

ACTIVITY 1.X

Peano's Axioms for the Natural Numbers

- (1) Consider the set \mathbb{N} of all positive odd integers. For each odd integer n , define $n+$ to be $n+2$. Which of the Peano axioms are satisfied by this system?
- (2) Use the principle of mathematical induction to show that $1 + 3 + 5 + \dots + (2n - 1) = n^2$ for every positive integer n .
- (3) Give a recursive definition for the sequence of odd natural numbers.