

Nth Fibonacci Numbers in O(log n) complexity:

$$\begin{pmatrix} 0 & 1 \\ 1 & 1 \end{pmatrix}^n = \begin{pmatrix} F_{n-1} & F_n \\ F_n & F_{n+1} \end{pmatrix}$$

```
void multiply(int F[2][2], int M[2][2])
{
    int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
    int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
    int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
    int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

    F[0][0] = x;
    F[0][1] = y;
    F[1][0] = z;
    F[1][1] = w;
}

void power(int F[2][2], int n)
{
    if( n == 0 || n == 1)
        return;
    int M[2][2] = {{1,1},{1,0}};

    power(F, n/2);
    multiply(F, M);

    if (n%2 != 0)
        multiply(F, M);
}

int fib(int n)
{
    int F[2][2] = {{1,1},{1,0}};
    if (n == 0)
        return 0;
    power(F, n-1);
    return F[0][0];
}
```