

Formula Analysis

Data Structure: Stack (Last in First Out)

Algorithm: Shunting yard algorithm, working as operator-precedence parsing.

Formula: $4*(7+9)+9/3$

Check hierarchy

'(' or ')' = 3

'/' or '*' = 2

'+' or '-' = 1

Let's break the formula by each char and consider each item as a token

Step 1: $4*(7+9)+9/3$

Token = '4'

Operand stack

								4
--	--	--	--	--	--	--	--	---

Step 2: $4*(7+9)+9/3$

Token = '*'

Operator stack

									*
--	--	--	--	--	--	--	--	--	---

Step 3: $4*(7+9)+9/3$

Token = '('

Operator stack

								(*
--	--	--	--	--	--	--	--	---	---

Step 4: $4*(7+9)+9/3$

Token = '7'

Operand stack

						7	4
--	--	--	--	--	--	---	---

Step 5: $4*(7+9)+9/3$

Token = '+'

Operator stack

[illegible]

Step 6: $4 \cdot (7+9) + 9/3$

Token = '9'

Operand stack

					9	7	4
--	--	--	--	--	---	---	---

Step 7: $4*(7+9)+9/3$

Token= ')

```
if(token == '')
```

Run till the last operator in not '('

Pop operator

Pop operand twice

Perform operation with the operator pop_operand2 operator pop_operand1 => 9+7=16

Push the operand to the operand stack

Pop operator

Operator stack

								*
--	--	--	--	--	--	--	--	---

Operand stack

						16	4
--	--	--	--	--	--	----	---

Step 8: $4*(7+9)+9/3$

Token = '+'

If the hierarchy of the token is less than the last operator in the stack, in this case, + < *

Pop operator

Pop operand twice

Perform operation with the operator pop_operand2 operator pop_operand1 => $16*4=64$

Push the operand to the operand stack

Operator stack

--	--	--	--	--	--	--	--	--	--

Operand stack

							64
--	--	--	--	--	--	--	----

Step 9: $4*(7+9)+9/3$

Token = '+'

Operator stack

									+
--	--	--	--	--	--	--	--	--	---

Step 10: $4*(7+9)+9/3$

Token = '9'

Operand stack

						9	64
--	--	--	--	--	--	---	----

Step 11: $4*(7+9)+9/3$

Token = '/'

Operator stack:

Hierarchy of token > hierarchy of the last operator in the stack, so it will be pushed

						/	+
--	--	--	--	--	--	---	---

Step 12: $4*(7+9)+9/3$

Token = '3'

Operand stack

					3	9	64
--	--	--	--	--	---	---	----

Step 13: $4*(7+9)+9/3$

Pop operator

Pop operand twice

Perform operator with the operator pop_operand operator pop_operand1 => $9/3=3$

Push the operand to the operand stack

Operator stack

								+
--	--	--	--	--	--	--	--	---

Operand stack

						3	64
--	--	--	--	--	--	---	----

Step 14: $4*(7+9)+9/3$

Pop operator

Pop operand twice

Perform operator with the operator popval2 operator popval1 $\Rightarrow 64+3=67$

Push the operand to the operand stack

Step 15: $4*(7+9)+9/3$

Output: last index of operand stack = 67