

# **CS 8803 Mobile Manipulation: Project Report**

## **Software Project Type- A**

### **Obstacle Avoidance for Kinematically Redundant Mobile Manipulators**

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# 1 Introduction

## 1.1 Problem description

In order for a mobile manipulator to execute its task smoothly, it must take into account environment variables such as moving agents or obstacles. This can be done by moving the manipulator into a configuration that is atleast at a threshold distance from obstacles. To make sure this motion doesn't affect the movement of the end-effector, redundant degrees of freedom have to be utilized to achieve collision-free configuration. The amount of flexibility depends on the degree of redundancy, i.e., on the number of redundant DOFs. Redundancy is defined as the difference between the required and available DOFs. The execution of obstacle avoidance is of prime importance in tasks such as spray painting, arc welding, etc.

The goal of this project is to utilize redundant degrees of freedom of a 6-link mobile manipulator to tackle the problem of obstacle avoidance. The end-effector of the manipulator with stationary base is subject to obstacles in its path to a goal pose. The primary objective of this project is to avoid coming in contact with obstacles under different scenarios.

Thus, we are going to present a Software Project of type A, where we implement obstacle avoidance algorithms as are presented in [2] using GTSAM library. The code should determine the trajectory of the end-effector of the redundant manipulator in order to avoid obstacles.

## 1.2 Related work

[1] presents a computationally efficient algorithm to deal with real-time demands of obstacle avoidance in practical applications. Their approach is to determine the required joint angle rates for the manipulator under the constraints of specified end-effector trajectories and obstacle avoidance criterion. The obstacle avoidance technique used is to identify for each period in time the point on the manipulator that is nearest to the obstacle and assign to it a desired velocity component in the direction opposite to the obstacle surface.

[2] presents a method of on-line obstacle avoidance of redundant manipulators based on redundancy resolution at the velocity level. The obstacle avoidance algorithms presented in this paper assign each point on the body of the manipulator, which is close to the obstacle, a velocity or force component in a direction that is away from the obstacle. This paper also presents a method of prioritizing between various tasks and utilizing this concept for multiple obstacle avoidance. A method for smooth transition between tasks as well as for varying the avoiding velocity has been presented in this paper.

### 1.3 Project contribution

The two main goals performed by the manipulator with stationary base are :

**End-Effector Motion** - The redundant manipulator's end-effector should reach the desired final destination from a given initial position.

**Obstacle Avoidance** - The mobile robot should avoid obstacles along the path traversed without colliding. We assume that the links of manipulator arm are not counted as obstacles, so they are free to overlap.

The above goals were achieved for the following scenarios:

- Scenario I : End-effector motion in the absence of obstacles
- Scenario II : Manipulator arm motion disturbed by the stationary obstacle
- Scenario III : End-effector motion disturbed by the stationary obstacle
- Scenario IV : Manipulator motion disturbed by moving obstacle

## 2 Approach

### 2.1 Methodology

In a manipulator system, the relationship between the configuration variable  $q$  and the position of the end-effector  $x$  can be described by the following equation:

$$x = f(q) \quad (1)$$

where  $q$  is an  $m$  dimensional vector for an  $m$  link arm.  $x$  gives the task space vector of  $n$  dimensions. The corresponding relationship between the joint velocities  $\dot{q}$  and the task velocities  $\dot{x}$  is obtained by differentiating (1)

$$\dot{x} = J\dot{q} \quad (2)$$

Here,  $J$  is the  $n \times m$  Jacobian matrix. According to this equation, a motion in the joints results in a motion in the task space. This means that in order to calculate motion in joints that result from desired movement in the task space, the following equation is taken into account

$$\dot{q} = J^{-1}\dot{x} \quad (3)$$

where  $J^{-1}$  is the inverse of the Jacobian matrix  $J$ . An inverse is achieved for a square  $J$  matrix (Full-rank). But this is the case for a non-redundant manipulator. For a redundant manipulator (which is desired in our case), the dimensions of the joint space exceeds the dimensions of task space. Thus, the Jacobian matrix doesn't turn out to be a square one. The inverse of  $J$  doesn't

exist. For a generalized  $J^\#$ , there can be infinite solutions for  $\dot{q}$ . Therefore we take the Moor-Penrose inverse  $J^+$ . A solution can be given as

$$\dot{q} = J^+ \dot{x} + N \dot{\phi} = J^+ \dot{x} + (I - J^+ J) \dot{\phi} \quad (4)$$

$N$  represents projection into the null space of  $J$  and  $\dot{\phi}$  can be any  $n$  dimensional velocity vector. The 2nd term in rhs can be utilized to achieve obstacle avoidance or some other constraints. To perform this additional subtask, the velocity  $\dot{\phi}$  is used. Then the secondary task is defined by some motion  $x_t = f_t(q)$  like in the case of obstacle avoidance, the velocity  $\dot{\phi}$  can be defined as

$$\dot{\phi} = J_A^+ \dot{x}_A \quad (5)$$

To avoid any possible obstacles the manipulator has to move away from them into a configuration where the distance between them becomes larger. Usually, the basic strategy for obstacle avoidance is to identify the points on the robotic arm that are near obstacles and then assign to them the motion component that moves those points away from the obstacle. The robot motion (configuration) is changed if at least one part of the robot is at a critical distance from an obstacle. We denote the obstacles that are closer to the critical distance as the active obstacles and the corresponding closest points on the body of the manipulator as the critical points. At any moment, if an active obstacle exists in the vicinity of the manipulator, then the equation for joint velocity is represented as

$$\dot{\phi} = J_e^+ \dot{x}_e + (I - J^+ J) J_A^+ \dot{x}_A \quad (6)$$

where  $J_A^+$  is the inverse Jacobian of the critical point and  $x_A$  is the motion of this critical point in a direction away from obstacle. However, there is a need to prioritize between end-effector motion and obstacle avoidance. In the above case, end-effector motion is given a higher priority because we are finding configurations in the null space of the first task for obstacle avoidance. In this case, if an obstacle comes in the way of the motion of end-effector, it collides with it. Hence, we give a higher priority to obstacle avoidance. this is done with the below equation.

$$\dot{\phi} = J_A^+ \dot{x}_A + (I - J_A^+ J_A) J_e^+ \dot{x}_e \quad (7)$$

where  $J_e^+$  is the inverse Jacobian of end-effector. In this case, we are computing the viable position of end-effector in the null-space of obstacle avoiding configurations.

In obstacle avoidance, the priority of the avoiding task may depend on the type of obstacle and on the distance to the obstacle. Therefore, it is beneficial if the control method enables a smooth change of task priorities. Therefore, a method for smooth transition was proposed by [2]:

$$\dot{\phi} = J_A^+ \dot{x}_A + (I - \lambda(x_A) J_A^+ J_A) J_e^+ \dot{x}_e \quad (8)$$

where  $\lambda(x_A)$  is a scalar measure of how “active” is the primary task, scaling the vector  $x_A$  to the interval  $[0, 1]$ . When the primary task is active  $\lambda$  is  $\lambda(x_A) = 1$ , and when the primary task is not active, it is  $\lambda(x_A) = 0$ .

We take  $\lambda(x_A) = \alpha$ . Formulation (8) allows an unconstrained joint movement while  $\alpha$  is close to zero ( $\alpha \approx 0$ ). Thus, the robot can track the desired task-space path while it is away from the obstacle. On the other hand, when the robot is close to the obstacle ( $\alpha \approx 1$ ), the formulation in (8) takes the form (7) and only allows movement in the null space of the primary task, i.e., the obstacle-avoidance task.

## 2.2 Implementation

**Environment:** The project was implemented on Google Colaboratory in Python 3.6.7 using the GTSAM Library.

**Manipulator motion execution:** The *animation* module of *matplotlib* library was used to execute manipulator motion. A 100 frame animation was used for the simulation of each scenario. The animations were then saved as .mp4 and .gif files.

**Functions:** A manipulator class for 6-link arm performs the following functions-

- *\_init\_*: Initialize six-link arm manipulator
- *fk*: Forward kinematics.
- *jacobian*: Calculate manipulator Jacobian.
- *get\_joint\_positions*: Returns the x and y coordinates of each joint.
- *first\_task*: Calculates Jacobian and velocity of critical point.
- *get\_obstacle\_distances*: Calculates distance of joints and mid points of links from obstacle.
- *joint\_mid\_jacobian*: Calculates critical point Jacobian.
- *avoid\_obstacle*: Calculates velocity of critical point along opposite direction to the obstacle.

**Algorithm:** The pseudo-code of the algorithm used has been presented in this report. The *Project.ipynb* notebook can be viewed for further clarification on the methods implemented.

**Novel implementation:** In [2], the poses along the trajectory are calculated once. However, in our implementation, we calculate in every iteration the set of poses along a trajectory that joins the current position of end-effector and the goal pose. This allows a shorter traversal path for the manipulator.

### 3 Results

The algorithm is evaluated based on four scenarios. For the sake of simplicity, we use a single circular obstacle for each scenario. The obstacle is represented by the blue circle. The goal is represented as the red dot. The plot of distance of EE from goal is given to evaluate the smoothness of the end-effector path as we vary the alpha value.

The algorithm was repeated multiple times using random positions of the goal pose, random initial joint angles and random centres of the obstacle. The results of this experiment are presented in table 1. The two variables we consider are- whether collision occurs and whether the end-effector reaches the goal pose.

**Scenario 1:** In the first scenario, no obstacle is present. This scenario gives an estimate of the natural path of the end-effector in the absence of obstacles. Any deviations from this path will be evaluated in the subsequent scenarios. For the no obstacle scenario, the plot in Figure 1 is a linear one, given the value of alpha is 1.

[Link: No obstacle, alpha = 1](#)

**Scenario 2:** In this scenario, an obstacle is placed in a position so as to make the manipulator go around it to reach the goal pose. The manipulator is successful in reaching the goal while avoiding the obstacle, as can be observed in the results. The distance vs frame plots in Figure 2 are given for values of alpha 1, 0.5 and 0.05.

[Link: Stationary obstacle, alpha = 1](#)

[Link: Stationary obstacle, alpha = 0.5](#)

[Link: Stationary obstacle, alpha = 0.05](#)

**Scenario 3:** In this scenario, an obstacle is placed directly on the path of the end-effector. The end-effector successfully reaches the goal pose after deviating from its path, just enough to avoid the obstacle. The distance vs frame plots in Figure 3 are given for values of alpha 1, 0.5 and 0.05.

[Link: Stationary obstacle on path, alpha = 1](#)

[Link: Stationary obstacle on path, alpha = 0.5](#)

[Link: Stationary obstacle on path, alpha = 0.05](#)

**Scenario 4:** This scenario consists of two runs of the program. In the first run, a moving obstacle is orchestrated to move diagonally such that it doesn't cross the path of the end-effector. The movement of the manipulator is given for values of alpha 3, 1 and 0.5 (See Figure 4). In run 2, the moving obstacle is made to cross the path of the end-effector. This time the program takes the alpha values 2, 1 and 0.5 (See Figure 5).

[Link: Moving obstacle, alpha = 3](#)

[Link: Moving obstacle, alpha = 1](#)

[Link: Moving obstacle, alpha = 0.5](#)

Table 1: Algorithm statistics over 1000 runs. Alpha = 1.5 and Frames = 200

Collision occurred	EE didn't reach goal	Meaning	Frequency	Percentage
True	True	Goal out of reach/ ran out of frames	288	5.76 %
True	False	Low alpha value	332	6.64 %
False	True	Failure scenario	376	7.52 %
False	False	Success!	4004	80.08 %
Total			5000	100.00 %

[Link: Moving obstacle crossing path, alpha = 2](#)  
[Link: Moving obstacle crossing path, alpha = 1](#)  
[Link: Moving obstacle crossing path, alpha = 0.5](#)

**Failure scenario:** There are scenarios where the end-effector fails to reach the goal pose. One such scenario is presented in Figure 6 and the alpha value is set as 1.

[Link: Failure scenario](#)

## 4 Discussion

**Evaluation of plots:** The alpha value helps in the smooth transition between the tasks. If alpha value is set high, then greater weight is given to the first task and vice versa. In the plots, it is observed that the greater the value of alpha, the greater is the weight placed on deviation due to obstacle avoidance, and the greater is the displacement of the end-effector with respect to the goal. On the other hand, too low a value of alpha makes the manipulator move over the obstacle without avoiding it. A middle ground is decided for each scenario, where the movements of end-effector are relatively smooth and the manipulator manages to avoid the obstacle. This is true for all the scenarios. In the failure scenario, for a very low level of alpha, the end-effector manages to reach the goal, but by moving over the obstacle.

**Evaluation of table 1:** From the table, it is observed that our algorithm is successful (reaches goal without bumping into the obstacle) 80% of the times it runs. However, there are certain other scenarios where reaching the goal is not that straight-forward.

Collisions mainly occur due to a low value of alpha, whereby avoiding obstacles is not given as high a priority as is required from the situation. Other reasons of collision occurrence could be the initialization of obstacle center in very close proximity to the arm links and joints, since we are randomly selecting obstacle coordinates.

The reasons for the end-effector not reaching its goal could be due to the constant backtracking of EE due to displacement accountable to obstacle avoidance. This leads to the slowing down of the progress of EE, as a result of which, it doesn't complete its journey within the given number of frames.

A failure scenario occurs when the manipulator is capable of reaching the goal by avoiding the obstacle, but it doesn't. This happens in cases where the extension of manipulator arm is limited due to the presence of the obstacle. This is, clearly, a flaw in the algorithm. An obvious solution is to find reach around the obstacle in the other direction and extend the EE towards the goal pose. Incorporating this method is beyond the scope of this project and is left for future work.

**Future Work:** As observed in Table 1, collisions occur in some scenarios, and not in others. This is purely dictated by the value of  $\alpha$ . The closer the obstacle, the greater should be the weight placed on avoiding it. Therefore, instead of fixing a value for  $\alpha$ , it can be a function of the distance of the critical point from the obstacle.

In this project, we have fixed the value of the velocity both during obstacle avoidance as well as trajectory tracking. Collisions can be prevented by tweaking the avoiding velocity to increase in close proximity to the obstacle. This method can be implemented in a future work.

In this project, we assigned a motion in the opposite direction to the obstacle at the critical point. Instead of doing this, we can make the critical point move in a tangential direction when it is in close proximity to the obstacle. Essentially, when the critical point hits the threshold from the obstacle, it can either move to its right or left side (this is the tangential motion). If the goal lies to the left, the critical point moves left. Same for the other side. In future work, we'd want to investigate failure cases for this novel method.

Another method to avoid failure cases is to make the manipulator bend in the other direction if it is unable to stretch itself enough to reach the goal pose due to obstacle.

Environmental agents can be very complex and very unlike the simplistic model implemented in this project. Some features may be added to the model to make it realistic in a future work. This includes treating the manipulator links as obstacles, using multiple obstacles, obstacles with irregular boundaries, etc.



## 5 Meta-Learning

This project has been a very rewarding experience in terms of understanding obstacle avoidance. A summary of these experiences have been presented below:

- Understanding of null space and task prioritization gained. Essentially, a manipulator arm sets aside a configuration for first task, and then the other task configurations are found in the null space (set of configurations available after first task) of first task.
- Calculation of Jacobian matrices of not just the end-effector, but also points on the manipulator arm and how to move them in certain directions.
- We tried out a novel method of moving the critical point along a tangential direction instead of moving it in opposite direction from obstacle. However, we found this impossible to execute using the angles from base frame. This method would require us to figure out the critical point frame. It was not executed because of time constraints, so we stuck to the standard  $\angle 180$  movement of critical point.
- We understood the need for an alpha value to weight the tasks. In the absence of this, we had very little control over the movements of the arm. We also saw the need for varying the alpha value as the situation demands.
- Setting goal path tracking as the first priority and obstacle avoidance as the second priority gave poorer results than otherwise.
- Gained knowledge of possible scenarios where EE doesn't reach the goal. In such cases, we usually observed a tug of war between movements resulting from both the tasks.

## References

- [1] Klein et al. *Obstacle avoidance for kinematically redundant manipulators in dynamically varying environments.*
- [2] L. Zlajpah et al. *Obstacle avoidance with industrial robots"*

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**Algorithm 1** Perform obstacle avoidance

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```
N ← 50 {Number of time intervals}
vel ← 0.5 {Velocity of end-effector}
F ← frames {Number of frames}
q ← 1 × 7 vector {Initialize joint angles}
sTt_initial ← arm.fk(q) {Get initial EE position}
sTt_goal ← 1 × 3 vector {Initialize goal pose}
poses ← trajectory(sTt_initial, sTt_goal, N) {Get intermediate poses between
start and goal poses}
i ← 0 {Frame counter}
while Frame i ≤ F do
  centre_x ← scalar {Set X coordinate of obstacle center}
  centre_y ← scalar {Set Y coordinate of obstacle center}
  x_d, y_d ← arm.get_joint_positions(q)
  dist, mid_dist, x_mid, y_mid ← arm.get_obstacle_distances(x_d, y_d)
  JA, x, y ← arm.first_task(x_d, y_d, mid_dist, dist, x_mid, y_mid)
  q1 ← JA · [x, y, 0]
  sTt ← arm.fk(q) {Get present EE position}
  dist ← distance between present and goal poses
  N ← dist/vel
  poses ← trajectory(sTt, sTt_goal, N) {Get intermediate poses between
present and goal poses}
  Je ← arm.jacobian(q) {Get EE jacobian}
  xe ← sTt − poses(1) {Get error in desired EE poses}
  alpha ← scalar
  q2 ← (I − alpha * JA+ JA) · Je+ xe {Find 2nd term}
  q ← q1 + q2
  i ← i + 1
  frames ← frames ∪ q
end while
```

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Figure 1: Plot for no obstacle scenario with  $\alpha = 1$

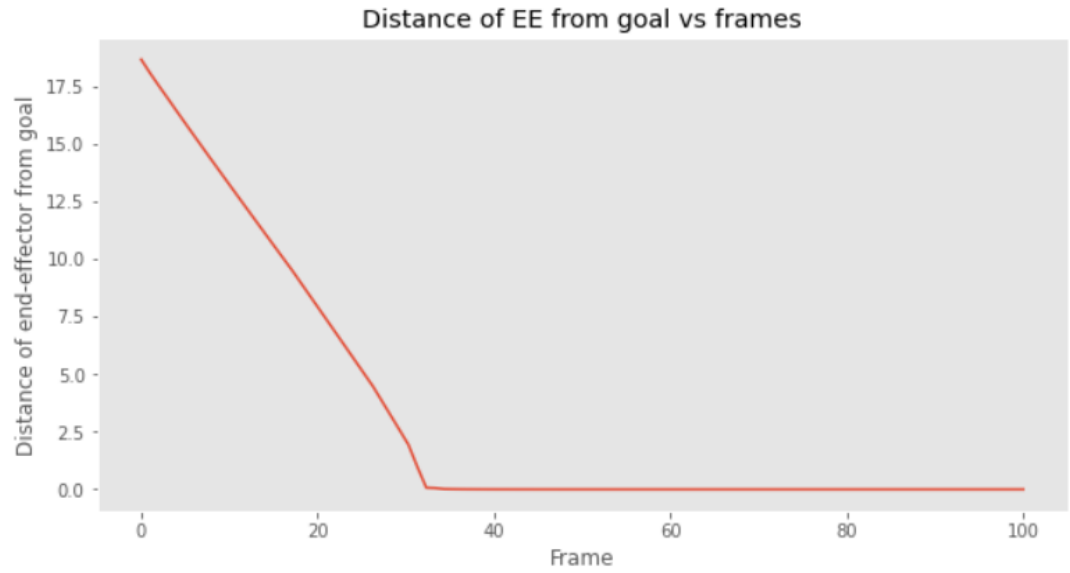


Figure 2: Plot for stationary obstacle scenario with  $\alpha = 1, 0.5, 0.05$

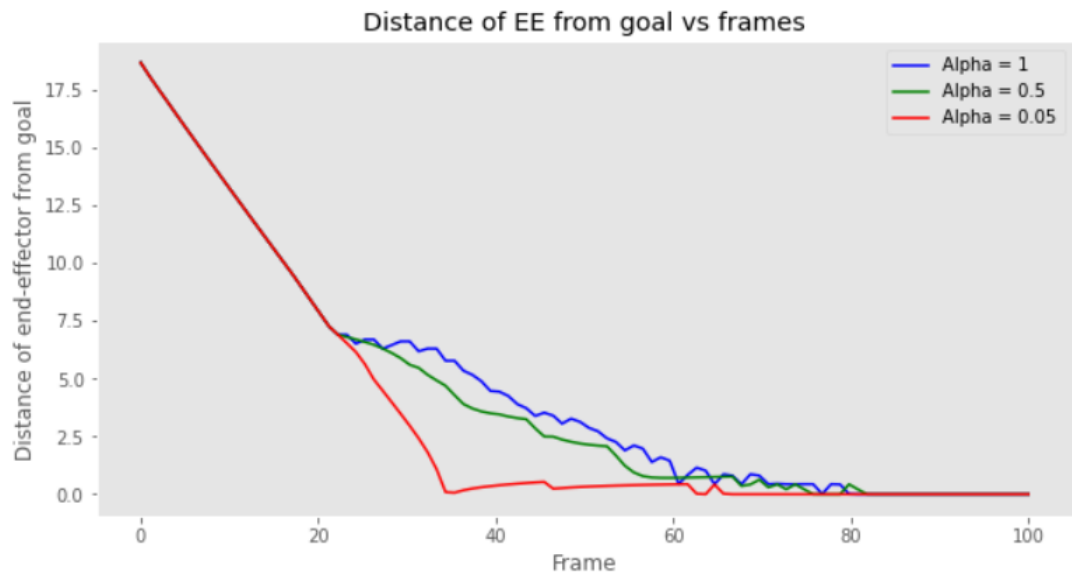


Figure 3: Plot for stationary obstacle in EE path scenario with  $\alpha = 1, 0.5, 0.05$

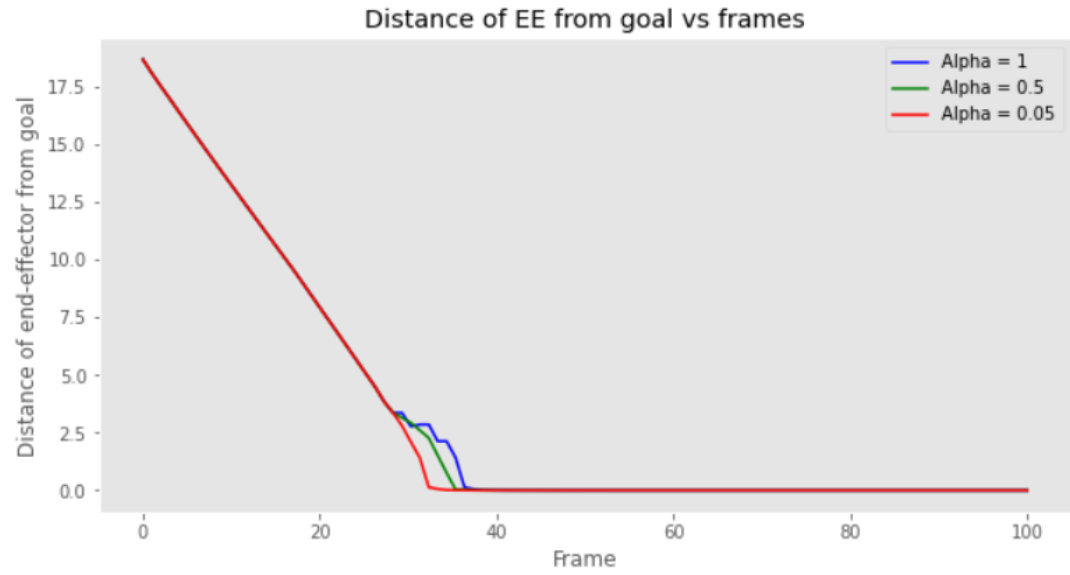


Figure 4: Plot for moving obstacle not crossing EE path scenario with  $\alpha = 3, 1, 0.5$

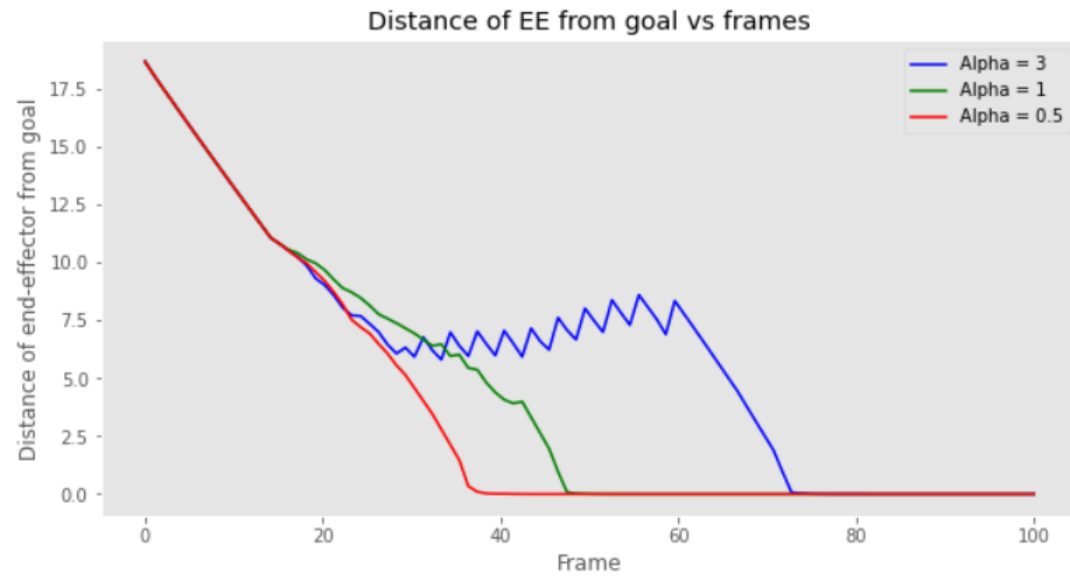


Figure 5: Plot for moving obstacle crossing EE path scenario with  $\alpha = 2, 1, 0.5$

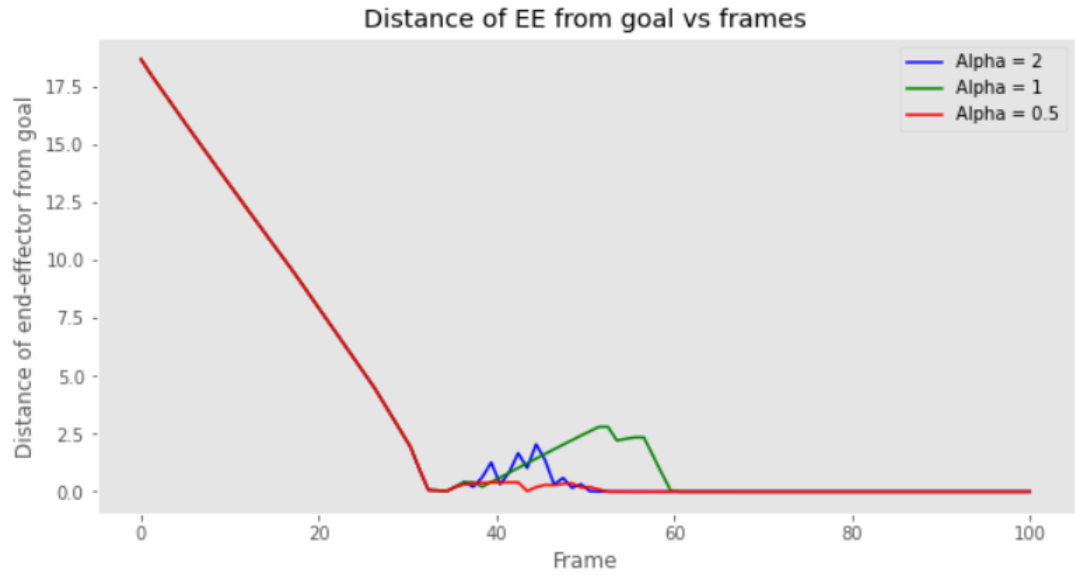


Figure 6: Plot for failure scenario with  $\alpha = 1, 0.5, 0.05$

