

Questions on Eigen Values and Eigen Vectors and Simultaneous Equations and Linear Dependency and Independency:

1.

Example 46. Examine the following vectors for linear dependence and find the relation if it exists.

$$X_1 = (1, 2, 4), X_2 = (2, -1, 3), X_3 = (0, 1, 2), X_4 = (-3, 7, 2) \quad (U.P., I Sem. Winter 2002)$$

2.

Example 47. Define linear dependence and independence of vectors.

Examine for linear dependence $[1, 0, 2, 1]$, $[3, 1, 2, 1]$, $[4, 6, 2, -4]$, $[-6, 0, -3, -4]$ and find the relation between them, if possible.

3. Examine the following set of vectors for linear dependence and if dependent find relation between them

5. $X_1 = (1, 1, -1, 1), X_2 = (1, -1, 2, -1), X_3 = (3, 1, 0, 1).$

6. $X_1 = (1, -1, 2, 0), X_2 = (2, 1, 1, 1), X_3 = (3, -1, 2, -1), X_4 = (3, 0, 3, 1).$

7. Show that the column vectors of following matrix A are linearly independent:

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 6 & 2 & 1 \\ 4 & 3 & 2 \end{bmatrix}$$

8. Show that the vectors $x_1 = (2, 3, 1, -1), x_2 = (2, 3, 1, -2), x_3 = (4, 6, 2, 1)$ are linearly dependent. Express one of the vectors as linear combination of the others.

9. Find whether or not the following set of vectors are linearly dependent or independent:

(i) $(1, -2), (2, 1), (3, 2)$

(ii) $(1, 1, 1, 1), (0, 1, 1, 1), (0, 0, 1, 1), (0, 0, 0, 1).$

4.

Example 72. Find the eigen values and eigen vectors of matrix $A = \begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$

5.

Example 73. Find all the Eigen values and Eigen vectors of the matrix

$$A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix} \quad (AMIETE, Dec. 2009)$$

6.

Example 74. Find the eigen values and the corresponding eigen vectors of the matrix

$$\begin{bmatrix} -2 & 5 & 4 \\ 5 & 7 & 5 \\ 4 & 5 & -2 \end{bmatrix}$$

7.

Example 75. Find all the eigen values and eigen vectors of the matrix

$$\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$$

8.