## Lab 1: Data Manipulation, Random Number Generation

July 7, 2020

Today's agenda: Manipulating data objects; using the built-in functions, doing numerical calculations, and basic plots; reinforcing core probabilistic ideas.

0. Open a new R Markdown file; set the output to HTML mode and "Knit". This should produce a web page with the knitting procedure executing your code blocks. You can edit this new file to produce your homework submission.

## Background

The exponential distribution is defined by its cumulative distribution function

$$F(x) = 1 - e^{-\lambda x}$$

The R function rexp generates random variables with an exponential distribution.

```
rexp(n=10, rate=5)
```

```
## [1] 0.06245306 0.01175221 0.06019736 0.12696691 0.12991669 0.25367367
## [7] 0.25272588 0.79918075 1.02300899 0.30887984
```

produces 10 exponentially-distributed numbers with rate ( $\lambda$ ) of 5. If the second argument is omitted, the default rate is 1; this is the standard exponential distribution.

## Part I

- 1. Generate 200 random values from the standard exponential distribution and store them in a vector exp.draws.1. Find the mean and standard deviation of exp.draws.1.
- 2. Repeat, but change the rate to 0.1, 0.5, 5 and 10, storing the results in vectors called exp.draws.0.1, exp.draws.0.5, exp.draws.5 and exp.draws.10.
- 3. The function plot() is the generic function in R for the visual display of data. hist() is a function that takes in and bins data as a side effect. To use this function, we must first specify what we'd like to plot.
  - a. Use the hist() function to produce a histogram of your standard exponential distribution.
  - b. Use plot() with this vector to display the random values from your standard distribution in order.
  - c. Now, use plot() with two arguments any two of your other stored random value vectors to create a scatterplot of the two vectors against each other.

- 4. We'd now like to compare the properties of each of our vectors. Begin by creating a vector of the means of each of our five distributions in the order we created them and saving this to a variable name of your choice. Using this and other similar vectors, create the following scatterplots:
  - a. The five means versus the five rates used to generate the distribution.
  - b. The standard deviations versus the rates.
  - c. The means versus the standard deviations.

For each plot, explain in words what's going on.

## Part II

- 5. R's capacity for data and computation is large to what was available 10 years ago.
  - a. To show this, generate 1.1 million numbers from the standard exponential distribution and store them in a vector called big.exp.draws.1. Calculate the mean and standard deviation.
  - b. Plot a histogram of big.exp.draws.1. Does it match the function  $1 e^{-x}$ ? Should it?
  - c. Find the mean of all of the entries in big.exp.draws.1 which are strictly greater than 1. You may need to first create a new vector to identify which elements satisfy this.
  - d. Create a matrix, big.exp.draws.1.mat, containing the values in big.exp.draws.1, with 1100 rows and 1000 columns. Use this matrix as the input to the hist() function and save the result to a variable of your choice. What happens to your data?
  - e. Calculate the mean of the 371st column of big.exp.draws.1.mat.
  - f. Now, find the means of all 1000 columns of big.exp.draws.1.mat simultaneously. Plot the histogram of column means. Explain why its shape does not match the histogram in problem 5b).
  - g. Take the square of each number in big.exp.draws.1, and find the mean of this new vector. Explain this in terms of the mean and standard deviation of big.exp.draws.1. *Hint:* think carefully about the formula R uses to calculate the standard deviation.