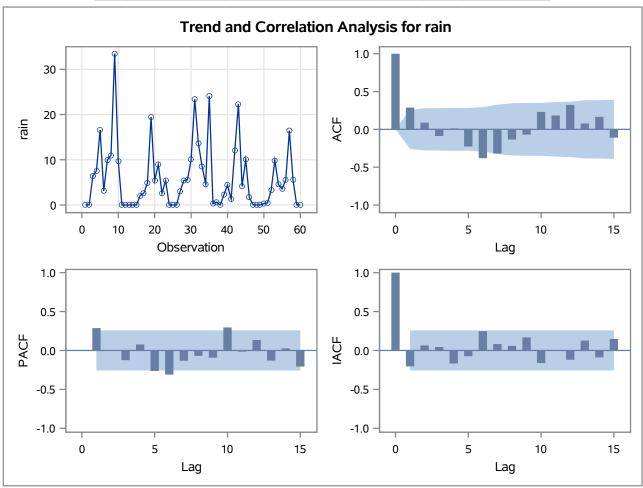
| Name of Variable = rain | | | | |
|-------------------------|----------|--|--|--|
| Mean of Working Series | 5.931944 | | | |
| Standard Deviation | 7.186866 | | | |
| Number of Observations | 60 | | | |

| | Autocorrelation Check for White Noise | | | | | | | | | |
|-----------|---------------------------------------|----|------------|------------------|--------|--------|-------|--------|--------|--|
| To Lag | Chi-Square | DF | Pr > ChiSq | Autocorrelations | | | | | | |
| 6 | 19.71 | 6 | 0.0031 | 0.287 | 0.088 | -0.088 | 0.012 | -0.227 | -0.381 | |
| 12 | 43.15 | 12 | <.0001 | -0.320 | -0.134 | -0.070 | 0.231 | 0.183 | 0.323 | |



Warning: The model defined by the new estimates is unstable. The iteration process has been terminated.

Warning: Estimates may not have converged.

| ARIMA Estimation Optimization Summary | | | | | | |
|---------------------------------------|--------------------------------------|--|--|--|--|--|
| Estimation Method | Maximum Likelihood | | | | | |
| Parameters Estimated | 9 | | | | | |
| Termination Criteria | Maximum Relative Change in Estimates | | | | | |
| Iteration Stopping Value | 0.001 | | | | | |
| Criteria Value | 10.61544 | | | | | |
| Maximum Absolute Value of Gradient | 332.036 | | | | | |

| ARIMA Estimation Optimization Summary | | | | | | |
|---|-----------------------------------|--|--|--|--|--|
| R-Square Change from Last Iteration | 0.317028 | | | | | |
| Objective Function | Log Gaussian Likelihood | | | | | |
| Objective Function Value | -190.825 | | | | | |
| Marquardt's Lambda Coefficient | 0.0001 | | | | | |
| Numerical Derivative Perturbation Delta | 0.001 | | | | | |
| Iterations | 17 | | | | | |
| Warning Message | Estimates may not have converged. | | | | | |

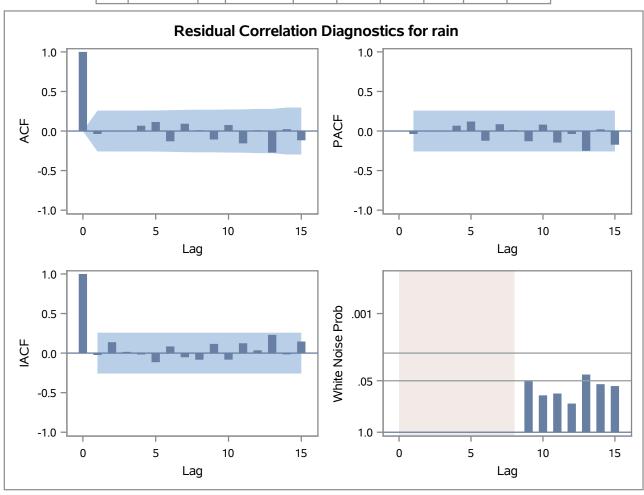
| Maximum Likelihood Estimation | | | | | | | | | | |
|-------------------------------|----------|-------------------|---------|-------------------|-----|--|--|--|--|--|
| Parameter | Estimate | Standard Error | t Value | Approx Pr > t | Lag | | | | | |
| MU | 6.02291 | 0.68561 | 8.78 | <.0001 | 0 | | | | | |
| MA1,1 | 1.17314 | 9.81378 | 0.12 | 0.9048 | 1 | | | | | |
| MA1,2 | -0.21093 | 7.26747 | -0.03 | 0.9768 | 2 | | | | | |
| MA1,3 | -0.47787 | 5.58956 | -0.09 | 0.9319 | 3 | | | | | |
| AR1,1 | 1.19975 | 0.36218 | 3.31 | 0.0009 | 1 | | | | | |
| AR1,2 | -0.30858 | 0.64536 | -0.48 | 0.6325 | 2 | | | | | |
| AR1,3 | -0.48308 | 0.42854 | -1.13 | 0.2596 | 3 | | | | | |
| AR1,4 | 0.32307 | 0.19737 | 1.64 | 0.1017 | 4 | | | | | |
| AR1,5 | -0.29276 | 0.13647 | -2.15 | 0.0319 | 5 | | | | | |

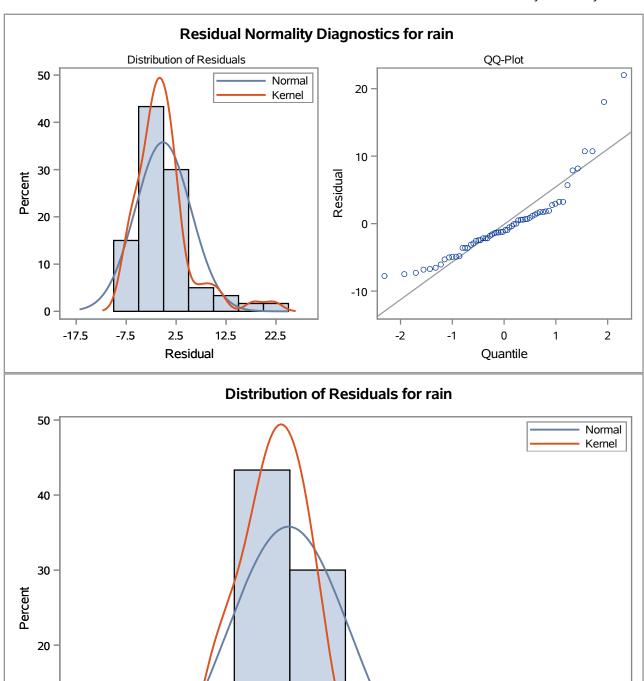
| Constant Estimate | 3.382486 |
|---------------------|----------|
| Variance Estimate | 35.95339 |
| Std Error Estimate | 5.996115 |
| AIC | 399.6491 |
| SBC | 418.4982 |
| Number of Residuals | 60 |

| Correlations of Parameter Estimates | | | | | | | | | |
|-------------------------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| Parameter | MU | MA1,1 | MA1,2 | MA1,3 | AR1,1 | AR1,2 | AR1,3 | AR1,4 | AR1,5 |
| MU | 1.000 | -0.035 | 0.035 | 0.036 | -0.003 | -0.004 | 0.003 | 0.014 | -0.023 |
| MA1,1 | -0.035 | 1.000 | -0.999 | -0.994 | 0.253 | -0.210 | 0.133 | 0.018 | 0.144 |
| MA1,2 | 0.035 | -0.999 | 1.000 | 0.987 | -0.299 | 0.259 | -0.180 | -0.015 | -0.139 |
| MA1,3 | 0.036 | -0.994 | 0.987 | 1.000 | -0.151 | 0.106 | -0.035 | -0.030 | -0.146 |
| AR1,1 | -0.003 | 0.253 | -0.299 | -0.151 | 1.000 | -0.965 | 0.843 | -0.017 | 0.064 |
| AR1,2 | -0.004 | -0.210 | 0.259 | 0.106 | -0.965 | 1.000 | -0.934 | 0.043 | 0.086 |
| AR1,3 | 0.003 | 0.133 | -0.180 | -0.035 | 0.843 | -0.934 | 1.000 | -0.333 | 0.003 |

| Correlations of Parameter Estimates | | | | | | | | | |
|-------------------------------------|--------|-------|--------|--------|--------|-------|--------|--------|--------|
| Parameter | MU | MA1,1 | MA1,2 | MA1,3 | AR1,1 | AR1,2 | AR1,3 | AR1,4 | AR1,5 |
| AR1,4 | 0.014 | 0.018 | -0.015 | -0.030 | -0.017 | 0.043 | -0.333 | 1.000 | -0.740 |
| AR1,5 | -0.023 | 0.144 | -0.139 | -0.146 | 0.064 | 0.086 | 0.003 | -0.740 | 1.000 |

| | Autocorrelation Check of Residuals | | | | | | | | | |
|-----------|------------------------------------|----|------------|------------------|--------|--------|-------|--------|--------|--|
| To Lag | Chi-Square | DF | Pr > ChiSq | Autocorrelations | | | | | | |
| 6 | | 0 | | -0.037 | -0.000 | -0.003 | 0.067 | 0.115 | -0.130 | |
| 12 | 6.13 | 4 | 0.1897 | 0.091 | 0.009 | -0.106 | 0.076 | -0.155 | 0.010 | |
| 18 | 14.25 | 10 | 0.1617 | -0.272 | 0.023 | -0.118 | 0.003 | -0.093 | -0.063 | |
| 24 | 18.80 | 16 | 0.2791 | 0.006 | -0.164 | -0.044 | 0.137 | 0.007 | -0.011 | |





10 -

-17.5

-12.5

-7.5

-2.5

2.5

7.5

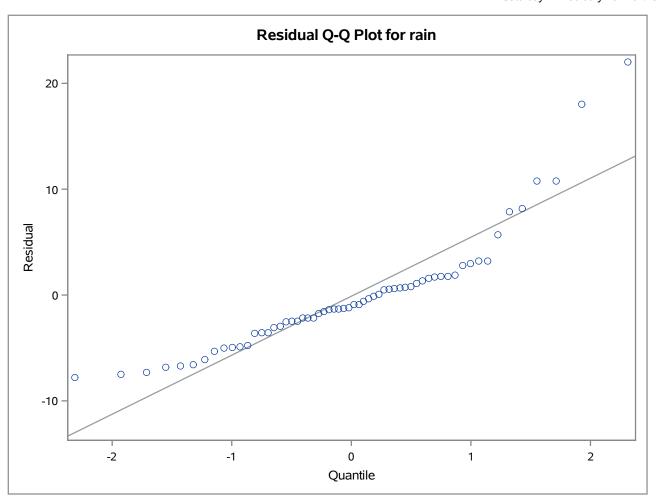
Residual

12.5

17.5

22.5

27.5



Model for variable rain 6.022905 **Estimated Mean**

| | Autoregressive Factors |
|-----------|--|
| Factor 1: | 1 - 1.19975 B**(1) + 0.30858 B**(2) + 0.48308 B**(3) - 0.32307 B**(4) + 0.29276 B**(5) |

| Moving Average Factors | | | | | | | |
|------------------------|--|--|--|--|--|--|--|
| Factor 1: | 1 - 1.17314 B**(1) + 0.21093 B**(2) + 0.47787 B**(3) | | | | | | |

| Name of Variable = pollution | | | | |
|------------------------------|----------|--|--|--|
| Mean of Working Series | 94.20369 | | | |
| Standard Deviation | 27.42528 | | | |
| Number of Observations | 60 | | | |

| | Autocorrelation Check for White Noise | | | | | | | | | |
|-----------|---------------------------------------|----|------------|------------------|--------|--------|--------|--------|--------|--|
| To Lag | Chi-Square | DF | Pr > ChiSq | Autocorrelations | | | | | | |
| 6 | 17.55 | 6 | 0.0075 | 0.127 | -0.028 | -0.041 | -0.061 | -0.214 | -0.435 | |
| 12 | 26.25 | 12 | 0.0099 | -0.151 | 0.049 | -0.026 | -0.113 | 0.110 | 0.254 | |

| Correlation of pollution and rain | | | | | |
|--|----------|--|--|--|--|
| Number of Observations | 60 | | | | |
| Variance of transformed series pollution | 837.1362 | | | | |
| Variance of transformed series rain | 50.16757 | | | | |

Both series have been prewhitened.

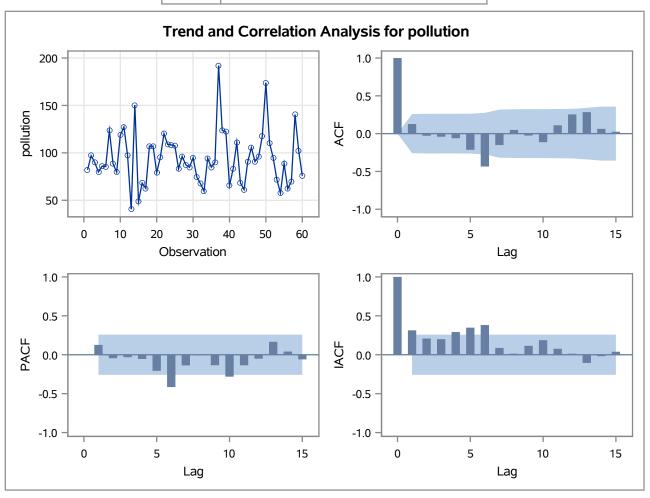
| | Crosscorrelation Check Between Series | | | | | | | | | |
|-----------|---------------------------------------|----|------------|-------------------|-------|-------|--------|--------|--------|--|
| To Lag | Chi-Square | DF | Pr > ChiSq | Crosscorrelations | | | | | | |
| 5 | 15.26 | 6 | 0.0183 | 0.208 | 0.041 | 0.192 | -0.227 | -0.321 | -0.132 | |
| 11 | 24.35 | 12 | 0.0182 | -0.176 | 0.105 | 0.030 | 0.209 | 0.227 | 0.117 | |

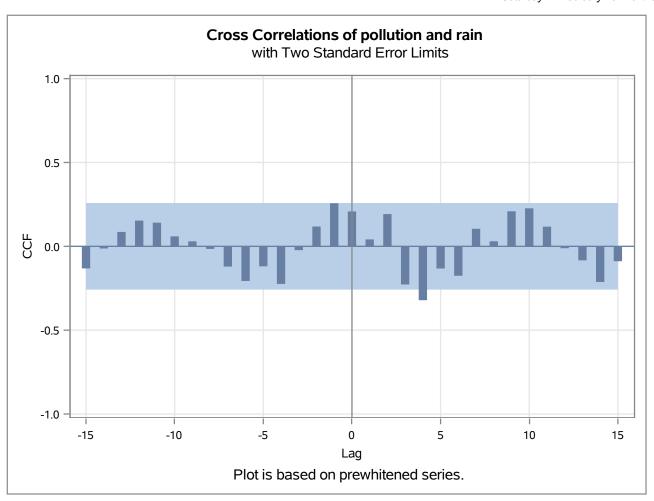
Both variables have been prewhitened by the following filter:

Prewhitening Filter

| | Autoregressive Factors |
|-----------|--|
| Factor 1: | 1 - 1.19975 B**(1) + 0.30858 B**(2) + 0.48308 B**(3) - 0.32307 B**(4) + 0.29276 B**(5) |

| Moving Average Factors | | | | | |
|------------------------|--|--|--|--|--|
| Factor 1: | 1 - 1.17314 B**(1) + 0.21093 B**(2) + 0.47787 B**(3) | | | | |



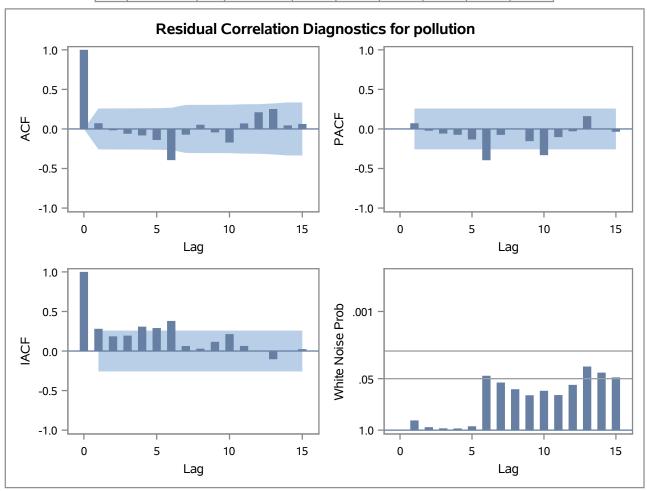


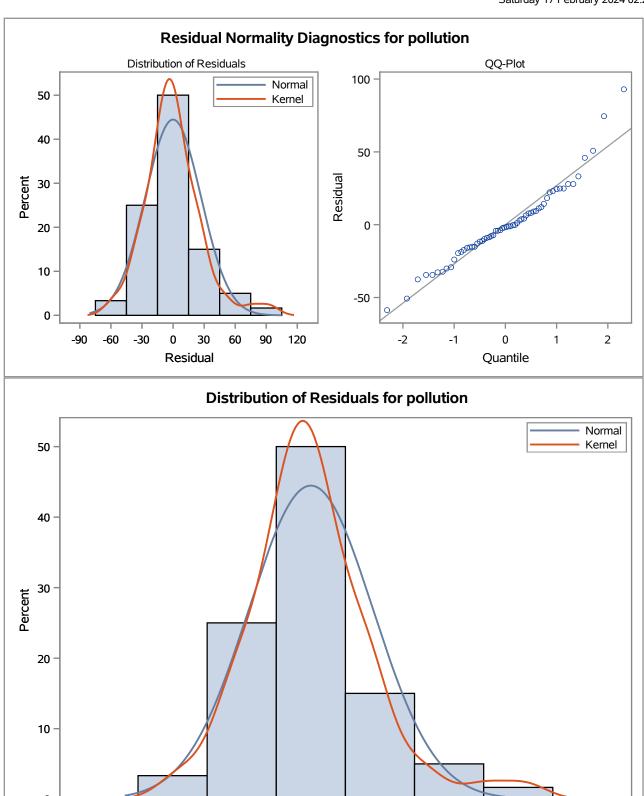
| Maximum Likelihood Estimation | | | | | | | | | |
|-------------------------------|----------|-------------------|---------|-------------------|-----|-----------|-------|--|--|
| Parameter | Estimate | Standard Error | t Value | Approx Pr > t | Lag | Variable | Shift | | |
| MU | 99.40738 | 4.54428 | 21.88 | <.0001 | 0 | pollution | 0 | | |
| NUM1 | -0.87723 | 0.48765 | -1.80 | 0.0720 | 0 | rain | 0 | | |

| Constant Estimate | 99.40738 |
|---------------------|----------|
| Variance Estimate | 736.964 |
| Std Error Estimate | 27.14708 |
| AIC | 568.3909 |
| SBC | 572.5796 |
| Number of Residuals | 60 |

| Correlations of Parameter Estimates | | | | | | |
|-------------------------------------|-----------------|--------------|--|--|--|--|
| Variable Parameter | pollution MU | rain NUM1 | | | | |
| pollution MU | 1.000 | -0.637 | | | | |
| rain NUM1 | -0.637 | 1.000 | | | | |

| | Autocorrelation Check of Residuals | | | | | | | | | | |
|-----------|------------------------------------|----|------------|------------------|--------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square | DF | Pr > ChiSq | Autocorrelations | | | | | | | |
| 6 | 13.05 | 6 | 0.0422 | 0.072 | -0.017 | -0.060 | -0.082 | -0.140 | -0.394 | | |
| 12 | 19.76 | 12 | 0.0717 | -0.072 | 0.053 | -0.044 | -0.172 | 0.070 | 0.211 | | |
| 18 | 29.27 | 18 | 0.0452 | 0.252 | 0.045 | 0.063 | 0.094 | -0.167 | -0.097 | | |
| 24 | 37.60 | 24 | 0.0381 | -0.066 | 0.027 | -0.008 | -0.262 | 0.065 | -0.084 | | |





0

30

Residual

60

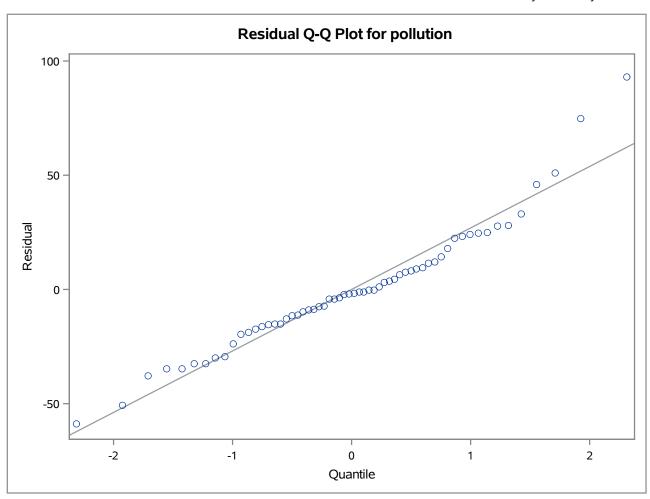
90

120

-90

-60

-30



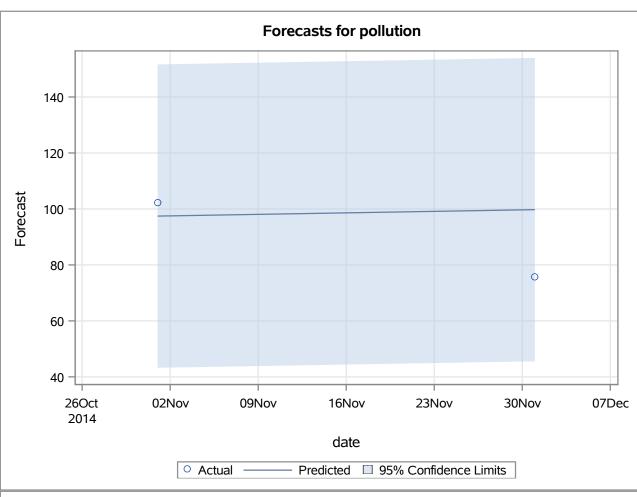
| | Crosscorrelation Check of Residuals with Input rain | | | | | | | | | | |
|-----------|---|----|------------|-------------------|--------|--------|--------|--------|--------|--|--|
| To Lag | Chi-Square | DF | Pr > ChiSq | Crosscorrelations | | | | | | | |
| 5 | 8.50 | 6 | 0.2037 | 0.189 | -0.076 | 0.291 | -0.053 | -0.086 | 0.075 | | |
| 11 | 11.28 | 12 | 0.5052 | -0.024 | 0.148 | -0.145 | -0.049 | 0.015 | -0.007 | | |
| 17 | 18.36 | 18 | 0.4319 | -0.051 | 0.013 | 0.034 | 0.251 | 0.071 | -0.214 | | |
| 23 | 20.00 | 24 | 0.6965 | 0.075 | -0.005 | 0.027 | -0.104 | -0.096 | 0.031 | | |

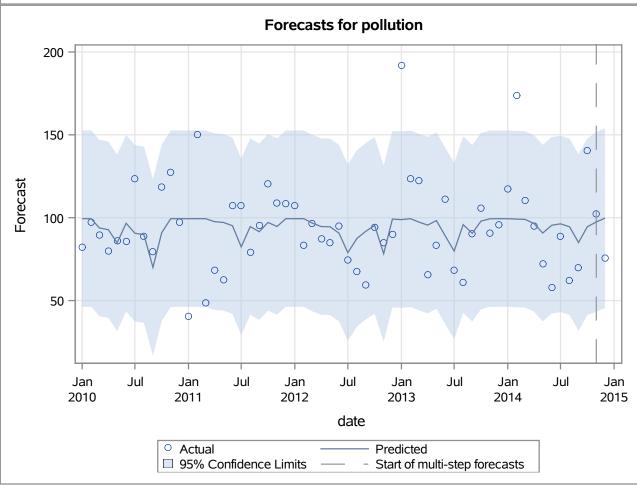
| Model for variable pollution | | | | | |
|------------------------------|----------|--|--|--|--|
| Estimated Intercept | 99.40738 | | | | |

| Input Number 1 | | | | |
|---------------------------|----------|--|--|--|
| Input Variable | rain | | | |
| Overall Regression Factor | -0.87723 | | | |

| Forecasts for variable pollution | | | | | | | |
|----------------------------------|----------|-----------|--------------------------|----------|----------|----------|--|
| Obs | Forecast | Std Error | 95% Confidence Limits | | Actual | Residual | |
| 1 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 82.0264 | -17.3810 | |
| 2 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 97.0893 | -2.3181 | |
| 3 | 93.8150 | 27.1471 | 40.6077 | 147.0223 | 89.6734 | -4.1416 | |
| 4 | 92.7550 | 27.1471 | 39.5477 | 145.9623 | 79.8069 | -12.9481 | |
| 5 | 84.8600 | 27.1471 | 31.6527 | 138.0673 | 86.0820 | 1.2220 | |
| 6 | 96.6660 | 27.1471 | 43.4587 | 149.8733 | 85.5375 | -11.1285 | |
| 7 | 90.6351 | 27.1471 | 37.4278 | 143.8424 | 123.6478 | 33.0128 | |
| 8 | 89.7578 | 27.1471 | 36.5505 | 142.9651 | 88.6815 | -1.0764 | |
| 9 | 70.0567 | 27.1471 | 16.8494 | 123.2640 | 79.6319 | 9.5753 | |
| 10 | 90.9275 | 27.1471 | 37.7202 | 144.1348 | 118.6626 | 27.7352 | |
| 11 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 127.3778 | 27.9704 | |
| 12 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 97.3333 | -2.0740 | |
| 13 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 40.5470 | -58.8603 | |
| 14 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 150.3214 | 50.9140 | |
| 15 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 48.6546 | -50.7528 | |
| 16 | 97.5798 | 27.1471 | 44.3725 | 150.7871 | 68.1806 | -29.3993 | |
| 17 | 97.1412 | 27.1471 | 43.9339 | 150.3485 | 62.5121 | -34.6291 | |
| 18 | 95.1674 | 27.1471 | 41.9601 | 148.3747 | 107.1111 | 11.9437 | |
| 19 | 82.3745 | 27.1471 | 29.1672 | 135.5818 | 107.1384 | 24.7640 | |
| 20 | 94.6192 | 27.1471 | 41.4119 | 147.8265 | 79.2366 | -15.3826 | |
| 21 | 91.5488 | 27.1471 | 38.3415 | 144.7561 | 95.1403 | 3.5914 | |
| 22 | 97.1412 | 27.1471 | 43.9339 | 150.3485 | 120.2406 | 23.0994 | |
| 23 | 94.6923 | 27.1471 | 41.4850 | 147.8996 | 108.8708 | 14.1786 | |
| 24 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 108.3737 | 8.9663 | |
| 25 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 107.4435 | 8.0362 | |
| 26 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 83.2730 | -16.1344 | |
| 27 | 96.7391 | 27.1471 | 43.5318 | 149.9464 | 96.3360 | -0.4031 | |
| 28 | 94.6557 | 27.1471 | 41.4484 | 147.8630 | 87.3972 | -7.2585 | |
| 29 | 94.5461 | 27.1471 | 41.3388 | 147.7534 | 84.7782 | -9.7678 | |
| 30 | 90.5985 | 27.1471 | 37.3912 | 143.8058 | 94.9861 | 4.3876 | |
| 31 | 78.9021 | 27.1471 | 25.6948 | 132.1094 | 74.6707 | -4.2314 | |
| 32 | 87.4551 | 27.1471 | 34.2478 | 140.6624 | 67.7137 | -19.7414 | |
| 33 | 91.8778 | 27.1471 | 38.6705 | 145.0851 | 59.5014 | -32.3764 | |
| 34 | 95.3502 | 27.1471 | 42.1429 | 148.5575 | 94.3293 | -1.0209 | |
| 35 | 78.3173 | 27.1471 | 25.1100 | 131.5246 | 84.8806 | 6.5633 | |
| 36 | 99.1515 | 27.1471 | 45.9442 | 152.3588 | 90.1169 | -9.0346 | |

| Forecasts for variable pollution | | | | | | | |
|----------------------------------|----------|-----------|--------------------------|----------|----------|----------|--|
| Obs | Forecast | Std Error | 95% Confidence Limits | | Actual | Residual | |
| 37 | 98.8591 | 27.1471 | 45.6518 | 152.0664 | 191.9745 | 93.1154 | |
| 38 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 123.6176 | 24.2102 | |
| 39 | 97.4336 | 27.1471 | 44.2263 | 150.6409 | 122.2379 | 24.8043 | |
| 40 | 95.5329 | 27.1471 | 42.3256 | 148.7402 | 65.6542 | -29.8788 | |
| 41 | 98.2743 | 27.1471 | 45.0670 | 151.4816 | 83.1801 | -15.0942 | |
| 42 | 88.8440 | 27.1471 | 35.6367 | 142.0513 | 111.1069 | 22.2629 | |
| 43 | 79.8524 | 27.1471 | 26.6451 | 133.0597 | 68.3347 | -11.5177 | |
| 44 | 95.8253 | 27.1471 | 42.6180 | 149.0326 | 61.1586 | -34.6667 | |
| 45 | 90.5985 | 27.1471 | 37.3912 | 143.8058 | 90.3694 | -0.2291 | |
| 46 | 97.9453 | 27.1471 | 44.7380 | 151.1526 | 105.5901 | 7.6447 | |
| 47 | 99.3708 | 27.1471 | 46.1635 | 152.5781 | 90.7931 | -8.5778 | |
| 48 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 95.8629 | -3.5445 | |
| 49 | 99.4074 | 27.1471 | 46.2001 | 152.6147 | 117.4422 | 18.0348 | |
| 50 | 99.1515 | 27.1471 | 45.9442 | 152.3588 | 173.8378 | 74.6863 | |
| 51 | 99.0053 | 27.1471 | 45.7980 | 152.2126 | 110.3374 | 11.3321 | |
| 52 | 96.5198 | 27.1471 | 43.3125 | 149.7271 | 94.8361 | -1.6837 | |
| 53 | 90.7447 | 27.1471 | 37.5374 | 143.9520 | 72.0605 | -18.6842 | |
| 54 | 95.4598 | 27.1471 | 42.2525 | 148.6671 | 57.6875 | -37.7723 | |
| 55 | 96.3005 | 27.1471 | 43.0932 | 149.5078 | 88.6142 | -7.6863 | |
| 56 | 94.5461 | 27.1471 | 41.3388 | 147.7534 | 62.0121 | -32.5340 | |
| 57 | 85.0062 | 27.1471 | 31.7989 | 138.2135 | 69.8056 | -15.2006 | |
| 58 | 94.5461 | 27.1471 | 41.3388 | 147.7534 | 140.3669 | 45.8209 | |
| 59 | 97.4450 | 27.6520 | 43.2482 | 151.6419 | 102.3486 | 4.9036 | |
| 60 | 99.7498 | 27.6523 | 45.5523 | 153.9474 | 75.6882 | -24.0616 | |





| Outlier Detection Summary | | |
|---------------------------|------|--|
| Maximum number searched | 2 | |
| Number found | 2 | |
| Significance used | 0.05 | |

| Outlier Details | | | | | | |
|-----------------|----------|----------|------------|----------------------|--|--|
| Obs | Туре | Estimate | Chi-Square | Approx Prob>ChiSq | | |
| 37 | Additive | 93.11535 | 17.14 | <.0001 | | |
| 50 | Additive | 74.68628 | 12.50 | 0.0004 | | |