

Template

```
/**
 *   @author      : Maruf Tuhin
 *   @School      : CUET CSE 11
 *   @Topcoder    : the_redback
 *   @CodeForces  : the_redback
 *   @UVA         : the_redback
 *   @link        : maruf.2hin@gmail.com
 */

//#include <bits/stdc++.h>

#include<cstdio>
#include<cstring>
#include<cstdlib>
#include<cctype>
#include<cmath>
#include<iostream>
#include<fstream>
#include<string>
#include<vector>
#include<queue>
#include<map>
#include<algorithm>
#include<set>
#include<sstream>
#include<stack>
using namespace std;

typedef long long          ll;
typedef unsigned long long llu;

#define ft      first
#define sd      second
#define mp      make_pair
#define pb(x)   push_back(x)
#define all(x)  x.begin(),x.end()
#define allr(x) x.rbegin(),x.rend()
#define mem(a,b) memset(a,b,sizeof(a))
#define meminf(a)
memset(a,126,sizeof(a))
#define inf     1e11
#define eps     1e-9
#define mod     1000000007
#define NN      30100

//cout << setfill('0') << setw(3) << a;
//cout << fixed << setprecision(20)<< a;

main()
{
    //ios_base::sync_with_stdio(0);
    //cin.tie(0);
}
```

Manually Sort

```
bool comp(char b,char c)
{
    if(tolower(b)==tolower(c))
        return b<c;
    //porer ta Capital hoile
    //swap kore age jabe.
    else
        return tolower(b)<tolower(c);
    //normal compare kore sort korebe.
}

/*
Input:
aAabB

Output:
AaaBb
*/
//bool false return korle sort hobe.
```

BigMod

```
// (m^n) %p;
long p;
long check(long m,long n)
{
    int sum;
    if(n==0)
        return 1;
    if(n%2==0)
    {
        sum=check(m,n/2);
        return ((sum%p)*(sum%p))%p;
    }
    else
    {
        sum=check(m,n-1);
        return ((m%p)*(sum%p))%p;
    }
}

int main()
{
    long m,n,sum;
    while(scanf("%ld %ld %ld",
                &m,&n,&p)==3)
    {
        sum=check(m,n);
        printf("%ld\n",sum);
    }
    return 0;
}
```

MST & Disjoint Set (Fast)

```

typedef long long ll;
#define inf 100000000
#define mem(a,b) memset(a,b,sizeof(a))
#define NN 10010
int root[NN+7];
int rank[NN+7];

struct edge {
    int u,v,w;
};

vector<edge>e;

bool comp(edge n,edge m) {
    return n.w>m.w;
}

void init(int n) {
    for(int i = 1; i <= n; i++) {
        root[i] = i;
        rank[i] = 0;
    }
}

int find(int u) {
    if(u != root[u])
        root[u] = find(root[u]);
    return root[u];
}

void Union(int u, int v) {
    if(rank[u] > rank[v])
        root[v] = u;
    else {
        root[u] = v;
        if(rank[u]==rank[v])
            rank[v]++;
    }
}

int mst(int n) {
    init(n);
    int i,j,k;
    sort(e.begin(),e.end(),comp);
    int count=0,sum=0;
    for(i=0; i<e.size(); i++) {
        int u=find(e[i].u);
        int v=find(e[i].v);
        if(u!=v) {
            Union(u,v);
        }
        else
            sum+=e[i].w;
    }
    return sum;
}

main()
{
    int i,j,k,l,n,r,c,u,v,w;

```

```

edge ed;
int tc,t=1,x=-1,m;
cin>>tc;
while(tc--)
{
    cin>>n>>m;
    while(m--)
    {
        cin>>ed.u>>ed.v>>ed.w;
        e.push_back(ed);
    }
    int sum=mst(n);
    cout<<sum<<"\n";
    e.clear();
}
cin>>n;

return 0;
}

```

Extended GCD

```

intsii,si,tii,ti; // ii=i-1, i=i,
s/t=i+1
integcd(inta,int b)
{
    intr,q,s,t;
    sii=1,si=0;
    tii=0,ti=1;
    while(b>0)
    {
        q=a/b;
        r=a%b;
        s=sii-(q*si);
        t=tii-(q*ti);
        sii=si,si=s;
        tii=ti,ti=t;
        a=b,b=r;
    }
    return a; // return a,sii,tii
}

```

LCM

```

int gcd(int a,int b)
{
    while(b>0)
    {
        a=a%b;
        swap(a,b);
    }
    return a;
}

int lcm(int a, int b)
{
    int temp = gcd(a, b);
    //__gcd(a, b)
    return ((a / temp) * b);
}

```

Sieve of PHI (Co-primes of 2 to n)

```

unsigned long long a[NN+7];
void sieve(void)
{
    inti,j,k,n=2237;
    for(i=2; i<NN; i++)
        a[i]=i;
    for(i=2; i<NN; i+=2)
    {
        a[i]*=(2-1);
        a[i]/=2;
    }
    for(i=3; i<NN; i+=2)
        if(a[i]==i)
            for(j=i; j<NN; j+=i)
            {
                a[j]*=(i-1);
                a[j]/=i;
            }
}

```

PHI (Co-primes of n)

```

int phi(int n)
{
    int res=n;
    int i;
    for(i=2; i*i<=n; i++)
    {
        if(!(n%i))
            res-=res/i;
        while(!(n%i))
            n/=i;
        if(n==1)
            break;
    }
    if(n>1)
        res-=res/n;
    return res;
}

```

nCr (normal)

```

long longnCr(intn,int r) //
{
    long long sum=1,l,k,l,j=1;
    k=max((r,n-r)), l=min((r,n-r));
    for(i=k+1;i<=n;i++)
    {
        sum*=i;
        if(j<=l &&sum%j==0)
        {
            sum/=j;
            j++;
        }
    }
    return sum;
}

```

nCr (DP)

```

i64 dp[70][70];
i64 nCr(intn,int r)
{
    if(r==1) return n;
    if(n==r) return 1;

    if(dp[n][r]!=-1)
        return dp[n][r];
    dp[n][r]=nCr(n-1,r)+nCr(n-1,r-1);

    return dp[n][r];
}

int main()
{
    Mem(dp,-1);
    printf("%d\n",nCr(20,2));
}

```

BitMask DP

```

intdp[70000];
int a[20][20];
int n;

int go(int x,int mask)
{
    if(x>=n)
        return 0;

    int&t=dp[mask];

    if(t!=-1)
        return t;
    int k=0;

    for(int i=0; i<n; i++)
        if((mask & (1<<i))==0)
            k=max(k,go(x+1,mask |
                1<<i)+a[x][i]);

    dp[mask]=k;
    return dp[mask];
}

main()
{
    inttc,t=1;
    scanf("%d",&tc);
    while(tc--)
    {
        scanf("%d",&n);
        for(int i=0; i<n; i++)
            for(int j=0; j<n; j++)
                scanf("%d",&a[i][j]);
        memset(dp,-1,sizeof(dp));
        int sum=go(0,0);
        printf("Case %d: %d\n",t++,sum);
    }
    return 0;
}

```

Topological Sort

```
#define mem(a,b) memset(a,b,sizeof(a))
#define pbpush_back
#define pppop_back
#define inf 1000000000
#define NN 1000010

vector<int>e[NN+7],v;
int view[NN+7];
int f,fl;

void dfs(int u) {
    inti,k,l;
    view[u]=0;
    for(i=0; i<e[u].size(); i++) {
        if(view[e[u][i]]==-1)
            dfs(e[u][i]);
        else if(view[e[u][i]]==0) {
            //then there is a cycle;
            fl=1;
            return;
        }
    }
    view[u]=1;
    v.pb(u);
}

int main()
{
    int i,j,k,l;
    int tc,t;
    int n,m;
    while(~scanf("%d%d",&n,&m))
    {
        if(n==0 && m==0)
            return 0;
        mem(view,-1);
        for(i=0; i<m; i++)
            scanf("%d%d",&k,&l),e[k].pb(l);

        fl=0;
        for(i=1; i<=n; i++)
        {
            f=i;
            if(view[i]==-1)
                dfs(i);
        }
        if(fl)
            printf("IMPOSSIBLE\n");
        else
        {
            reverse(v.begin(),v.end());
            for(i=0; i<v.size(); i++)
                printf("%d\n",v[i]);
        }
        v.clear();
        for(i=0; i<=n; i++)
            e[i].clear();
    }
    return 0;
}
```

MiniMax (MaxiMin is also same)

```
int pr[NN+7];
int a[NN+7][NN+7];

main()
{
    while(~scanf("%d%d%d",&n,&r,&l))
    {
        for(i=0; i<=n; i++)
        {
            for(j=0; j<=n; j++)
                a[i][j]=inf;
            //a[i][j]=-inf
            //FOR MaxiMin
            a[i][i]=0;
        }
        while(r--)
        {
            scanf("%d%d%d",&u,&v,&w);
            a[u][v]=w;
            a[v][u]=w;
        }
        for(k=1; k<=n; k++)
            for(i=1; i<=n; i++)
                for(j=1; j<=n; j++)
                    a[i][j]=min(a[i][j],
                                max(a[i][k],a[k][j]));
            //a[i][j]=max(a[i][j],
            //              min(a[i][k],a[k][j]));
            //For MaxiMin.

        while(l--)
        {
            scanf("%d",&n,&r);
            int sum=a[n][r];
            if(sum>=inf)
                //sum<=inf For MaxiMin
                puts("no path");
            else
                printf("%d\n",sum);
        }
        return 0;
    }
}
```

Power (n^k)

```
typedef long long LL;
LL power(LL n,LL m)
{
    LL sum=1;
    while(m>0)
    {
        sum*=n;
        m--;
    }
    return sum;
}
```

Highest Factors (range)

```
long b[10000001],c[10000001];
int main()
{
    long i,j,m,mx,t;
    b[1]=1;
    mx=0;
    c[1]=1;
    for(i=2; i<10000001; i++)
    {
        for(j=i; j<10000001; j+=i)
            b[j]++;
        if(b[i]>=mx)
        {
            mx=b[i];
            m=i;
        }
        c[i]=m;
    }
    scanf("%ld",&t);
    while(t--)
    {
        scanf("%ld",&m);
        printf("%ld\n",c[m]);
    }
    return 0;
}
```

Divisors sums (range)

```
#include<cstdio>
#define Z 500003
long Sum[Z];
int main()
{
    long t,n,i,j;
    for(i=1; i<Z; i++)
    {
        for(j=2*i; j<Z; j+=i)
            Sum[j]+=i;
    }
    scanf("%ld",&t);
    while(t--)
    {
        scanf("%ld",&n);
        printf("%ld\n",Sum[n]);
    }
    return 0;
}
```

Nim Game

```
#define NN 1050
main() {
    int t=1,tc;
    int k,l,n;
    cin>>tc;
    while(tc--) {
        cin>>n;
        int res=0;
        while(n--) {
            cin>>k;
            res^=k;
        }
        if(res)
            printf("Case %d: Alice\n",t++);
            //First move
        else
            printf("Case %d: Bob\n",t++);
    }
    return 0;
}
```

Misere Nim Game

```
#define NN 1050
main() {
    int t=1,tc;
    int k,l,n;
    cin>>tc;
    while(tc--) {
        cin>>n;
        int res=0,cnt=0,i;
        for(i=0; i<n; i++) {
            cin>>k;
            res^=k;
            if(k==1)
                cnt++;
        }
        if(cnt==n) {
            if(!res)
                printf("Case %d: Alice\n",t++);
            else
                printf("Case %d: Bob\n",t++);
        }
        else {
            if(res)
                printf("Case %d: Alice\n",t++);
            else
                printf("Case %d: Bob\n",t++);
        }
    }
    return 0;
}
```

Prime Sieve

```

===== [ For storing ] =====
#define NN 47000

bool p[NN+7]; //Hashing
vector<int>pr; //storing prime

void sieve(int n)
{
    int i,j,k,l;
    p[1]=1;
    pr.push_back(2);
    for(i=4; i<=n; i+=2)
        p[i]=1;
    for(i=3; i<=n; i+=2)
    {
        if(p[i]==0)
        {
            pr.push_back(i);
            for(j=i*i; j<=n; j+=2*i)
                p[j]=1;
        }
    }
}

===== [ For Hashing ] =====
#define NN 47000

bool p[NN+7]; //Hashing

void sieve(int n)
{
    int i,j,k,l;
    p[1]=1;
    for(i=4; i<=n; i+=2)
        p[i]=1;
    for(i=3; i*i<=n; i+=2)
    {
        if(p[i]==0)
        {
            for(j=i*i; j<=n; j+=2*i)
                p[j]=1;
        }
    }
}

```

Prime Factor

```

#define NN 47000

bool p[NN+7]; //Hashing
vector<int>pr; //storing prime
void sieve(int n)
{
    int i,j,k,l;
    p[1]=1;
    pr.push_back(2);
    for(i=4; i<=n; i+=2)
        p[i]=1;
    for(i=3; i<=n; i+=2)
    {
        if(p[i]==0)
        {
            pr.push_back(i);
            for(j=i*i; j<=n; j+=2*i)
                p[j]=1;
        }
    }
}

int factor(int n)
{
    int count,k,i;
    for(i=0; i<pr.size() &&
pr[i]*pr[i]<=n; i++)
    {
        k=pr[i];
        count=0;
        while(n%k==0)
        {
            n/=k;
            count++;
        }
        if(n==1)
            break;
    }
    if(n>1)
        then, n is another prime factor;
}

```

LIS (nlog(n)) & Print

```

#define mem(x,y) memset(x,y,sizeof(x));
vector <int> v;
vector <int> L;
vector <int> I;
stack <int> ans;

void prework(void)
{
    I.clear();
    L.clear();
    int i,k;
    k=2000000000;
    I.push_back(-1*k);

    for(i=0; i<v.size(); i++)
        L.push_back(1);
    return;
}

int LIS(void)
{
    int i,low,mid,high;
    for(i=0; i<v.size(); i++)
    {
        low=0;
        high=L.size()-1;
        while(low<=high)
        {
            mid=(low+high)/2;
            if(v[i]>I[mid])
                low=mid+1;
            else
                high=mid-1;
        }
        if(low==L.size())
            I.push_back(v[i]);
        else
            I[low]=v[i];
        L[i]=low;
    }
    return I.size()-1;
}

void show(void)
{
    int i,j,k,max;
    max=0;
    for(i=0; i<L.size(); i++)
    {
        if(max<L[i])
        {
            max=L[i];
            j=i;

```

```

        }
    }
    ans.push(v[j]);
    for(i=j-1; i>=0 ; i--)
    {
        if(v[i]<v[j] && L[i]==L[j]-1)
        {
            ans.push(v[i]);
            j=i;
        }
    }
    while(ans.size())
    {
        printf("%d\n",ans.top());
        ans.pop();
    }
    return;
}

main()
{
    char a[10];
    int i,j,k,l,m,n,t=0,T;
    scanf("%d",&T);
    getchar();
    getchar();
    while(T--)
    {
        //input taking methode in uva 497
        t++;
        v.clear();
        while(gets(a) && strlen(a))
        {
            sscanf(a,"%d",&n);
            v.push_back(n);
        }
        if(v.size())
        {
            prework();
            if(t!=1)
                puts("");
            printf("Max hits:
                                %d\n",LIS());

            show();
        }
    }
    return 0;
}

```

LDS (n^2) [Decreasing]

```
#define mem(x,y) memset(x,y,sizeof(x));
```

```
int dp[1000];
bool dc[1000];
vector <int>v;
int LDS(int u)
{
    if(dc[u])
        return dp[u];
    int max=0;
    for(int i=u+1; i<v.size(); i++)
    {
        if(v[i]<=v[u])
        {
            if(max<LDS(i))
            {
                max=LDS(i);
            }
        }
    }
    dp[u]=max+1;
    dc[u]=1;
    return dp[u];
}
```

```
main()
{
    int i=0,k,n,j;
    while(scanf("%d",&n)==1)
    {
        if(n==-1)
            return 0;
        i++;
        mem(dc,0);
        v.clear();
        v.push_back(n);
        while(1)
        {
            scanf("%d",&n);
            if(n==-1)
                break;
            v.push_back(n);
        }
        k=0;
```

```
for(j=0; j<v.size(); j++)
{
    if(k<LDS(j))
    {
        k=LDS(j);
    }
}
if(i!=1)
    puts("");
printf("Test #d: %d\n",i,k);
}
```

Ternary Search

```
/*
    some points are given initially.
    Now, we have to find a area consists
    with K,L no points and third one
    which area is equal or gretter than S.
*/

int ternary_search(int k,int l,int s)
{
    int low=0, high=v.size()-1;
    int midleft, midright;

    while(high-low>3)
    {
        midleft = low + (high-low)/3 ;
        midright = high - (high-low)/3;

        int area1=area(k,l,midleft);
        int area2=area(k,l,midright);

        if( area1 < area2 )
            low = midleft ;
        else
            high = midright ;
    }

    for(int i=low; i<=high; i++)
    {
        int temp=area(k,l,i);
        if(s <= temp )
            return i+1;
    }
    return 0;
}
```


String Multiplication (500!)

```

char a[1001][10000];
void swap(char b[10000])
{
    int temp,i,j,l;
    l=strlen(b);
    for(i=0,j=l-1; i<l/2; i++,j--)
    {
        temp=b[i];
        b[i]=b[j];
        b[j]=temp;
    }
}
void work(char a[10000],char
b[10000],int n)
{
    int i,j,onhand=0,k,l;
    l=strlen(a);
    for(i=l-1,j=0; i>=0; i--)
    {
        k=((a[i]-48)*n)+onhand;
        b[j]=(k%10)+48;
        onhand=k/10;
        j++;
    }
    while(onhand>0)
    {
        b[j]=(onhand%10)+48;
        onhand/=10;
        j++;
    }
    b[j]='\0';
    swap(b);
}

main()
{
    int i,j,n;
    strcpy(a[0],"1");
    strcpy(a[1],"1");
    for(i=2; i<1001; i++)
    {
        work(a[i-1],a[i],i);
    }
    while(scanf("%d",&n)==1)
    {
        printf("%d!\n%s\n",n,a[n]);
    }
    return 0;
}

```

String Addition (fibonacchi Freeze)

```

const int max=1111;
char a[5001][max];
void add(char b[max],char b1[max],char
b2[max]) {
    char c[max];
    int carry=0,i,k,j,m,n,l=0;
    m=strlen(b1);
    n=strlen(b2);
    for(i=m-1,k=n-1;i>=0||k>=0;i--,k--){
        if(i>=0 && k>=0) {
            j= b1[i]-48+b2[k]-48+carry;
            carry=j/10;
            c[l]=j%10+48;
            l++;
        }
        else if(i>=0) {
            j=b1[i]-48+carry;
            carry=j/10;
            c[l]=j%10+48;
            l++;
        }
        else {
            j=b2[k]-48+carry;
            carry=j/10;
            c[l]=j%10+48;
            l++;
        }
    }
    j=0;
    if(carry==1) {
        b[j]=49;
        j++;
    }
    for(i=l-1; i>=0; i--) {
        b[j]=c[i];
        j++;
    }
    b[j]='\0';
}

void check(void) {
    strcpy(a[0],"0");
    strcpy(a[1],"1");
    for(int i=2; i<=5000; i++)
        add(a[i],a[i-1],a[i-2]);
}

main() {
    check(); int n;
    while(scanf("%d",&n)==1) {
        printf("The Fibonacci number for
        %d is %s\n",n,a[n]);
    }
    return 0;
}

```

String Division & Modulus

```
long long div(char a[], long long n, char
c[])
{
    int i, j, t=0, l, d=0, r=0;
    long long rem=0;
    l=strlen(a);
    for(i=0; i<l; i++)
    {
        rem=(rem*10)+a[i]-48;

        if(rem>=n || r!=0)
        {
            j=rem/n;
            rem=rem%n;
            c[d]=j+48;
            d++;
            r=1;
        }
    }
    if(d==0)
    {
        c[d]='0';
        d++;
    }
    c[d]='\0';
    return rem;
}
```

String Modulus

```
int mod(char a[], int divider)
{
    int rem, i;
    rem=0;
    for(i=0; a[i]; i++)
    {
        rem=rem*10+a[i]-48;
        rem=rem%divider;
    }
    return rem;
}
```

Geometry Area

```
=====[ Polygon Area ]=====
double area(void)
{
    double total = 0.0;
    /* total area so far */
    int i, j;
    /* counters */
    //V is storage of polygon points
    for (i=0; i<v.size(); i++)
    {
        j = (i+1) % v.size();
        total += (v[i].x*v[j].y) -
                (v[j].x*v[i].y);
    }
    return(total / 2.0);
}

=====[ Triangle Area ]=====

P MV(P a, P b)
{
    return P(b.x-a.x, b.y-a.y);
}

double CP(P a, P b)
{
    return a.x*b.y-a.y*b.x;
}

double area(int x, int y, int z)
{
    double total = 0;
    /* total area so far */

    total=CP(MV(v[x], v[y]),
            MV(v[x], v[z]));

    return(total / 2);
}
```

Convex Hull Points

```
#define mp make_pair
#define pb(x) push_back(x)
#define pp(x) pop_back(x)
#define all(x) x.begin(),x.end()
#define mem(a,b) memset(a,b,sizeof(a))
#define inf 1e9
#define eps 1e-9
#define NN 1050

struct P {
    double x,y;
    P(double X,double Y) {
        x=X;
        y=Y;
    }
    P() { }
};
vector<P>v;

P MV(P a,P b) {
    return P(b.x-a.x,b.y-a.y);
}

double DP(P a, P b) {
    return a.x*b.x+a.y*b.y;
}

double CP(P a,P b) {
    return a.x*b.y-a.y*b.x;
}

double A(P a) {
    return sqrt(a.x*a.x+a.y*a.y);
}

P ADD(P a,P b) {
    return P(a.x+b.x,a.y+b.y);
}

P LV(P a,double l) {
    return P(a.x*l/A(a),a.y*l/A(a));
}

P pvt;

bool comp(P a,P b){
//False hoile sort korbe
    long long c=CP(MV(pvt,a),MV(pvt,b));
    if(c)
        return c>0;
    return A(MV(pvt,a))<A(MV(pvt,b));
}
```

```
void checkPvt(void) {
    pvt.x=inf;
    pvt.y=inf;
    for(int i=0; i<v.size(); i++) {
        if(pvt.x>v[i].x)
            pvt=v[i];
        else if(pvt.x==v[i].x
                && pvt.y>v[i].y)
            pvt=v[i];
    }
}

vector<P>q;

void go(void) {
    q.clear();
    int n=v.size();
    q.pb(v[n-1]);
    v.pp();
    for(int i=v.size()-1;i>=0;i--) {
        if(CP(MV(v[0],q[q.size()-1]),
            MV(v[0],v[i]))==0) {
            q.pb(v[i]);
            v.pp();
        }
        else
            break;
    }
    for(int i=0;i<q.size();i++)
        v.pb(q[i]);
}

main() {
    int t=1,tc,i,j,k,l,m,n;
    double x,y,z,u,w,xx,yy,zz,d;
    double aa,bb,cc,dd;
    cin>>tc;
    while(tc--) {
        cin>>n;
        v.clear();
        for(i=0; i<n; i++) {
            cin>>k>>l;
            v.pb(P(k,l));
        }
        checkPvt();
        sort(v.begin(),v.end(),comp);
        go();
        cout<<(int)v.size()<<"\n";
        for(i=0; i<v.size(); i++)
            cout<<(int)v[i].x<<
                " "<<(int)v[i].y<<"\n";
    }
    return 0;
}
```

Lower-Upper Bound

```
#include <iostream>
#include <algorithm>
#include <vector>
using namespace std;

int main ()
{
    int myints[] = {10,20,30,30,20,10,10,20};
    std::vector<int> v(myints,myints+8);           // 10 20 30 30 20 10 10 20

    std::sort (v.begin(), v.end());               // 10 10 10 20 20 20 30 30

    std::vector<int>::iterator low,up;

    low=std::lower_bound (v.begin(), v.end(), 20); // 0 index system
    up= std::upper_bound (v.begin(), v.end(), 20); // 0 index system

    cout << "lower_bound at position " << (low- v.begin()) << '\n'; //ans: 3
    cout << "upper_bound at position " << (up - v.begin()) << '\n'; //ans: 6

    low=lower_bound (v.begin(), v.end(), 25); //
    up= upper_bound (v.begin(), v.end(), 25); //

    cout << "lower_bound at position " << (low- v.begin()) << '\n'; //ans: 6
    cout << "upper_bound at position " << (up - v.begin()) << '\n'; //ans: 6

    low=lower_bound (v.begin(), v.end(), 50); //
    up= upper_bound (v.begin(), v.end(), 50); //

    cout << "lower_bound at position " << (low- v.begin()) << '\n'; //ans: 8
    cout << "upper_bound at position " << (up - v.begin()) << '\n'; //ans: 8

    return 0;
}
```

LCM of n numbers [Prime and mod]

```

using namespace std;
#define inf 1e9
#define NN 100010
#define mod 1000000007

vector<int>arr;

bool pr[350];
vector<int>prim;
int mx;
int fact[NN];
void sieve(int n) {
    memset(pr,0,sizeof(pr));
    long i,j,k,l;
    pr[1]=1;
    prim.push_back(2);
    for(i=4; i<=n; i+=2)
        pr[i]=1;
    for(i=3; i<=n; i+=2) {
        if(pr[i]==0) {
            prim.push_back(i);
            for(j=i*i; j<=n; j+=2*i)
                pr[j]=1;
        }
    }
}

void factor(int n) {
    int i,j,count;
    for(j=0; j<prim.size() &&
        prim[j]*prim[j]<=n; j++) {
        i=prim[j];
        count=0;
        if(n%i==0)
            mx=max(i,mx);
        while(n%i==0) {
            n/=i;
            count++;
        }
        fact[i]=max(fact[i],count);
        if(n==1)
            break;
    }
    if(n>1) {
        mx=max(n,mx);
        fact[n]=max(fact[n],1);
    }
}

int bigmod(int m,int n) {
    int sum;
    if(n==0)
        return 1;
    if(n%2==0) {

```

```

        sum=bigmod(m,n/2);
        return
        ((sum%mod)*(sum%mod))%mod;
    }
    else {
        sum=bigmod(m,n-1);
        return
        ((m%mod)*(sum%mod))%mod;
    }
}

int LCM(void) {
    //LCM of elemets of arr with mod
    long long sum=1;
    int i,j,k;
    mx=-inf;
    mem(fact,0);
    for(i=0; i<arr.size(); i++)
        factor(arr[i]);
    for(i=2; i<=mx; i++)
        if(fact[i])

sum=(sum*bigmod(i,fact[i]))%mod;
return sum;
}

main(){
    int t,tc;
    cin>>tc;
    int cnt=0,sum=0;
    int i,j,k,l,n,m;
    sieve(345); //Sieve
    while(tc-->0) {
        cin>>n;
        arr.clear();
        for(i=1; i<=n; i++)
            cin>>k,arr.pb(k);
        sum=LCM();
        printf("%d\n",sum);
    }
    return 0;
}

```

Input:

```

4
5
1 2 3 4 5
6
1 2 3 4 5 6
7
1 2 3 4 5 6 7
5
7 11 13 19 21

```

Output:

```

60
60
420
57057

```

LCM of n numbers -String [without mod]

```

using namespace std;
#define mem(a,b) memset(a,b,sizeof(a))

bool pr[106];
vector<int>prim;
int mx, fact[10001];
void sieve(int n) {
    memset(pr,0,sizeof(pr));
    long i,j,k,l;
    pr[1]=1;
    prim.push_back(2);
    for(i=4;i<=n;i+=2)
        pr[i]=1;
    for(i=3;i<=n;i+=2) {
        if(pr[i]==0) {
            prim.push_back(i);
            for(j=i*i;j<=n;j+=2*i)
                pr[j]=1;
        }
    }
}

void factor(int n) {
    int i,j,count;
    for(j=0;j<prim.size() &&
        prim[j]*prim[j]<=n;j++) {
        i=prim[j];
        count=0;
        if(n%i==0)    mx=max(i,mx);
        while(n%i==0) {
            n/=i;
            count++;
        }
        fact[i]=max(fact[i],count);
        if(n==1)
            break;
    }
    if(n>1) {
        mx=max(n,mx);
        fact[n]=max(fact[n],1);
    }
}

string s;
void mult(int n,int r) {
    while(r--) {
        long long k,i,carry=0;
        for(i=0;i<s.size();i++)
        {
            k=s[i]-'0';
            k=(n*k)+carry;
            s[i]=k%10+'0';
            carry=k/10;
        }
    }
}

```

```

while(carry>0)
{
    s+=carry%10+'0';
    carry/=10;
}
}

main()
{
    sieve(101);
    int n,k,i,m,c;
    int tc,t=1;
    cin>>tc;
    while(tc--)
    {
        cin>>n;
        mem(fact,0);
        mx=-inf;
        while(n--)
        {
            cin>>k;
            factor(k);
        }
        s="1";
        for(i=2;i<=mx;i++)
        {
            if(fact[i])
            {
                mult(i,fact[i]);
            }
        }
        reverse(s.begin(),s.end());
        printf("Case %d: %s\n"
            ,t++,s.c_str());
    }
    return 0;
}

/*
Input:
2
3
2 20 10
4
5 6 30 60

Output:
Case 1: 20
Case 2: 60
*/

```

Base Conversion

```

void dec2other(char a[],char b[],int m) {
    long long sum=atoi(a);
    itoa(sum,b,m); //m-> required base.
}

void other2dec(char a[],char b[],int n) {
    long long sum=0;
    int i,j=0,k,l;
    l=strlen(a);
    j=0;
    for(i=l-1;i>=0;i--) {
        if(a[i]>='A')      k=a[i]-'A'+10;
        else      k=a[i]-48;

        sum+=k*pow(n,j);
        j++;
    }
    sprintf(b,"%lld",sum);
}

main() {
    char a[100],b[100];
    int i,j,k,l,m,n;
    printf("CURRENT base: ");
    scanf("%d",&n);
    printf("\nNumber: ");
    scanf("%s",&a);
    printf("\nREQUIRED base: ");
    scanf("%d",&m);
    for(i=0;a[i]!=0;i++) {
        a[i]=toupper(a[i]);
        if(a[i]>='A')      k=a[i]-'A'+10;
        else      k=a[i]-'0';
        if(k>=n) {
            printf("\n**%s is not of %d base.\n\n",a,n);
            return 0;
        }
    }
    if(n==10) {
        dec2other(a,b,m);
        printf("\nNumber in %d base: %s\n\n",m,b);
    }
    else if(m==0) {
        other2dec(a,b,n);
        printf("\nNumber in %d base: %s\n\n",m,b);
    }
    else {
        other2dec(a,b,n);
        dec2other(b,a,m);
        printf("\nNumber in %d base: %s\n\n",m,a);
    }
    return 0;
}

```

BFS

```

#define NIL -1
#define white 0
#define gray 1
#define black 2
using namespace std;

int dis[MAX], parent[MAX], color[MAX];
vector<int> g[MAX];

void BFS(int s,int v){
    int len,x,k;
    queue<int> Q;
    parent[s]=NIL;
    dis[s]=0;
    color[s]=gray;
    Q.push(s);

    while(!Q.empty()){
        x=Q.front(),Q.pop();
        len=g[x].size();
        for(int i=0; i<len; i++){
            if(g[x][i] && color[g[x][i]]==white) {
                k=g[x][i];
                color[k]=gray;
                dis[k]=dis[x]+1;
                parent[k]=x;
                Q.push(k);
            }
            color[x]=black;
        }
        printf("\n***distances***\n");
        for(int i=1; i<=v; i++){
            printf("distance[%d]= %d\n",i,dis[i]);
        }
        return;
    }
}

int main() {
    int v,e,s,d;
    printf("Enter no of vertices: ");
    scanf("%d",&v);
    printf("Enter no of edges: ");
    scanf("%d",&e);
    for(int i=1; i<=e; i++) {
        printf("Enter source and destination: ");
        scanf("%d %d",&s,&d);
        g[s].push_back(d);
        g[d].push_back(s);
    }
    printf("Enter source of graph: ");
    scanf("%d",&s);
    BFS(s,v);
    return 0;
}

```


Dijkstra

```

#include <bits/stdc++.h>

using namespace std;

typedef long long          ll;
typedef unsigned long long llu;

#define ft      first
#define sd      second
#define mp      make_pair
#define pb(x)   push_back(x)
#define all(x)  x.begin(),x.end()
#define allr(x) x.rbegin(),x.rend()
#define mem(a,b) memset(a,b,sizeof(a))
#define meminf(a) memset(a,126,sizeof(a))
#define inf     1e11
#define eps     1e-9
#define mod     1000000007
#define NN      30100
#define mx      100002

vector<int>g[mx],cost[mx];

struct node
{
    int u,w;
    node(int a,int b)
    {
        u=a;
        w=b;
    }
    bool operator < ( const node& p ) const
    {
        return w > p.w;
    }
};

int d[mx],par[mx];

int dijkstra(int n)
{
    memset(d,63,sizeof(d)); //huge value=63
    memset(par,-1,sizeof(par));
    priority_queue<node>q;
    q.push(node(1,0));
    d[1]=0;
    while(!q.empty())
    {
        node top=q.top();
        q.pop();
        int u=top.u;

```

```

        if(u==n)
            return d[n];

        for(int i=0; i<(int)g[u].size(); i++)
        {
            int v=g[u][i];
            if(d[u]+cost[u][i]<d[v])
            {
                d[v]=d[u]+cost[u][i];
                par[v]=u;
                q.push(node(v,d[v]));
            }
        }
    }
    return -1;
}

int main()
{
    int n,e;
    cin>>n>>e;
    for(int i=0; i<e; i++)
    {
        int u,v;
        int w;
        cin>>u>>v>>w;
        g[u].push_back(v);
        g[v].push_back(u);
        cost[u].push_back(w);
        cost[v].push_back(w);
    }
    int ret=dijkstra(n);
    if(ret==-1) puts("No path!");
    else
    {
        int u=n;
        vector<int>out;
        while(u!=-1)
        {
            out.push_back(u);
            u=par[u];
        }
        reverse(out.begin(),out.end());
        for(int i=0; i<(int)out.size(); i++)
            cout<<out[i]<<" ";
        puts("");
    }
}

```

Floyd–Warshall

```

#define inf 100000000
#define NN 300
int a[NN+7][NN+7];
int next[NN+7][NN+7];
int main()
{
    int i,j,k,l,n,r,c,u,v,w,tc,t=1,m;
    scanf("%d%d",&n,&r); //r = edges, n=nodes
    for(i=0; i<=n; i++) {
        for(j=0; j<=n; j++) {
            a[i][j]=d[i][j]=inf;
            next[i][j]=j;
        }
        a[i][i]=d[i][i]=0;
    }

    while(r--) {
        scanf("%d%d%d",&u,&v,&k);
        a[u][v]=a[v][u]=k;
    }

    for(k=1; k<=n; k++)
        for(i=1; i<=n; i++)
            for(j=1; j<=n; j++)
                if(a[i][j]>a[i][k]+a[k][j]) {
                    a[i][j]=a[i][k]+a[k][j];
                    next[i][j]=k;
                }

    int first,last;

    while(scanf("%d %d",&first,&last)==2) {
        printf("From %d to %d :\n",first,last);
        printf("Path: ");
        i=first;
        j=last;

        printf("%d-->",i);
        while(i!=j) {
            i=next[i][j];
            if(i==j) {
                printf("%d",j);
                break;
            }
            printf("%d-->",i);
        }

        printf("\nTotal cost : %d\n\n",mat[first][last]);
    }
    return 0;
}

```

Articulation Bridge

```

#define mp make_pair
#define pb(x) push_back(x)
#define all(x) x.begin(),x.end()
#define mem(a,b) memset(a,b,sizeof(a))
#define inf 1e9
#define eps 1e-9
#define NN 10010

vector<int>e[NN];
vector< pair<int,int> >bridge;
int depth[NN];
int par[NN];
int low[NN];
bool color[NN];
int Time;

int dfs(int u)
{
    low[u]=depth[u]=++Time;
    color[u]=true;
    int i;
    for(i=0; i<e[u].size(); i++)
    {
        int v=e[u][i];
        if(!color[v])
        {
            par[v]=u;
            dfs(v);
            low[u]=min(low[u],low[v]);
            if(depth[u]<low[v])
                bridge.pb(mp(u,v));
        }
        else if(v!=par[u])
            low[u]=min(low[u],depth[v]);
    }
    return 0;
}

int articulation_Point(int n)
{
    mem(depth,0);
    mem(par,-1);
    mem(low,0);
    mem(color,0);
    Time=0;
    bridge.clear();

    for(int i=0; i<n; i++)
        if(!color[i])
            dfs(i);
}

```

```

    int ans=bridge.size();
    printf("%d critical links\n",ans);
    for(int i=0; i<bridge.size(); i++)
        printf("%d - %d\n",bridge[i].first,bridge[i].second);
    return 0;
}

main()
{
    ios_base::sync_with_stdio(false);
    int t=1,tc;
    cin>>tc;          //Test Case
    int i,j,k,l,m,n;
    int node,edge;
    while(tc--)
    {
        cin>>node>>edge;
        for(i=0; i<edge; i++)
        {
            cin>>k>>l;
            e[k].pb(l);
            e[l].pb(k);
        }
        printf("Case %d:\n",t++);
        articulation_Point(node);
        for(i=0; i<=node; i++)
            e[i].clear();
    }
    return 0;
}

```

Input

```

3
8 6
0 1
1 2
1 3
2 3
3 4
6 7

4 4
0 1
1 2
2 3
3 1

2 1
0 1

```

Output

```

Case 1:
3 critical links
3 - 4
0 - 1
6 - 7

Case 2:
1 critical links
0 - 1

Case 3:
1 critical links
0 - 1

```

Articulation Point

```

#define mp make_pair
#define pb(x) push_back(x)
#define all(x) x.begin(),x.end()
#define mem(a,b) memset(a,b,sizeof(a))
#define inf 1e9
#define eps 1e-9
#define NN 10010

vector<int>e[NN];
int depth[NN];
int par[NN];
int low[NN];
bool color[NN],Flag[NN];
int Time;

int dfs(int u)
{
    low[u]=depth[u]=++Time;
    color[u]=true;
    int i,call=0;
    for(i=0; i<e[u].size(); i++)
    {
        int v=e[u][i];
        if(!color[v])
        {
            call++;
            par[v]=u;
            dfs(v);
            low[u]=min(low[u],low[v]);
            if(depth[u]<=low[v])
                Flag[u]=true;
        }
        else if(v!=par[u])
            low[u]=min(low[u],depth[v]);
    }
    if(par[u]==-1)
        Flag[u]=(call>1);
}

int articulation_Point(int n)
{
    mem(depth,0);
    mem(par,-1);
    mem(low,0);
    mem(color,0);
    mem(Flag,0);
    Time=0;

    for(int i=1; i<=n; i++)
        if(!color[i])
            dfs(i);

    int ans=0;

```

```

    for(int i=1; i<=n; i++)
        if(Flag[i])
            ans++;
    return ans;
}

main()
{
    ios_base::sync_with_stdio(false);
    int t=1,tc;
    cin>>tc;          //Test Case
    int i,j,k,l,m,n;
    int node,edge;
    while(tc--)
    {
        cin>>node>>edge;
        for(i=0; i<edge; i++)
        {
            cin>>k>>l;
            e[k].pb(l);
            e[l].pb(k);
        }

        int ans=articulation_Point(node);
        printf("Case %d: %d\n",t++,ans);

        for(i=0; i<=node; i++)
            e[i].clear();
    }
    return 0;
}

```

Input

```

3          //Test Case

5 4        //node edge
2 1
1 3
5 4
4 1

3 3
1 2
2 3
1 3

5 5
1 2
2 3
3 4
2 5
5 3

```

Output

```

Case 1: 2
Case 2: 0
Case 3: 2

```

SCC - DFS (Strongly Connected Component)

```

int color[NN];
vector<int>arr; //topological sorted node
vector<int>Graph[NN], transGraph[NN], newGraph[NN]
vector<pair<int,int> >v; //Edges Before SCC
int id[NN], amount[NN]; //Amount of original node in a SCC node

int dfs_1st(int u) {
    color[u]=true;
    for(int i=0; i<Graph[u].size(); i++) {
        if(!color[Graph[u][i]])
            dfs_1st(Graph[u][i]);
    }
    arr.pb(u);
}

int dfs_2nd(int u,int k) {
    color[u]=true;
    id[u]=k;

    for(int i=0; i<transGraph[u].size(); i++) {
        if(!color[transGraph[u][i]])
            dfs_2nd(transGraph[u][i],k);
    }
}

int scc(int n) {
    arr.clear();
    mem(color,0);
    int i,j,k,l;
    for(i=1; i<=n; i++) //Topological Sort
        if(color[i]==0)
            dfs_1st(i);

    reverse(all(arr));

    mem(id,-1);
    mem(color,0);
    k=0;
    for(i=0; i<arr.size(); i++) //Identify SCC {
        if(!color[arr[i]]) {
            dfs_2nd(arr[i],k+1);
            amount[id[arr[i]]]=1; //Amount of actual node
            //in SCC node
            k++;
        }
        else
            amount[id[arr[i]]]++;
    }
    int node=k; //Number of SCC node
}

```



```

    for(i=0; i<v.size(); i++) //Build SCC graph
    {
        k=v[i].first;
        l=v[i].second;

        if(id[k]!=id[l])
            newGraph[id[k]].pb(id[l]);
    }
    return node; //Number of SCC node.
}

main()
{
    int t=1,tc,i,j,k,l,m,n,man;
    cin>>tc; //Test Case
    while(tc--)
    {
        cin>>n>>m; //n=node, m=edge
        for(i=0; i<=n; i++)
            Graph[i].clear(), transGraph[i].clear(), newGraph[i].clear();
        v.clear();

        for(i=0; i<m; i++)
        {
            cin>>k>>l;
            Graph[k].pb(l);
            transGraph[l].pb(k);
            v.pb(make_pair(k,l));
        }

        int sum=scc(n);
        printf("Case %d: %d\n",t++,sum);
    }
    return 0;
}

===== [ input ] =====
2
4 4
1 2
2 1
3 4
4 3

3 3
1 2
2 3
3 1
===== [ output ] =====
Case 1: 2
Case 2: 1

```

SCC - Tarjan (Strongly Connected Component)

```

#define mp make_pair
#define pb(x) push_back(x)
#define all(x) x.begin(),x.end()
#define mem(a,b) memset(a,b,sizeof(a))
#define NN 1050
#define MAX 1000000

bool Flag[MAX];           //If a node already belongs to a scc or not.
int depth[MAX];           //The time when a node is visited
int Lowlink[MAX];         //A node connected with lowest timed node [if scc
exist]
bool color[MAX];
int belong[MAX];          //A node belongs to which SCC
vector<int> G[MAX];        //Graph Store
stack<int> mystack;        //order of nodes r visited
int time,top,scc;

void tarjan(int u)
{
    int v,i;
    depth[u]=Lowlink[u]=++time;
    color[u]=true;
    mystack.push(u);
    Flag[u]=true;
    for(i=0; i<G[u].size(); i++)
    {
        v=G[u][i];
        if(!color[v])
        {
            tarjan(v);
            Lowlink[u]=min(Lowlink[u],Lowlink[v]);
        }
        else if(Flag[v])
            Lowlink[u]=min(Lowlink[u],depth[v]);
    }
    if(Lowlink[u]==depth[u])
    {
        scc++;
        do
        {
            v=mystack.top(),mystack.pop();
            Flag[v]=false;
            belong[v]=scc;
        }
        while(u!=v);
    }
}

```

```

void findSCC(int n)
{
    mystack=stack<int>();
    scc=top=time=0;
    mem(depth,-1);
    mem(Flag,0);
    mem(color,0);
    mem(Lowlink,126);
    for(int i=1; i<=n; i++)
        if(!color[i])
            tarjan(i);
}

int main()
{
    int node,edge;
    cin>>node>>edge;
    for(int i=0; i<edge; i++)
    {
        int k,l;
        cin>>k>>l;
        G[k].pb(l);
    }
    findSCC(node);
    cout<<scc;

    return 0;
}

/*
Input:
5 5
1 2
2 3
3 4
5 2
3 5

Output:
3
*/

```

BCC [Biconnected Component]

/*Undirected Graph.

One Biconnected component means a region where nodes will Be connected after deleting exactly one edge.

*/

```
vector<int>Graph[NN];           //Graph Before BCC
vector<int>newGraph[NN];       //Graph after BCC
vector< pair<int,int> >edge;    //Input edges
stack<int>mystack;             //order of nodes r visited
int depth[NN];                 //The depth(time) when a node is visited
int par[NN];                   //Parent of node
int low[NN];                   //A node connected with lowest timed node [if bcc exist]
bool color[NN];                //Color if a node is visited or not
int belong[NN];                //A node blongs to which BCC
int Time,bcc;
```

```
int dfs(int u) {
    low[u]=depth[u]=++Time;
    color[u]=true;
    mystack.push(u);
    int i,v;
    for(i=0; i<Graph[u].size(); i++) {
        v=Graph[u][i];
        if(!color[v]) {
            par[v]=u;
            dfs(v);
            low[u]=min(low[u],low[v]);
        }
        else if(v!=par[u])
            low[u]=min(low[u],depth[v]);
    }
    if(low[u]==depth[u]) {
        bcc++;
        do {
            v=mystack.top();
            mystack.pop();
            belong[v]=bcc;
        }
        while(u!=v);
    }
    return 0;
}
```

```
int findbcc(int n) {
    mem(depth,0);
    mem(par,-1);
    mem(low,0);
    mem(color,0);
    mystack=stack<int>();
    Time=bcc=0;

    for(int i=0; i<n; i++) //lowest node=0
        if(!color[i])
```

```

        dfs(i);
    int Highest_Node=bcc;

    for(int i=0; i<edge.size(); i++) {
        int u=belong[edge[i].first];
        int v=belong[edge[i].second];
        if(u!=v) {
            newGraph[u].pb(v);
            newGraph[v].pb(u);
        }
    }
    return Highest_Node;
}

int Print_NewGraph(int n) {
    int i,j;
    for(i=1; i<=n; i++) {          //lowest node=1
        if(newGraph[i].size()) {
            printf("%d :",i);
            for(j=0; j<newGraph[i].size(); j++)
                printf(" %d",newGraph[i][j]);
            puts("");
        }
    }
    return 0;
}

main() {
    int t=1,tc,i,j,k,l,m,n,e;
    cin>>tc;          //Test Cas
    while(tc--) {
        cin>>n>>e;
        for(i=0; i<e; i++) {
            cin>>k>>l;
            Graph[k].pb(l);
            Graph[l].pb(k);
            edge.pb(mp(k,l));
        }
        printf("Case %d:\n",t++);
        k=findbcc(n);
        Print_NewGraph(k);
        for(i=0; i<=n; i++)
            Graph[i].clear(),newGraph[i].clear();
        edge.clear();
    }
    return 0;
}

```

```

/*
Input:
2

4 4
0 1
1 2
2 3
3 1

6 6
0 1
1 2
1 3
3 4
4 5
1 4

Output:

Case 1:
1 : 2
2 : 1
Case 2:
1 : 3
2 : 3
3 : 4 1 2
4 : 3

*/

```

Matrix Expo - Fibonacci

```

/*
===== [ Theme ] =====
    |1 1|^k * |f(1)| = |f(k+1)|
    |1 0|      |f(0)|   | f(k) |

    here,
    f(0)=aa;
    f(1)=bb;
===== [ END ] =====
*/

ll M;

ll m[3][3];

void mult(ll a[3][3], ll b[3][3])
{
    ll temp[3][3];
    int i, j, k;
    mem(temp, 0);
    for(i=0; i<2; i++)
        for(j=0; j<2; j++)
            for(k=0; k<2; k++)
                temp[i][j] +=
                    a[i][k] * b[k][j];
    for(i=0; i<2; i++)
        for(j=0; j<2; j++)
            a[i][j] = temp[i][j] % M;
    return;
}

void BigMat(ll a[3][3], int pos)
{
    int i, j, k;
    if(pos==1)
        return;
    if(pos%2==1)
    {
        BigMat(a, pos-1);
        mult(a, m);
    }
    else
    {
        BigMat(a, pos/2);
        mult(a, a);
    }
    return;
}

```

```

main()
{
    int t=1, tc;
    cin >> tc;
    ll i, j, k, l, n;
    ll aa, bb;
    while(tc--)
    {
        cin >> aa >> bb >> n >> M;

        if(n==0)
        {
            printf("Case %d: %lld\n",
                t++, aa);
            continue;
        }
        if(n==1)
        {
            printf("Case %d: %lld\n",
                t++, bb);
            continue;
        }

        ll a[3][3];
        a[0][0] = m[0][0] = 1;
        a[0][1] = m[0][1] = 1;
        a[1][0] = m[1][0] = 1;
        a[1][1] = m[1][1] = 0;

        if(M==1)
            M=10;
        else if(M==2)
            M=100;
        else if(M==3)
            M=1000;
        else if(M==4)
            M=10000;

        BigMat(a, n);

        m[0][0] = bb;
        m[1][0] = aa;
        ll temp[3][3];
        mem(temp, 0);
        for(i=0; i<2; i++)
            for(j=0; j<1; j++)
                for(k=0; k<2; k++)
                    temp[i][j] +=
                        a[i][k] * m[k][j];
        printf("Case %d: %lld\n",
            t++, temp[1][0] % M);
    }
    return 0;
}

```

Matrix Expo - nth term of Function

```

/*
f(n) =a*f(n-1)+b*f(n-3)+c, if(n > 2)
      =0 if(n <= 2)
f(n+1)= a*f(n)+0*f(n-1)+b*f(n-2)+c

|a 0 b 1|^k * |f(2)|   |f(k+2)|
|1 0 0 0|      |f(1)| = |f(k+1)|
|0 1 0 0|      |f(0)|   |f(k)|
|0 0 0 1|      |c|      |c|
here,
a = aa;
b = bb;
c = cc;
*/

ll m[5][5];

void mult(ll a[5][5], ll b[5][5]) {
    ll temp[5][5];
    int i, j, k;
    mem(temp, 0);
    for(i=0; i<4; i++)
        for(j=0; j<4; j++)
            for(k=0; k<4; k++)
                temp[i][j] +=
                    a[i][k]*b[k][j];
    for(i=0; i<4; i++)
        for(j=0; j<4; j++)
            a[i][j] = temp[i][j] % mod;
    return;
}

void BigMat(ll a[5][5], int pos)
{
    int i, j, k;
    if(pos==1)
        return;
    if(pos%2==1)
    {
        BigMat(a, pos-1);
        mult(a, m);
    }
    else
    {
        BigMat(a, pos/2);
        mult(a, a);
    }
    return;
}

```

```

main()
{
    int t=1, tc;
    cin >> tc;
    ll i, j, k, l, n;
    ll aa, bb, cc;
    while(tc--)
    {
        cin >> n >> aa >> bb >> cc;
        if(n <= 2)
        {
            printf("Case %d: 0\n", t++);
            continue;
        }

        ll a[5][5];
        a[0][0] = m[0][0] = aa;
        a[0][1] = m[0][1] = 0;
        a[0][2] = m[0][2] = bb;
        a[0][3] = m[0][3] = 1;
        a[1][0] = m[1][0] = 1;
        a[1][1] = m[1][1] = 0;
        a[1][2] = m[1][2] = 0;
        a[1][3] = m[1][3] = 0;
        a[2][0] = m[2][0] = 0;
        a[2][1] = m[2][1] = 1;
        a[2][2] = m[2][2] = 0;
        a[2][3] = m[2][3] = 0;
        a[3][0] = m[3][0] = 0;
        a[3][1] = m[3][1] = 0;
        a[3][2] = m[3][2] = 0;
        a[3][3] = m[3][3] = 1;

        BigMat(a, n);

        ll b[5][2];

        b[0][0] = 0, b[1][0] = 0;
        b[2][0] = 0, b[3][0] = cc;

        ll temp[5][5];

        mem(temp, 0);
        for(i=0; i<4; i++)
            for(j=0; j<4; j++)
                for(k=0; k<4; k++)
                    temp[i][j] +=
                        a[i][k]*b[k][j];

        printf("Case %d: %lld\n",
                t++, temp[2][0] % mod);
    }
    return 0;
}

```

Matrix Expo - Two Functions

```

/*
f(n+1)= a1*f(n) + b1*f(n-1)+ c1*g(n-2)
g(n+1)= a2*g(n) + b2*g(n-1)+ c2*f(n-2)

|a1 b1 0 0 0 c1 | ^k | f(2) | | f(k+2) |
|1 0 0 0 0 0 | | f(1) | | f(k+1) |
|0 1 0 0 0 0 | | f(0) | | f(k) |
|0 0 c2 a2 b2 0 | * | g(2) | = | g(k+2) |
|0 0 0 1 0 0 | | g(1) | | g(k+1) |
|0 0 0 0 1 0 | | g(0) | | g(k) |
*/

ll M;
ll a1,b1,c1;
ll a2,b2,c2;

ll m[8][8];
ll g[4],f[4];

void mult(ll a[8][8],ll b[8][8])
{
    ll temp[8][8];
    int i,j,k;
    mem(temp,0);
    for(i=0; i<6; i++)
        for(j=0; j<6; j++)
            for(k=0; k<6; k++)
                temp[i][j]+=
                    a[i][k]*b[k][j];
    for(i=0; i<6; i++)
        for(j=0; j<6; j++)
            a[i][j]=temp[i][j]%M;
    return;
}

void BigMat(ll a[8][8],int pos)
{
    int i,j,k;
    if(pos==1)
        return;
    if(pos%2==1)
    {
        BigMat(a,pos-1);
        mult(a,m);
    }
    else
    {
        BigMat(a,pos/2);
        mult(a,a);
    }
    return;
}

```

```

void init(ll a[8][8])
{
    ll i,j,k;
    mem(a,0);
    mem(m,0);
    m[0][0]=a1, m[0][1]=b1, m[0][5]=c1;
    m[1][0]=1, m[2][1]=1;
    m[3][2]=c2, m[3][3]=a2, m[3][4]=b2;
    m[4][3]=1, m[5][4]=1;
    for(i=0;i<6;i++)
        for(j=0;j<6;j++)
            a[i][j]=m[i][j];
}

main()
{
    int t=1,tc;
    cin>>tc;
    ll i,j,k,l,n,r;
    while(tc--)
    {
        cin>>a1>>b1>>c1;
        cin>>a2>>b2>>c2;
        cin>>f[0]>>f[1]>>f[2];
        cin>>g[0]>>g[1]>>g[2];
        cin>>M;

        cin>>r;
        printf("Case %d:\n",t++);

        ll b[8][2],a[8][8],temp[8][2];
        b[0][0]=f[2], b[1][0]=f[1],
        b[2][0]=f[0], b[3][0]=g[2],
        b[4][0]=g[1], b[5][0]=g[0];

        while(r--)
        {
            cin>>n;
            if(n<=2)
            {
                printf("%lld %lld\n",
                    f[n]%M,g[n]%M);
                continue;
            }
            init(a);
            BigMat(a,n);
            mem(temp,0);
            for(i=0; i<6; i++)
                for(j=0; j<1; j++)
                    for(k=0; k<6; k++)
                        temp[i][j]+=
                            a[i][k]*b[k][j];

            printf("%lld %lld\n",
                temp[2][0]%M,temp[5][0]%M);
        }
        return 0;
    }
}

```


Segment Tree [Sum of a segment, update & query]

```

/*
===== [ Input and Operation ] =====
1. 0 x y v - add v to all numbers in the range of x to y (inclusive).
2. 1 x y   - Total sum in x,y
*/

struct data
{
    long long sum;
    long long xtra;
}tree[300010];

void update(int node, int low, int high, int rlow, int rhigh, int value)
{
    if(low>=rlow && high<=rhigh)
    {
        tree[node].sum += (high-low+1)*value;
        tree[node].xtra += value;
        return;
    }
    int left = node*2;
    int right = left+1;
    int mid = (low+high)/2;

    if(rhigh <= mid)
        update(left, low, mid, rlow, rhigh, value);
    else if(rlow > mid)
        update(right, mid+1, high, rlow, rhigh, value);
    else
    {
        update(left, low, mid, rlow, mid, value);
        update(right, mid+1, high, mid+1, rhigh, value);
    }
    tree[node].sum=tree[left].sum+tree[right].sum+tree[node].xtra*(highlow+1);
}

long long query(int node,int low,int high,int rlow,int rhigh,long long carry)
{
    if(low>=rlow && high<=rhigh)
    {
        return tree[node].sum + carry*(high-low+1);
    }
    int left = node*2;
    int right = left + 1;
    int mid = (low + high)/2;

    long long p1=0, p2=0;
    if(rhigh<=mid)
        p1=query(left, low, mid, rlow, rhigh, carry+tree[node].xtra);
    else if(rlow>mid)
        p2=query(right, mid+1, high, rlow, rhigh, carry+tree[node].xtra);

```

```

else
{
    p1=query(left, low, mid, rlow, mid, carry+tree[node].extra);
    p2=query(right, mid+1, high, mid+1, rhigh, carry+tree[node].extra);
}
return p1+p2;
}

main()
{
    ios_base::sync_with_stdio(false);
    int tc, t=1;
    cin>>tc;
    while(tc--)
    {
        int n, q;
        cin>>n>>q;
        printf("Case %d:\n", t++);
        mem(tree, 0);
        while(q--)
        {
            int i, j, k, l;
            cin>>i;
            if(i==0)
            {
                cin>>j>>k>>l;
                update(1, 1, n, j+1, k+1, l);
            }
            else if(i==1)
            {
                cin>>j>>k;
                long long ans=query(1, 1, n, j+1, k+1, 0);
                printf("%lld\n", ans);
            }
        }
    }
    return 0;
}

```

Input:

```

2
10 5
0 0 9 10
1 1 6
0 3 7 2
0 4 5 1
1 5 5
20 3
0 10 12 1
1 11 12
1 19 19

```

Output:

```

Case 1:
60
13
Case 2:
2
0

```

Segment Tree[Maximum sum of a segment,init & query]

```

struct data
{
    int totalsum, maxsum, leftmax, rightmax;
    data(int k)
    {
        totalsum = maxsum = leftmax = rightmax = k;
    }
    data()
    {

    }
}arr[NN];

int a[65010];

data merge(data a, data b)
{
    data ret;
    ret.totalsum = (a.totalsum + b.totalsum);
    ret.maxsum = max(max(a.maxsum, b.maxsum), a.rightmax + b.leftmax);
    ret.leftmax = max(a.leftmax, a.totalsum + b.leftmax);
    ret.rightmax = max(b.rightmax, b.totalsum + a.rightmax);
    return ret;
}

void init(int node, int low, int high)
{
    if(low==high)
    {
        arr[node] = data(a[low]);
        return;
    }
    int left = node*2;
    int right = left + 1;
    int mid = (low + high)/2;

    init(left, low, mid);
    init(right, mid + 1, high);
    arr[node] = merge(arr[left], arr[right]);
    return;
}

data query(int node, int low, int high, int rlow, int rhigh)
{
    if(low>=rlow && high<=rhigh)
        return arr[node];
    int left = node*2;
    int right = left + 1;
    int mid = (low + high)/2;

    if(rhigh<=mid)
        return query(left, low, mid, rlow, rhigh);

```

```

    else if(rlow>mid)
        return query(right, mid + 1, high, rlow, rhigh);
    else
    {
        data L = query(left, low, mid, rlow, mid);
        data R = query(right, mid + 1, high, mid + 1, rhigh);
        return merge(L, R);
    }
}

```

```

main()
{
    ios_base::sync_with_stdio(false);
    int t, tc;
    int i, j, k;
    int res, u,w,p,n,x,y,z,m,q,r,v,zero;
    //cin>>tc;
    while(cin>>n)
    {
        for(i=1;i<=n;i++)
            cin>>a[i];
        init(1, 1, n);
        cin>>k;
        while(k--)
        {
            cin>>x>>y;
            data l = query(1, 1, n, x, y);
            printf("%d\n", l.maxsum);
        }
    }
    return 0;
}

```

```

/*
Input:
3
-1 2 3
1
1 2
Output:
2
*/

```

BIT (Binary Indexed Tree)

*** 1 base indexing

(I) Point Update, Range Query:

Add v at point x : $\text{update}(x, v)$

$\text{Sum}[a, b] = \text{query}(b) - \text{query}(a-1)$

(II) Range Update, Point Query:

Add v at range $[a, b]$: $\text{update}(a, v), \text{update}(b+1, -v)$

Value at point $x = \text{query}(x)$

(III) Range Update, Range Query:

We have to use 2 BIT

Add v at range $[a, b]$: $\text{update}(a, v), \text{update}(b+1, -v),$

$\text{update2}(a, v * (a-1)), \text{update2}(b+1, -v * b)$

$\text{Sum}[0, x] = x * \text{query}(x) - \text{query2}(x)$

$\text{Sum}[a, b] = \text{Sum}[0, b] - \text{Sum}[0, a-1]$

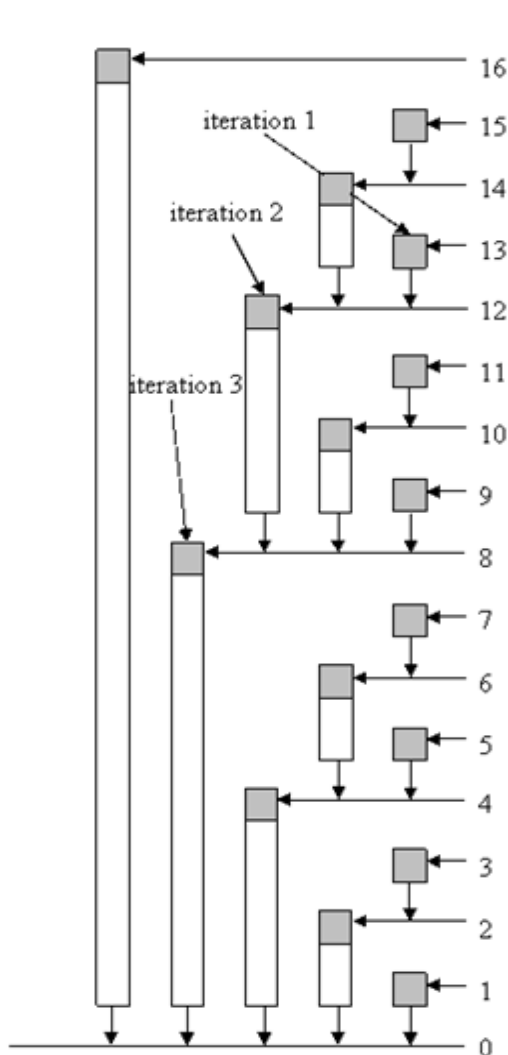
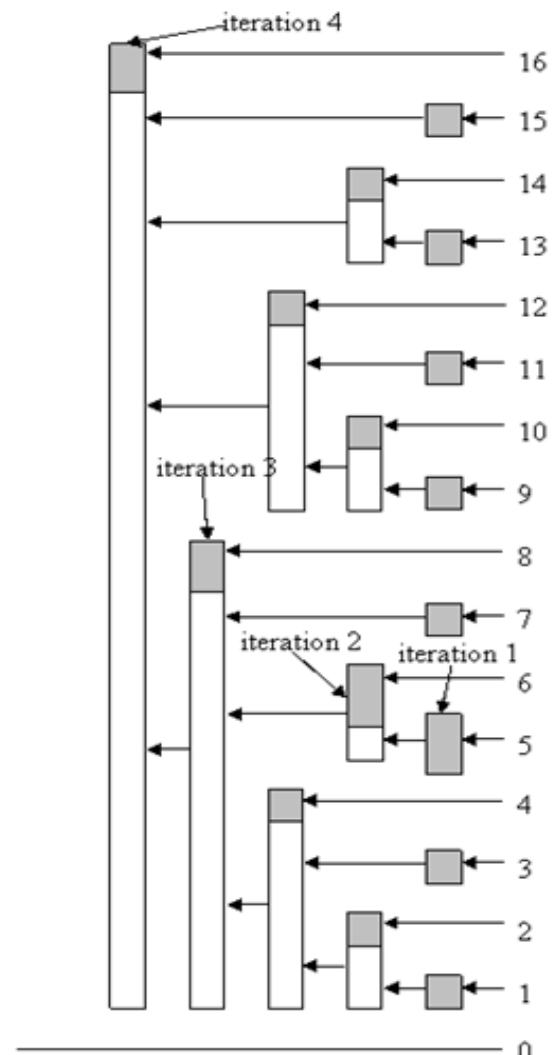


Fig-Query: arrows show path from index to zero which we use to get sum



*Fig-Update: arrows show path while we update tree from index to **MaxVal***

BIT-1 (Point Update, Range Query:)

```
===== [ Theme ] =====
```

```
j=1 => input k      => a[k]=0;
j=2 => input k,value=> a[k]+=value
j=3 => input k,l     =>
      output=a[k]+a[k+1]+...+a[l]
```

```
===== [ END ] =====
```

```
ll MaxVal;

ll tree[NN];
ll arr[NN];

ll update(ll idx,ll val)
{
    while(idx<=MaxVal)
    {
        tree[idx]+=val;
        idx+=idx & (-idx);
    }
    return 0;
}

ll query(ll idx)
{
    ll sum=0;
    while(idx>0)
    {
        sum+=tree[idx];
        idx-=idx & (-idx);
    }
    return sum;
}
```

```
main() {
    int t=1,tc;
    scanf("%d",&tc);
    ll i,j,k,l,m,n;
    while(tc--)
    {
        scanf("%lld %lld",&n,&m);
        mem(tree,0), MaxVal=n;
        for(i=1;i<=n;i++)
        {
            scanf("%lld",&arr[i]);
            update(i,arr[i]);
        }
        printf("Case %d:\n",t++);
        while(m--) {
            scanf("%lld",&j);
            if(j==1) {
                scanf("%lld",&k);
                k++;
                update(k,-arr[k]);
                printf("%lld\n",arr[k]);
                arr[k]=0;
            }
            else if(j==2) {
                scanf("%lld %lld",&k,&l);
                k++;
                update(k,l);
                arr[k]+=l;
            }
            else {
                scanf("%lld %lld",&k,&l);
                k++,l++;
                ll temp=query(l);
                temp-=query(k-1);
                printf("%lld\n",temp);
            }
        }
    }
    return 0;
}
```

BIT - 2D (Points in rectangle)

```

/*
1)=> 0 x y, Add a point in x,y
if a point (x, y) is already
listed, then skip this query.

2)=> 1 x1 y1 x2 y2, Total point
in (x1,y1) to (x2,y2) rectangle
*/

int tree[NN][NN];
bool flag[NN][NN];
int max_x,max_y;

void update(int idx,int idy,int val)
{
    int y;
    while(idx<=max_x)
    {
        y=idy;
        while(y<=max_y)
        {
            tree[idx][y]+=val;
            y+=y & -y;
        }
        idx+=idx & -idx;
    }
    return;
}

int query(int idx,int idy)
{
    int sum=0,y;
    while(idx>0)
    {
        y=idy;
        while(y>0)
        {
            sum+=tree[idx][y];
            y-=y & -y;
        }
        idx-=idx & -idx;
    }
    return sum;
}

```

```

main()
{
    int t=1,tc;
    cin>>tc;
    int i,j,k,l,n;
    int x1,x2,y1,y2;
    int r;
    while(tc--)
    {
        printf("Case %d:\n",t++);
        cin>>n;
        mem(flag,0);
        mem(tree,0);
        max_x=max_y=1001;
        while(n--)
        {
            cin>>j;
            if(j==0)
            {
                cin>>x1>>y1;
                x1++,y1++;
                if(flag[x1][y1]==0)
                {
                    flag[x1][y1]=1;
                    update(x1,y1,1);
                }
            }
            else
            {
                cin>>x1>>y1>>x2>>y2;
                x1++,y1++,x2++,y2++;
                int temp=query(x2,y2);
                temp-=query(x2,y1-1);
                temp-=query(x1-1,y2);
                temp+=query(x1-1,y1-1);
                printf("%d\n",temp);
            }
        }
        return 0;
    }
}

```

LCA (Lowest Common Ancestor)

```

ll par[NN];          //Parent
ll level[NN];        //level in tree
bool color[NN];      //DFS color
ll P[NN][20];        //Sparse table
vector<ll>g[NN];      //Graph store
//1 based index.
void dfs(ll u)
{
    ll i,v;
    color[u]=1;

    for(i=0;i<g[u].size();i++)
    {
        v=g[u][i];
        if(color[v]==0)
        {
            par[v]=u;
            level[v]=level[u]+1;
            dfs(v);
        }
    }
    return;
}

ll lca_query(ll p,ll q)
{
    if(level[p]<level[q])
        swap(p,q);
    ll i,j,k,log;
    log=1;
    while(1)
    {
        ll next=log+1;
        if(1<<next >level[p])
            break;
        log++;
    }
    for(i=log;i>=0;i--)
        if(level[p]-(1<<i) >= level[q])
            p=P[p][i];
    if(p==q)
        return p;
    for(i=log;i>=0;i--)
        if(P[p][i]!=-1 &&
P[p][i]!=P[q][i])
            p=P[p][i],q=P[q][i];
    return par[p];
}

```

```

void lca_init(ll n)
{
    mem(color,0);
    mem(P,-1);
    level[1]=0;
    dfs(1);

    ll i,j;

    for(i=1;i<=n;i++)
        P[i][0]=par[i];

    for(j=1;1<<j <= n;j++)
        for(i=1;i<=n;i++)
            if(P[i][j-1]!=-1)
                P[i][j]=P[P[i][j-1]][j-1];

    return;
}

main()
{
    int t=1,tc;
    scanf("%d",&tc);
    ll i,j,k,l,n,r;
    while(tc--)
    {
        scanf("%lld",&n);
        for(i=0;i<=n;i++)
            g[i].clear();

        for(i=0;i<n-1;i++)
        {
            scanf("%lld %lld",&k,&l);
            g[k].pb(l);
            g[l].pb(k);
        }
        lca_init(n);

        cin>>r;
        while(r--)
        {
            cin>>k>>l;
            cout<<lca_query(k,l)<<"\n";
        }
        puts("");
    }
    return 0;
}

```


LCA (Lowest Common Ancestor)

```

/*
DIST a b : ask for the distance between
node a and node b
KTH a b k : ask for the k-th node on
the path from node a to node b
*/
ll par[NN], level[NN], dist[NN];
bool color[NN]; //DFS color
ll P[NN][20]; //Sparse table
vector<ll>g[NN], cost[NN];

void dfs(ll u)
{
    ll i, v;
    color[u]=1;
    for(i=0; i<g[u].size(); i++)
    {
        v=g[u][i];
        if(color[v]==0)
        {
            par[v]=u;
            level[v]=level[u]+1;
            dist[v]=dist[u]+cost[u][i];
            dfs(v);
        }
    }
    return;
}

ll lca_query(ll p, ll q)
{
    if(level[p]<level[q]) swap(p, q);
    ll i, j, k, log;
    log=1;
    while(1)
    {
        ll next=log+1;
        if(1<<next >level[p]) break;
        log++;
    }
    for(i=log; i>=0; i--)
        if(level[p]-(1<<i) >= level[q])
            p=P[p][i];
    if(p==q)
        return p;
    for(i=log; i>=0; i--)
        if(P[p][i]!=-1&&P[p][i]!=P[q][i])
            p=P[p][i], q=P[q][i];
    return par[p];
}

```

```

void lca_init(ll n)
{
    mem(color, 0), mem(P, -1);
    level[1]=0, dist[1]=0;
    dfs(1);
    ll i, j;

    for(i=1; i<=n; i++)
        P[i][0]=par[i];

    for(j=1; 1<<j <= n; j++)
        for(i=1; i<=n; i++)
            if(P[i][j-1]!=-1)
                P[i][j]=P[P[i][j-1]][j-1];
    return;
}

ll DIST(ll p, ll q)
{
    ll temp=dist[p]+dist[q];
    ll node=lca_query(p, q);
    temp-=2*dist[node];
    return temp;
}

ll KTH(ll p, ll q, ll k)
{
    k--;
    int i, j;
    ll node=lca_query(p, q);
    ll temp=level[p]-level[node];
    if(temp>=k)
    {
        ll LVL=level[p]-k;
        for(j=20; j>=0; j--)
            if(level[p]-(1<<j)>=LVL)
                p=P[p][j];
        return p;
    }
    k-=temp;
    temp=level[q]-level[node];
    temp-=k;
    ll LVL=level[q]-temp;
    for(j=15; j>=0; j--)
        if(level[q]-(1<<j)>=LVL)
            q=P[q][j];
    return q;
}

```

```

char s[10];

main() {
    int t=1,tc;
    scanf("%d",&tc);
    ll i,j,k,l,n,r;
    while(tc--) {
        scanf("%lld",&n);
        for(i=0;i<=n;i++) {
            g[i].clear();
            cost[i].clear();
        }

        for(i=0;i<n-1;i++) {
            scanf("%lld %lld %lld",&k,&l,&r);
            g[k].pb(l);
            g[l].pb(k);
            cost[k].pb(r);
            cost[l].pb(r);
        }
        lca_init(n);
        while(1) {
            scanf("%s",s);
            if(strcmp(s,"DONE")==0)
                break;
            if(strcmp(s,"DIST")==0) {
                scanf("%lld %lld",&k,&l);
                ll ret=DIST(k,l);
                printf("%lld\n",ret);
            }
            else {
                scanf("%lld %lld %lld",&k,&l,&r);
                ll ret=KTH(k,l,r);
                printf("%lld\n",ret);
            }
        }
    }
    return 0;
}

```

```

input:
1

6
1 2 1
2 4 1
2 5 2
1 3 1
3 6 2
DIST 4 6
KTH 4 6 4
DONE

```

```

Output:
5
3

```

Trie

```

struct node
{
    bool endmark;
    node *next[26+1];
    node()
    {
        endmark=false;
        for(int i=0; i<26; i++)
            next[i]=NULL;
    }
}*root;

void insert(char *str,int len)
{
    node *curr=root;
    for(int i=0; i<len; i++)
    {
        int id=str[i]-'a';
        if(curr->next[id]==NULL)
            curr->next[id]=new node();
        curr=curr->next[id];
    }
    curr->endmark=true;
}

bool search(char *str,int len)
{
    node *curr=root;
    for(int i=0; i<len; i++)
    {
        int id=str[i]-'a';
        if(curr->next[id]==NULL)
            return false;
        curr=curr->next[id];
    }
    return curr->endmark;
}

void del(node *cur)
{
    for(int i=0; i<26; i++)
        if(cur->next[i])
            del(cur->next[i]) ;

    delete(cur) ;
}

```

```

int main()
{
    puts("ENTER NUMBER OF WORDS");
    root=new node();
    int num_word;
    cin>>num_word;
    for(int i=1; i<=num_word; i++)
    {
        char str[50];
        scanf("%s",str);
        insert(str,strlen(str));
    }
    puts("ENTER NUMBER OF QUERY");
    int query;
    cin>>query;
    for(int i=1; i<=query; i++)
    {
        char str[50];
        scanf("%s",str);
        if(search(str,strlen(str)))
            puts("FOUND");
        else
            puts("NOT FOUND");
    }
    del(root); //destroy trie;
    return 0;
}

```

Bitmask DP (No of Permutation of distinct number)

```
/*
===== [ Theme ] =====
LightOj: Painful Bases.

you are given a base, an integer K
and
a valid number in the base which
contains distinct digits.
output number of permutations of the
given number
which are divisible by K. K is given
in decimal.
*/
long long dp[66000][20];
char a[20];
int n,k,l;

int modul(char ch,int carry) {
    int x;
    if(ch>='0' &&ch<='9') x=ch-'0';
    else x=ch-'A'+10;
    x+=carry*n;
    x=x%k;
    return x;
}

long long call(int pos,int mod) {
    if(pos==(1<<l)-1) {
        if(mod==0) return 1;
        else return 0;
    }
    long long &t=dp[pos][mod];
    if(t!=-1) return t;
    long long sum=0;
    for(int i=0;i<l;i++) {
        if(!(pos&1<<i)) {
            int x=modul(a[i],mod);
            sum+=call(pos|1<<i,x);
        }
    }
    t=sum;
    return sum;
}

main() {
    int tc,t=1;
    scanf("%d",&tc);
    while(tc--) {
        scanf("%d%d",&n,&k);
        getchar();
        gets(a);
        memset(dp,-1,sizeof(dp));
        l=strlen(a);
        long long sum=call(0,0);
        printf("Case %d: %lld\n",t++,sum);
    }
    return 0;
}
```

Bitmask DP (No of Permutation of repeat numbers)

```
/*
===== [ Theme ] =====
LightOj: Anagram Division

Given a string s and a positive integer d,
determine how many permutations of s are
divisible by d.
Numbers can be repeated.
*/
int dp[1050][1050];
char arr[20];
int n,N;

int go(int mask,int mod) {
    if(mask==(1<<N)-1) {
        if(mod==0)
            return 1;
        else
            return 0;
    }
    int &t=dp[mask][mod];
    if(t!=-1)
        return t;
    int sum=0;
    int i,k;
    for(i=0; i<N; i++)
    {
        if(!(mask&1<<i))
            if(i==0||arr[i]!=arr[i-1]
                ||(mask&1<<(i-1)))
            {
                sum+=go(mask|1<<i,
                    (mod*10+arr[i]-'0')%n);
            }
    }
    t=sum;
    return sum;
}

main()
{
    int t=1,tc;
    scanf("%d",&tc);
    while(tc--)
    {
        scanf("%s %d",&arr,&n);
        N=strlen(arr);
        sort(arr,arr+N);
        memset(dp,-1,sizeof(dp));
        int sum=go(0,0);
        printf("Case %d: %d\n",t++,sum);
    }
    return 0;
}
```

DP (no of distinc LCS)

```
/*
===== [ Theme ] =====
LightOj: LCS Revisited

find the number of distinct LCS of s and
t. modulo 1000007.
*/
int dp[1010][1010];
int dp2[1010][1010];
char a[1010], b[1010];
int mid, ans, sum;
int N, K, S;
int LCS(int i, int j) {
    if(i < 0 || j < 0) return 0;
    int &t = dp2[i][j];
    if(t != -1) return t;
    int ret = 0;
    if(a[i] == b[j]) ret = LCS(i-1, j-1) + 1;
    else {
        ret = LCS(i, j-1);
        ret = max(ret, LCS(i-1, j));
    }
    t = ret;
    return t;
}

int go(int i, int j) {
    if(i < 0 || j < 0) return 0;
    int &t = dp[i][j];
    if(t != -1) return t;
    int ret = 0;
    if(a[i] == b[j]) {
        if(LCS(i, j) == 1)
            return 1;
        else
            ret = go(i-1, j-1);
    }
    else {
        int n = LCS(i-1, j);
        int m = LCS(i, j-1);
        if(n == m) {
            ret = (ret + go(i-1, j) % mod) % mod;
            ret = (ret + go(i, j-1) % mod) % mod;
            if(LCS(i, j) == LCS(i-1, j-1))
                ret = ((ret - go(i-1, j-1))
                    % mod + mod) % mod;
        }
        else if(n > m)
            ret = go(i-1, j);
        else if(n < m)
            ret = go(i, j-1);
    }
    t = ret;
    return t;
}

n = strlen(a);
l = strlen(b);
Answer = go(n-1, l-1);
```

DP (No. of ways to the pallindrome)

```
/*
===== [ Theme ] =====
LightOj: The Specials Menu

number of ways he could remove
letters
from a particular word so that it
would become a palindrome.
*/

long long dp[70][70];
int I, J, K, L, N;
char a[70];
long long go(int i, int j)
{
    if(i > j)
    {
        return 0;
    }
    long long &t = dp[i][j];
    if(t != -1)
        return t;
    long long ret = 0;
    ret = go(i+1, j);
    ret += go(i, j-1);
    if(a[i] == a[j])
        ret += go(i+1, j-1) + 1;
    t = ret;
    return t;
}

main()
{
    int t = 1, tc;
    scanf("%d", &tc);
    getchar();
    while(tc--)
    {
        memset(dp, -1, sizeof(dp));
        int n, k, l, i;
        gets(a);
        l = strlen(a);
        long long sum = go(0, l-1);
        printf("Case %d: %lld\n", t++, sum);
    }
    return 0;
}
```

DP-Coin Change (Limited Coin)

```
/*
===== [ Theme ] =====
n types of coins of value A1, A2 ... An.
C1, C2, ... Cn denote the number of
coins of value A1, A2 ... An.
find the number of ways you can make K
using the coins.

*/
int n,k;
int tc[51];
int coin[51];
long long dp[51][1001];

long long check(int i, int amount)
{
    int j;
    long long y=0;
    if(i>=n)
    {
        if(amount==k)
            return 1;
        else
            return 0;
    }
    long long &t=dp[i][amount];
    if(t!=-1)
        return t;

    y=check(i+1,amount)%mod;
    for(j=1;j<=tc[i];j++)
    {
        if(amount+coin[i]*j<=k)
            y+=check(i+1,
                amount+coin[i]*j)%mod;
    }
    return t=y%mod;
}

main()
{
    int i,j,t;
    long long m;
    scanf("%d",&t);
    for(i=1;i<=t;i++)
    {
        memset(dp,-1,sizeof(dp));
        scanf("%d %d",&n,&k);
        for(j=0;j<n;j++)
            scanf("%d",&coin[j]);
        for(j=0;j<n;j++)
            scanf("%d",&tc[j]);
        m=(check(0,0))%mod;
        printf("Case %d: %lld\n",i,m);
    }
    return 0;
}
```

LCS of K strings

```
/*
Lcs of K strings.
each string initially contains
element from 1 to n.
1<=K<=5.
Solution: Golam Mazid Vai.

*/

#define eps 1e-9
#define Pi 2*acos(0)
#define inf 1<<30
#define mod 1000000007
#define Sz 100005

int dp[1005][1005];
int A[10][10005],B[10][1005];
int f(int v,int p,int n,int k)
{
    if(p>n)
        return 0;
    if(dp[v][p]!=-1)
        return dp[v][p];
    int c=0,d,i;
    c=f(v,p+1,n,k);
    d=B[1][p];
    for(i=2,i<=k;i++)
    {
        if(A[i][d]>A[i][v])
            continue;
        break;
    }
    if(i>k)
        c=Max(c,f(d,p+1,n,k)+1);
    return dp[v][p]=c;
}

int main()
{
    LL n,k,i,j,a;
    while(cin>>n>>k)
    {
        mem(dp,-1);
        for(i=1,i<=k;i++)
        {
            for(j=1,j<=n;j++)
            {
                cin>>a;
                A[i][a]=j;
                B[i][j]=a;
            }
        }
        printf("%d\n",f(0,1,n,k));
    }
    return 0;
}
```

BIT (All possible Increasing Subsequences)

```
/*
An increasing subsequence from a
sequence A1, A2 ... An is defined by
Ai1, Ai2 ... Aik,
where the following properties hold
1.      i1 < i2 < i3 < ... < ik and
2.      Ai1 < Ai2 < Ai3 < ... < Aik
Now you are given a sequence, you have
to find the number of all possible
increasing subsequences.

*/

ll MaxVal;

ll tree[NN];
pair<ll,ll> a[NN];
ll b[NN];

ll update(ll idx,ll val)
{
    while(idx<=MaxVal)
    {
        tree[idx]=(tree[idx]+val)%mod;
        idx+=idx & (-idx);
    }
    return 0;
}

ll query(ll idx)
{
    ll sum=0;
    while(idx>0)
    {
        sum=(sum+tree[idx])%mod;
        idx-=idx & (-idx);
    }
    return sum;
}
```

```
main()
{
    int t=1,tc;
    cin>>tc;

    ll i,j,k,l,m,n;
    while(tc--)
    {
        cin>>n;

        for(i=1;i<=n;i++)
        {
            cin>>a[i].ft;
            a[i].second=i;
        }
        sort(a+1,a+n+1);
        memset(tree,0,sizeof(ll)*(n+2));

        b[0]=0;
        b[a[1].sd]=1;
        for(i=2;i<=n;i++)
        {
            if(a[i].ft==a[i-1].ft)
                b[a[i].sd]=b[a[i-1].sd];
            else
                b[a[i].sd]=b[a[i-1].sd]+1;
        }

        ll ret=0;
        MaxVal=b[a[n].sd];
        for(i=1;i<=n;i++)
        {
            ret=(query(b[i]-1)+1)%mod;
            update(b[i],ret);
        }
        printf("Case %d: %lld\n",t++,query(MaxVal));
    }
    return 0;
}
```

the_redback

Code Library

Maruf Tuhin
CUET CSE 11
maruf.2hin@gmail.com

By Maruf_Tuhin