

Svanberg's (strict) conservatism

QP subproblem at x^k :

$$x^k = 0.500$$

$$F^k = -0.175$$

$$d_x^k F = -18.413$$

$$dd_x^k F = 73.650$$

$$\alpha_F = 1.000$$

$$G^k = -0.239$$

$$d_x^k G = 2.303$$

$$dd_x^k G = 9.213$$

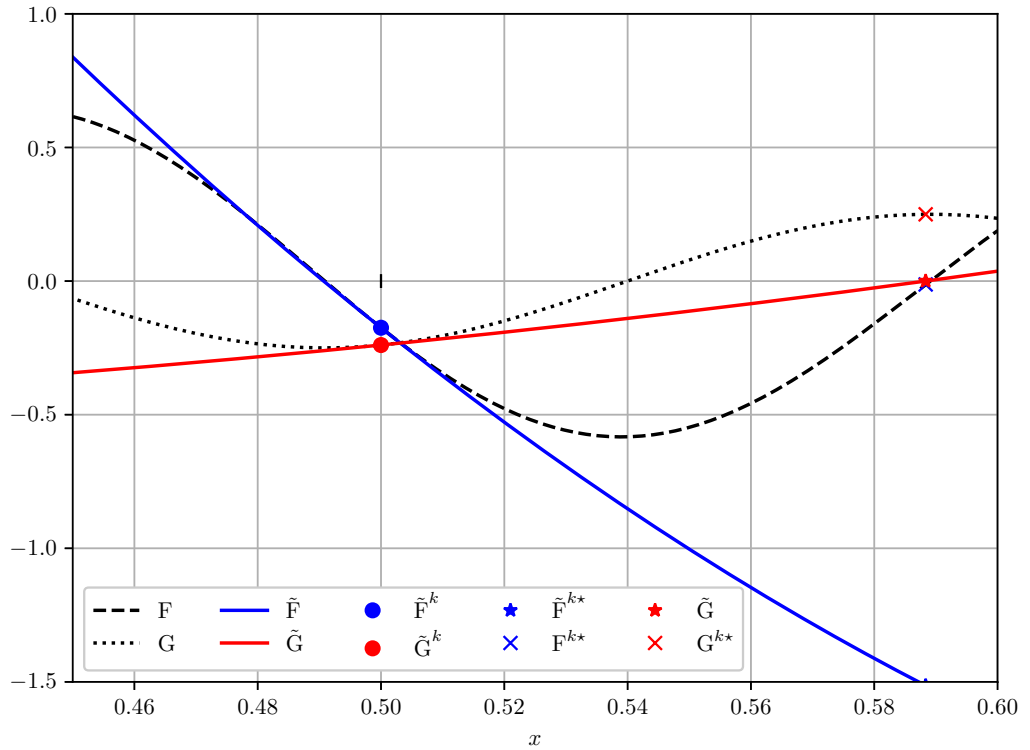
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k*} = 3.820$$

at the solution

$$x^{k*} = 0.588$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -1.514$$

$$\tilde{G}^{k*} = -0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.013$$

$$G^{k*} = 0.250$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

→ the value of the constraint function approximation is less than the actual function value, at the new design point, $\tilde{G}^{k*} < G^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.500$$

$$F^k = -0.175$$

$$d_x^k F = -18.413$$

$$dd_x^k F = 73.650$$

$$\alpha_F = 2.000$$

$$G^k = -0.239$$

$$d_x^k G = 2.303$$

$$dd_x^k G = 9.213$$

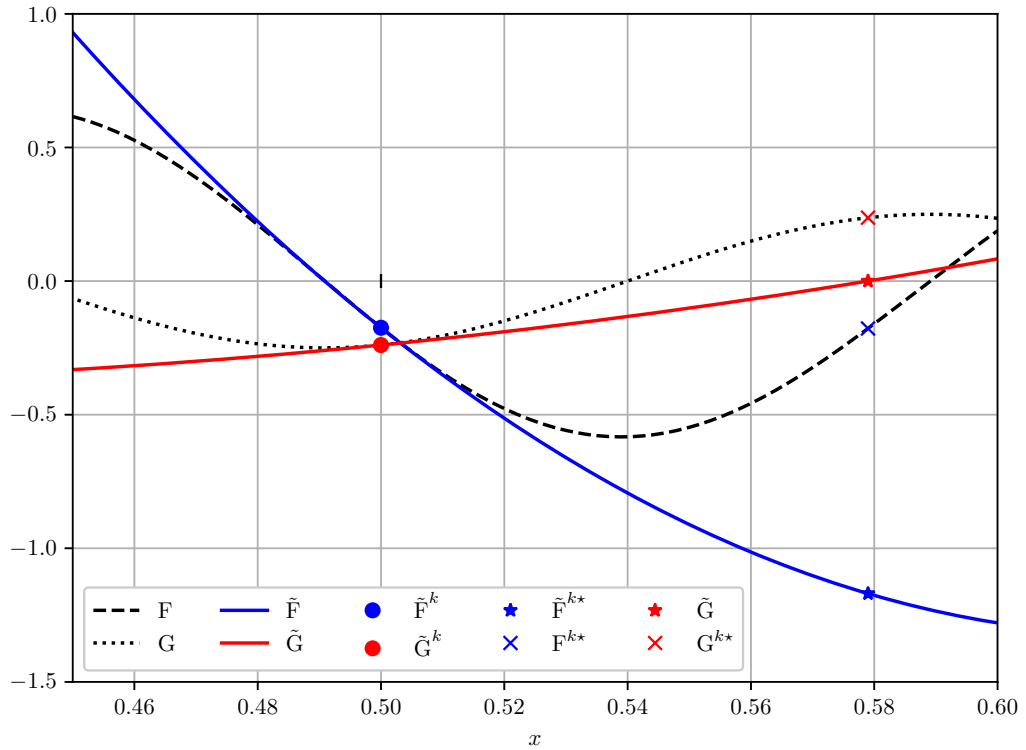
$$\alpha_G = 2.000$$

with Lagrange multiplier

$$\lambda^{k*} = 1.803$$

at the solution

$$x^{k*} = 0.579$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -1.169$$

$$\tilde{G}^{k*} = 0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.177$$

$$G^{k*} = 0.237$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

→ the value of the constraint function approximation is less than the actual function value, at the new design point, $\tilde{G}^{k*} < G^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.500$$

$$F^k = -0.175$$

$$d_x^k F = -18.413$$

$$dd_x^k F = 73.650$$

$$\alpha_F = 4.000$$

$$G^k = -0.239$$

$$d_x^k G = 2.303$$

$$dd_x^k G = 9.213$$

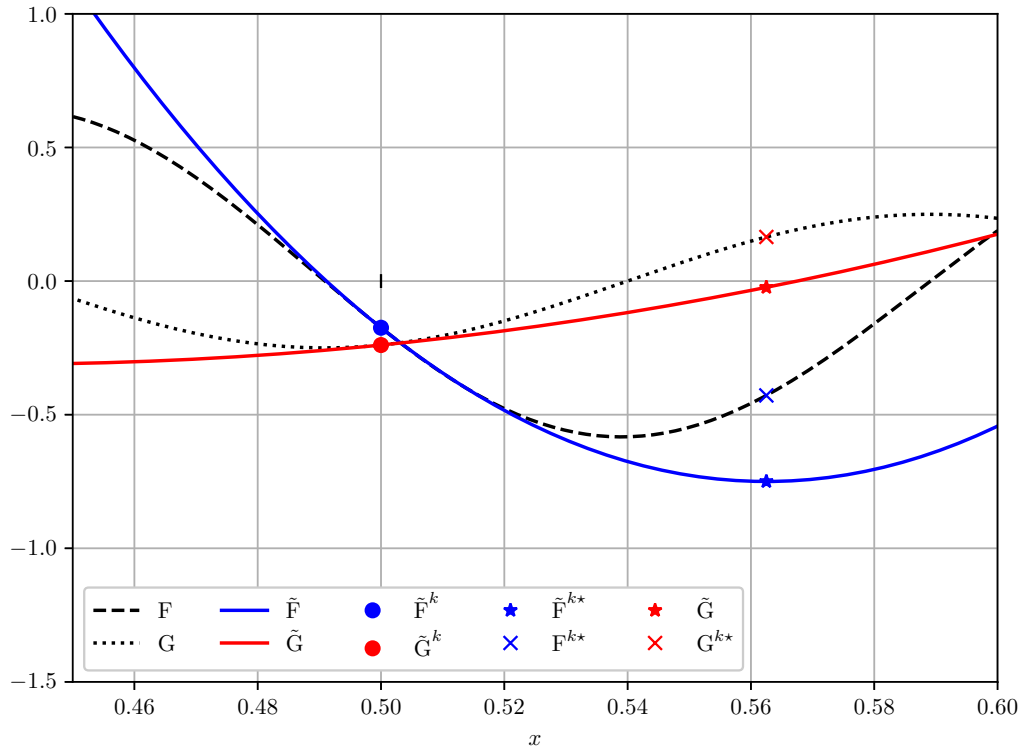
$$\alpha_G = 4.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.562$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.750$$

$$\tilde{G}^{k*} = -0.023$$

while the actual functions are evaluated to be

$$F^{k*} = -0.428$$

$$G^{k*} = 0.165$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

→ the value of the constraint function approximation is less than the actual function value, at the new design point, $\tilde{G}^{k*} < G^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.500$$

$$F^k = -0.175$$

$$d_x^k F = -18.413$$

$$dd_x^k F = 73.650$$

$$\alpha_F = 8.000$$

$$G^k = -0.239$$

$$d_x^k G = 2.303$$

$$dd_x^k G = 9.213$$

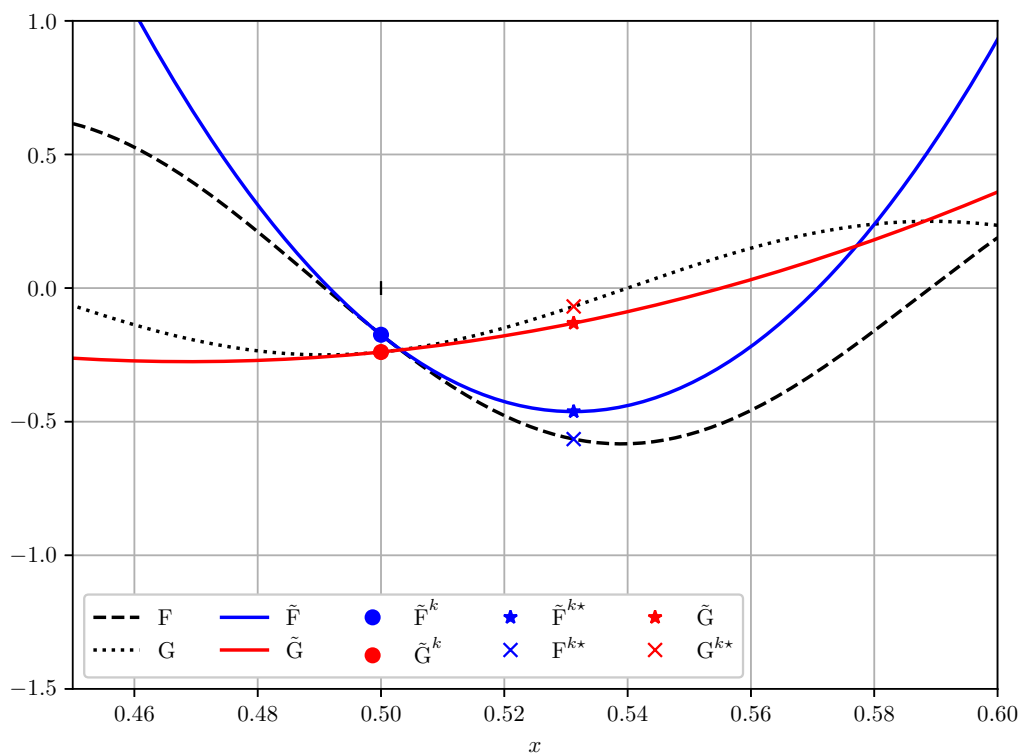
$$\alpha_G = 8.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.531$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.462$$

$$\tilde{G}^{k*} = -0.131$$

while the actual functions are evaluated to be

$$F^{k*} = -0.565$$

$$G^{k*} = -0.069$$

The solution leads to a feasible descent step and is therefore deemed *acceptable*, as is.

(Note that the objective and/or constraint function approximation is not conservative in this case.)

QP subproblem at x^k :

$$x^k = 0.531$$

$$F^k = -0.565$$

$$d_x^k F = -4.611$$

$$dd_x^k F = 17.360$$

$$\alpha_F = 1.000$$

$$G^k = -0.069$$

$$d_x^k G = 7.691$$

$$dd_x^k G = 28.955$$

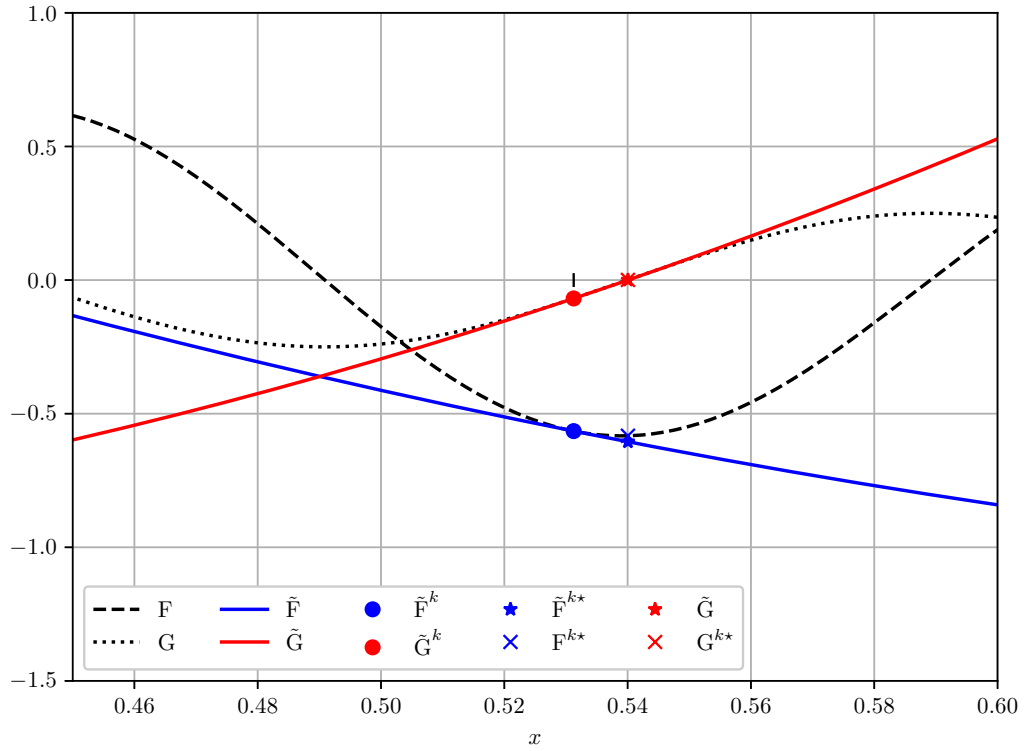
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.561$$

at the solution

$$x^{k*} = 0.540$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.605$$

$$\tilde{G}^{k*} = 0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = 0.001$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

→ the value of the constraint function approximation is less than the actual function value, at the new design point, $\tilde{G}^{k*} < G^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.531$$

$$F^k = -0.565$$

$$d_x^k F = -4.611$$

$$dd_x^k F = 17.360$$

$$\alpha_F = 2.000$$

$$G^k = -0.069$$

$$d_x^k G = 7.691$$

$$dd_x^k G = 28.955$$

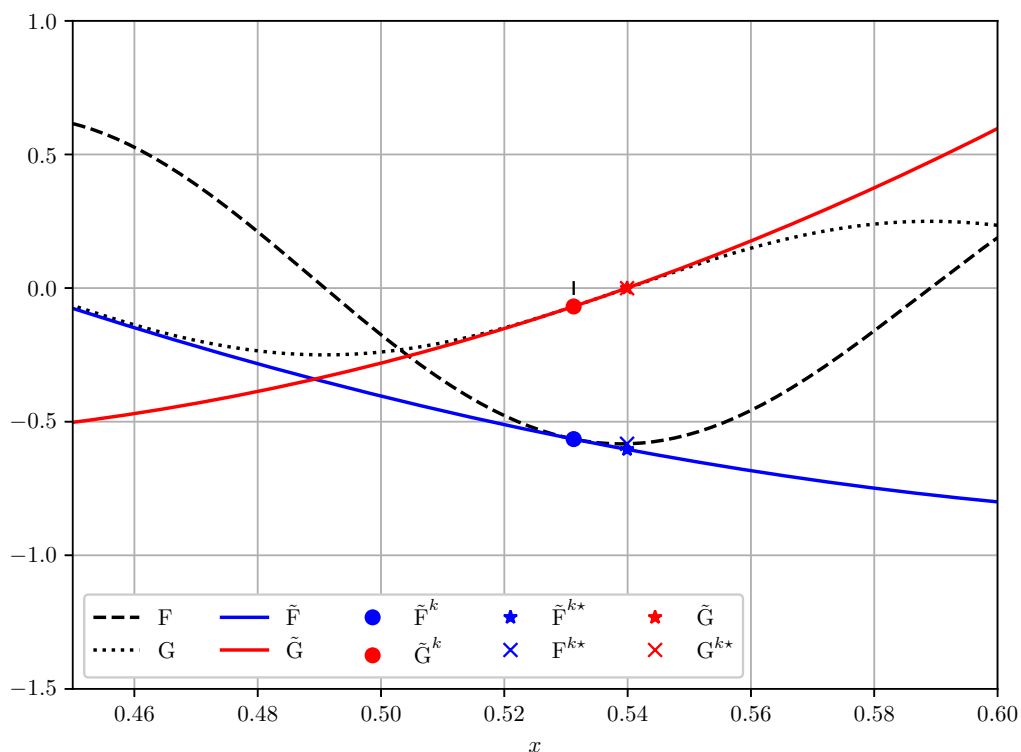
$$\alpha_G = 2.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.526$$

at the solution

$$x^{k*} = 0.540$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.604$$

$$\tilde{G}^{k*} = 0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = -0.000$$

The solution leads to a feasible descent step and is therefore deemed *acceptable*, as is.

(Note that the objective and/or constraint function approximation is not conservative in this case.)

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 1.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

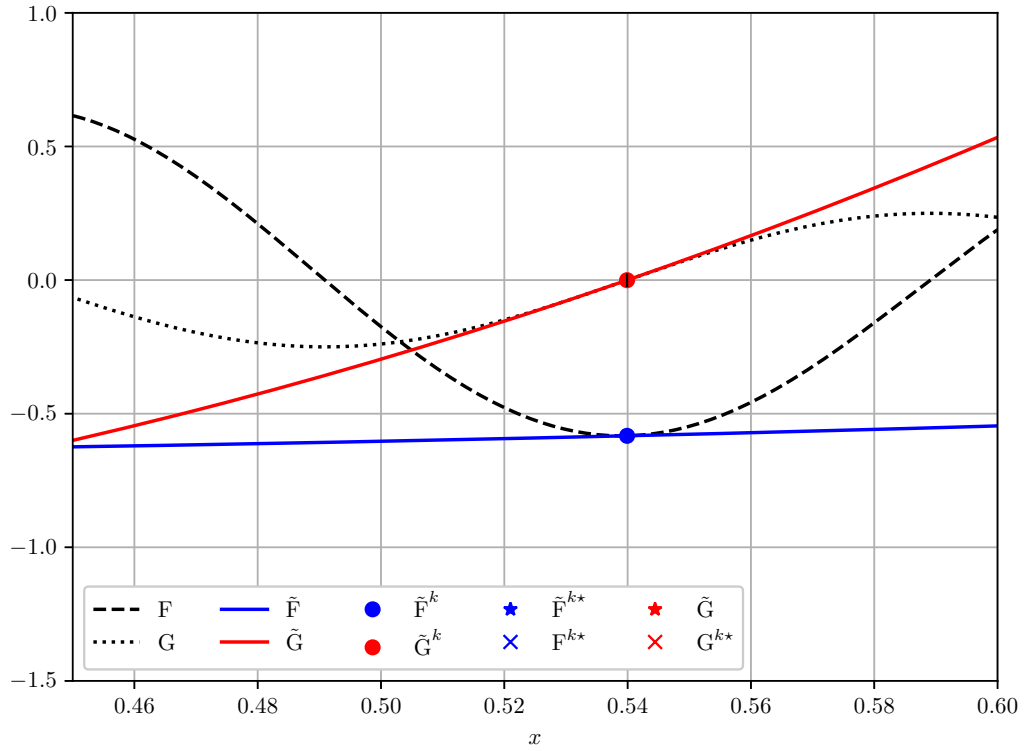
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.440$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.628$$

$$\tilde{G}^{k*} = -0.652$$

while the actual functions are evaluated to be

$$F^{k*} = 0.643$$

$$G^{k*} = 0.015$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

→ the value of the constraint function approximation is less than the actual function value, at the new design point, $\tilde{G}^{k*} < G^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 2.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

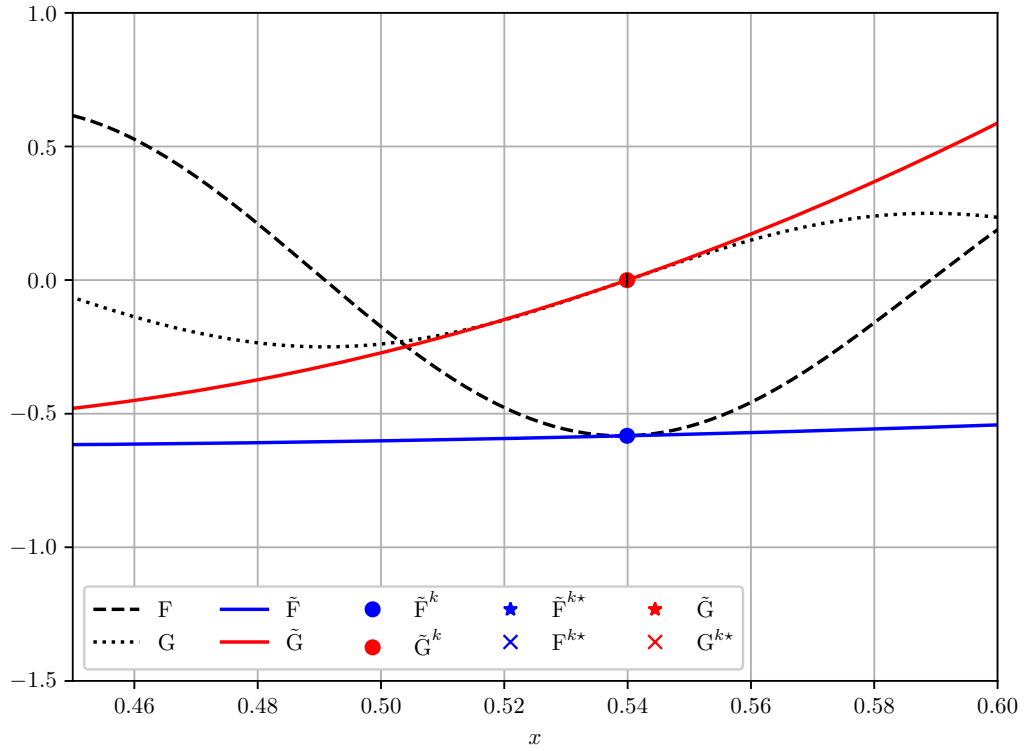
$$\alpha_G = 2.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.440$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.618$$

$$\tilde{G}^{k*} = -0.504$$

while the actual functions are evaluated to be

$$F^{k*} = 0.643$$

$$G^{k*} = 0.015$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

→ the value of the constraint function approximation is less than the actual function value, at the new design point, $\tilde{G}^{k*} < G^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 4.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

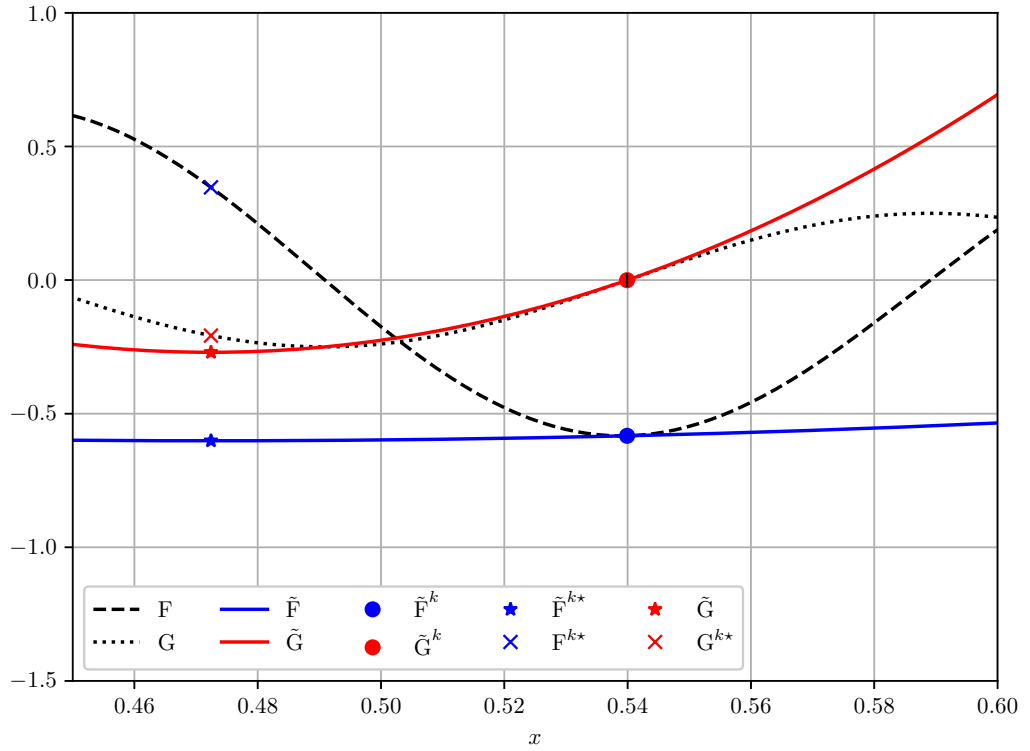
$$\alpha_G = 4.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.472$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.601$$

$$\tilde{G}^{k*} = -0.270$$

while the actual functions are evaluated to be

$$F^{k*} = 0.347$$

$$G^{k*} = -0.208$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

→ the value of the constraint function approximation is less than the actual function value, at the new design point, $\tilde{G}^{k*} < G^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 8.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

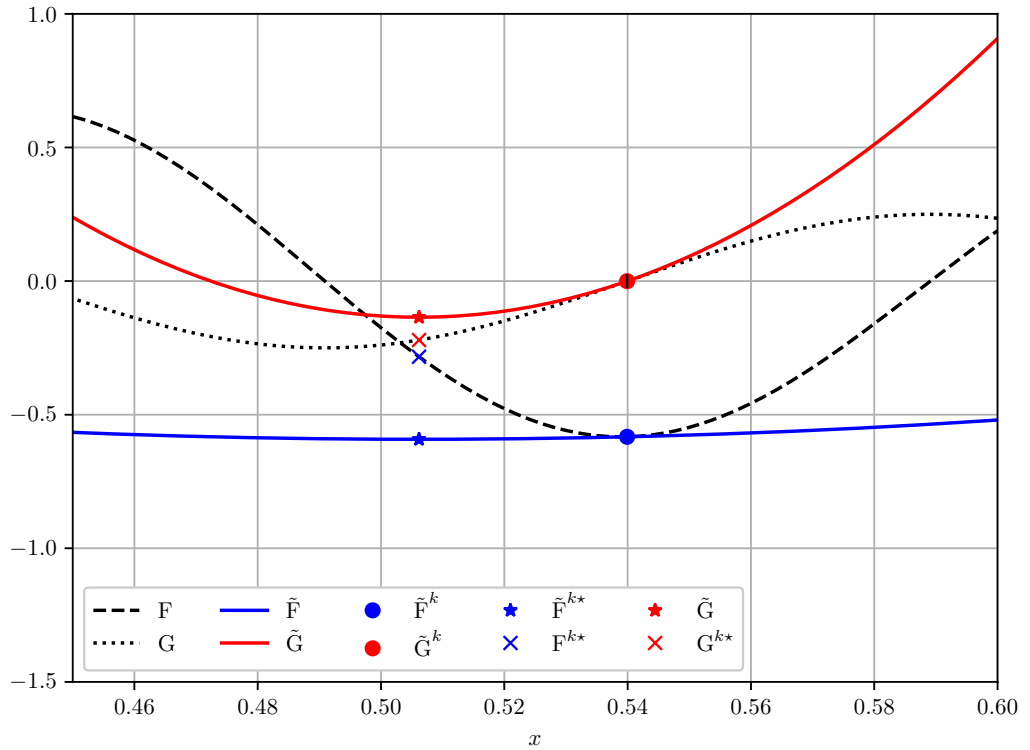
$$\alpha_G = 8.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.506$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.592$$

$$\tilde{G}^{k*} = -0.135$$

while the actual functions are evaluated to be

$$F^{k*} = -0.283$$

$$G^{k*} = -0.221$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 16.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

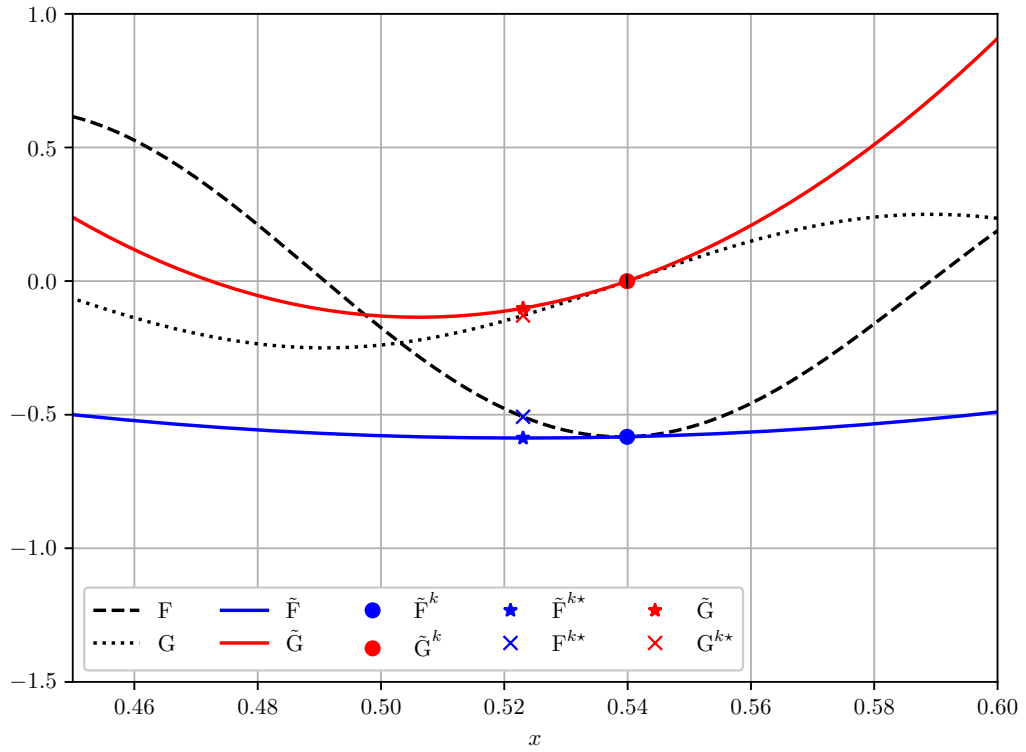
$$\alpha_G = 8.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.523$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.587$$

$$\tilde{G}^{k*} = -0.102$$

while the actual functions are evaluated to be

$$F^{k*} = -0.508$$

$$G^{k*} = -0.129$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 32.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

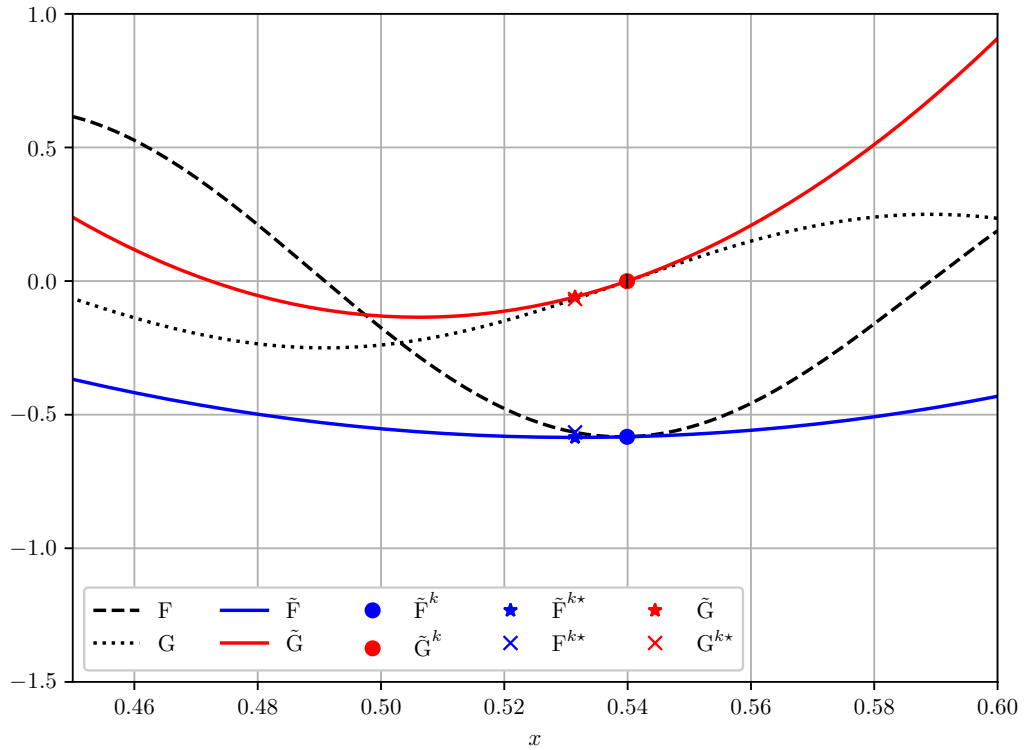
$$\alpha_G = 8.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.531$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.585$$

$$\tilde{G}^{k*} = -0.059$$

while the actual functions are evaluated to be

$$F^{k*} = -0.566$$

$$G^{k*} = -0.067$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 64.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

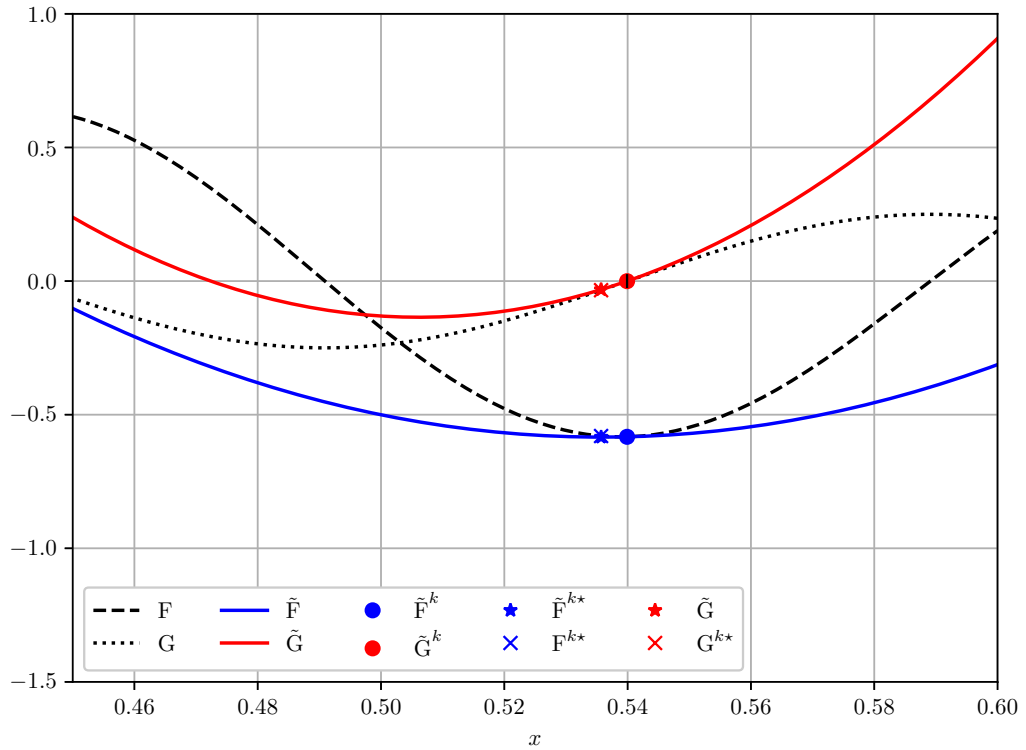
$$\alpha_G = 8.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.536$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.584$$

$$\tilde{G}^{k*} = -0.032$$

while the actual functions are evaluated to be

$$F^{k*} = -0.580$$

$$G^{k*} = -0.034$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 128.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

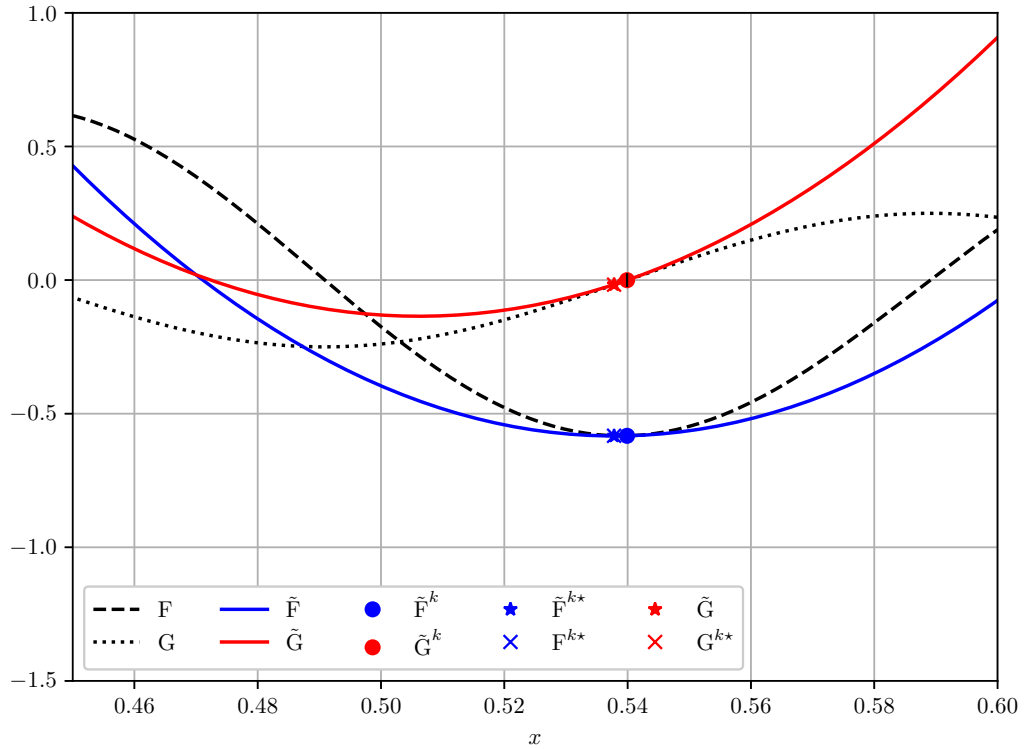
$$\alpha_G = 8.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.538$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.583$$

$$\tilde{G}^{k*} = -0.017$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = -0.017$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.540$$

$$F^k = -0.583$$

$$d_x^k F = 0.553$$

$$dd_x^k F = 2.049$$

$$\alpha_F = 256.000$$

$$G^k = -0.000$$

$$d_x^k G = 8.000$$

$$dd_x^k G = 29.634$$

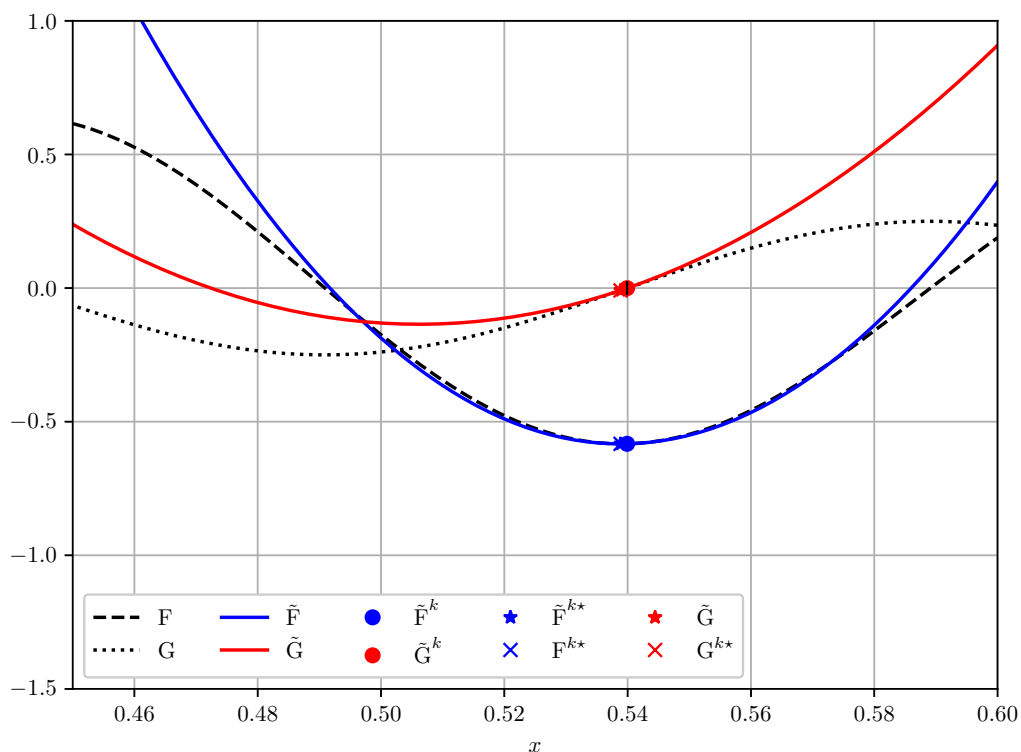
$$\alpha_G = 8.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.000$$

at the solution

$$x^{k*} = 0.539$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.583$$

$$\tilde{G}^{k*} = -0.009$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = -0.009$$

The solution leads to a feasible descent step and is therefore deemed *acceptable*, as is.

(Note that the objective and/or constraint function approximation is not conservative in this case.)

QP subproblem at x^k :

$$x^k = 0.539$$

$$F^k = -0.583$$

$$d_x^k F = -0.076$$

$$dd_x^k F = 0.284$$

$$\alpha_F = 1.000$$

$$G^k = -0.009$$

$$d_x^k G = 7.995$$

$$dd_x^k G = 29.674$$

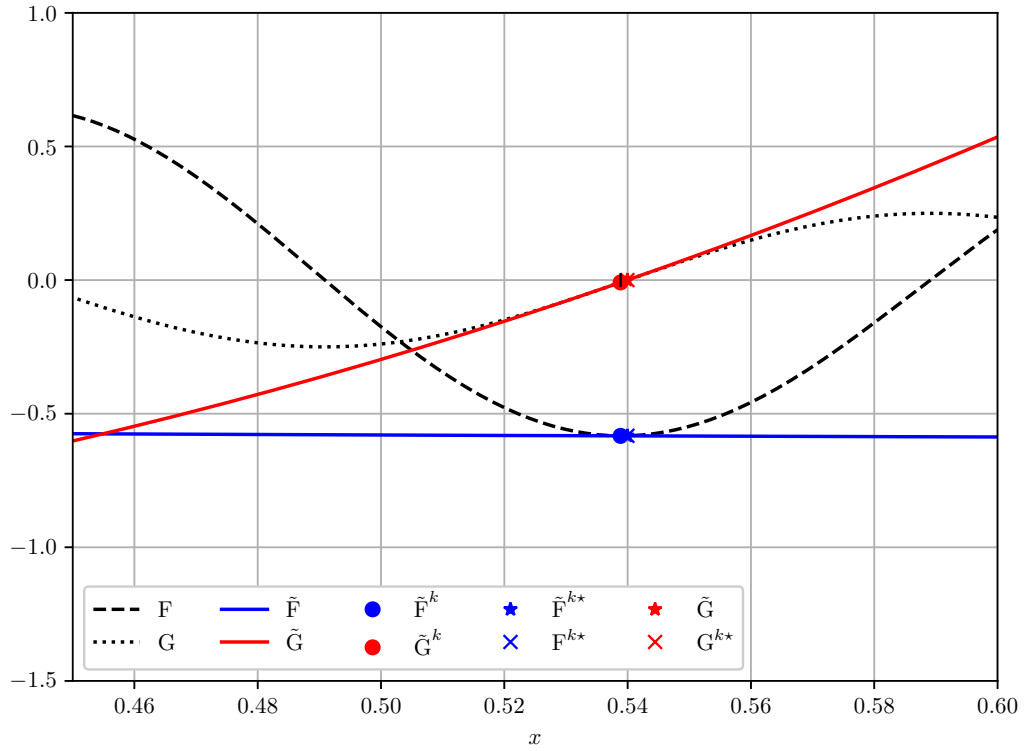
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.009$$

at the solution

$$x^{k*} = 0.540$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.583$$

$$\tilde{G}^{k*} = 0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = -0.000$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.539$$

$$F^k = -0.583$$

$$d_x^k F = -0.076$$

$$dd_x^k F = 0.284$$

$$\alpha_F = 2.000$$

$$G^k = -0.009$$

$$d_x^k G = 7.995$$

$$dd_x^k G = 29.674$$

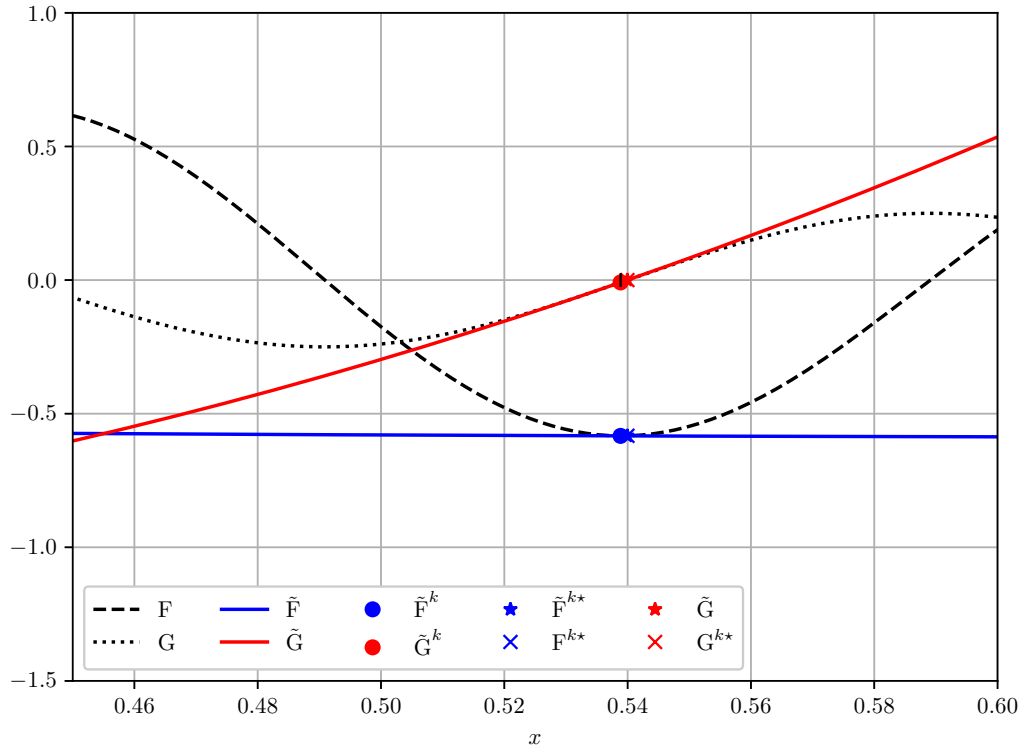
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.009$$

at the solution

$$x^{k*} = 0.540$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.583$$

$$\tilde{G}^{k*} = -0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = -0.000$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.539$$

$$F^k = -0.583$$

$$d_x^k F = -0.076$$

$$dd_x^k F = 0.284$$

$$\alpha_F = 4.000$$

$$G^k = -0.009$$

$$d_x^k G = 7.995$$

$$dd_x^k G = 29.674$$

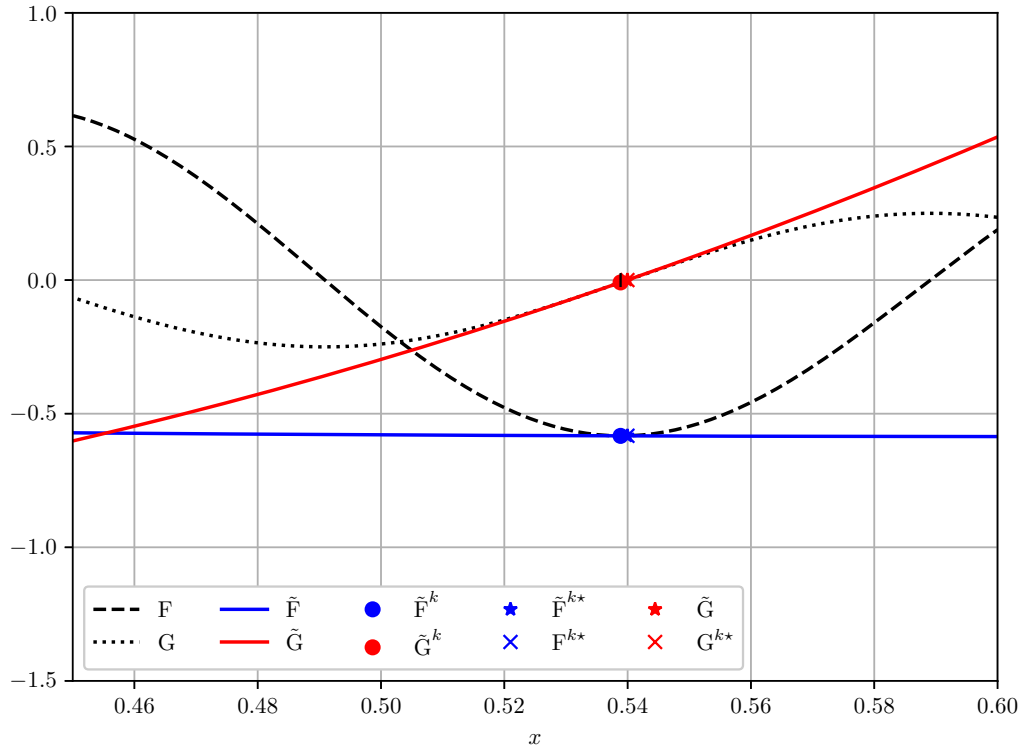
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.009$$

at the solution

$$x^{k*} = 0.540$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.583$$

$$\tilde{G}^{k*} = 0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = -0.000$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.539$$

$$F^k = -0.583$$

$$d_x^k F = -0.076$$

$$dd_x^k F = 0.284$$

$$\alpha_F = 8.000$$

$$G^k = -0.009$$

$$d_x^k G = 7.995$$

$$dd_x^k G = 29.674$$

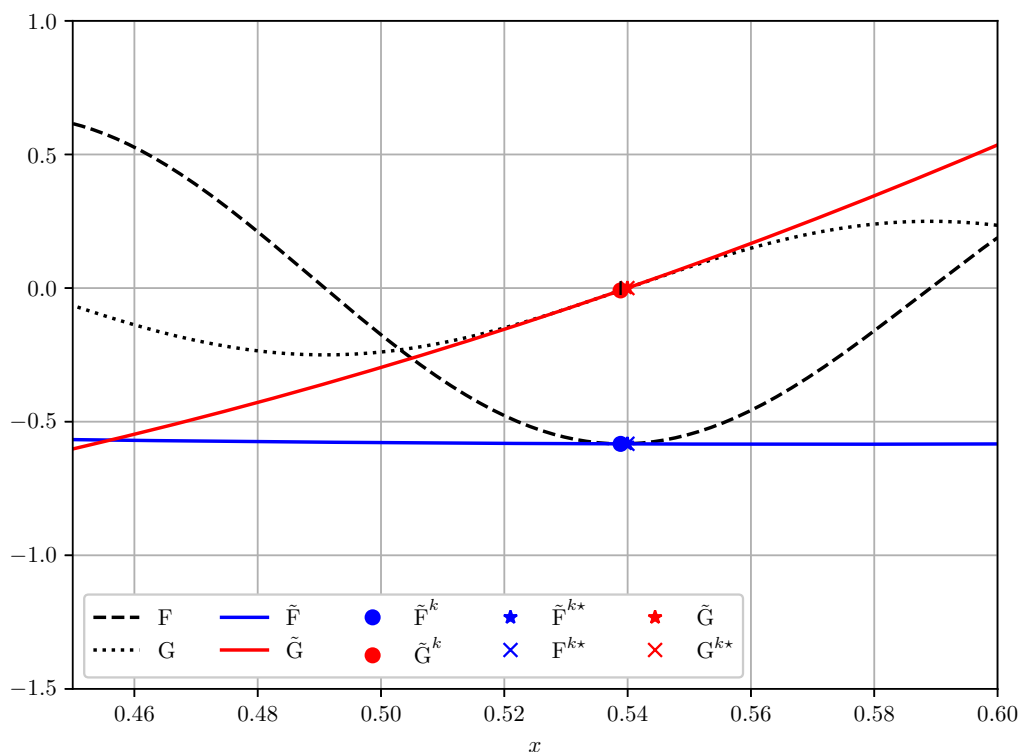
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k*} = 0.009$$

at the solution

$$x^{k*} = 0.540$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k*} = -0.583$$

$$\tilde{G}^{k*} = 0.000$$

while the actual functions are evaluated to be

$$F^{k*} = -0.583$$

$$G^{k*} = -0.000$$

However, the solution (step) is deemed *unacceptable*, because

→ the value of the objective function approximation is less than the actual function value, at the new design point, $\tilde{F}^{k*} < F^{k*}$.

That is, at least one approximation function is not *conservative*.

QP subproblem at x^k :

$$x^k = 0.539$$

$$F^k = -0.583$$

$$d_x^k F = -0.076$$

$$dd_x^k F = 0.284$$

$$\alpha_F = 16.000$$

$$G^k = -0.009$$

$$d_x^k G = 7.995$$

$$dd_x^k G = 29.674$$

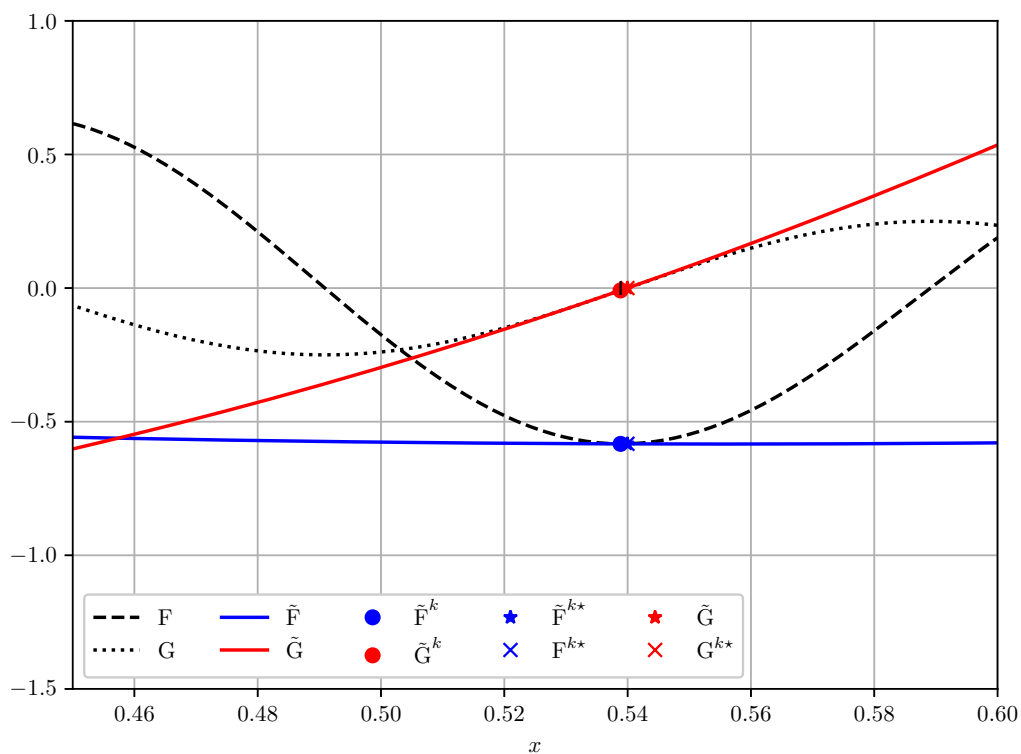
$$\alpha_G = 1.000$$

with Lagrange multiplier

$$\lambda^{k\star} = 0.009$$

at the solution

$$x^{k\star} = 0.540$$



At the solution of the QP the function approximations have the values

$$\tilde{F}^{k\star} = -0.583$$

$$\tilde{G}^{k\star} = -0.000$$

while the actual functions are evaluated to be

$$F^{k\star} = -0.583$$

$$G^{k\star} = -0.000$$