

$$\mathbb{P}\big(\xi^{-1}(S)\big) = \mathbb{P}(\{\omega \in \Omega | \xi(\omega) \in S\}) =: \mathbb{P}_{\xi}(S)$$