

$$\begin{array}{c}
\frac{\cdot 34() \vdash [34()] \cdot \mid 34()}{\cdot 34() \vdash \cdot \mid \cdot 34() \mid} \\
\frac{\cdot 34() \vdash \cdot 34() \mid \cdot \mid}{\cdot \vdash \cdot (34?())^{\perp} \vee^{-} (34?()) \mid \cdot \mid}
\end{array}$$

Definition 1 (Formulae)

$$\begin{aligned} P &= p \mid A \wedge^+ B \mid A \vee^+ B \\ N &= p^\perp \mid A \wedge^- B \mid A \vee^- B \\ A, B &= P \mid N \end{aligned}$$

Definition 2 (Negation)

$(p)^\perp$	$:= p^\perp$	$(p^\perp)^\perp$	$:= p$
$(A \wedge^+ B)^\perp$	$:= A^\perp \vee^- B^\perp$	$(A \wedge^- B)^\perp$	$:= A^\perp \vee^+ B^\perp$
$(A \vee^+ B)^\perp$	$:= A^\perp \wedge^- B^\perp$	$(A \vee^- B)^\perp$	$:= A^\perp \wedge^+ B^\perp$

Definition 3 (System)

$\frac{\Gamma \vdash [A]\Delta \quad \Gamma \vdash [B]\Delta}{\Gamma \vdash [A \wedge^+ B]\Delta} \quad \frac{\Gamma \vdash [A_i]\Delta}{\Gamma \vdash [A_1 \vee^+ A_2]\Delta}$	
$\overline{\Gamma, p \vdash [p]\Delta}$	
$\frac{\Gamma \vdash N \mid \Delta}{\Gamma \vdash [N]\Delta} \text{ } N \text{ negative}$	
$\frac{\Gamma \vdash A, \Pi \mid \Delta \quad \Gamma \vdash B, \Pi \mid \Delta}{\Gamma \vdash A \wedge^- B, \Pi \mid \Delta} \quad \frac{\Gamma \vdash A_1, A_2, \Pi \mid \Delta}{\Gamma \vdash A_1 \vee^- A_2, \Pi \mid \Delta}$	
$\frac{\Gamma \vdash \Pi \mid \Delta, P}{\Gamma \vdash P, \Pi \mid} P \text{ positive}$	$\frac{\Gamma, p \vdash \Pi \mid \Delta}{\Gamma \vdash p^\perp, \Pi \mid} p^\perp \text{ negative atom}$
$\frac{\Gamma \vdash [P]\Delta, P}{\Gamma \vdash \mid \Delta, P}$	