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/*
Name: Divyashree HB
Program 2b:
    The following program computes the coefficients of an interpolating polynomial
    using newtons forward difference method.
    Furthermore, the program computes the first and second derivative using Three-point
    midpoint formula.
    This program runs on the function  $f(x)=(e^x)^2$ . Moreover, this program also
    prompts user the choice of inputing  $f(x)$  values or compute itself.
    Program calculates:
        Datapoints(equally interval points)
         $f(x)$  values using  $f(x)=(e^x)^2$  for all datapoints
        Computes the newtons forward difference table (saved in funval(functional_values))
        Computes the first and second derivative using Three-point midpoint formula.
User Input:
    Intervals
    Number of datapoints
    A choice to input  $f(x)$  or functional_values through console.
    X value of the interpolating polynomial.
Output:
    Prints the table.
     $f'(x)$  and  $f''(x)$ 
*/

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#include<iostream>
#include<vector>
#include <math.h>//exp
#include<iomanip>//precision

using namespace std;

void printhead() {
    cout << "Divyashree H B" << endl;
    cout << "Newtons differential difference" << endl;
}

double fun_x(double x) {
    cout << fixed;
    std::setprecision(6);
    return exp(x*x);
}

vector<double> computeXval(int x, int y, int points) {
    vector<double> fun(points);
    //fun = computeXval(x, y, points);
    cout << fixed;
    std::setprecision(6);
    double tempsu = (y - x) / (double)(points - 1);
    fun[0] = (x);
    for (int i = 1; i < points; i++)
    {
        //cout << tempsu << endl;
        fun[i] = fun[i - 1] + tempsu;
        //cout << fun[i] << endl;
    }
    return fun;
    //cout <<"datapoint"<< fun[0] << endl;
}

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vector<vector< double>> computefx(vector<vector< double>> &funval, vector<double> fun,
char testf, int datapt) {
    if (testf == 'N' || testf == 'n')
    {
        cout << endl << "Enter the values :" << endl;
        double tempin;
        for (int i = 0; i < datapt; i++)
        {
            cin >> tempin;
            funval[i][0] = (tempin);
        }
    }
    else
    {
        double temp;
        for (int i = 0; i < datapt; i++)
        {
            temp = fun_x(fun[i]);
            //cout << "y0\t" << temp<<endl;
            funval[i][0] = temp;
        }
    }
    return funval;
}

vector<vector< double>> filltable(vector<vector< double>> &funval, vector<double> fun,
int datapt) {
    for (int i = 1; i < datapt; i++) {
        for (int j = 0; j < (datapt - i); j++) {
            //cout << i << " " << j << " " << funval[i - 1][j + 1] << " " <<
funval[i - 1][j] << " " << endl;
            funval[j][i] = ((funval[j + 1][i - 1]) - (funval[j][i - 1])) /
(fun[j + i] - fun[j]);
        } //for (int i = 0; i < tempfun.size(); i++)cout << tempfun[i] << "tempfun"
<< endl;
    }
    return funval;
}

void printtable(vector<vector< double>> funval, vector<double> fun, int datapt) {
    cout << endl << "Differential Table :" << endl;
    //// printing the elements
    for (int i = 0; i < datapt; i++)
    {
        cout << fun[i] << " ";
        for (int j = 0; j < (datapt - i); j++) {
            cout << funval[i][j] << " ";
        }
        cout << endl;
    }
}

void computepx(vector<vector< double>>funval, vector<double> fun) {
    double X;
    cout << "\n" << "Enter the value of X:" << endl;
    cin >> X;
    //calculating P(X) for a given X
    //double prod_x=1; //(x-xi)
    double sumval = funval[0][funval[0].size() - 1]; //p(x)

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    for (int i = funval[0].size() - 2; i >= 0; i--)
    {
        sumval = funval[0][i] + (X - fun[i])*sumval;
    }

    cout << "P(" << X << ") = " << sumval << endl;
    //condition to quiet
    cout << endl;
}

int main() {

    double Xo;
    double h, f1x, f2x;
    printhead();
    int mov = 1; //exit
    double x, y; //intervals
    char testf; //testcase for N and Y
    int datapt;
    while (mov == 1)
    {
        //read data
        cout << endl << "Enter N to give functional values else enter Y" << endl;
        cin >> testf;
        cout << endl << "Enter the intervals " << endl;
        cin >> x >> y;
        //cout << x << y << endl;
        cout << endl << "Enter the number of data points" << endl;
        cin >> datapt;
        vector<double> fun = computeXval(x, y, datapt);
        //calculate data point values and save in fun array i.e x value array
        vector<vector< double>> funval(datapt, vector<double>(datapt)); //f(x)
value array
        int temp = 1;
        while (temp == 1) {
            int chint;
            cout << "\n" << "Enter 1 to print the difference table \n      2 To
compute interpolating polynomial \n      3 For computing first derivative \n      ";
            cout << "4 For computing second derivative \n      5 For computing
both derivative \n      Anything else to break : " << endl;
            cin >> chint;
            switch (chint) {
            case 1:
                funval = computeFX(funval, fun, testf, datapt);
                // fun vector holds all data points in the given interval
                //funval[i][0] in i all the initial f(x) or functional values
are found

                //starting with iteration
                funval = filltable(funval, fun, datapt);
                printtable(funval, fun, datapt);
                //computeFX(funval, fun);
                break;
            case 2:
                funval = computeFX(funval, fun, testf, datapt);
                // fun vector holds all data points in the given interval
                //funval[i][0] in i all the initial f(x) or functional values
are found

                //starting with iteration

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        funval = filltable(funval, fun, datapt);
        printtable(funval, fun, datapt);
        computepx(funval, fun);
        break;
    case 3:
        cout << "\n" << "Enter the value of Xo in f'(Xo) :" << endl;
        cin >> Xo;
        cout << "The following approximation is calculated using
three-point midpoint formula." << endl;
        h = (y - x) / (double)(datapt - 1);
        //for (int i = 1; i < datapt - 2; i++){
        f1x = (1 / (2 * h))*(fun_x(Xo + h) - fun_x(Xo - h));
        cout << "f'(" << Xo << ") = " << f1x << endl;
        break;
    case 4:
        cout << "\n" << "Enter the value of Xo in f''(Xo) :" << endl;
        cin >> Xo;
        cout << "The following approximation is calculated using
three-point midpoint formula." << endl;
        h = (y - x) / (double)(datapt - 1);
        f2x = (1 / (h * h))*(fun_x(Xo - h) - (2 * fun_x(Xo)) +
fun_x(Xo + h));

        cout << "f''(" << Xo << ") = " << f2x << endl;
        break;
    case 5:
        cout << "\n" << "Enter the value of Xo in f'(Xo) and f''(Xo):"
<< endl;

        cin >> Xo;
        cout << "The following approximation is calculated using
three-point midpoint formula." << endl;
        h = (y - x) / (double)(datapt - 1);
        //for (int i = 1; i < datapt - 2; i++){
        f1x = (1 / (2 * h))*(fun_x(Xo + h) - fun_x(Xo - h));
        cout << "f'(" << Xo << ") = " << f1x << endl;
        f2x = (1 / (h * h))*(fun_x(Xo - h) - (2 * fun_x(Xo)) +
fun_x(Xo + h));

        cout << "f''(" << Xo << ") = " << f2x << endl;
        break;
    default:
        temp = 0;
        break;
    }
}
cout << endl << "To continue enter 1 else enter 0" << endl;
cin >> mov;
}

return 0;
}

```

Output: console screen

Divyashree H B

Newtons differential difference

Enter N to give functional values else enter Y

N

Enter the intervals

0 1.1

Enter the number of data points

6

Enter 1 to print the difference table

2 To compute interpolating polynomial

3 For computing first derivative

4 For computing second derivative

5 For computing both derivative

Anything else to break :

2

Enter the values :

-6.0

-5.89483

-5.65014

-5.17788

-4.28172

-3.99583

Differential Table :

0.000000 -6.000000 0.525850 1.744000 1.834375 2.819792 -34.864062

0.200000 -5.894830 1.223450 2.844625 4.090208 -32.044271

0.400000 -5.650140 2.361300 5.298750 -21.545208

0.600000 -5.177880 4.480800 -7.628375

0.800000 -4.281720 1.429450

1.000000 -3.995830

Enter the value of X:

0.34

$P(0.340000) = -5.729433$

Enter 1 to print the difference table

2 To compute interpolating polynomial

3 For computing first derivative

4 For computing second derivative

5 For computing both derivative

Anything else to break :

5

Enter the value of X_0 in $f'(X_0)$ and $f''(X_0)$:

0.6

The following approximation is calculated using three-point midpoint formula.

$f'(0.600000) = 1.826334$

$f''(0.600000) = 5.116125$

Enter 1 to print the difference table

2 To compute interpolating polynomial

3 For computing first derivative

4 For computing second derivative

5 For computing both derivative

Anything else to break :

6

To continue enter 1 else enter 0

1

Enter N to give functional values else enter Y

Y

Enter the intervals

-1 1

Enter the number of data points

11

Enter 1 to print the difference table

2 To compute interpolating polynomial

3 For computing first derivative

4 For computing second derivative

5 For computing both derivative

Anything else to break :

3

Enter the value of X_0 in $f'(X_0)$:

-0.4

The following approximation is calculated using three-point midpoint formula.

$$f'(-0.400000) = -0.981297$$

Enter 1 to print the difference table

2 To compute interpolating polynomial

3 For computing first derivative

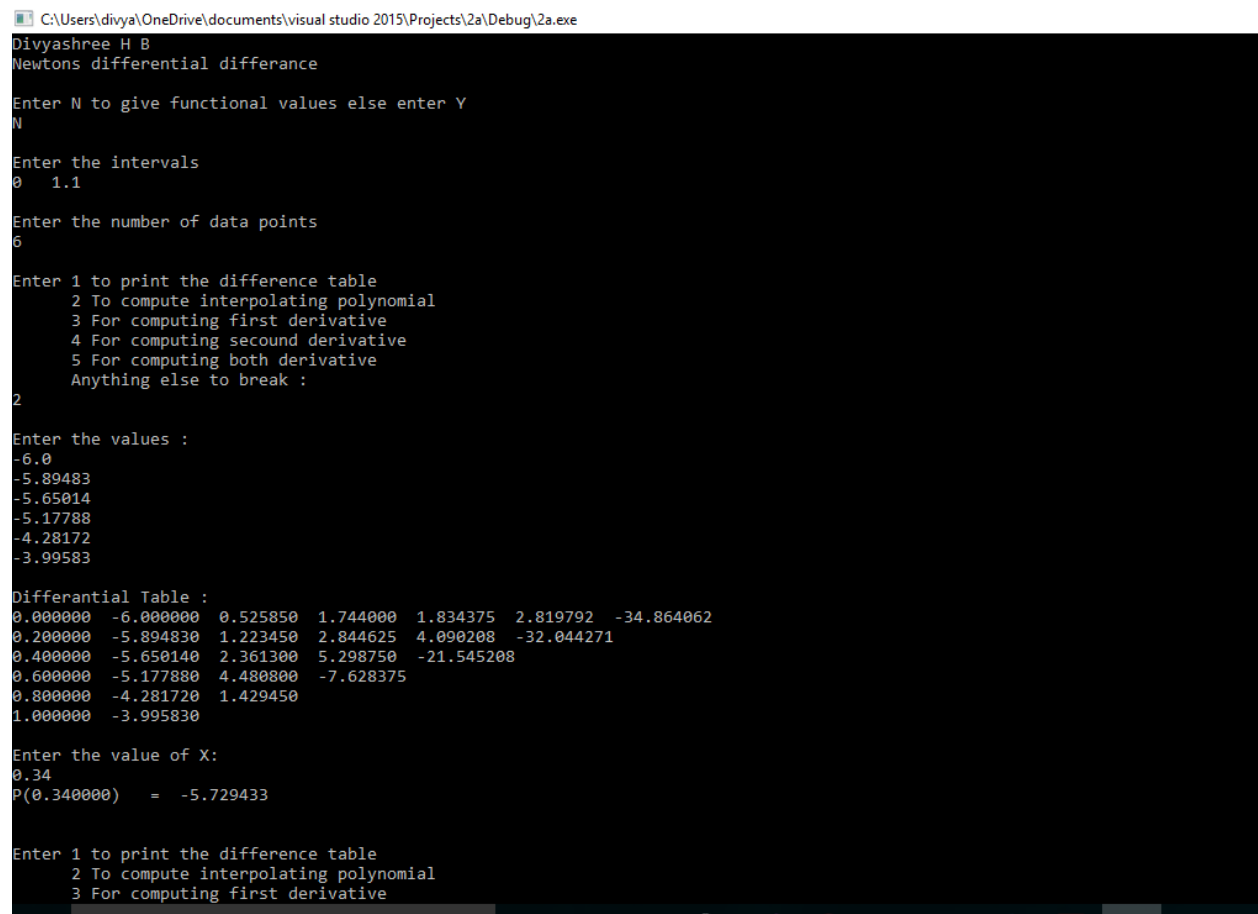
4 For computing second derivative

5 For computing both derivative

Anything else to break :

6

//screen shot



```
C:\Users\divya\OneDrive\documents\visual studio 2015\Projects\2a\Debug\2a.exe
Divyashree H B
Newtons differential difference

Enter N to give functional values else enter Y
N

Enter the intervals
0 1.1

Enter the number of data points
6

Enter 1 to print the difference table
2 To compute interpolating polynomial
3 For computing first derivative
4 For computing second derivative
5 For computing both derivative
Anything else to break :
2

Enter the values :
-6.0
-5.89483
-5.65014
-5.17788
-4.28172
-3.99583

Differential Table :
0.000000 -6.000000 0.525850 1.744000 1.834375 2.819792 -34.864062
0.200000 -5.894830 1.223450 2.844625 4.090208 -32.044271
0.400000 -5.650140 2.361300 5.298750 -21.545208
0.600000 -5.177880 4.480800 -7.628375
0.800000 -4.281720 1.429450
1.000000 -3.995830

Enter the value of X:
0.34
P(0.340000) = -5.729433

Enter 1 to print the difference table
2 To compute interpolating polynomial
3 For computing first derivative
```


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```
Enter the value of X:
0.34
P(0.340000) = -5.729433

Enter 1 to print the difference table
2 To compute interpolating polynomial
3 For computing first derivative
4 For computing secound derivative
5 For computing both derivative
Anything else to break :
5

Enter the value of Xo in f'(Xo) and f''(Xo):
0.6
The following approximation is calculated using three-point midpoint formula.
f'(0.600000) = 1.826334
f''(0.600000) = 5.116125

Enter 1 to print the difference table
2 To compute interpolating polynomial
3 For computing first derivative
4 For computing secound derivative
5 For computing both derivative
Anything else to break :
6

To continue enter 1 else enter 0
1

Enter N to give functional values else enter Y
Y

Enter the intervals
-1 1

Enter the number of data points
11

Enter 1 to print the difference table
2 To compute interpolating polynomial
3 For computing first derivative
4 For computing secound derivative
```

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Anything else to break :

6

To continue enter 1 else enter 0

1

Enter N to give functional values else enter Y

Y

Enter the intervals

-1 1

Enter the number of data points

11

Enter 1 to print the difference table

2 To compute interpolating polynomial

3 For computing first derivative

4 For computing secound derivative

5 For computing both derivative

Anything else to break :

3

Enter the value of X_0 in $f'(X_0)$:

-0.4

The following approximation is calculated using three-point midpoint formula.

$f'(-0.400000) = -0.981297$

Enter 1 to print the difference table

2 To compute interpolating polynomial

3 For computing first derivative

4 For computing secound derivative

5 For computing both derivative

Anything else to break :

6

To continue enter 1 else enter 0