


# Graph Algorithms

CS3104

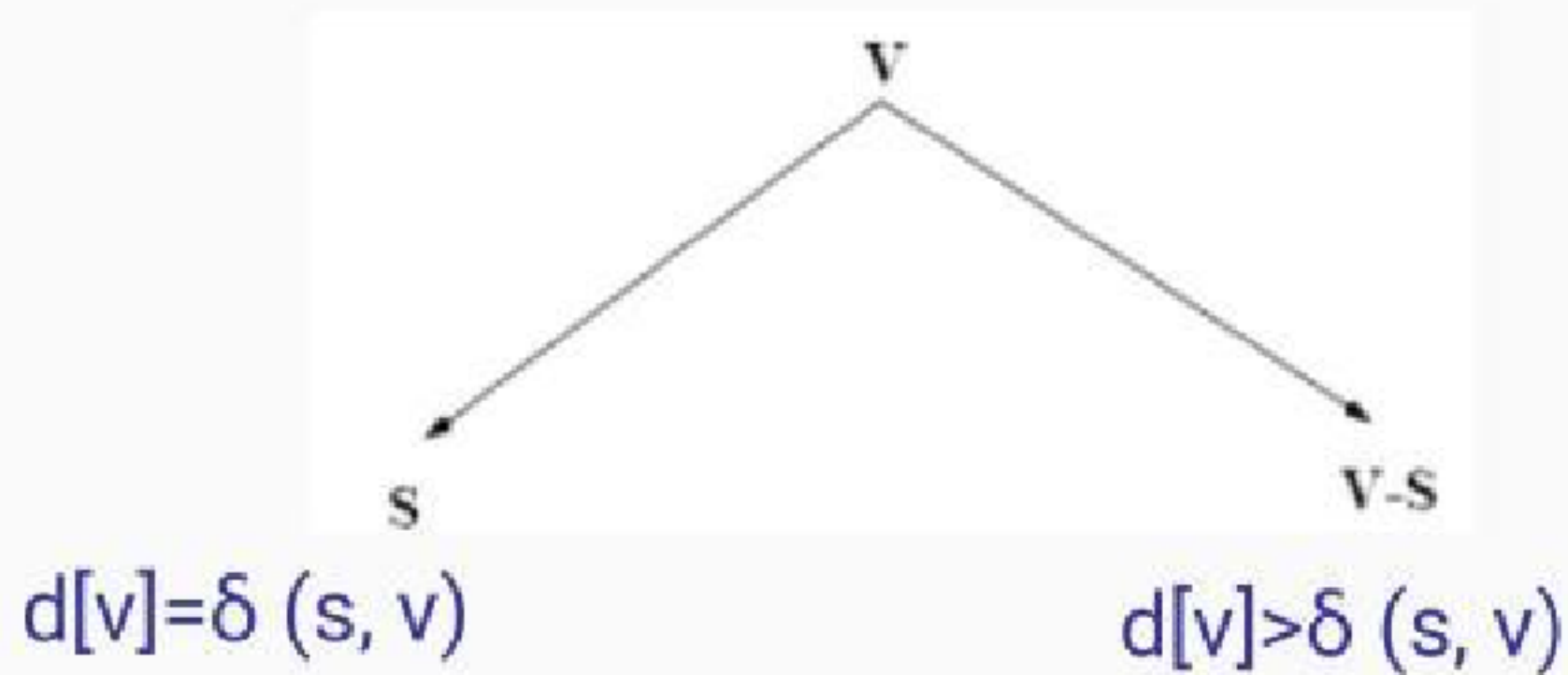
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# Dijkstra's Algorithm

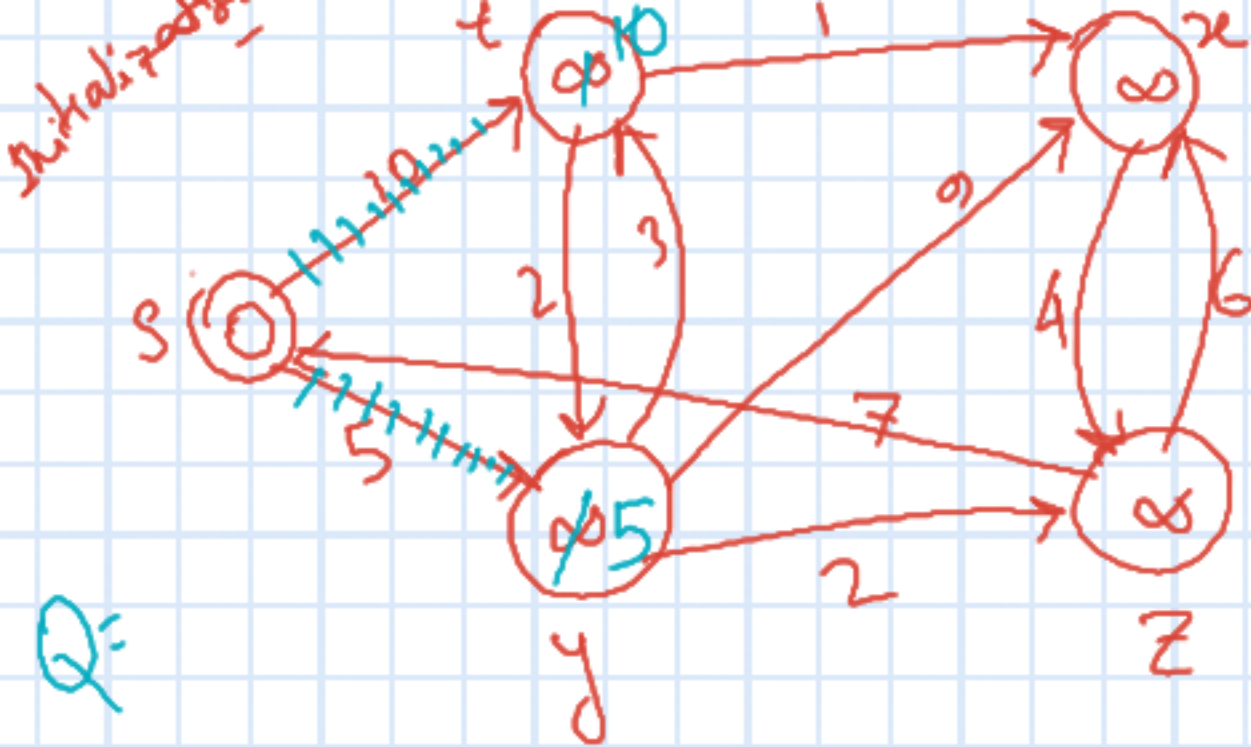
- Single-source shortest path problem:
  - No negative-weight edges:  $w(u, v) > 0, \forall (u, v) \in E$
- Each edge is relaxed **only once!**
- Maintains two sets of vertices:



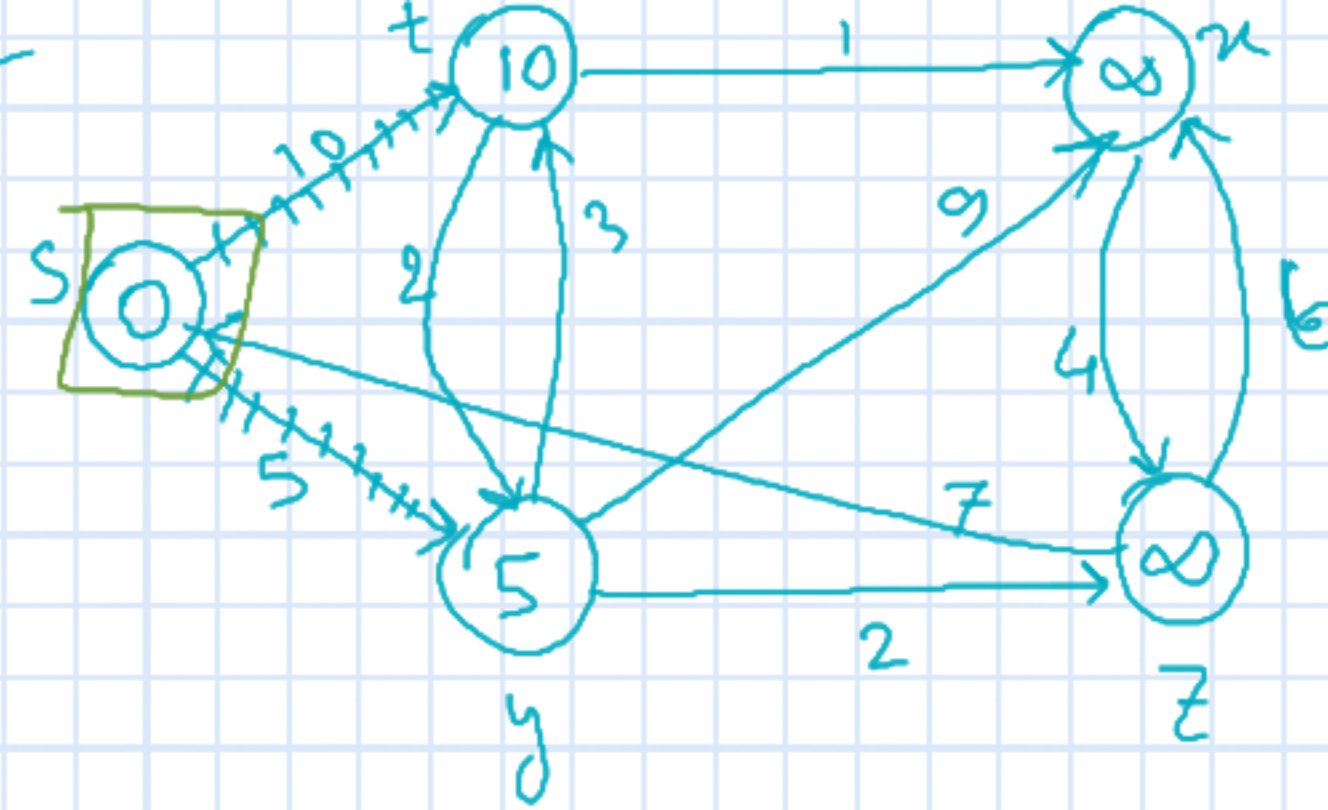
# Dijkstra's Algorithm

```
1.  INITIALIZE-SINGLE-SOURCE(V, s)
2.   $S \leftarrow \emptyset$ 
3.   $Q \leftarrow V[G]$ 
4.  while  $Q \neq \emptyset$ 
5.      do  $u \leftarrow \text{EXTRACT-MIN}(Q)$ 
6.       $S \leftarrow S \cup \{u\}$ 
7.      for each vertex  $v \in \text{Adj}[u]$ 
8.          do  $\text{RELAX}(u, v, w)$ 
9.          Update  $Q$  ( $\text{DECREASE\_KEY}$ )
```





Part 1



$S = \{s\}$   
 $Q = \{t, y, z\}$