

## 2. TWO-ZONE MODEL FOR OBSERVED TEMPERATURE STRUCTURE

At each position along the spectrograph slit, the line of sight will cross several zones with different physical conditions. These may include:

- A1:** The compressed shell behind the bow-shock, which is in photoionization equilibrium;
- A2:** The main body of the jet bullet, also in photoionization equilibrium;
- B1:** The immediate post-shock cooling zone of the bow shock;
- B2:** The post-shock cooling zone of the jet shock.

In HH 204, the relative velocity between the unshocked jet and the working surface is very low ( $\approx 15 \text{ km s}^{-1}$ ), so the jet shock is much weaker than the bow shock, implying that the emission from zone B2 can be neglected compared with B1. Zones A1 and A2 should have similar conditions, and so can be merged into a single zone with density  $n_A$  and temperature  $T_A$ . Although the zone B1 should have a range of temperatures, for simplicity we assume a single characteristic temperature  $T_B$ . The density of zone B is found by assuming pressure equilibrium with zone A:  $n_B = n_A T_A / T_B$ . We define  $f_B$  for a given ion as the fraction of the total ionic emission measure,  $\int n_e n_{\text{ion}} dz$ , that comes from zone B, with the remainder,  $f_A = 1 - f_B$ , coming from zone A.

The appropriate value of  $T_B$  is rather uncertain, since it depends on the non-equilibrium evolution of ionization and temperature in the post-shock radiative relaxation layer. Most published shock models (Cox & Raymond 1985; Sutherland & Dopita 2017) are calculated on the assumption that the far upstream and downstream ionization states are determined by the radiation from the shock itself. Care must therefore be exercised when translating their results to cases such as HH 204, where external irradiation from O stars is a dominant factor. The curved bow shock in HH 204 should give a range of shock velocities, up to a maximum of  $V \approx 84 \text{ km s}^{-1}$  (assuming the pre-shock medium is stationary). In principle, this corresponds to post-shock temperatures as high as  $2 \times 10^5 \text{ K}$ , but the gas at such temperatures will be too highly ionized to significantly emit optical lines. The cooling timescale is generally shorter than the recombination timescale, so the gas is over-ionized as it cools. It is only when the temperature falls below about  $50\,000 \text{ K}$  that the abundance of  $\text{O}^{++}$  becomes significant (e.g., Fig. 11 of Allen et al. 2008), allowing the emission of the optical [O III] lines. A similar situation is seen

in middle-aged supernova remnants, such as the Cygnus Loop (Raymond et al. 2020).

We look for solutions where both  $T_A$  and  $T_B$  are constant along the slit, so that any spatial variation in the temperature diagnostics is driven primarily by variation in  $f_B$ . Although the density diagnostics do show a gradient with position, both  $T([\text{O III}])$  and  $T([\text{S III}])$  are relatively insensitive to density, so for simplicity we assume  $n_A$  is constant. We use the Python library PyNeb to calculate the per-zone emission coefficients,  $j(T_A, n_A)$  and  $j(T_B, n_B)$ , for each emission line. For a given diagnostic line pair, 1 and 2, the ratio is calculated as

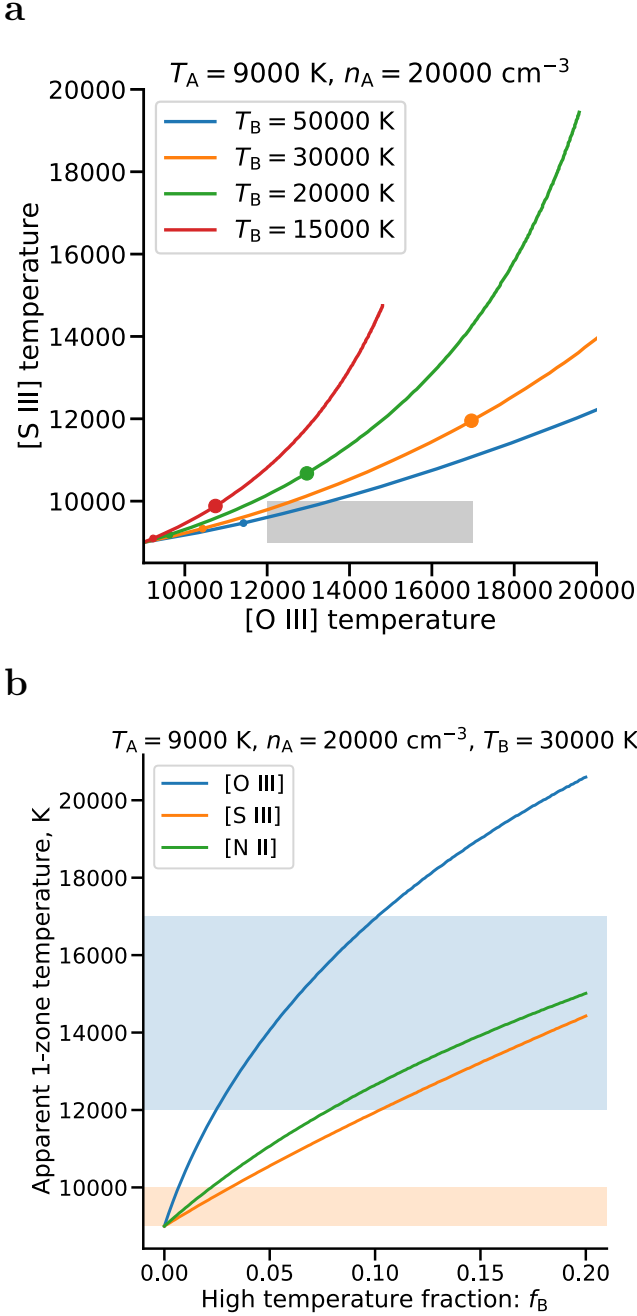
$$R_{12} = \frac{(1 - f_B) j_1(T_A, n_A) + f_B j_1(T_B, n_B)}{(1 - f_B) j_2(T_A, n_A) + f_B j_2(T_B, n_B)}. \quad (2)$$

This is then fed into PyNeb's `getTemDen` function to find the equivalent single-zone temperature that would give the same ratio (assuming a density of  $n_A$ ). It is clear from equation (2) that for  $f_B = 0$  one must recover  $T_e = T_A$  and that for  $f_B = 1$  one must recover  $T_e = T_B$ . But for intermediate values of  $f_B$ , the derived temperature will differ between ions because of variations in the temperature sensitivity of the diagnostic ratios.

We first investigate the case of a common  $f_B$  for all ions, but we find that this is unable to reproduce the observations. This is demonstrated in Figure 4a, which shows the relation between  $T_e([\text{O III}])$  and  $T_e([\text{S III}])$  for 4 different values of  $T_B$  between  $15\,000$  and  $50\,000 \text{ K}$ . We set  $T_A = 9000 \text{ K}$  and  $n_A = 20\,000 \text{ cm}^{-3}$  in all cases and  $f_B$  increases from left to right along each curve. The gray rectangle shows the observed range of temperatures along the spectrograph slit (Figure 6):  $T_e([\text{O III}])$  shows a systematic decline from  $\approx 17\,000 \text{ K}$  near the bow shock to  $\approx 12\,000 \text{ K}$  further away, while  $T_e([\text{S III}])$  is roughly constant at  $9000$  to  $10\,000 \text{ K}$ , with no apparent correlation with  $T_e([\text{O III}])$ . The two-zone models with  $T_B \geq 30\,000 \text{ K}$  all show  $T_e([\text{O III}]) > T_e([\text{S III}])$  as  $f_B$  increases, but this is insufficient to explain the observations. For example, in order to achieve  $T_e([\text{O III}]) = 17\,000 \text{ K}$  the models predict  $T_e([\text{S III}]) > 11\,000 \text{ K}$ , which is significantly higher than observed.

In Figure 4b, we relax the assumption of a common  $f_B$  for all ions, showing separately the predicted values of  $T_e([\text{N II}])$ ,  $T_e([\text{S III}])$ , and  $T_e([\text{O III}])$  as a function of  $f_B$ , assuming  $T_B = 30\,000 \text{ K}$ . The ranges of observed values are shown by colored bands, blue for [O III] and orange for [N II] and [S III]. From the figure it is apparent that a decline from  $f_B([\text{O III}]) \approx 0.1$  at  $x = 0$  to  $f_B([\text{O III}]) \approx 0.02$  for  $x > 5 \text{ mpc}$  is required to explain the  $T_e([\text{O III}])$  profile, whereas  $f_B([\text{S III}]) < 0.01$  and  $f_B([\text{N II}]) < 0.01$  is required at all positions.

It is not surprising that  $f_B$  should vary between ions since the photoionization equilibrium ion fraction of  $\text{O}^{2+}$



**Figure 4.** Simple two-zone model for spatial variations in temperature diagnostics. (a) Correlation between derived  $T_e$  from [O III] and [S III] lines, assuming that the fraction  $f_B$  of ionic emission measure that arises in the hot component (with temperature  $T_B$ ) is the same for both ions. Values of  $f_B = 0.01$  (small dots) and  $f_B = 0.1$  (large dots) are indicated on each curve. The gray rectangle shows the observed range of values, which cannot be explained under this assumption (see text). (b) Derived  $T_e$  for [O III], [S III], and [N II] lines as a function of  $f_B$ , assuming  $T_B = 30\,000 \text{ K}$ . Colored bands show the observed ranges, which imply that  $f_B$ ([O III]) must be larger than for the other ions (see text).

from zone A is much lower than that of  $\text{N}^+$  or  $\text{S}^{2+}$ . Assuming  $f_B \ll 1$ , then the ionic abundances given in the “Cut 1, HH 204” column of Table 4 correspond to zone A. These yield  $\text{O}^{2+}/\text{O} = 0.005$  and  $\text{S}^{2+}/\text{S} = 0.61$  if the abundances of unobserved ion stages are negligible. The lack of [N III] lines means that  $\text{N}^+/\text{N}$  cannot be estimated directly, but is likely of order unity. The fact that  $\text{O}^{2+}$  is only present in trace amounts in the photoionization equilibrium gas means that the relative contribution from the post-shock cooling zone is much larger than for  $\text{S}^{2+}$  and  $\text{N}^+$ . This is confirmed by emission line imaging of HH 204 (Weilbacher et al. 2015), which shows a morphology in [S III] and [N II] that is clearly dominated by the compact jet bullet, whereas the emission in [O III] is more diffuse within the parabolic envelope of the bow shock.

## REFERENCES

- Allen, M. G., Groves, B. A., Dopita, M. A., Sutherland, R. S., & Kewley, L. J. 2008, *ApJS*, 178, 20
- Cox, D. P., & Raymond, J. C. 1985, *ApJ*, 298, 651
- Doi, T., O’Dell, C. R., & Hartigan, P. 2002, *AJ*, 124, 445
- . 2004, *AJ*, 127, 3456
- García-Díaz, M. T., Henney, W. J., López, J. A., & Doi, T. 2008, *RMxAA*, 44, 181
- Kissler-Patig, M., Pirard, J. F., Casali, M., et al. 2008, *A&A*, 491, 941
- Muench, A. A., Lada, E. A., Lada, C. J., & Alves, J. 2002, *ApJ*, 573, 366
- O’Dell, C. R. 2009, *PASP*, 121, 428
- O’Dell, C. R., & Doi, T. 2003, *AJ*, 125, 277
- O’Dell, C. R., Ferland, G. J., Henney, W. J., et al. 2015, *AJ*, 150, 108
- O’Dell, C. R., Hartigan, P., Lane, W. M., et al. 1997, *AJ*, 114, 730
- O’Dell, C. R., & Wong, K. 1996, *AJ*, 111, 846
- Raymond, J. C., Chilingarian, I. V., Blair, W. P., et al. 2020, *ApJ*, 894, 108
- Rosado, M., de La Fuente, E., Arias, L., & Le Coarer, E. 2002, in *Revista Mexicana de Astronomía y Astrofísica Conference Series*, Vol. 13, *Revista Mexicana de Astronomía y Astrofísica Conference Series*, ed. W. J. Henney, W. Steffen, L. Binette, & A. Raga, 90–93
- Sutherland, R. S., & Dopita, M. A. 2017, *ApJS*, 229, 34
- Weilbacher, P. M., Monreal-Ibero, A., Kollatschny, W., et al. 2015, *A&A*, 582, A114