$$\beta_a(\mathcal{X}, \hat{\Theta}_d) =$$