$$2\sum_{n=1}^{\infty} \frac{n^7}{e^{2^{-k}n\pi} - 1} = \sum_{n=0}^{2k+1} 16^{n-1}$$