Imrob Documentation

Release 20180828

CONTENTS:

1	System Requirements	3
2	Installation 2.1 Issues	5 5
3	Testing the code 3.1 Unitary Test	7 7 8
4	Componet Description 4.1 lmrob 4.2 utils	11 11 19
5	Indices and tables	23
Рy	ython Module Index	25

The lmrob package is a translation of the lmrob functions of the robustbase package of R code. The included functions are the following:

- lmrob
- lmrob_control
- lmrob_fit
- lmrob_S
- lmrob_D_fit
- lmrob_M_fit
- lmrob_M_S
- lmrob_lar

CONTENTS: 1

2 CONTENTS:

ONE

SYSTEM REQUIREMENTS

Additional to the repository the following packages must be in the system before installing the package.

- lapack
- blas
- R

TWO

INSTALLATION

Installing the required packages

```
$ sudo apt install r-base -y
```

Install a virtualenv

sudo apt install virtualenv

Create virtualev

\$ virtualenv -p python3 /path/to/env

Activate the virtualenv

\$ source /path/to/env/bin/activate

Installing lmrob

(env) \$ python setup.py install_lib

2.1 Issues

The following compilers must be installed in the system:

- gcc
- gfortran

If the Python.h is not found install python-devel to the system

THREE

TESTING THE CODE

There are two kinds of test, unitary an advanced tests. To try the unitary test do the following steps

3.1 Unitary Test

1. Move to tests directory

```
(env) $ cd tests/unittest
```

2. Try all the tests

```
(env) $ python -m unittest test_lmrob -v
```

and you should get a the following

```
test_lm_fit (test_lmrob.LmrobTestCase) ... ok
test_lmrob (test_lmrob.LmrobTestCase) ... ok
test_lmrob_D_fit (test_lmrob.LmrobTestCase) ... ok
test_lmrob_M_S (test_lmrob.LmrobTestCase) ... ok
test_lmrob_M_fit (test_lmrob.LmrobTestCase) ... ok
test_lmrob_S (test_lmrob.LmrobTestCase) ... ok
test_lmrob_categorical (test_lmrob.LmrobTestCase) ... ok
test_lmrob_categorical_offset (test_lmrob.LmrobTestCase) ... ok
test_lmrob_categorical_offset_weights (test_lmrob.LmrobTestCase) ... ok
test_lmrob_categorical_weights (test_lmrob.LmrobTestCase) ... ok
test_lmrob_fit (test_lmrob.LmrobTestCase) ... ok
test_lmrob_lar (test_lmrob.LmrobTestCase) ... ok
test_lmrob_offset (test_lmrob.LmrobTestCase) ... ok
test_lmrob_offset_weights (test_lmrob.LmrobTestCase) ... ok
test_lmrob_tau (test_lmrob.LmrobTestCase) ... ok
test_lmrob_weights (test_lmrob.LmrobTestCase) ... ok
test_ghq (test_lmrob.LmrobUtilities) ... ok
test_lmrob_hat (test_lmrob.LmrobUtilities) ... ok
test_lmrob_kappa (test_lmrob.LmrobUtilities) ... ok
test_lmrob_rweights (test_lmrob.LmrobUtilities) ... ok
test_mchi (test_lmrob.LmrobUtilities) ... ok
test_mpsi (test_lmrob.LmrobUtilities) ... ok
test_mwqt (test_lmrob.LmrobUtilities) ... ok
```

3.2 Advanced Test

1. Move to tests directory

```
(env) $ cd tests/advancedtest/
```

2. Try all the tests

```
(env) $ cd tests/advancedtest/
```

3. Run the following command

```
(env) $ ./test_lmrob.sh
```

4. Getting something like that

```
METHOD: S
+----+
| R Coefficients | Python Coefficients | Diff
   -36.92541589 |
                    -36.92541690 | 1.00995e-06 |
    0.84957481 |
                       0.84957481 | 1.51956e-10 |
                       0.43047399 | 1.38134e-08 |
    0.43047400 |
    -0.07353895 | -0.07353894 | 1.51891e-08 |
 R residuals | Python residuals | Diff
     5.88160019 | 5.88160023 | 3.48700e-08 |
     0.80806118 |
                       0.80806125 | 6.27125e-08 |
    6.06396134 |
                       6.06396129 | 4.22755e-08 |
                       8.31829086 | 1.93947e-08 |
    8.31829084 |
                       -0.82076109 | 3.12389e-08 |
    -0.82076106 |
    -1.25123511 |
                      -1.25123512 | 5.92210e-09 |
    -0.24047511 |
                       -0.24047525 | 1.47660e-07 |
    0.75952489 |
                       0.75952475 | 1.47660e-07 |
    -0.85293589 |
                      -0.85293589 | 4.85767e-09 |
                       -0.21533863 | 6.34561e-08 |
    -0.21533869 |
                       0.44651220 | 1.87127e-07 |
    0.44651239 |
    -0.19655257 |
                       -0.19655275 | 1.84601e-07 |
    -3.06826068 |
                       -3.06826067 | 7.77104e-09 |
    -1.68980562 |
                       -1.68980590 | 2.73180e-07 |
     1.24311084 |
                       1.24311065 | 1.84998e-07 |
    0.02249381 |
                       0.02249371 | 1.01470e-07 |
    -0.43752638 |
                      -0.43752606 | 3.13642e-07 |
                       0.07724681 | 1.18744e-07 |
    0.07724669 |
    0.72031165 |
                       0.72031176 | 1.16218e-07 |
    1.76994083 |
                       1.76994089 | 5.89368e-08 |
                       -9.46225556 | 1.95371e-07 |
METHOD: MM
| R Coefficients | Python Coefficients | Diff
   0.93884534 | 0.93884535 | 9.05454e-09 | 0.57955324 | 0.57955314 | 1.0000
                      -41.52461530 | 1.35669e-06 |
   -41.52461665 |
```

(continues on next page)

(continued from previous page)

				(continued from previous page)
	-0.11292183	-0.11292182	7.40542e-10	
R	residuals	•	Diff	
	2.81909429	+ 2.81909491	+	
	-2.29382753			•
		-2.29302091	0.19331e-07	
	3.78534931		4.58453e-07	
	7.23112652		4./5948e-0/	
	-1.60976700			
	-2.18932024	-2.18931987	3.73513e-07	
	-1.09134253	-1.09134206	4.71505e-07	
	-0.09134253	-0.09134206	4.71505e-07	
	-1.43393887	-1.43393846	4.09731e-07	
	-0.32662546	-0.32662556	9.72605e-08	
	0.68967097	0.68967087	1.03925e-07	
	0.15630238	0.15630218	2.05620e-07	
	-3.10078181	-3.10078191	9.87416e-08	
	-1.43819497	-1.43819497	4.45245e-09	I
	2.20043371			
	0.86166823		2.92674e-08	
	-0.29879056		8.35353e-08	
	0.49166222			
	1.02503080	1.02503098		
		•		•
	1.61780240	-10.50973598		
		+	+	F
ЕТНС	DD: SMD			
		+ Python Coefficients		+
R C	Coefficients	Python Coefficients	Diff +	+ -
R C	Coefficients 	Python Coefficients 	Diff +	
R C	Coefficients 	Python Coefficients 	Diff + 1.20792e-13 7.77156e-16	
R C	Coefficients 	Python Coefficients 	Diff 	
R C	Coefficients 	Python Coefficients 	Diff +	
R C	-41.76557868 0.91122641 0.66967312 -0.11296643 residuals	Python Coefficients 	Diff 	
R C	Coefficients 	Python Coefficients 	Diff 	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 Python residuals 2.84030349 -2.27266294	Diff	
R C	Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 Python residuals 2.84030349 -2.27266294 3.84874822	Diff	
R C	Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 residuals -2.84030349 -2.27266294 3.84874822 7.02546544	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals 2.84030349 -2.27266294 3.84874822 7.02546544	Diff	
R C	-41.76557868 0.91122641 0.66967312 -0.11296643 	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals 2.84030349 -2.27266294 3.84874822 7.02546544 -1.63518832	Diff	
R C	Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals 2.84030349 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 -2.27266294 2.84030349 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 -2.27266294 2.84030349 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -1.65995579	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals 2.84030349 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals 2.84030349 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519 0.91434267	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals 2.84030349 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519 0.91434267	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519 0.91434267 0.47104936	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals Python residuals -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519 0.91434267 0.47104936 -2.87642233	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519 0.91434267 0.47104936 -2.87642233	Diff 	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals Python residuals -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519 0.91434267 0.47104936 -2.87642233 -2.87642233 -1.30346474 2.20415398	Diff	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals Python residuals -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.29673599 -0.10235519 0.91434267 0.47104936 -2.87642233 -2.30346474 2.20415398 0.86525469	Diff 	
R C	Coefficients	Python Coefficients -41.76557868 0.91122641 0.66967312 -0.11296643 -0.11296643 Python residuals Python residuals -2.27266294 3.84874822 7.02546544 -1.63518832 -2.30486144 -1.29673599 -0.29673599 -0.10235519 0.91434267 0.47104936 -2.87642233 -1.30346474 2.20415398 0.86525469 -0.38594843	Diff 	

(continues on next page)

3.2. Advanced Test 9

(continued from previous page)

			(continued from previous page
1.60668426		1.04361e-14	
-10.13378768	-10.13378768	1.77636e-15	
	+	++	
METHOD: SMDM			
	+	++	
R Coefficients	Python Coefficients	Diff	
-41.68557185	-41.68557188	 3.71171e-08	
0.83626010	0.83626010		
0.93445082	0.93445081		
-0.12585903	-0.12585903		
	+	++	
R residuals	Python residuals	Diff	
2.75604537	+ l 2.75604536	++ 7.84833e-09	
-2.36981366	-2.36981367		
3.93210653	'	1.34059e-08	
6.36036156		2.52814e-08	
-1.77073681	-1.77073681		
-2.70518763	-2.70518761		
-1.88448427	-1.88448425		
-0.88448427	-0.88448425	2.09719e-08	
-2.36014723	-2.36014720	1 2.84264e-08 I	
0.43109366	0.43109363	2.50160e-08	
1.56382492	1.56382489	3.14803e-08	
1.37241671	1.37241667	4.24561e-08	
-2.31718828	-2.31718831	2.64525e-08	
-0.86718978	-0.86718981	2.26593e-08	
2.25390572	2.25390571		
0.87632863	0.87632863	3.52415e-10	
-0.82014859	-0.82014857	2.21021e-08	
0.06086461	0.06086463	1.70742e-08	
0.25227282	0.25227285	2.80500e-08	
1.48643028	1.48643029	4.35506e-09	
		5.40456e-08	

COMPONET DESCRIPTION

4.1 Imrob

4.1.1 Imrob

Parameters

formula [str] A symbolic description of the model to be fit.

data [dict] An optional data frame, dict containing the variables in the model.

subset: array_like An optional vector specifying a subset of observations to be used in the fitting process.

weights: array_like An optional vector of weights to be used in the fitting process (in addition to the robustness weights computed in the fitting process).

na_action: str A function which indicates what should happen when the data contain nan. The default is set by the na_action setting of options, and is na_fail if that is unset. The "factory-fresh" default is na_omit. Another possible value is NULL, no action. Value na_exclude can be useful.

method: str string specifying the estimator-chain. "MM" is interpreted as SM. See Notes, notably the currently recommended setting = "KS2014".

model, return_x, return_y: bool. If TRUE the corresponding components of the fit (the model frame, the model matrix, the response) are returned.

singular_ok: bool If FALSE (the default in S but not in R) a singular fit is an error.

contrasts: dict An optional list. See the contrasts.arg of model.matrix.default.

offset: array_like This can be used to specify an a priori known component to be included in the linear predictor during fitting. An offset term can be included in the formula instead or as well, and if both are specified their sum is used.

control: object Instances of class LmrobControl.

init: dict An optional argument to specify or supply the initial estimate. See Notes.

kwargs: additional arguments can be used to specify control parameters directly instead of (but not in addition to!) via control.

Returns

```
coefficients: array_like The estimate of the coefficient vector scale: The scale as used in the M estimator.

residuals: array_like Residuals associated with the estimator.

converged: bool TRUE if the IRWLS iterations have converged.

iter: int Number of IRWLS iterations

rweights: array_like The "robustness weights" \psi(r i / S)/(r i / S).

fitted_values: array_like Fitted values associated with the estimator.

init: dict A similar dict that contains the results of intermediate estimates.

rank: int the numeric rank of the fitted linear model.
```

See also:

```
LmrobControl, lmrob_S, lmrob_M_S, lmrob_fit
```

Notes

Overview: This function computes an MM-type regression estimator as described in Yohai (1987) and Koller and Stahel (2011). By default it uses a bi-square redescending score function, and it returns a highly robust and highly efficient estimator (with 50% breakdown point and 95% asymptotic efficiency for normal errors). The computation is carried out by a call to lmrob.fit(). The argument setting of lmrob.control is provided to set alternative defaults as suggested in Koller and Stahel (2011) (setting="KS2011"; now do use its extension setting="KS2014"). For further details, see lmrob_control.

Initial Estimator init: The initial estimator may be specified using the argument init. This can either be a string, a function or a list. A string can be used to specify built in internal estimators (currently S and M-S, see See also below). A function taking arguments x, y, control, mf (where mf stands for model.frame) and returning a list containing at least the initial coefficients as coefficients and the initial scale estimate scale. Or a list giving the initial coefficients and scale as coefficients and scale. See also Examples. Note that if the init argument is a function or list, the method argument must not contain the initial estimator, e.g., use MDM instead of SMDM. The default, equivalent to init = "S", uses as initial estimator an S-estimator (Rousseeuw and Yohai, 1984) which is computed using the Fast-S algorithm of Salibian-Barrera and Yohai (2006), calling lmrob.S(). That function, since March 2012, by default uses nonsingular subsampling which makes the Fast-S algorithm feasible for categorical data as well, see Koller (2012). Note that convergence problems may still show up as warnings, e.g.,S refinements did not converge (to refine.tol=1e-07) in 200 (= k.max) steps and often can simply be remedied by increasing (i.e. weakening) refine.tol or increasing the allowed number of iterations k.max, see lmrob.control.

Examples

(continues on next page)

(continued from previous page)

```
"stack_loss" : rpyn.ri2py(stackloss.rx2("stack.loss"))
... }
>>> formula = 'stack_loss ~ AirFlow + WaterTemp + AcidConc'
>>> # S Method
>>> m0 = lmrob(formula, data=data, method="S")
```

lmrob.lmrob_fit (x, y, control, init)

Compute MM-type estimators of regression: An S-estimator is used as starting value, and an M- estimator with fixed scale and redescending psi-function is used from there. Optionally a D-step (Design Adaptive Scale estimate) as well as a second M-step is calculated. Returns a dictionary object.

Parameters

```
x: array_like design matrix (n × p) typically including a column of 1s for the intercept.
y: array_like numeric response vector (of length n).
control: object An instance of the LmrobControl Class
init: dict Optional list of initial estimates. See Notes.
```

Returns

```
residuals: array_like Xβ, i.e., X.dot (coefficients)
residuals: array_like the raw residuals, y - fitted_values
rweights: array_like robustness weights derived from the final M-estimator residuals (even when not converged).
rank: int degree_freedom n - rank
coefficients: array_like estimated regression coefficient vector.
scale: float the robustly estimated error standard deviation
cov: array_like variance-covariance matrix of coefficients, if the RWLS iterations have converged (and control.cov is not "none").
control: object
iter: int
converged: bool boolean indicating if the RWLS iterations have converged.
init: dict A similar dict that contains the results of intermediate estimates (not for MM- estimates).
```

See also:

```
lmrob, lmrob_M_fit, lmrob_D_fit, lmrob_S
```

Notes

This function is the basic fitting function for MM-type estimation, called by lmrob and typically not to be used on its own. If given, init must be a list of initial estimates containing at least the initial coefficients and scale as coefficients and scale. Otherwise it calls $lmrob_S(...)$ and uses it as initial estimator.

4.1. Imrob 13

Examples

```
>>> from lmrob import *
>>> from rpy2.robjects.packages import importr
>>> from rpy2.robjects import pandas2ri, r
>>> import rpy2.robjects.numpy2ri as rpyn
```

```
>>> stackloss = r("stackloss")
>>> data = {"AirFlow": rpyn.ri2py(stackloss.rx2("Air.Flow")),
            "WaterTemp": rpyn.ri2py(stackloss.rx2("Water.Temp")),
            "AcidConc": rpyn.ri2py(stackloss.rx2("Acid.Conc.")),
            "stack_loss": rpyn.ri2py(stackloss.rx2("stack.loss"))
. . .
          }
>>> formula = 'stack_loss ~ AirFlow + WaterTemp + AcidConc'
>>> Y, X = patsy.dmatrices(formula, data, NA_action="drop",
                           return_type='matrix')
>>> control = LmrobControl()
>>> m0 = lmrob_fit(X, Y, control=control, init=None)
>>> coefficients = m0.get("coefficients")
>>> residuals = m0.get("residuals")
>>> scale = m0.get("scale")
>>> converged = m0.get("converged")
```

 $lmrob.lmrob_S(x_, y_, control, only_scale=False)$

Computes an S-estimator for linear regression, using the "fast S" algorithm and returns a dictionary object.

Parameters

```
x_: array_like Design matrix (n × p)
y_: array_like Numeric vector of responses (or residuals for only_scale=TRUE).
control: object Instances of class LmrobControl.
```

only_scale: bool Boolean indicating if only the scale of y should be computed. In this case, y will typically contain residuals.

Returns

```
coefficients: array_like
```

numeric vector (length p) of S-regression coefficient estimates.

scale: float The S-scale residual estimate

fitted_values: array_like numeric vector (length n) of the fitted values.

residuals: array like numeric vector (length n) of the residuals.

rweights: array_like numeric vector (length n) of the robustness weights.

k_iter: int (maximal) number of refinement iterations used.

converged: bool boolean indicating if all refinement iterations had converged.

control: object the same object as the control argument.

Notes

This function is used by lmrob_fit and typically not to be used on its own (because an S-estimator has too low efficiency 'on its own'). By default, the subsampling algorithm uses a customized LU decomposition which

ensures a non singular subsample (if this is at all possible). This makes the Fast-S algorithm also feasible for categorical and mixed continuous-categorical data. One can revert to the old subsampling scheme by setting the parameter subsampling in control to "simple".

Examples

```
>>> from lmrob import *
>>> from rpy2.robjects.packages import importr
>>> from rpy2.robjects import pandas2ri, r
>>> import rpy2.robjects.numpy2ri as rpyn
>>> stackloss = r("stackloss")
>>> data = {"AirFlow" : rpyn.ri2py(stackloss.rx2("Air.Flow")),
            "WaterTemp" : rpyn.ri2py(stackloss.rx2("Water.Temp")),
            "AcidConc" : rpyn.ri2py(stackloss.rx2("Acid.Conc.")),
            "stack_loss" : rpyn.ri2py(stackloss.rx2("stack.loss"))
. . .
         }
. . .
>>> formula = 'stack_loss ~ AirFlow + WaterTemp + AcidConc'
>>> Y, X = patsy.dmatrices(formula, data, NA_action="drop", return_type='matrix')
>>> control = LmrobControl()
>>> m0 = lmrob_S(X, Y, control)
>>> coefficients = m0.get("coefficients")
>>> residuals = m0.get("residuals")
>>> scale = m0.get("scale")
>>> converged = m0.get("converged")
>>> k_iter = m0.get("k_iter")
>>> fitted_values = m0.get("fitted_values")
>>> rweights = m0.get("rweights")
```

$lmrob.lmrob_M_S(x, y, control, mf)$

Computes an M-S-estimator for linear regression using the "M-S" algorithm.

Parameters

```
x: array_like Design matrix (n × p)
y: array_like Numeric vector of responses (or residuals for only_scale=TRUE).
control: object Instances of class LmrobControl.
mf: array_like a model matrix as returned by model_frame.
Returns
coefficients: array_like Numeric vector (length p) of M-S-regression coefficient estimates.
scale: float The M-S-scale residual estimate
residuals: array_like numeric vector (legnth n) of the residuals.
rweights: array_like numeric vector (length n) of the robustness weights.
control: object the same as the control argument.
converged: bool Convergence status (always TRUE), needed for lmrob.fit.
```

See also:

lmrob

4.1. Imrob 15

Notes

This function is used by Imrob and not intended to be used on its own (because an M-S-estimator has too low efficiency 'on its own'). An M-S estimator is a combination of an S-estimator for the continuous variables and an L1- estimator (i.e. an M-estimator with $\psi(t) = \text{sign}(t)$) for the categorical variables. The S-estimator is estimated using a subsampling algorithm. If the model includes interactions between categorical (factor) and continuous variables, the subsampling algorithm might fail. In this case, one can choose to assign the interaction to the categorical side of variables rather than to the continuous side.

Note that the return status converged does not refer to the actual convergence status. The algorithm used does not guarantee convergence and thus true convergence is almost never reached. This is, however, not a problem if the estimate is only used as initial estimate part of an MM or SMDM estimate.

The algorithm sometimes produces the warning message "Skipping design matrix equilibration (dgeequ): row ?? is exactly zero.". This is just an artifact of the algorithm and can be ignored safely.

Examples

```
>>> from lmrob import *
>>> from rpy2.robjects.packages import importr
>>> from rpy2.robjects import pandas2ri, r
>>> import rpy2.robjects.numpy2ri as rpyn
>>>
>>> stackloss = r("stackloss")
>>> data = {"AirFlow" : rpyn.ri2py(stackloss.rx2("Air.Flow")),
            "WaterTemp" : rpyn.ri2py(stackloss.rx2("Water.Temp")),
            "AcidConc" : rpyn.ri2py(stackloss.rx2("Acid.Conc.")),
. . .
            "stack_loss" : rpyn.ri2py(stackloss.rx2("stack.loss"))
         }
>>> formula = 'stack_loss ~ AirFlow + WaterTemp + AcidConc'
>>> mf_dict = model_frame(formula, data, None, [], 'drop', [])
>>> Y, X = patsy.dmatrices(formula, data, NA_action="drop", return_type='matrix')
>>> control = LmrobControl()
>>> m0 = lmrob M S(X, Y, control, mf dict)
>>> coefficients = m0.get("coefficients")
>>> residuals = m0.get("residuals")
>>> scale = m0.get("scale")
```

lmrob.lmrob__D__fit (obj, x=array([], dtype=float64), control=None, method=None)

This function calculates a Design Adaptive Scale estimate for a given MM-estimate. This is sup- posed to be a part of a chain of estimates like SMD or SMDM. Returns a dictionart object

Parameters

```
obj: dict based on which the estimate is to be calculated.
x: array_like The design matrix; if missing, the method tries to get it from obj.get ("x").
control: object Instances of class LmrobControl.
method: str (optional) the method used for obj computation.
```

Returns

```
scale: float The Design Adaptive Scale estimateconverged: bool TRUE if the scale calculation converged, FALSE other.
```

See also:

```
lmrob fit, lmrob
```

Notes

This function is used by <code>lmrob_fit</code> and typically not to be used on its own. Note that <code>lmrob_fit()</code> specifies control potentially differently than the default, but does use the default for method.

Examples

```
>>> from lmrob import *
>>> from rpy2.robjects.packages import importr
>>> from rpy2.robjects import pandas2ri, r
>>> import rpy2.robjects.numpy2ri as rpyn
>>>
>>> stackloss = r("stackloss")
>>> data = {"AirFlow": rpyn.ri2py(stackloss.rx2("Air.Flow")),
            "WaterTemp": rpyn.ri2py(stackloss.rx2("Water.Temp")),
            "AcidConc": rpyn.ri2py(stackloss.rx2("Acid.Conc.")),
. . .
            "stack_loss": rpyn.ri2py(stackloss.rx2("stack.loss"))
         }
. . .
>>> formula = 'stack_loss ~ AirFlow + WaterTemp + AcidConc'
>>> Y, X = patsy.dmatrices(formula, data, NA_action="drop",
                           return_type='matrix')
>>> control = LmrobControl()
>>> init = lmrob_S(X, Y, control)
>>> m0 = lmrob_D_fit(init, X, control)
>>> # Getting the computed values
>>> converged_py = m0.get("converged")
>>> scale_py = m0.get("scale")
```

This function performs RWLS iterations to find an M-estimator of regression. When started from an S-estimated beta.initial, this results in an MM-estimator. Returns a dictionary

Parameters

```
x: array_like design matrix (n × p) typically including a column of 1s for the intercept.
y: array_like numeric response vector (of length n).
beta_initial: array_like numeric vector (of length p) of initial estimate. Usually the result of an S- regression estimator.
scale: float robust residual scale estimate. Usually an S-scale estimator.
control: object Instances of class LmrobControl.
obj: dict If specified, this is typically used to set values for the other arguments.
method: str (optional) the method used for obj computation.
```

Returns

```
coefficients: array_like the M-estimator (or MM-estim.) of regression
control: the control obj input used
scale: float The residual scale estimate
```

4.1. Imrob

converged: bool TRUE if the RWLS iterations converged, FALSE otherwise

See also:

```
lmrob_fit, lmrob
```

Notes

This function is used by lmrob_fit and typically not to be used on its own.

Examples

```
>>> from lmrob import *
>>> from rpy2.robjects.packages import importr
>>> from rpy2.robjects import pandas2ri, r
>>> import rpy2.robjects.numpy2ri as rpyn
>>>
>>> stackloss = r("stackloss")
>>> data = {"AirFlow": rpyn.ri2py(stackloss.rx2("Air.Flow")),
            "WaterTemp": rpyn.ri2py(stackloss.rx2("Water.Temp")),
            "AcidConc": rpyn.ri2py(stackloss.rx2("Acid.Conc.")),
. . .
            "stack_loss": rpyn.ri2py(stackloss.rx2("stack.loss"))
. . .
         }
>>> formula = 'stack_loss ~ AirFlow + WaterTemp + AcidConc'
>>> Y, X = patsy.dmatrices(formula, data, NA_action="drop",
                           return_type='matrix')
>>> control = LmrobControl()
>>> init = lmrob_S(X, Y, control)
>>> beta_inital = init.get("coefficients")
>>> scale = init.get("scale")
>>> m0 = lmrob M fit(X, Y, beta_inital, scale,
                       control, method="MM")
>>> # Getting the computed values
>>> coefficients = m0.get("coefficients")
>>> residuals = m0.get("residuals")
>>> scale = m0.get("scale")
>>> converged = m0.get("converged")
>>> iter = m0.get("iter")
```

$lmrob.lmrob_lar(x, y, control=None)$

Compute MM-type estimators of regression: An S-estimator is used as starting value, and an M- estimator with fixed scale and redescending psi-function is used from there. Optionally a D-step (Design Adaptive Scale estimate) as well as a second M-step is calculated. Usage. Return a dictionary object.

Parameters

```
x: array_like Design matrix (n × p)y: array_like Numeric vector of responses (or residuals for only_scale=TRUE).control: object Instances of class LmrobControl.
```

Returns

```
fitted_values: array_like X\beta, i.e., X.dot (coefficients).
residuals: array_like the raw residuals, y - fitted_values
```

```
rweights: array_like robustness weights derived from the final M-estimator residuals (even when not converged).
```

```
rank: int degree_freedom n - rank
```

coefficients: array_like estimated regression coefficient vector.

scale: float the robustly estimated error standard deviation.

control: object the same as the control argument.

iter: bool converged boolean indicating if the RWLS iterations have converged.

init: dict A similar dict that contains the results of intermediate estimates (not for MM- estimates).

See also:

```
lmrob, lmrob__M__fit, lmrob__D__fit, lmrob_S
```

Notes

This function is the basic fitting function for MM-type estimation, called by lmrob and typically not to be used on its own. If given, init must be a list of initial estimates containing at least the initial coefficients and scale as coefficients and scale. Otherwise it calls lmrob.S(..) and uses it as initial estimator.

Examples

```
>>> from lmrob import *
>>> from rpy2.robjects.packages import importr
>>> from rpy2.robjects import pandas2ri, r
>>> import rpy2.robjects.numpy2ri as rpyn
>>>
>>> stackloss = r("stackloss")
>>> data = {"AirFlow" : rpyn.ri2py(stackloss.rx2("Air.Flow")),
            "WaterTemp" : rpyn.ri2py(stackloss.rx2("Water.Temp")),
            "AcidConc" : rpyn.ri2py(stackloss.rx2("Acid.Conc.")),
. . .
            "stack_loss" : rpyn.ri2py(stackloss.rx2("stack.loss"))
. . .
>>> formula = 'stack_loss ~ AirFlow + WaterTemp + AcidConc'
>>> mf_dict = model_frame(formula, data, None, [], 'drop', [])
>>> Y, X = patsy.dmatrices(formula, data, NA_action="drop", return_type='matrix')
>>> control = LmrobControl()
>>> m0 = lmrob_lar(X, Y, control)
>>> coefficients = m0.get("coefficients")
>>> residuals = m0.get("residuals")
>>> scale = m0.get("scale")
```

4.2 utils

```
lmrob.utils.huberM(x, k=1.5, weights=None, tol=1e-06, mu=None, s=None, s=False, warnOscale=True) (Generalized) Huber M-estimator of location with MAD scale.
```

Example

4.2. utils 19

```
>>> module.huberM([1,2,4,5,6,8,10,12])
```

Parameters

- **x** (list) numeric vector.
- **k** (float) positive factor; the algorithm winsorizes at k standard deviations.
- weights (list) numeric vector of non-negative weights of same length as x, or None.
- tol (float) convergence tolerance.
- mu (float) initial location estimator.
- **s** (*float*) scale estimator held constant through the iterations.
- **se** (bool) logical indicating if the standard error should be computed and returned (as SE component). Currently only available when weights is None.
- warn0scale (bool) logical; if True, and s is 0 and len(x) > 1, this will be warned about.

Returns The tuple (mu, s, it, se) containing the location, scale parameters, number of iterations used and the se component.

Return type tuple

 $lmrob.utils.mad(x, center=None, constant=1.4826, na_rm=False, low=False, high=False)$

Compute the median absolute deviation, i.e., the (lo-/hi-) median of the absolute deviations from the median, and (by default) adjust by a factor for asymptotically normal consistency.

Example

```
>>> module.mad([1,2,4,5,6,8,10,12])
```

Parameters

- **x** (list) numeric vector.
- **center** (*float*) optionally, the centre: defaults to the median.
- **constant** (*float*) scale factor.
- na_rm (bool) if True then NaN values are stripped from x before computation takes place.
- **low** (bool) if True, compute the 'lo-median', i.e., for even sample size, do not average the two middle values, but take the smaller one.
- **high** (bool) if True, compute the 'hi-median', i.e., take the larger of the two middle values for even sample size.

Returns the median absolute deviation

Return type float

Raises ValueError

class lmrob.utils.psi_func (rho, psi, wgt, Dpsi, Dwgt, tDefs, Erho, Epsi2, EDpsi, name, xtras)

The class "psi_func" is used to store ψ (psi) functions for M-estimation. In particular, an object of the class contains $\rho(x)$ (rho), its derivative $\psi(x)$ (psi), the weight function $\psi(x)/x$, and rst derivative of ψ , Dpsi = ψ 0(x)

```
__init__ (rho, psi, wgt, Dpsi, Dwgt, tDefs, Erho, Epsi2, EDpsi, name, xtras)
Example of docstring on the __init__ method.
```

The __init__ method may be documented in either the class level docstring, or as a docstring on the __init__ method itself.

Either form is acceptable, but the two should not be mixed. Choose one convention to document the __init__ method and be consistent with it.

Note: Do not include the *self* parameter in the Args section.

Args: rho (function): the ρ () function. This is used to formulate the objective function; ρ () can be regarded as generalized negative log-likelihood. psi (function): ψ () is the derivative of ρ . wgt (function): The weight function $\psi(x)/x$. Dpsi (function): the derivative of ψ , Dpsi(x) = psi0(x). Dwgt (function): the derivative of the weight function. tDefs (list): named numeric vector oftuning parameterDefault values. Epsi2 (function): The function for computing $E[\psi 2(X)]$ when X is standard normal. EDpsi (function): The function for computing $E[\psi 0(X)]$ when X is standard normal. name (string): Name of ψ -function used for printing. xtras (string): Potentially further information.

```
lmrob.utils.sumU(x, weights)
```

Calculate weighted sum

Example

```
>>> module.sumU([1,2,4,5,6,8,10,12], [52,44,82,24,68,42,82,20])
```

Parameters

- **x** (list) numeric vector.
- weights (list) numeric vector of weights; of the same length as x.

Returns The weighted sum.

Return type float

Raises ValueError

lmrob.utils.tauHuber (x, mu, k=1.5, s=None, resid=None)

Calculate correction factor Tau for the variance of Huber-M-Estimators.

Example

```
>>> module.tauHuber([1,2,4,5,6,8,10,12])
```

Parameters

- **x** (list) numeric vector.
- **mu** (float) location estimator.
- **k** (float) tuning parameter of Huber Psi-function.
- \mathbf{s} (float) scale estimator held constant through the iterations.
- resid (float) the value of (x mu)/s.

Returns The correction factor Tau for the variance of Huber-M-Estimators.

Return type float

```
lmrob.utils.wgtHighMedian(x, weights=None)
```

Compute the weighted Hi-Median of x.

4.2. utils 21

Example

```
>>> module.wgtHighMedian([1,2,4,5,6,8,10,12])
```

Parameters

- **x** (list) numeric vector
- weights (list) numeric vector of weights; of the same length as x.

Returns The weighted Hi-Median of x.

Return type float

Raises ValueError

FIVE

INDICES AND TABLES

- genindex
- modindex

PYTHON MODULE INDEX

lmrob, 11
lmrob.utils, 19

26 Python Module Index

INDEX

Symbols __init__() (lmrob.utils.psi_func method), 20 Η huberM() (in module lmrob.utils), 19 lmrob (module), 11 lmrob() (in module lmrob), 11 lmrob.utils (module), 19 lmrob__D__fit() (in module lmrob), 16 lmrob_M_fit() (in module lmrob), 17 lmrob fit() (in module lmrob), 13 lmrob_lar() (in module lmrob), 18 lmrob_M_S() (in module lmrob), 15 lmrob_S() (in module lmrob), 14 M mad() (in module lmrob.utils), 20 psi_func (class in lmrob.utils), 20 sumU() (in module lmrob.utils), 21 tauHuber() (in module lmrob.utils), 21 W wgtHighMedian() (in module lmrob.utils), 21