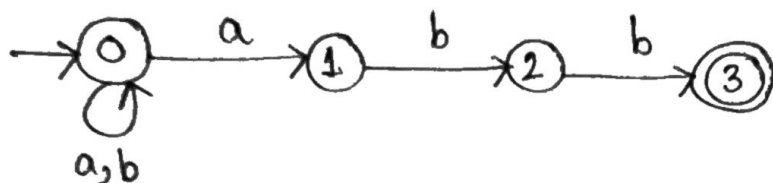
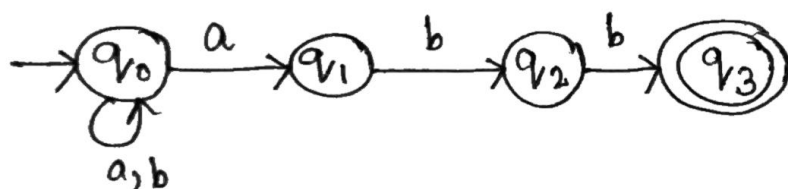


Topic Assignment → 431/01/2023Prayas MazumderEnrollment : 2021C3B071

1. Below is a NFA over the language  $\{a, b\}$



for sake of convenience, I'm newriting the NFA as:



The language accepted by the above NFA is  $L_1$  (say)

Suppose the above NFA is described by  $N$ .

$N = \{Q, \Sigma, \delta, q_0, F\}$ , where,  $Q = \{q_0, q_1, q_2, q_3\}$ ,  $\Sigma = \{a, b\}$ ,

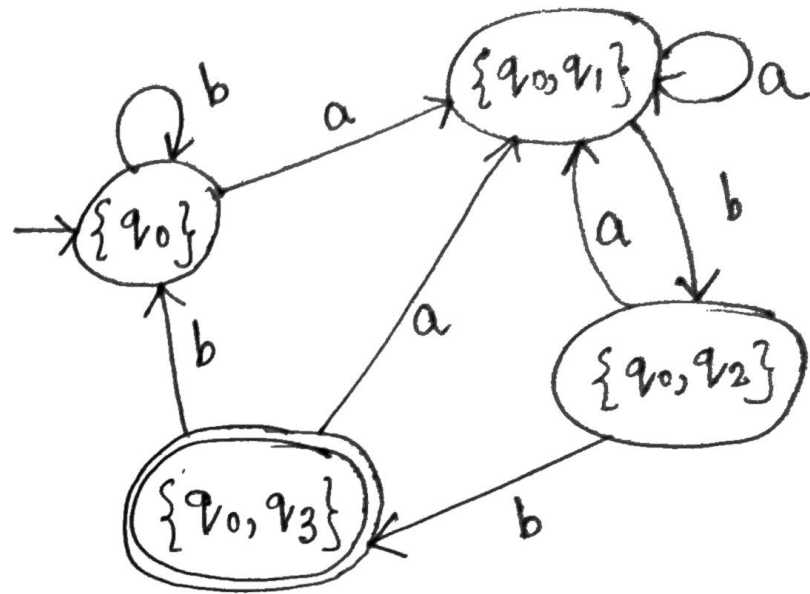
$q_0 \rightarrow$  initial state,  $F = \{q_3\}$ ,  $\delta: Q \times \Sigma \rightarrow P(Q)$ .

$L_1(N) = \{w \in \{a, b\}^* : \text{the lastmost substring of length 3 is 'abb'}$

or, last 3 symbols of string  $w$  is  
 $\{ 'a', 'b' \text{ and } 'b' \}$ .

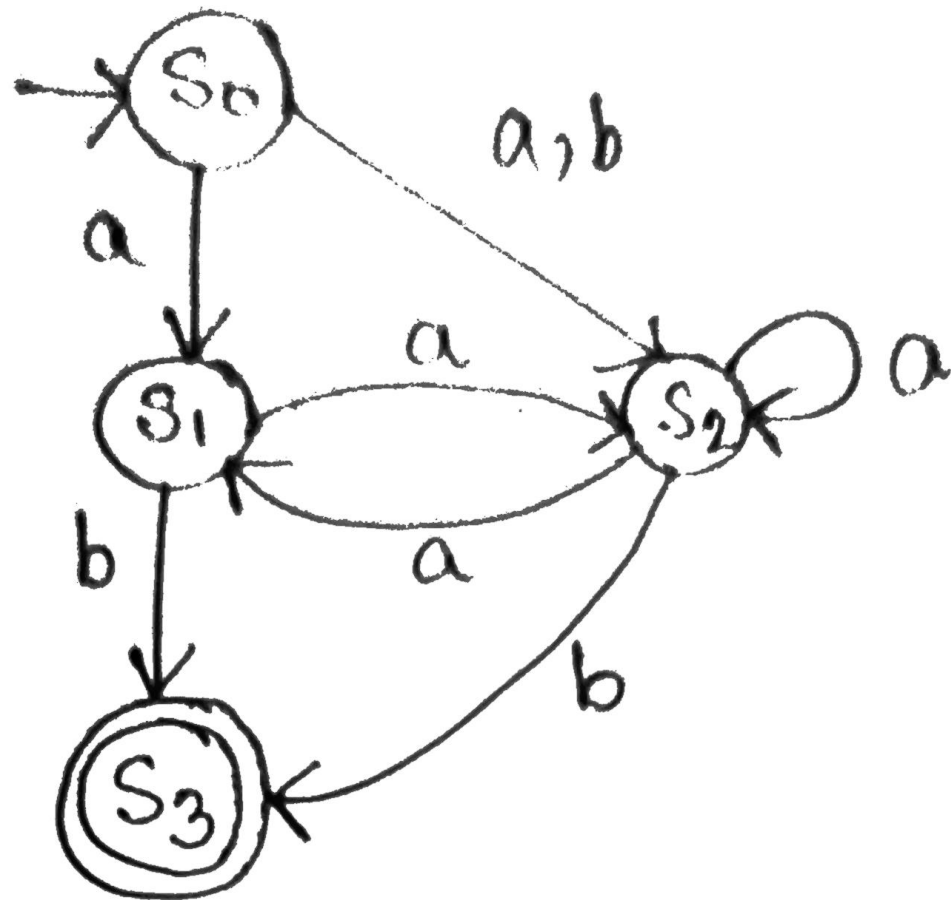
| State                 | Symbols        |                |
|-----------------------|----------------|----------------|
|                       | a              | b              |
| $\rightarrow \{q_0\}$ | $\{q_0, q_1\}$ | $\{q_0\}$      |
| $\{q_0, q_1\}$        | $\{q_0, q_1\}$ | $\{q_0, q_2\}$ |
| $\{q_0, q_2\}$        | $\{q_0, q_1\}$ | $\{q_0, q_3\}$ |
| $\{q_0, q_3\}$        | $\{q_0, q_1\}$ | $\{q_0\}$      |
| final                 |                |                |

State transition table  
for the DFA.



Converted DFA from NFA N

2.



The language accepted by the above NFA  $N_1$  is  $L_2$  (say). Where,  $N_1 = \{Q, \Sigma, q_0, F, \delta\}$

$Q = \{s_0, s_1, s_2, s_3\}$ ,  $\Sigma = \{a, b\}$ ,  $q_0 = s_0$  (initial state),  $F = \{s_3\}$

$\delta: (Q \times \Sigma) \rightarrow P(Q)$ .

Language  $L_2(N_1) = \{w \in \Sigma^* : w = a^m b \text{ or } w = b a^n b, \text{ where } n \in \mathbb{I}, m \in \mathbb{I}^+ \}$   
( $n = 0, 1, 2, \dots$ ) ( $m = 1, 2, 3, \dots$ ).

| State                 | Symbol         |             |
|-----------------------|----------------|-------------|
|                       | a              | b           |
| $\rightarrow \{s_0\}$ | $\{s_1, s_2\}$ | $\{s_2\}$   |
| $\{s_2\}$             | $\{s_1, s_2\}$ | $\{s_3\}$   |
| $\{s_1, s_2\}$        | $\{s_1, s_2\}$ | $\{s_3\}$   |
| $\{s_3\}$             | $\emptyset$    | $\emptyset$ |

So, the DFA of the NFA would be :

