

# Report for Forward-Planning agent

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## Introduction

In this report we focused on solving a deterministic logistics planning problem for an air cargo transport system by implementing a search and planning agent.

In this project, we were given 4 problems, each having different numbers of aeroplanes, cargo items, and airports and as a result, varying complexities. There are 11 search algorithms given to us to experiment on these 4 problems. They are as follows:

1. Breadth First Search
2. Depth First Graph Search
3. Uniform Cost Search
4. Greedy Best First Graph Search with heuristic `h_unmet_goals`
5. Greedy Best First Graph Search with heuristic `h_pg_levelsum`
6. Greedy Best First Graph Search with heuristic `h_pg_maxlevel`
7. Greedy Best First Graph Search with heuristic `h_pg_setlevel`
8. A\* Search with heuristic `h_unmet_goals`
9. A\* Search with heuristic `h_pg_levelsum`
10. A\* Search with heuristic `h_pg_maxlevel`
11. A\* Search with heuristic `h_pg_setlevel`

The goal of this project is to perform an analysis of the search algorithms on each of the 4 problems and record the following information about the algorithms:

- number of actions in the domain
- number of new node expansions
- time to complete the plan search

In addition to recording this information, this report seeks to answer the following questions:

- Which algorithm or algorithms would be most appropriate for planning in a very restricted domain (i.e., one that has only a few actions) and needs to operate in real time?
- Which algorithm or algorithms would be most appropriate for planning in very large domains (e.g., planning delivery routes for all UPS drivers in the U.S. on a given day)
- Which algorithm or algorithms would be most appropriate for planning problems where it is important to find only optimal plans?

## Problem Description

The 4 problems use the below action schema:

Action(Fly(p, from, to),

PRECOND:  $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

EFFECT:  $\neg At(p, from) \wedge At(p, to)$

Action(Load(c,p,a),

PRECOND:  $At(c, a) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT:  $\neg At(c, a) \wedge In(c, p)$





Action(Unload(c,p,a),

PRECOND:  $In(c, p) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT:  $At(c, a) \wedge \neg In(c, p)$

## Analysis on the problems

### Problem 1

<u>Aa</u> Search Algorithm	 Actions	 Expansions	 Path Length	 Execution Time
<u>Breadth First Search</u>	20	43	6	0.006757973000048878
<u>Depth First Graph Search</u>	20	21	20	0.003534721000050922
<u>Uniform Cost Search</u>	20	60	6	0.010460765999937394
<u>Greedy Best First Graph Search with heuristic <math>h_{unmet\_goals}</math></u>	20	7	6	0.0024077629999510464
<u>Greedy Best First Graph Search with heuristic <math>h_{pg\_levelsum}</math></u>	20	6	6	0.4692074989999355

<u>Aa</u> Search Algorithm	≡ Actions	≡ Expansions	≡ Path Length	≡ Execution Time
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	20	6	6	0.35779809600001045
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	20	6	6	0.6142740919999596
<u>A* Search with heuristic h_unmet_goals</u>	20	50	6	0.009698603000060757
<u>A* Search with heuristic h_pg_levelsum</u>	20	28	6	1.191269531999751
<u>A* Search with heuristic h_pg_maxlevel</u>	20	43	6	1.2406019310001284
<u>A* Search with heuristic h_pg_setlevel</u>	20	33	6	1.4630804359999274

The optimal path length in Problem 1 is 6

## Problem 2

<u>Aa</u> Search Algorithm	≡ Actions	≡ Expansions	≡ Path Length	≡ Execution Time
<u>Breadth First Search</u>	72	3343	9	1.9982181989998935
<u>Depth First Graph Search</u>	72	624	619	3.0761934849997488
<u>Uniform Cost Search</u>	72	5154	9	3.3623013939999282
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	72	17	9	0.019361825999567372
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	72	9	9	10.810248023999975
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	72	27	9	21.229660099000284
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	72	9	9	14.85959442999956
<u>A* Search with heuristic h_unmet_goals</u>	72	2467	9	2.2257588270003907
<u>A* Search with heuristic h_pg_levelsum</u>	72	357	9	267.2171387919998
<u>A* Search with heuristic h_pg_maxlevel</u>	72	2887	9	1543.3977732800004

<u>Aa</u> Search Algorithm	≡ Actions	≡ Expansions	≡ Path Length	≡ Execution Time
<u>A* Search with heuristic h_pg_setlevel</u>	72	1037	9	1473.381522091

The optimal path length in Problem 2 is 9





### Problem 3

<u>Aa</u> Search Algorithm	≡ Actions	≡ Expansions	≡ Path Length	≡ Execution Time
<u>Breadth First Search</u>	88	14663	12	10.589345288999993
<u>Depth First Graph Search</u>	88	408	392	1.1678024960001494
<u>Uniform Cost Search</u>	88	18510	12	14.493687367999883
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	88	25	15	0.03679395900007876
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	88	14	14	23.35424014499995
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	88	21	13	28.397349992999807
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	88	35	17	81.99345919200005
<u>A* Search with heuristic h_unmet_goals</u>	88	7388	12	8.495581813000172
<u>A* Search with heuristic h_pg_levelsum</u>	88	369	12	425.12412937399995

The optimal path length is 12





### Problem 4





<u>Aa</u> Search Algorithm	≡ Actions	≡ Expansions	≡ Path Length	≡ Execution Time
<u>Breadth First Search</u>	104	99736	14	95.2429285280001
<u>Depth First Graph Search</u>	-	-	-	-
<u>Uniform Cost Search</u>	104	113339	14	191.60442371800002
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	104	29	18	0.06220758300014495
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	104	17	17	42.276428506999764

<u>Aa</u> Search Algorithm	 Actions	 Expansions	 Path Length	 Execution Time
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	104	56	17	100.87494778499968
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	104	107	23	481.362857686
<u>A* Search with heuristic h_unmet_goals</u>	104	34330	14	57.13325663600017
<u>A* Search with heuristic h_pg_levelsum</u>	104	1208	15	2368.3028229680003

The optimal path length is 14.





#### Number of nodes expanded vs number of actions





<u>Aa</u> Search Algorithm	 Nodes expanded-1	 Number of Actions-1	 Nodes Expanded-2	 Number of Actions-2
<u>Breadth First Search</u>	43	20	3343	72
<u>Depth First Graph Search</u>	21	20	624	72
<u>Uniform Cost Search</u>	60	20	5154	72
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	7	20	17	72
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	6	20	9	72
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	6	20	27	72
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	6	20	9	72
<u>A* Search with heuristic h_unmet_goals</u>	50	20	2467	72
<u>A* Search with heuristic h_pg_levelsum</u>	28	20	357	72
<u>A* Search with heuristic h_pg_maxlevel</u>	43	20	2887	72
<u>A* Search with heuristic h_pg_setlevel</u>	33	20	1037	72

<u>Aa</u> Search Algorithms	 Nodes Expanded-3	 Number of Actions-3	 Nodes Expanded-4	 Number of Actions-4
<u>Breadth First Search</u>	14663	88	99736	104
<u>Depth First Graph Search</u>	408	88	-	-
<u>Uniform Cost Search</u>	18510	88	113339	104
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	25	88	29	104
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	14	88	17	104
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	21	88	56	104
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	35	88	107	104
<u>A* Search with heuristic h_unmet_goals</u>	7388	88	34330	104
<u>A* Search with heuristic h_pg_levelsum</u>	369	88	1208	104

From the above 2 tables, we see that the number of nodes expanded increases as the number of actions increases. As we solve and move from one problem on to another, the number of actions required to find a path to the goal increases and so does the number of nodes. The amount of increase in the expanded nodes when going from one problem to another varies from algorithm to algorithm. In the case of the uninformed search algorithms and A\* with heuristic h\_pg\_levelsum, the number of nodes expanded increases significantly as the number of actions increases. However, in the case of A\* search with heuristic h\_pg\_levelsum, the number of nodes expanded increases when going from problem 1 to problem 2 but fewer nodes are expanded in problem 3 (compared to problem 2). Finally, from problem 3 to problem 4, we see an increase in the number of nodes expanded.

#### Search time vs number of actions

<u>Aa</u> Search Algorithms	 Search time-1	 Number of actions-1	 Search time-2	 Number of actions-2
<u>Breadth First Search</u>	0.006757973000048878	20	1.9982181989998935	72

<u>Aa</u> Search Algorithms	 Search time-1	 Number of actions-1	 Search time-2	 Number of actions-2
<u>Depth First Graph Search</u>	0.003534721000050922	20	3.0761934849997488	72
<u>Uniform Cost Search</u>	0.010460765999937394	20	3.3623013939999282	72
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	0.0024077629999510464	20	0.019361825999567372	72
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	0.4692074989999355	20	10.810248023999975	72
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	0.35779809600001045	20	21.229660099000284	72
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	0.6142740919999596	20	14.85959442999956	72
<u>A* Search with heuristic h_unmet_goals</u>	0.009698603000060757	20	2.2257588270003907	72
<u>A* Search with heuristic h_pg_levelsum</u>	1.191269531999751	20	267.2171387919998	72
<u>A* Search with heuristic h_pg_maxlevel</u>	1.2406019310001284	20	1543.3977732800004	72
<u>A* Search with heuristic h_pg_setlevel</u>	1.4630804359999274	20	1473.381522091	72

<u>Aa</u> Search Algorithms	 Search time-3	 Number of Actions-3	 Search time-4	 Number of Actions-4
<u>Breadth First Search</u>	10.589345288999993	88	95.2429285280001	104
<u>Depth First Graph Search</u>	1.1678024960001494	88	-	-
<u>Uniform Cost Search</u>	14.493687367999883	88	191.60442371800002	104
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	0.03679395900007876	88	0.06220758300014495	104
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	23.35424014499995	88	42.276428506999764	104
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	28.397349992999807	88	100.87494778499968	104
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	81.99345919200005	88	481.362857686	104
<u>A* Search with heuristic h_unmet_goals</u>	8.495581813000172	88	57.13325663600017	104
<u>A* Search with heuristic h_pg_levelsum</u>	425.12412937399995	88	2368.3028229680003	104

As we can see above, the search time increases with the number of actions needed to find a path to the goal. The number of actions, in turn, increases with a problem's complexity. How much the search time increases is dependent on the search algorithm. In the cases of all search algorithms, we can see a gradual increase in the search time from one problem to another except for Depth First Graph Search where it increases from Problem 1 to 2 and then drops at Problem



3(Problem 4's time couldn't be found due to search time being too long). Out of all the algorithms, A\* search with heuristic h\_pg\_levelsum takes the longest time to execute.

<u>Aa</u> Name	☰ Plan Length-1	☰ Plan Length-2	☰ Plan Length-3	☰ Plan Length-4
<u>Breadth First Search</u>	6	9	12	14
<u>Depth First Graph Search</u>	20	619	392	-
<u>Uniform Cost Search</u>	6	9	12	14
<u>Greedy Best First Graph Search with heuristic h_unmet_goals</u>	6	9	15	18
<u>Greedy Best First Graph Search with heuristic h_pg_levelsum</u>	6	9	14	17
<u>Greedy Best First Graph Search with heuristic h_pg_maxlevel</u>	6	9	13	17
<u>Greedy Best First Graph Search with heuristic h_pg_setlevel</u>	6	9	17	23
<u>A* Search with heuristic h_unmet_goals</u>	6	9	12	14
<u>A* Search with heuristic h_pg_levelsum</u>	6	9	12	15
<u>A* Search with heuristic h_pg_maxlevel</u>	6	9	-	-
<u>A* Search with heuristic h_pg_setlevel</u>	6	9	-	-

In the first and second problems, all the search algorithms except Depth First Graph Search, have the same plan length(which is the optimal plan length for the problem). In the third and fourth problems, nearly all the search problems give different plan lengths. The plan length increases with the complexity of the problem.

We can also see that the Greedy Best First Graph Search with heuristic h\_unmet\_goals is the fastest search algorithm overall and Greedy Best First Search with heuristic h\_pg\_levelsum is the algorithm that expands the least number of nodes.

## Final Questions

- Which algorithm or algorithms would be most appropriate for planning in a very restricted domain (i.e., one that has only a few actions) and needs to operate in real time?

A problem with a very restricted domain would be like Air Cargo Transport system problem 1. So the best algorithms for such problems would be algorithms with lower execution times. The algorithms with the lowest execution times in Problem 1 would be Greedy Best First Graph Search with heuristic  $h_{unmet\_goals}$  and Depth First Graph Search. These algorithms will also be most appropriate for planning in a very restricted domain and can operate in real time.

- Which algorithm or algorithms would be most appropriate for planning in very large domains (e.g., planning delivery routes for all UPS drivers in the U.S. on a given day)

A problem with larger domain would be like Problem 4. In that case, Greedy Best First Graph Search with heuristic  $h_{unmet\_goals}$  would be most appropriate because it has the fastest execution time and while it doesn't give the plan length that's optimal for the problem, its plan length isn't too far off from the optimal plan length (Problem 4's optimal plan length is 14, but the Greedy Best First Graph Search algorithm mentioned gave a plan length of 18)

- Which algorithm or algorithms would be most appropriate for planning problems where it is important to find only optimal plans?

If the aim is to find only optimal plans in a problem, then Breadth First search is the best algorithm for the job. A\* Search with heuristic  $h_{pg\_levelsum}$  is also an option for this, but it has a longer execution time than Breadth First Search.