{Q}{At}$$

Its SI unit is  $\text{W/m}^2$ .

## # Emissivity ( $\epsilon$ ):-

↪ The ratio of emissive power of a body to the emissive power of perfectly black body is called emissivity.

i.e.

$$\epsilon \text{ [Emissivity]} = \frac{\text{Emissive power of a body}}{\text{Emissive power of perfectly black body}}$$

i) For  $\epsilon < 1$ , the black body is not perfectly black;

ii) For  $\epsilon = 1$ , the black body is perfectly black body,

iii) For  $\epsilon > 1$ , the black body is impossible.

## # Stefan-Boltzmann's law:-

↪ It states, "The heat radiation emitted per second per unit area by the perfectly black body is directly proportional to the fourth power of its temperature."

If 'F' be the amount of heat radiation emitted by perfectly black body per second per unit area and  $T$  be its temperature. Then, according to Stefan-Boltzmann's law,

$$F \propto T^4$$

$$\Rightarrow E = \sigma T^4$$

Where 'σ' is proportionality constant called Stefan-Boltzmann Constant and its value is equal to  $5.67 \times 10^{-8} \text{ W/m}^2 \text{ K}^4$ .

If 'e' be the emissivity of a body then Stefan-Boltzmann's law can be written as,

$$E = e \sigma T^4$$

Again, If a body at temperature  $T_1$  is enclosed by another body at temperature  $T_2$  then Stefan's-Boltzmann law can be written as,

$$E = e \sigma (T_1^4 - T_2^4)$$

## # Measurement of thermal Conductivity of a Solid by Shearle's method:-

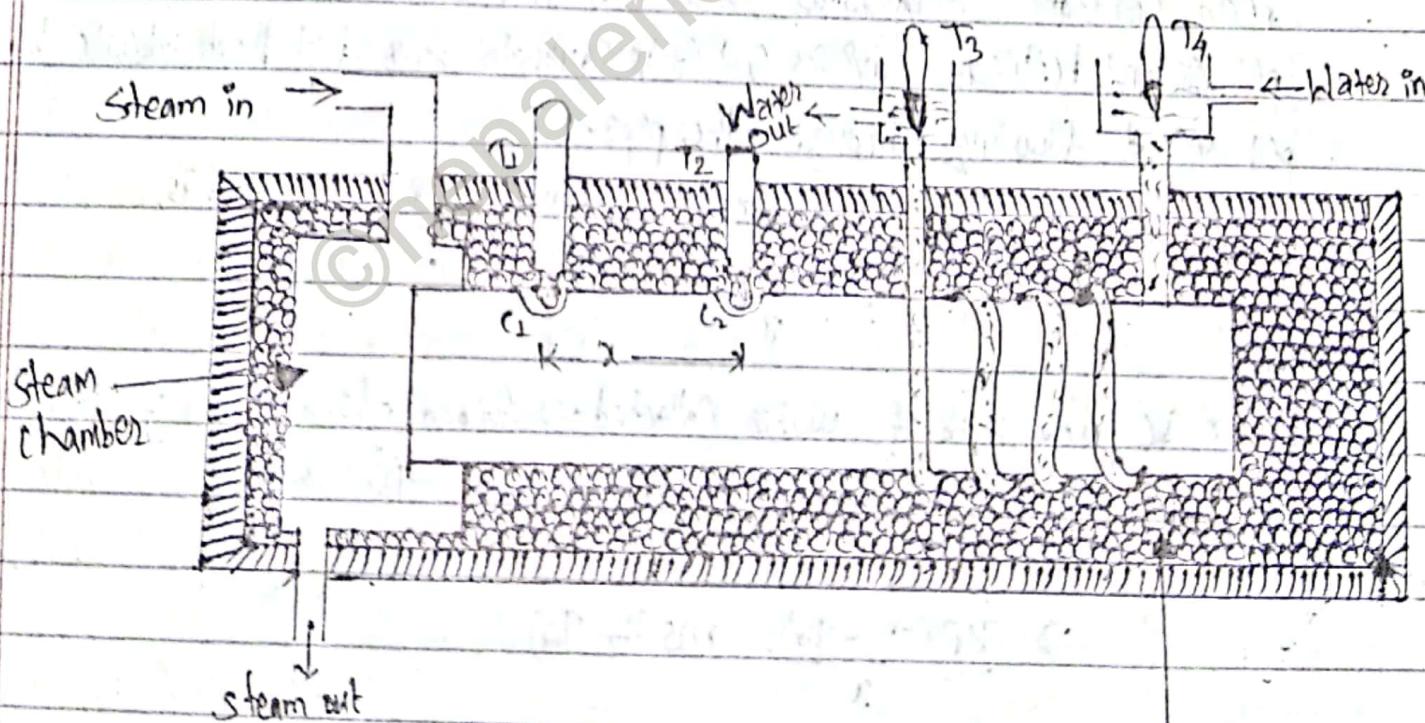


fig: Shearle's apparatus:

Insulating  
material

The measurement of thermal conductivity of solid by Shearle's method consists of experimental rod with uniform cross sectional area ( $A$ ) in which there are two cavities  $C_1$  &  $C_2$  separated by distance ' $x$ ' in left end. At right end of the rod the conducting pipe is rounded through which water is passing continuously. The left end of the rod is heated by passing steam. The thermometers  $T_1$  &  $T_2$  measure the temperature of cavities  $C_1$  &  $C_2$  and  $T_3$  &  $T_4$  measure the temperature of water out of water in respectively. The experimental rod is enclosed by insulating material such as wool, cotton, paper, etc. to prevent from exchange of heat with surrounding.

Initially the  $T_1$  &  $T_2$  shows rise in temperature after passing steam and also thermometers  $T_3$  initially shows the rise in temperature.

After continuously circulating steam & water, at certain stage thermometers  $T_1$ ,  $T_2$ ,  $T_3$  read constant temperature and at that condition, amount of heat transfer per second between cavities  $C_1$  &  $C_2$  is equal to amount of heat absorbed by water per second flowing through the pipe.

Now, amount of heat transfer between  $C_1$  &  $C_2$  per second is,

$$\frac{Q}{t} = \frac{KA(T_1 - T_2)}{x} \quad \text{(i)}$$

If  $m$  be the mass of water collected per second then amount of heat absorbed per second by water is;  $Q_t = ms(T_3 - T_4) \quad \text{(ii)}$

At equilibrium,  $\text{eq(i)} = \text{eq(ii)}$

$$\Rightarrow \frac{KA(T_1 - T_2)}{x} = ms(T_3 - T_4)$$

$$\Rightarrow K = \frac{ms(T_3 - T_4)x}{A(T_1 - T_2)} \quad \text{(iii)}$$

Using this relation we can calculate thermal conductivity of solid.

Numericals:-

B.1[A] A bar 0.2 m in length and  $2.5 \text{ cm}^2$  in cross section is ideally lagged. One end is maintained at  $100^\circ\text{C}$  and the other end is maintained at  $0^\circ\text{C}$  by immersing in melting ice. Calculate the mass of ice melt in one hour. Thermal conductivity of the material of the bar is  $4 \times 10^{-2} \text{ Wm}^{-1}\text{K}^{-1}$ .

$\star \leftarrow \text{Soln:-}$

$$x = 0.2 \text{ m}, A = 2.5 \text{ cm}^2 = \frac{2.5}{10000} = 2.5 \times 10^{-4} \text{ m}^2, T_1 = 100^\circ\text{C}, T_2 = 0^\circ\text{C}, m_i = ?, t = 1 \text{ hour} = 3600 \text{ sec.}$$

$$K = 4 \times 10^{-2} \text{ Wm}^{-1}\text{K}^{-1}$$

$$\text{Now, we have, } \frac{\dot{Q}}{t} = \frac{KA(T_1 - T_2)}{x}$$

$$\text{or, } \frac{m_i L_f}{t} = \frac{KA(T_1 - T_2)}{x} \Rightarrow m_i = \frac{KA(T_1 - T_2)t}{x L_f} = \frac{4 \times 10^{-2} \times 2.5 \times 10^{-4} (100 - 0) 3600}{0.2 \times 336000}$$

$$\Rightarrow m_i = \frac{3.6}{67200} = 5.36 \times 10^{-5} \text{ kg}$$

Hence,  $5.36 \times 10^{-5} \text{ kg}$  of ice is melt.

B.1[B] A rod 1.3 m long consists of a 0.8 m length of aluminium joined end to end to a 0.5 m length of brass. The free end of the aluminium section is maintained at  $150^\circ\text{C}$  and the free end of the brass piece is maintained at  $20^\circ\text{C}$ . No heat is lost through the sides of the rod. At a steady state, what is the temperature at the point where the two metals are joined? ( $K_{Al} = 205, K_b = 110 \text{ Wm}^{-1}\text{K}^{-1}$ )

$\star \text{Soln:- } x_1 = 0.8 \text{ m} \quad x_2 = 0.5 \text{ m}$

$$T_{1a} = 150^\circ\text{C} \quad T_{2b} = ? = T (\text{Let})$$

$$T_{2a} = ? \quad T_{2b} = 20^\circ\text{C}, A_1 = A_2$$

$$\text{Now, } \left(\frac{\dot{Q}}{t}\right)_1 = \left(\frac{\dot{Q}}{t}\right)_2$$

$$\text{or, } 256.25(150 - T) = 220(T - 20)$$

$$\text{or, } 38437.5 - 256.25T = 220T - 4400$$

$$\text{Or, } 42837.5 = 476.25T$$

$$\Rightarrow T = 89.94^\circ\text{C} = \text{approx. } 90^\circ\text{C}$$

$$\text{or, } \frac{K_1 A_1 (T_{1a} - T_{2a})}{x_1} = \frac{K_2 A_2 (T_{2b} - T_{2a})}{x_2}$$

$$\text{or, } \frac{205(150 - T)}{0.8} = \frac{110(T - 20)}{0.5}$$

$\therefore$  temp of joining point is  $90^\circ\text{C}$  #

**Q.1[C]** A slab of stone of area  $0.36 \text{ m}^2$  and thickness  $10 \text{ cm}$  is exposed on the surface to steam at  $100^\circ\text{C}$ . A block of ice at  $0^\circ\text{C}$  rests on the upper surface of the slab. In one hour,  $4.8 \text{ kg}$  of ice is melted. Calculate the 'K' of stone.

**Soln:-**

$$A = 0.36 \text{ m}^2, x = 10 \text{ cm} = 0.1 \text{ m}, T_1 = 100^\circ\text{C}, T_2 = 0^\circ\text{C}$$

$$t = 1 \text{ hour} = 3600 \text{ sec.}, m_i = 4.8 \text{ kg}, K_s = ?$$

$$\text{Now, } \frac{Q}{t} = \frac{K_s(A)(T_1 - T_2)}{x}$$

$$\text{or, } \frac{m_i L_f}{t} = \frac{K_s A (T_1 - T_2)}{x}$$

$$\text{Or, } \frac{4.8 \times 336000}{3600} = K_s \times 0.36 (100 - 0)$$

$$\text{Or, } 448 = K_s \times 360 \Rightarrow [K_s = 1.244 \text{ Watt m}^{-1}\text{K}^{-1}]$$

Hence, thermal conductivity of stone slab is  $1.244 \text{ Watt m}^{-1}\text{K}^{-1}$ .

**Q.1[D]** A metal of rod of length  $20 \text{ cm}$  and cross-sectional area  $3.14 \text{ cm}^2$  is covered with non-conducting substance. One of its end is maintained at  $100^\circ\text{C}$ , while the other end is put in ice at  $0^\circ\text{C}$ . It is found that  $25 \text{ gm}$  of ice melts in  $5 \text{ minutes}$ . Calculate the thermal conductivity of the metal.

**Soln:-**  $x = 20 \text{ cm} = 0.2 \text{ m}$

$$A = 3.14 \text{ cm}^2 = 3.14 \times 10^{-4} \text{ m}^2$$

$$T_1 = 100^\circ\text{C}, T_2 = 0^\circ\text{C}$$

$$m_i = 25 \text{ gm}, t = 5 \text{ min} = 300 \text{ sec}$$

$$K_m = ? \rightarrow 25 \times 10^{-3} \text{ kg}$$

We have,

$$\frac{m_i L_f}{t} = \frac{K_m A (T_1 - T_2)}{x}$$

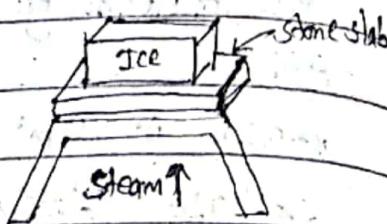
$$\text{Or, } \frac{25 \times 10^{-3} \times 336000}{300} = K_m \times 3.14 \times 10^{-4} (100 - 0)$$

$$\text{Or, } 28 = K_m \times 0.157$$

$$\Rightarrow K_m = 178.34 \text{ W/mK}$$

Hence,

Thermal Conductivity of metal is  $178.34 \text{ W/mK}$



Q.1[E] Estimate the rate of heat loss through a glass window of area  $2\text{m}^2$  and thickness 4mm when the temp<sup>r</sup> of the room is  $300\text{K}$  & temp<sup>r</sup> outside is  $5^\circ\text{C}$ .

\* Sol<sup>n</sup>: Given,  $K = 1.2 \text{ W m}^{-1} \text{ K}^{-1}$ ,  $A = 2 \text{ m}^2$ ,  $x_1 = 4\text{mm} = 4 \times 10^{-3} \text{ m}$ ,  $T_1 = 300\text{K} = 27^\circ\text{C}$ ,  $T_2 = 5^\circ\text{C}$

Now,  $\frac{Q}{t} = \frac{KA(T_1 - T_2)}{x} = \frac{1.2 \times 2(27 - 5)}{4 \times 10^{-3}} = 13.2 \times 10^3 \text{ J/s} = 13200 \text{ W}$

Hence, rate of heat loss =  $13200 \text{ W}$  #

Q.1[F] An ice box is made of wood 1.75 cm. thick lined inside with cork 2 cm. thick. If the temp<sup>r</sup> of inner surface of the wood is steady at  $12^\circ\text{C}$ , What is the temp<sup>r</sup> of the interface? The thermal conductivity of wood is five times that of Cork.

\* Sol<sup>n</sup>: Given,  $x_1 = 1.75\text{cm} = 0.0175 \text{ m}$ ,  $T_1 = 12^\circ\text{C}$ ,  $K_w = 5 \text{ K m W}^{-1}$ ,  $x_2 = 2\text{cm} = 0.02 \text{ m}$ ,  $T_{20} = 0^\circ\text{C}$

At steady state,  $(\frac{\theta}{x})_1 = (\frac{\theta}{x})_2$

Or,  $\frac{K_c A(T_{1c} - T_{20})}{x_1} = \frac{K_w A(T_{1w} - T_{20})}{x_2}$

Or,  $\frac{K_c (12 - 0)}{0.0175} = \frac{K_w (12 - T)}{0.02}$

Or,  $12 K_c \times 0.02 = 5 K_c \times 0.0175 (12 - T)$

Or,  $0.24 = 0.0875 (12 - T)$

Or,  $2.74 = 12 - T$

$\Rightarrow T_1 = 9.25^\circ\text{C}$

Hence, the temperature of the interface is  $9.25^\circ\text{C}$  #

**Q. 1(G)** Assuming that the thermal insulation provided by a woollen glove is equivalent to a layer of quiescent air 3 mm thick, determine that heat loss per minute from a man's hand, Surface area  $200 \text{ cm}^2$  on a winter day when the outside air temperature is  $-3^\circ\text{C}$ . The skin temp<sup>r</sup> is to be taken as  $35^\circ\text{C}$  & thermal conductivity of air as  $24 \times 10^{-3} \text{ W m}^{-1}\text{K}^{-1}$ .

\* Soln: -  $x = 3 \text{ mm} = 3 \times 10^{-3} \text{ m}$ .

$$A = 200 \text{ cm}^2 = 0.02 \text{ m}^2, T_1 = 35^\circ\text{C}, T_2 = -3^\circ\text{C}, k_A = 24 \times 10^{-3} \text{ W m}^{-1}\text{K}^{-1}$$

Now,

$$\frac{Q}{t} = \frac{KA(T_1 - T_2)}{x} = \frac{24 \times 10^{-3} (35 + 3) \times 0.02}{3 \times 10^{-3}} = 608000 \text{ J/sec} = 364.8 \text{ J/min}$$

Hence, Heat loss per minute from man's hand is  $364.8 \text{ J/min}$ .

**Q. 1(H)** Estimate the rate of heat loss through a glass window of area  $2 \text{ m}^2$  & thickness 3mm when the temperature of the room is  $20^\circ\text{C}$  and that of air outside is  $5^\circ\text{C}$ . Given  $k = 1.2 \text{ W m}^{-1}\text{K}^{-1}$ .

\* Soln: -  $B/t = ?$

$$A = 2 \text{ m}^2, x = 3 \times 10^{-3} \text{ m}, T_1 = 20^\circ\text{C}, T_2 = 5^\circ\text{C}, k = 1.2 \text{ W m}^{-1}\text{K}^{-1}$$

Now,

$$\frac{B}{t} = \frac{KA(T_1 - T_2)}{x} = \frac{1.2 \times 2 (20 - 5)}{3 \times 10^{-3}} = 12000 \text{ J/s} = 12000 \text{ W} = 12 \text{ kW}$$

Hence, Rate of heat loss is  $12 \text{ kW}$ .

**Q.1(I)** Estimate the rate at which ice would melt in a wooden box 2.5 cm thick of inside measurement 100 cm x 60 cm x 40 cm. assuming that the external temperature is 35°C & thermal conductivity of wood is 0.168 W/mK.

\* Soln:-

$$\alpha = 2.5 \text{ cm} = 2.5 \times 10^{-2} \text{ m}, l = 100 \text{ cm} = 1 \text{ m}, b = 60 \text{ cm} = 0.6 \text{ m} \text{ & } h = 40 \text{ cm} = 0.4 \text{ m}$$

$$\therefore A = 2(lb + bh + lh) = 2[(1 \times 0.6) + (0.6 \times 0.4) + (1 \times 0.4)] = 2.48 \text{ m}^2$$

$$T_1 = 35^\circ, T_2 = 0^\circ, k_w = 0.168 \text{ W/mK}$$

$$\text{Now, } \frac{\partial}{t} = \frac{kA(T_1 - T_2)}{\alpha}$$

$$\text{or, } \frac{m_i^o}{t} = \frac{kA(T_1 - T_2)}{\alpha L_f} = \frac{0.168 \times 2.48 \times (35)}{2.5 \times 10^{-2} \times 336000} = \frac{14.5824}{8400} = 0.001736 \text{ kg/sec.} \\ = 1.736 \times 10^{-3} \text{ kg/sec.}$$

Hence, rate of ice melt is  $1.736 \times 10^{-3} \text{ kg/sec.}$

**Q.4(J)** A bar 0.2 m in length and of cross-sectional area  $2.5 \times 10^{-4} \text{ m}^2$  is ideally lagged. One end is maintained at 373 K while the other is maintained at 273 K by immersing in melting ice. calculate the rate at which the ice melts owing to the flow of heat along the bar.

\* Soln:-

$$\alpha = 0.2 \text{ m}, A = 2.5 \times 10^{-4} \text{ m}^2, T_1 = 373 \text{ K}, T_2 = 273 \text{ K}, \frac{\partial}{t} = \frac{m_i^o}{t} \text{ then, } \frac{m_i^o}{t} = ?$$

We have,

$$\frac{\partial}{t} = \frac{kA(T_1 - T_2)}{\alpha L_f}$$

$$\frac{m_i^o}{t} = \frac{kA(T_1 - T_2)}{\alpha L_f} = \frac{4 \times 10^2 \times 2.5 \times 10^{-4} (373 - 273)}{0.2 \times 336000} = 1.48 \times 10^{-8} \text{ kg/sec.}$$

It

B.1[K] A pot with a steel bottom 8.5 mm thick rest on the hot sh. The area of the bottom of the pot is  $0.15 \text{ m}^2$ . The water inside pot is at  $100^\circ\text{C}$  & 390 g of water is evaporated every 3 min. Find the temp<sup>r</sup> of lower surface of the pot which is in contact with the sh. [K = 50.2 W/mK,  $L_v = 2256 \times 10^3 \text{ J/kg}$ ] ???

SOL:

$$z = 8.5 \text{ mm} = 0.0085 \text{ m}$$

$$A = 0.15 \text{ m}^2, m_v = 390 \text{ gm} = 0.39 \text{ kg}$$

$$t = 3 \text{ min} = 180 \text{ sec}, T_2 = ? \quad T_1 = 100^\circ\text{C} = 373 \text{ K}$$

$$\text{Now, } \frac{Q}{t} = \frac{KA(T_1 - T_2)}{z} = \frac{m_v L_v}{t}$$

$$\text{Or, } \frac{50.2 \times 0.15 (T_1 - 373)}{0.0085} \approx \frac{0.39 \times 2256 \times 10^3}{180}$$

$$\text{Or, } T_1 - 373 = 5.52$$

Hence, temp<sup>r</sup> of the bottom of the pot is  $105.52^\circ\text{C}$ .

B.2[A] The element of a electric fire with an output of 1.5 kW is a cylinder of 0.3 m long & 0.04 m in radius. Calculate its temp<sup>r</sup> if it behaves as a black body.

SOL: P = 1.5 kW = 1500 W, l = 0.3 m, r = 0.04 m

$$\text{Area of cylinder}(A) = 2\pi r l = 2\pi \times 0.04 \times 0.3 = 7.5 \times 10^{-2} \text{ m}^2, T = ?$$

$$\text{Now, } P = A \sigma T^4$$

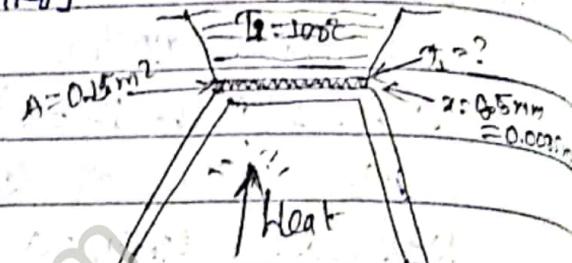
$$\text{Or, } 1500 = 7.5 \times 10^{-2} \times 5.67 \times 10^8 \times T^4$$

$$\text{Or, } T^4 = \frac{1500}{4.27 \times 10^{-9}} = 3.50 \times 10^{11}$$

$$\text{Or, } T^2 = 592343.385$$

$$\Rightarrow T = 769.6384 \text{ K}$$

Thus, its temp<sup>r</sup> is 769.6384 K.



Q.2[B] The Sun is a black body of surface temp about 6000K. If Sun's radius is  $7 \times 10^8$  m, calculate the energy per second radiated from its surface. The earth is about  $1.5 \times 10^{11}$  m from the Sun. Assuming all the radiation from the sun falls on the surface of sphere of this radius, estimate the energy per second per meter<sup>2</sup> received by the earth?

$\text{Sol: } T = 6000\text{K} =$

$$R_s = 7 \times 10^8 \text{ m}, A = 4\pi R_s^2 = 4\pi (7 \times 10^8)^2 = 196\pi \times 10^{16} \text{ m}^2$$

Note.

$$P = \sigma A T^4 = 5.67 \times 10^{-8} \times 196\pi \times 10^{16} \times (6000)^4 = 4.52 \times 10^{26} \text{ Watt.}$$

Again,

$$A' = 4\pi (d)^2 = 4\pi (1.5 \times 10^{11})^2 = 9\pi \times 10^{22} \text{ m}^2$$

$$\text{So, } \frac{P}{A'} = \frac{4.52 \times 10^{26}}{9\pi \times 10^{22}} = 1598.62 \text{ W/m}^2, \#$$

Hence, power =  $4.52 \times 10^{26}$  Watt & Energy per second per m<sup>2</sup> =  $1598.62 \text{ W/m}^2$ . #

Q.2[C] A sphere of radius 2.00 cm with a black surface is cooled & then suspended in a large evacuated enclosure with black walls maintained at 27°C. If the rate of change of thermal energy of sphere is 1.85 J/s. when its temp is -73°C, calculate the value of Stefan's Constant.

$\text{Sol: } r = 2 \text{ cm} = 0.02 \text{ m}, T_2 = 27^\circ\text{C} = 300 \text{ K}, P = 1.85 \text{ J/s}, T_1 = -73^\circ\text{C} = 200 \text{ K}$

Now,  $E = \sigma(T_1^4 - T_2^4)$ .

$$P = \sigma A (T_1^4 - T_2^4)$$

$$\Rightarrow \sigma = \frac{P}{A(T_1^4 - T_2^4)} = \frac{1.85}{4\pi (0.02)^2 [(300)^4 - (200)^4]} = \frac{1.85}{32672563.6} = 5.66 \times 10^{-8} \text{ W/m}^2\text{K}^4$$

Hence, Stefan's Constant is  $5.66 \times 10^{-8} \text{ W/m}^2\text{K}^4$  #

Q.2[D] Estimate the power loss through unit area from a perfectly black body at  $327^\circ\text{C}$  to the surrounding environment at  $27^\circ\text{C}$ .

Sol<sup>n</sup>: -  $P = ?$ ,  $A = 1 \text{ m}^2$ ,  $T_1 = 600 \text{ K}$ ,  $T_2 = 300 \text{ K}$

Now,

$$\Rightarrow P = \sigma A (T_1^4 - T_2^4) = 5.67 \times 10^{-8} \times [(600)^4 - (300)^4] = 6889.05 \text{ Watt. } \#$$

Hence, power loss = 6889.05 watt. \*

Q.2[E] A spherical blackbody of radius 5 cm has its temp  $127^\circ\text{C}$  & its emissivity is 0.6. Calculate its radiant power.

Solution:-

$$\text{Here, } A = 4\pi r^2 = 4\pi \left(\frac{5}{100}\right)^2 = 0.01\pi \text{ m}^2, T = 127^\circ\text{C} = 400 \text{ K}, \epsilon = 0.6, P = ?$$

Now,

$$P = \epsilon \sigma A T^4 = 0.6 \times 5.67 \times 10^{-8} \times 0.01\pi (400)^4 = 27.36 \text{ Watt. } \#$$

Hence, radiant power is 27.36 Watt. \*

Q.2[F] Estimate the radiant power loss from a human body at a temp  $38.5^\circ\text{C}$  to the environment at  $0^\circ\text{C}$  if the surface area of the body is  $1.5 \text{ m}^2$  & its emissivity is 0.6.

Sol<sup>n</sup>: -  $P = ?$ ,  $T_1 = 38.5^\circ\text{C} = 311.5 \text{ K}$ ,  $T_2 = 0^\circ\text{C} = 273 \text{ K}$ ,  $A = 1.5 \text{ m}^2$ ,  $\epsilon = 0.6$

Now,

$$\begin{aligned} P &= \epsilon \sigma A (T_1^4 - T_2^4) \\ &= 0.6 \times 5.67 \times 10^{-8} \times 1.5 [(311.5)^4 - (273)^4] \\ &= 5.103 \times 10^{-8} [3860685690] \end{aligned}$$

$$\Rightarrow P = 197.01 \text{ Watt. } \#$$

Hence, Radiant power loss = 197.01 Watt.

Q.2 [G] A man, the surface area of whose skin is  $2\text{m}^2$  is sitting in a room where the air temp<sup>r</sup> is  $20^\circ\text{C}$ . If his skin temp<sup>r</sup> is  $37^\circ\text{C}$ , find the rate at which his body loses heat. The emissivity of his skin is 0.97.

$\star \text{SOLN: } A = 2\text{m}^2, T_2 = 20^\circ\text{C} = 293\text{K}, T_1 = 37^\circ\text{C} = 310\text{K}, \frac{B}{t} = P = ?, \epsilon = 0.97$

Now,

$$\begin{aligned} P &= A \cdot \epsilon \cdot e(T_1^4 - T_2^4) \\ &= 2 \times 0.97 \times 5.67 \times 10^{-8} \times [(310)^4 - (293)^4] \\ &= 1.0864 \times 10^{-8} [1885159190] \\ \Rightarrow P &= 205.16 \text{ Watt.} \end{aligned}$$

Hence, rate of heat loss is 205.16 Watt. #

Q.2 [H] What is the ratio of the energy per second radiated by the filament of a lamp at  $2500\text{K}$  to that radiated at  $2000\text{K}$ , assuming the filament is a black body radiator?

$\star \text{SOLN: } T_1 = 2500\text{K}, T_2 = 2000\text{K}, P_1 : P_2 = ?$

Now,  $P_1 = A \epsilon (T_1)^4$  &  $P_2 = A \epsilon (T_2)^4$

Here,  $P_1 : P_2 = \frac{P_1}{P_2}$

$$\text{or, } \frac{A \epsilon (T_1)^4}{A \epsilon (T_2)^4} = \frac{T_1^4}{T_2^4} = \frac{25^4 \times 100^4}{20^4 \times 100^4} = \left(\frac{5 \times 8}{5 \times 4}\right)^4 = \frac{2.44}{1}.$$

∴ ratio of energy per second is (2.44:1) #