

# Assignment 3: Trajectory Optimization in Joint Space

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## Objective

The objective of this assignment is to introduce trajectory optimization by computing joint-space trajectories that are not only smooth, but also optimal with respect to a chosen performance criterion. Students will learn how to formulate an optimization problem and solve it numerically to generate improved robot motion.

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## Problem Description

Consider the same 2-link planar robotic arm used in previous assignments. The robot must move from an initial joint configuration ( $q1\_start$ ,  $q2\_start$ ) to a final joint configuration ( $q1\_end$ ,  $q2\_end$ ) over a fixed time duration  $T$ .

Instead of manually designing the trajectory, you will now compute the trajectory by solving an optimization problem that minimizes a specified cost function while satisfying boundary conditions.

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## Trajectory Parameterization

Discretize the time interval from 0 to  $T$  into  $N$  equally spaced time steps. At each time step, the joint angles  $q1$  and  $q2$  are treated as decision variables.

The trajectory is defined as the sequence of joint angles over time.

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## Cost Function

Choose one of the following cost functions:

- Minimize the sum of squared joint velocities (energy-efficient motion)
- Minimize the sum of squared joint accelerations (smooth motion)

You may optionally experiment with a weighted combination of both.

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## Constraints

The optimization must satisfy:

- The initial joint angles equal the specified start configuration
  - The final joint angles equal the specified end configuration
  - (Optional) Joint angle limits
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## Expected Work

Students are expected to:

- Formulate the trajectory optimization problem
  - Solve it using a numerical optimization method (such as SciPy's minimize)
  - Generate optimized joint trajectories
  - Compare optimized trajectories with the polynomial trajectories from Assignment 2
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## Comparison and Analysis

Students must compare:

- Joint angle profiles
- Smoothness of motion
- Cost values before and after optimization

A brief discussion should explain how optimization improves trajectory quality.

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## Submission Requirements

Each submission must include:

- Python code implementing trajectory optimization
- Plots of optimized joint trajectories
- Comparison plots with polynomial trajectories
- A short written discussion (6–8 sentences)

**Deadline - 2nd January, 2026, for submission follow the same instructions as for Assignment 2**