Lecture 4: Model checking



"perhaps the most important part of applied statistical modelling"

Simon Wood

Model checking

- As with detection functions, checking is important
- Checking *doesn't* mean your model is **right**
- Want to know the model conforms to assumptions
- What assumptions should we check?

Convergence

Convergence

- Fitting the GAM involves an optimization
- By default this is REstricted Maximum Likelihood (REML) score
- Sometimes this can go wrong
- R will warn you!

A model that converges

```
gam.check(dsm_tw_xy_depth)
```

```
##
## Method: REML Optimizer: outer newton
## full convergence after 7 iterations.
## Gradient range [-3.456333e-05,1.051004e-05]
## (score 374.7249 & scale 4.172176).
## Hessian positive definite, eigenvalue range [1.179219,301.267].
## Model rank = 39 / 39
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
              k' edf k-index p-value
##
## s(x,y) 29.00 11.11 0.65 <2e-16 ***
## s(Depth) 9.00 3.84 0.81 0.37
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

A bad model

```
Error in while (mean(ldxx/(ldxx + ldss)) > 0.4) { :
    missing value where TRUE/FALSE needed
In addition: Warning message:
In sqrt(w) : NaNs produced
Error in while (mean(ldxx/(ldxx + ldss)) > 0.4) { :
    missing value where TRUE/FALSE needed
```

This is rare

The Folk Theorem of Statistical Computing

"most statistical computational problems are due not to the algorithm being used but rather the model itself"

Andrew Gelman

Folk Theorem anecdata

- Often if there are fitting problems, you're asking too much from your data
- Model is too complicated
- Too little data (check n in summary, is it right?)
- Try something simpler, see what happens

Basis size

Basis size (k)

- Set k per term
- e.g. s(x, k=10) or s(x, y, k=100)
- Penalty removes "extra" wigglyness
 up to a point!
- (But computation is slower with bigger k)

Checking basis size

```
gam.check(dsm_x_tw)
```

```
##
## Method: REML Optimizer: outer newton
## full convergence after 7 iterations.
## Gradient range [-3.196351e-06,4.485625e-07]
## (score 409.936 & scale 6.041307).
## Hessian positive definite, eigenvalue range [0.7645492,302.127].
## Model rank = 10 / 10
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
## k' edf k-index p-value
## s(x) 9.00 4.96 0.76 0.38</pre>
```

Increasing basis size

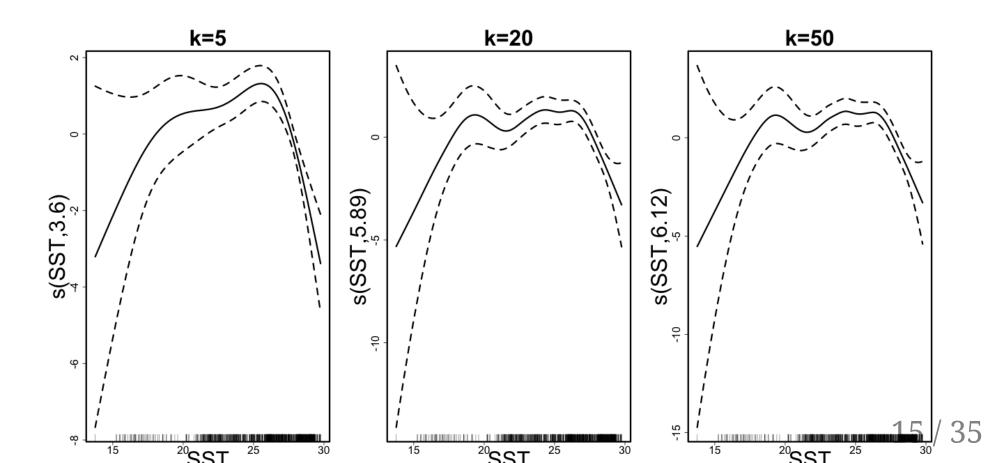
```
dsm_x_tw_k \leftarrow dsm(count \sim s(x, k=20), ddf.obj=df,
                   segment.data=segs, observation.data=obs,
                   family=tw())
gam.check(dsm x tw k)
##
## Method: REML Optimizer: outer newton
## full convergence after 7 iterations.
## Gradient range [-2.30124e-08,3.930703e-09]
## (score 409.9245 & scale 6.033913).
## Hessian positive definite, eigenvalue range [0.7678456,302.0336].
## Model rank = 20 / 20
##
## Basis dimension (k) checking results. Low p-value (k-index<1) may
## indicate that k is too low, especially if edf is close to k'.
##
           k' edf k-index p-value
##
## s(x) 19.00 5.25 0.76
                               0.35
```

Sometimes basis size isn't the issue...

- Easy rule:
 - double k and see what happens
- Didn't increase the EDF much here
- Other things can cause low "p-value" and "k-index"
- Increasing k increases computing time

k is a maximum

- Don't worry about things being too wiggly
- k gives the maximum complexity
- Penalty deals with the rest



Residuals

What are residuals?

- Residuals = (observed value) (fitted value)
- BUT hard to see patterns in these "raw" residuals
- Need to standardise \Rightarrow deviance residuals
- Expect these residuals $\sim N(0,1)$

Why are residuals important?

- Structure in the residuals means your model didn't capture something
- Maybe a missing covariate
- Model doesn't describe the data well

Fitting to residuals

- Refit our model but with the residuals as response
- Response is normal (for deviance residuals)
- What pattern is left in the residuals?

Example

• Example model with NPP and Depth

summary(resid_fit)

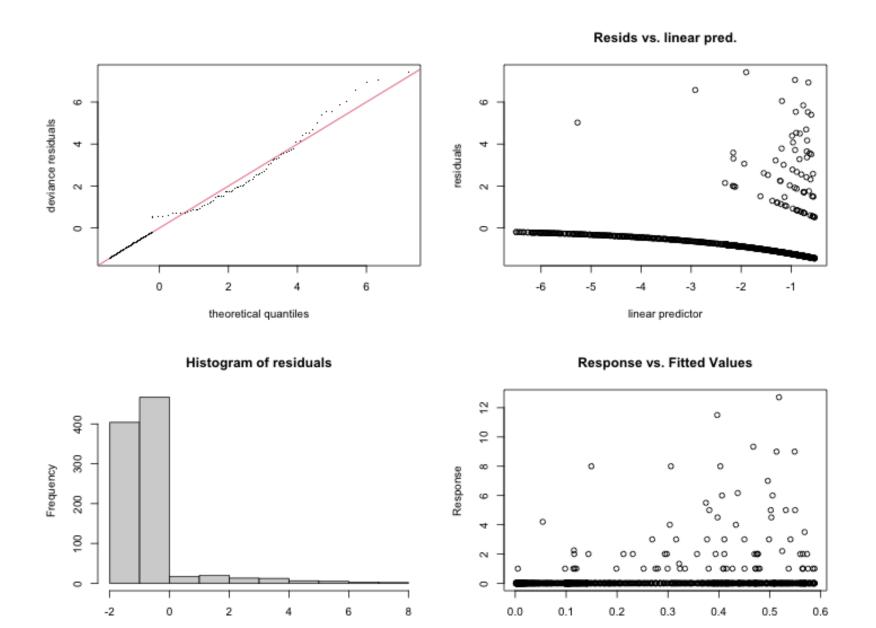
```
##
## Family: gaussian
## Link function: identity
##
## Formula:
## resid \sim s(Depth, bs = "ts", k = 20) + s(NPP, bs = "ts", k = 20)
##
## Parametric coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.49454 0.03274 -15.1 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
##
             edf Ref.df F p-value
## s(NPP) 0.03322 19 0.002 0.316
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) = 0.0241 Deviance explained = 2.67%
## -REML = 1362 Scale est. = 1.0174 n = 949
```

What's going on there?

- Something unexplained going on?
- Maybe Depth + NPP is not enough?
 - Add other smooths (s(x, y)?)
- Increase k?

Other residual checking

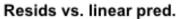
gam.check

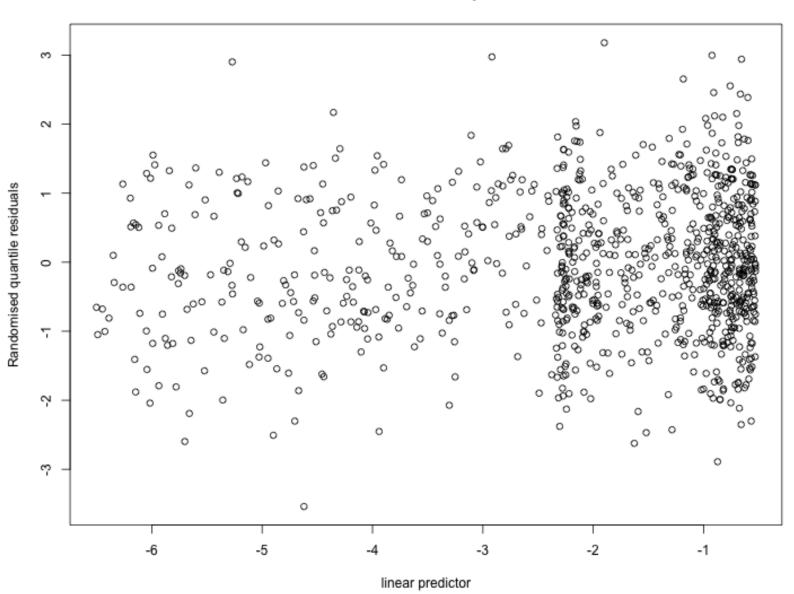


Shortcomings

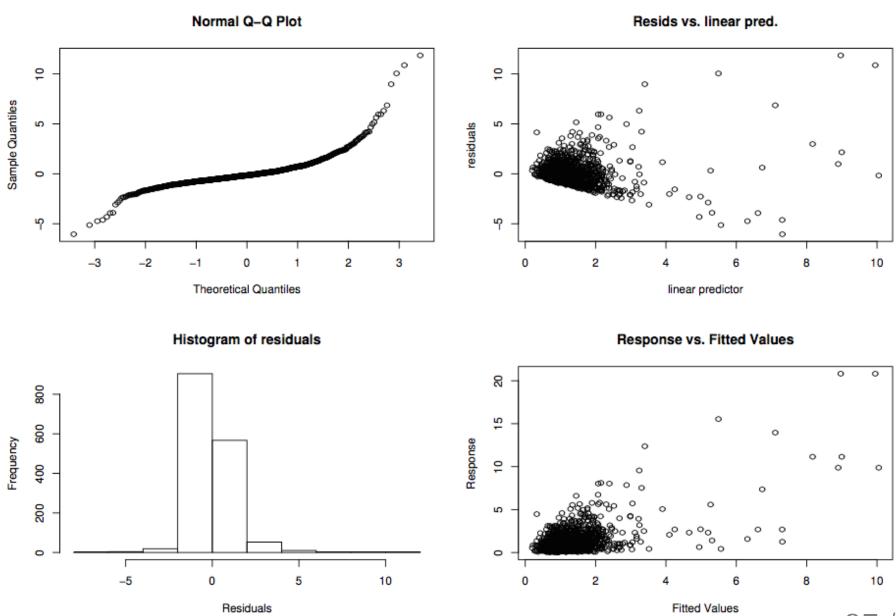
- gam.check can be helpful
- "Resids vs. linear pred" is victim of artifacts
- Need an alternative
- "Randomised quanitle residuals"
 - ∘ rqgam.check
 - Exactly normal residuals

Randomised quantile residuals

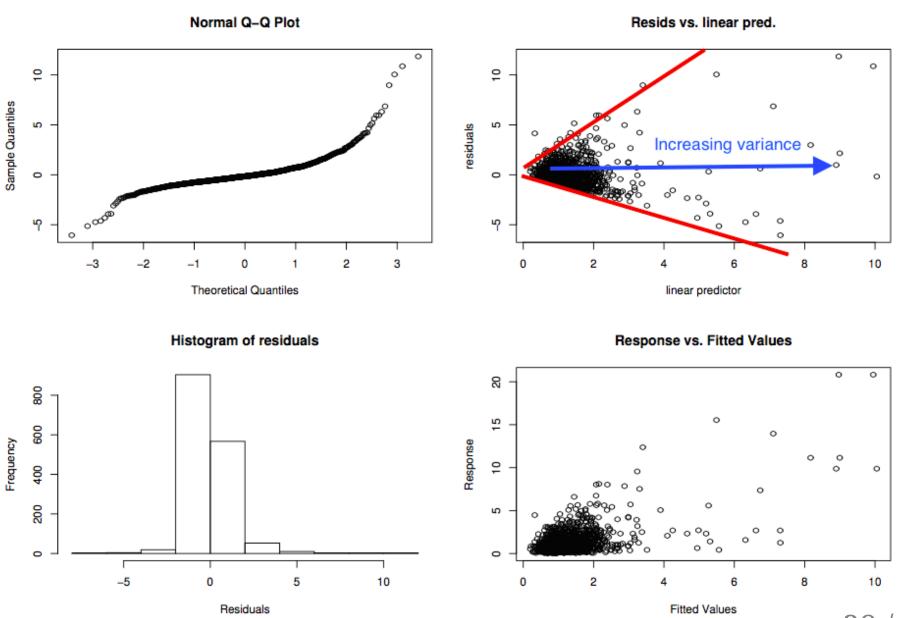




Example of "bad" plots

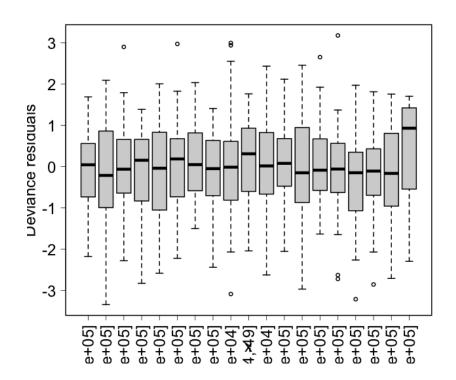


Example of "bad" plots



Looking for artefacts

- Want to avoid "pattern" in residuals
- How to visualise?
- Plot residuals vs. covariates
- Should look like this



Residual checks

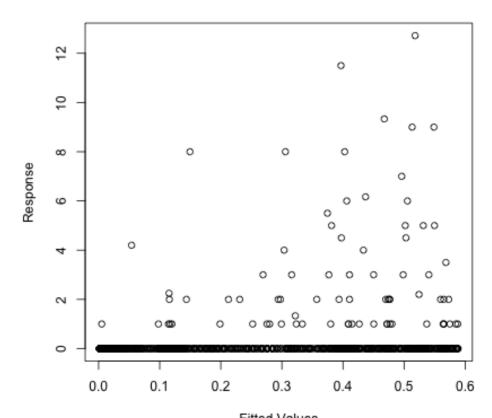
- Looking for patterns (not artifacts)
- This can be tricky
- Need to use a mixture of techniques
- Cycle through checks, make changes recheck

Observed vs. expected

Response vs. fitted values

- gam.check "response vs. fitted values"
- BUT smooths are "wrong" everywhere in particular (but "right" on average!)

Response vs. Fitted Values



Summarize over covariate chunks

- On average the smooth is right
- Check aggregations of count
- Here detection function has Beaufort as factor

Observed vs. expected for environmental covariates

• Just need to specify the cutpoints

```
obs_exp(dsm_bad, "Depth", c(0, 1000, 2000, 3000, 4000, 6000))
##
           (0,1e+03] (1e+03,2e+03] (2e+03,3e+03] (3e+03,4e+03] (4e+03,6e+03]
## Observed
           4.00000
                        52.53333
                                    139.16667
                                                  35.00000
                                                           8.00000
                                                  53.78726
                                                               30.32642
## Expected 85.65231
                        37.98341 63.40892
obs_exp(dsm_good, "Depth", c(0, 1000, 2000, 3000, 4000, 6000))
##
           (0,1e+03] (1e+03,2e+03] (2e+03,3e+03] (3e+03,4e+03] (4e+03,6e+03]
## Observed 4.000000
                        52.53333
                                     139.1667
                                                  35.00000
                                                               8.000000
                        48.14915 128.7962
                                                  38.76013
## Expected
           5.308628
                                                               8.359456
```

Summary

- Convergence
 - Rarely an issue
- Basis size
 - k is a maximum
 - Double and see what happens
- Residuals
 - Deviance and randomised quantile
 - check for artifacts
- Observed vs. expected
 - Compare aggregate information