Problem 1.2

a)

$$Q = \int dQ$$

$$= \int \lambda(\theta) dl$$

$$= \int_0^{\pi} \lambda_0 \cos \theta R d\theta$$

$$= 0$$

b)

$$\begin{split} dE_x &= \frac{1}{4\pi\epsilon_0} \frac{dQ}{R^2} \cos \theta \\ &= \frac{1}{4\pi\epsilon_0} \frac{\lambda_0 \cos \theta R d\theta}{R^2} \cos \theta \\ &= \frac{\lambda_0}{4\pi\epsilon_0 R} \cos^2 \theta d\theta \\ dE_y &= \frac{\lambda_0}{4\pi\epsilon_0 R} \cos \theta \sin \theta d\theta \\ \vec{E} &= \frac{\lambda_0}{4\pi\epsilon_0 R} \left(\int_0^\pi \cos^2 \theta d\theta \hat{i} + \int_0^\pi \cos \theta \sin \theta d\theta \hat{j} \right) \\ &= \frac{\lambda_0}{4\pi\epsilon_0 R} \left(\frac{\pi}{2} \hat{i} + 0 \hat{j} \right) \\ &= \frac{\lambda_0}{8\epsilon_0 R} \hat{i} \end{split}$$