

TASK 1

- ① You survey households in your area to find the average rent they are paying. Find the Standard deviation from the following data.

\$1550, \$1700, \$900, \$850, \$1000, \$950.

Sol: Mean = $\frac{\sum x}{N}$

$$= \frac{\$ (1550 + 1700 + 900 + 850 + 1000 + 950)}{6}$$

$$= \frac{\$6,950}{6} = \$1158.33$$

$$\text{Variance} = \frac{\sum (x - \mu)^2}{N - 1}$$

According to the formula of Variance

$(x - \mu)$

$$1: 1550 - 1158.33 = 391.67$$

$$2: 1700 - 1158.33 = 541.67$$

$$3: 900 - 1158.33 = -258.33$$

$$4: 850 - 1158.33 = -308.33$$

$$5: 1000 - 1158.33 = -158.33$$

$$6: 950 - 1158.33 = -208.33$$

$(x - \mu)^2$

$$(391.67)^2 = 153405.389$$

$$(541.67)^2 = 293406.389$$

$$(-258.33)^2 = 66734.3889$$

$$(-308.33)^2 = 95067.3889$$

$$(158.33)^2 = 25068.3889$$

$$(208.33)^2 = 43401.3889$$

$$\frac{\sum (x - \mu)^2}{N-1}$$

$$\frac{(153405.3889 + 293406.3889 + 66734.3889 + 95067.3889 + 25068.3889 + 43401.3889)}{(6-1)}$$

$$= 135416.66668$$

Standard Deviation

$$\sqrt{\frac{\sum (x - \mu)^2}{N-1}}$$

$$= \sqrt{135416.66668}$$

$$= \underline{367.99}$$

2. Find the variance for the following set of data representing trees in California (heights in feet)

3, 21, 98, 203, 17, 9.

$$3 + 21 + 98 + 203 + 17 + 9 = 351$$

$$(351)^{\sqrt{}} = 123201$$

$$123201 / 6 = 20533.5$$

$$\text{variance} = \frac{\sum (x - \bar{x})^2}{N - 1}$$

$$= \frac{3 \times 3 + 21 \times 21 + 98 \times 98 + 203 \times 203 + 17 \times 17 + 9 \times 9}{9}$$

$$= \frac{9 + 441 + 9604 + 41209 + 289 + 81}{9}$$

$$= \frac{51633}{9}$$

$$51633 - 20533.5$$

$$= 31099.5$$

$$= 31099.5 / 5 = 6219.9$$

3. In a class of 100 students, 80 students passed in all subjects, 10 failed in one subject, 7 failed in 2 subjects and 3 failed in 3 subjects. Find the probability distribution of the variable for no. of subjects a student from the given class has failed in.

The probability of failing in 0 subjects

$$P(x=0) = \frac{80}{100} = 0.8$$

The probability of failing in 1 subject

$$P(x=1) = \frac{10}{100} = 0.1$$

The probability of failing in 2 subjects

$$P(x=2) = \frac{7}{100} = 0.07$$

The probability of failing in 3 subjects

$$P(x=3) = \frac{3}{100} = 0.03$$

$$\text{Total probability} = 0.8 + 0.1 + 0.07 + 0.03$$

$$= 1$$

Task 2

1. A test conducted which is consisting of 20 MCQs with every MCQ having its four options out of which only one is correct. Determine the Probability that a person undertaking that test has answered exactly 5 Questions wrong.

Sol: $n = 20$ $n - k = 5$ $k = 20 - 5 = 15$.

Probability of Success (P) = $\frac{1}{4}$

Probability of failure $1 - P$

$$q = 1 - \frac{1}{4} = \frac{3}{4}$$

Binomial distribution

$$P(X=r) = \binom{n}{r} P^r q^{n-r}$$

$$P(5 \text{ out of } 20) = {}^{C(20)}_{15} * \left(\frac{1}{4}\right)^{15} \left(\frac{3}{4}\right)^{20-15}$$

$$= \frac{20 \times 19 \times 18 \times 17 \times 16}{5 \times 4 \times 3 \times 2 \times 1} \times \left(\frac{1}{4}\right)^{15} \left(\frac{3}{4}\right)^5$$

$$= 0.00000034.$$

2. A die marked A to E is rolled 50 times.
Find Probability of getting a 'D' exactly 5 times.

Sol: $n = 50$ $K = 5$ $n - K = 45$.

The Probability of Success $P = \frac{1}{5}$

" " " failure $= 1 - P$
 $= 1 - \frac{1}{5}$
 $= \frac{4}{5}$

3. Two balls are drawn at Random in Succession without replacement from an urn containing 4 red balls and 6 black balls.
Find the Probabilities of all possible outcomes.

Sol: possible ways

$$RBB = {}^4C_1 {}^6C_1 {}^5C_1$$

$$BRB = {}^6C_1 {}^4C_1 {}^5C_1$$

$$BBR = {}^6C_1 {}^5C_1 {}^4C_1$$

$$\text{no of ways} = 3$$

$$\text{Total Probabilities} = {}^{10}C_3 \text{ ways}$$

$$\frac{6 \times 5 \times 4 \times 3}{{}^{10}C_3} = \frac{\overset{B}{\cancel{6}} \times \overset{1}{\cancel{5}} \times \overset{1}{\cancel{4}} \times \overset{1}{\cancel{3}}}{\underset{2}{10} \times \underset{3}{9} \times \underset{2}{8}}$$

$$= \frac{1}{2}$$