

- Programming in a functional style
- Why functional programming?
- What is functional programming?
- Characteristics of functional programming
- What's missing?

Automatic type deduction

```
std::vector<int> myVec;
auto itVec= myVec.begin();
for ( auto v: myVec ) std::cout << v << " ";</pre>
```

Lambda-functions

```
int a= 2000;
int b= 11;
auto sum= std::async( [=] {return a+b;} );
std::cout << sum.get() << std::endl;</pre>
```





Partial function application (Currying)

- 1. std::function and std::bind
- 2. lambda-functions and auto





Haskell Curry

Moses Schönfinkel

```
int addMe(int a, int b) { return a+b; }
std::function<int(int)> add1= std::bind(addMe,2000, 1);
auto add2= []{int b){ return addMe(2000,b); };
auto add3= []{int a) { return addMe(a,11); };
addMe(2000,11) == add1(11) == add2(11) == add3(2000);
```



Higher-order functions

123456789

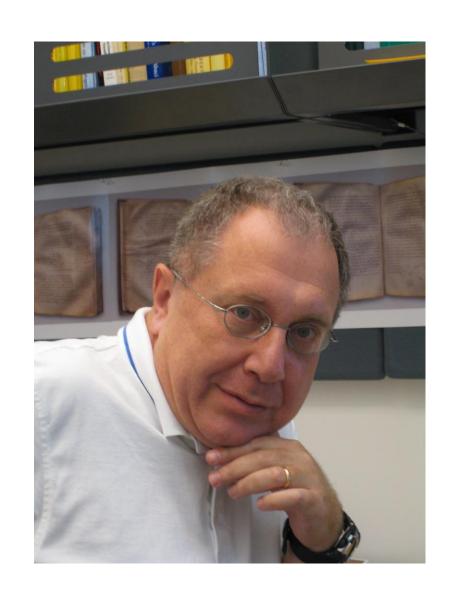
11 12 13 14 15 16 17 18 19





Generic Programming

- ML introduced generic programming.
- Alexander Stepanov (Father of the Standard Template Library) was influenced by Lisp.
- Template Metaprogramming ist a pure functional programming language in the imperative language C++.





Why functional?

More effective use of the Standard Template Library

Recognizing functional patterns

```
template <int N>
struct Fac{ static int const val= N * Fac<N-1>::val; };
template <>
struct Fac<0>{ static int const val= 1; };
```

- Better programming style
 - Reasoning about side effects (multithreading)
 - More concise





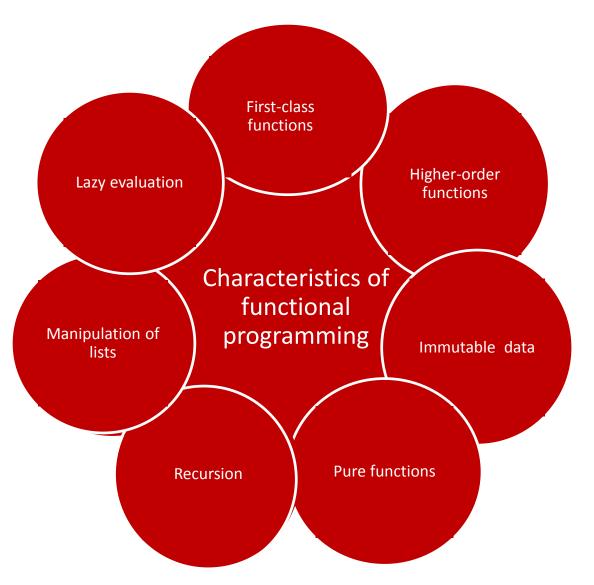
- Functional programming is programming with mathematical functions.
- Mathematical functions are functions that each time return the same value when given the same arguments (referential transparency).

Consequences:

- Functions are not allowed to have side effects.
- The function invocation can be replaced by the result, rearranged or given to an other thread.
- The program flow will be driven by the data dependencies.



Characteristics



First-class functions

Functions are first-class objects. They behave like data.

- Functions can be
 - used as arguments to other functions.

```
std::accumulate(vec.begin(), vec.end(),
                []{ int a, int b}{ return a+b; });
```

given back from functions.

```
std::function<int(int,int) > makeAdd() {
  return [](int a, int b) { return a + b; };
std::function<int(int,int)> myAdd= makeAdd();
myAdd(2000,11);
```

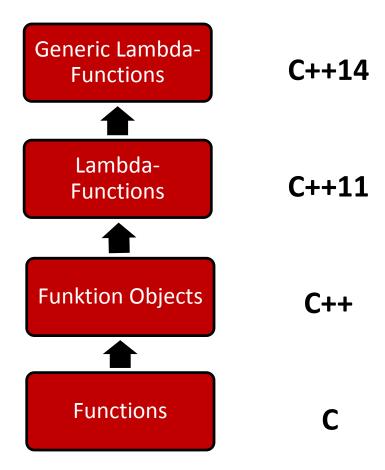
assigned to functions or stored in variables.



First-class functions

```
std::map<const char,function< double(double,double)>> tab;
tab.insert( {'+',[](double a, double b) {return a + b;} } );
tab.insert( {'-',[](double a, double b) {return a - b;} } );
tab.insert( {'*',[](double a, double b) {return a * b;} } );
tab.insert( {'/',[](double a, double b) {return a / b;} });
cout << "3.5+4.5= " << tab['+'](3.5,4.5) << endl;
cout << "3.5*4.5= " << tab['*'](3.5,4.5) << endl;</pre>
tab.insert( {'^',[](double a, double b) {return std::pow(a,b);} } );
cout << "3.5^4.5= " << tab['^'](3.5,4.5) << endl;</pre>
```

First-class functions







Higher-order functions are functions that accept other functions as argument or return them as result.

The three classics:

- map:
 - Apply a function to each element of a list.
- filter:
 - Remove elements from a list.



(source: http://musicantic.blogspot.de, 2012-10-16)

- fold:
 - Reduce a list to a single value by successively applying a binary operation to a list.

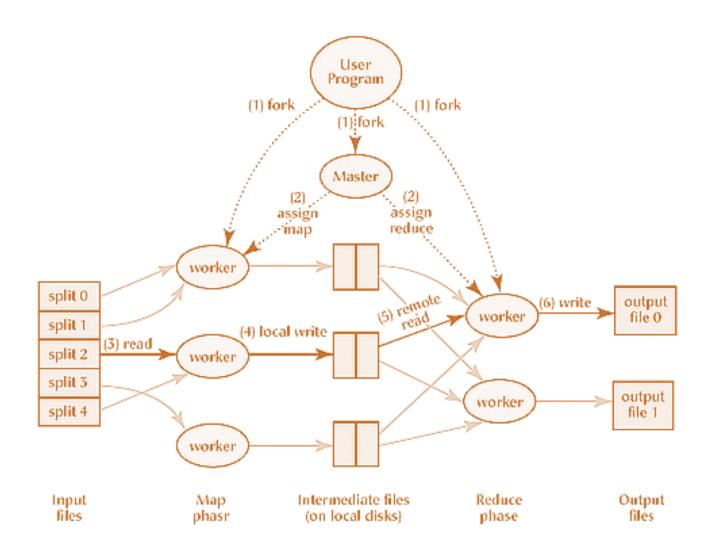




Each programming language supporting programming in a functional style offers **map**, **filter** and **fold**.

| Haskell | C++ | Python |
|---------|-----------------|--------|
| map | std::transform | map |
| filter | std::remove_if | filter |
| fold* | std::accumulate | reduce |





- Lists and vectors:
 - Haskell

```
vec= [1 . . 9]
str= ["Programming","in","a","functional","style."]
```

• C++

```
std::vector<int> vec{1,2,3,4,5,6,7,8,9}
std::vector<string>str{"Programming","in","a","functional",
"style."}
```

The results will be displayed in Haskell notation.

Higher-order functions: map

Haskell

```
map(\a \rightarrow a*a) vec map(\a -> length a) str
```

• C++



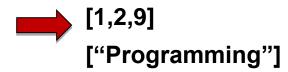


Higher-order functions: filter

Haskell

```
filter(\x-> x<3 \mid \mid x>8) vec
filter(\x \rightarrow \text{isUpper(head } x)) str
```

• C++





Higher-order functions: fold

Haskell

```
foldl (\a b \rightarrow a * b) 1 vec
foldl (\a b \rightarrow a ++ ":" ++ b ) "" str
```

• C++

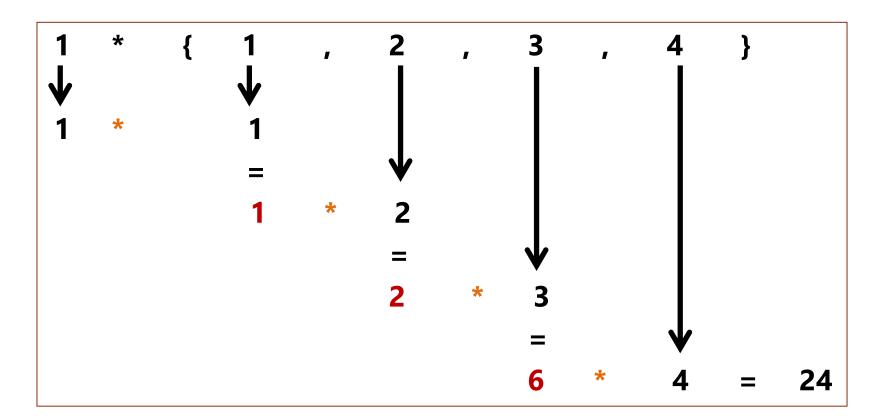


":Programming:in:a:functional:style."



Higher-order functions: fold

```
std::vector<int> v{1,2,3,4};
std::accumulate(v.begin(),v.end(),1,[](int a, int b){return a*b;});
```





Higher-order: fold expression

Reduce a parameter pack over a binary operator.

- Part of C++17
- A parameter pack is a parameter, that accepts zero or more arguments
- Simulates left and right fold with and without init value.
- foldl, foldl1, foldr and foldr1 in Haskell

```
template<typename ... Args>
bool all (Args ... args) {
  return ( ... && args);
bool b= all(true, true, true, false); // ((true && true)&& true)&& false;
```



Data is immutable in pure functional languages.

Consequences

- There is no
 - Assignment: x= x + 1, ++x
 - Loops: for, while , until
- In case of data modification
 - Changed copies of the data will be generated.
 - The original data will be shared.
- Immutable data is thread safe.



Haskell

```
qsort [] = []

qsort (x:xs) = qsort [y | y <- xs, y < x] ++ [x] ++ qsort [y | y <- xs, y >= x]
```

• C++

```
void quickSort(int arr[], int left, int right) {
  int i = left, j = right;
  int tmp;
  int pivot = arr[abs((left + right) / 2)];
  while (i <= j) {
    while (arr[i] < pivot) i++;
    while (arr[j] > pivot) j--;
    if (i <= j) {
        tmp = arr[i];
        arr[i] = arr[j];
        arr[j] = tmp;
        i++; j--;
    }
  }
  if (left < j) quickSort(arr,left,j);
  if (i < right) quickSort(arr,i,right);
}</pre>
```

Working with immutable data is based on discipline.

Use const data, Template Metaprogramming or constant expressions (constexpr).

const data
 const int value= 1;

- Template Metaprogramming
 - Is a pure functional language, embedded in the imperative language C++
 - Will be executed at compile time
 - There is no mutation at compile time



```
template <int N>
struct Factorial {
    static int const value= N * Factorial < N-1>::value;
};
template <>
struct Factorial<1>{
    static int const value = 1;
};
std::cout << Factorial<5>::value << std::endl;</pre>
std::cout << 120 << std::endl;
Factorial<5>::value
                             5*Factorial<4>::value
                             5*4*Factorial<3>::value
                             5*4*3*Factorial<2>::value
                             5*4*3*2*Factorial<1>::value = <math>5*4*3*2*1= 120
```



```
Datei
        Bearbeiten Ansicht Verlauf Lesezeichen
                                                   Einstellungen
                                                                  Hilfe
int main() {
  400874:
               55
                                               %rbp
                                        push
  400875
               48 89 e5
                                        mov.
                                               %rsp,%rbp
   std::cout << Factorial<5>::value << std::endl;_
                                             30x78, %esi
 400878:
               be 78 00 00 00
                                        mov
 40087d:
               bf 60 10 60 00
                                               $0x601060,%edi
                                        mov
 400882
               e8 89 fe ff ff
                                        callq 400710 <_ZNSolsEi@plt>
 400887
            be 70 07 40 00
                                               $0x400770,%esi
                                        mov
 40088c:
               48 89 c7
                                               %rax,%rdi
                                        mov
                                        callq 400760 <_ZNSolsEPFRSoS_E@plt>
 40088f:
               e8 cc fe ff ff
   std::cout << 120 << std::endl:
  400894:
                                             $0x78,%esi
             be 78 00 00 00
 400899:
                                               $0x601060,%edi
          bf 60 10 60 00
                                        mov.
 40089e:
               e8 6d fe ff ff
                                        callq 400710 <_ZNSolsEi@plt>
 4008a3:
             be 70 07 40 00
                                               $0x400770, %esi
                                        mov.
 4008a8:
               48 89 c7
                                               %rax, %rdi
                                        MOV
  4008ab
               e8 b0 fe ff ff
                                        callq 400760 < ZNSolsEPFRSoS_E@plt>
  return 0:
  4008b0:
               b8 00 00 00 00
                                               $0x0,%eax
                                        mov
      source : bash
```

- Constant expressions
 - are available as variables, user defined types and functions.
 - can be evaluated at compile time.
 - Variables
 - are implicit const.
 - must be initialized by a const expression.

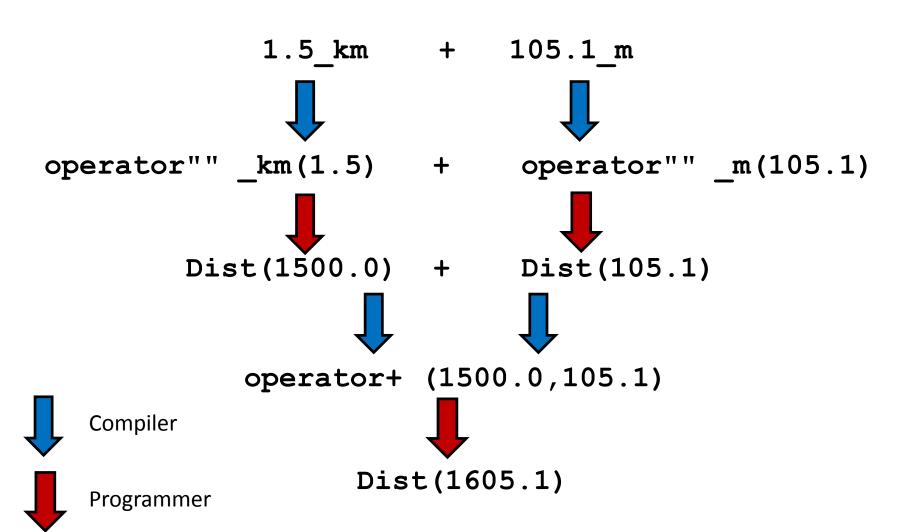
```
constexpr double pi= 3.14;
```

- User defined type
 - The constructor must be empty and a constant expression.
 - The methods must be constant expression and must not be virtual.



Objects can be created at compile time.

```
int main(){
  constexpr Dist work= 63.0 km;
  constexpr Dist workPerDay= 2 * work;
  constexpr Dist abbreToWork= 5400.0 m;
                                                      // abbrevation to work
  constexpr Dist workout= 2 * 1600.0 m;
  constexpr Dist shop= 2 * 1200.0 m;
                                                      // shopping
  constexpr Dist distPerWeek1= 4*workPerDay - 3*abbreToWork + workout + shop;
  constexpr Dist distPerWeek2= 4*workPerDay - 3*abbreToWork + 2*workout;
  constexpr Dist distPerWeek3= 4*workout + 2*shop;
  constexpr Dist distPerWeek4= 5*workout + shop;
  constexpr Dist perMonth= getAverageDistance({distPerWeek1,
                              distPerWeek2, distPerWeek3, distPerWeek4});
  std::cout << "Average per week: " << averagePerWeek << std::endl;</pre>
                                    bin: bash - Konsole <2>
                                  File Edit View Bookmarks Settings Help
                                 rainer@linux:~>constexprFunction
                                 Average per week: 255900 m
                                 rainer@linux:~>
                                            bin : bash
```



```
namespace Unit{
 Dist constexpr operator "" km(long double d) {
    return Dist(1000*d);
 Dist constexpr operator "" m(long double m) {
    return Dist(m);
 Dist constexpr operator "" dm(long double d) {
    return Dist(d/10);
 Dist constexpr operator "" cm(long double c) {
    return Dist(c/100);
constexpr Dist getAverageDistance(std::initializer list<Dist> inList) {
  auto sum= Dist(0.0);
  for ( auto i: inList) sum += i;
  return sum/inList.size();
```



```
class Dist{
public:
  constexpr Dist(long double i):m(i){}
  friend constexpr Dist operator + (const Dist& a, const Dist& b) {
    return Dist(a.m + b.m);
  friend constexpr Dist operator - (const Dist& a, const Dist& b) {
    return Dist(a.m - b.m);
  friend constexpr Dist operator* (double m, const Dist& a) {
    return Dist(m*a.m);
  friend constexpr Dist operator/(const Dist& a, int n) {
    return Dist(a.m/n);
  friend std::ostream& operator<< (std::ostream &out, const Dist& myDist) {</pre>
    out << myDist.m << " m";</pre>
    return out;
private:
  long double m;
};
```

| Pure functions | Impure functions |
|---|--|
| Always produce the same result when given the same arguments. | May produce different results for the same arguments. |
| Never have side effects. | May have side effects. |
| Never alter state. | May alter the global state of the program, system, or the world. |

Advantages

- Correctness of the code is easier to verify.
- Simplifies the refactoring and testing of the code.
- It is possible to save results of pure function invocations.
- Pure function invocations can be reordered or performed on other threads.



Working with pure functions is based on discipline.

Use ordinary functions, metafunctions or constant expression functions.

Function

```
int powFunc(int m, int n) {
  if (n == 0) return 1;
  return m * powFunc(m, n-1);
}
```

Metafunction

```
template<int m, int n>
struct PowMeta{
   static int const value = m * PowMeta<m,n-1>::value;
};

template<int m>
struct PowMeta<m,0>{
   static int const value = 1;
};
```

Constant expression functions

```
constexpr int powConst(int m, int n) {
  int r = 1;
  for(int k=1; k<=n; ++k) r*= m;
  return r;
}</pre>
```



Monads are the Haskell solution to deal with the impure world.

- Encapsulates the impure world
- Is a imperative subsystem
- Represents a computational structure
- Define the composition of computations





Functional patterns for generic types.



A Monad is a abstract data type, that transforms simple data types in higher (enriched) data types.

A Monad consists of a

- 1. Type constructor
 - Declares for the underlying type, how to become the monadic type.
- 2. Functions
 - Unit function: Inject the underlying type to a value in the corresponding monadic type. (return)
 - Function composition: Composition of monadic types. (bind)
- 3. The functions have to obey a few axioms
 - The unit function must be the left and right neutral element.
 - Die composition of operations must be associative.



Pure functions

List Monad

Reader Monad I/O MIONAL A

STW Monad

Error Monad

state Monad

Maybe Monad

Coroutine Monads

Exception Monad

optional and ranges

- std::experimental::optional
 - Is a value, the may or my not be present Maybe Monad
 - Part of the namespace std::experimental
 - Should be part of C++14
 - May become with high probability part of the next C++-Standard

```
std::optional<int> getFirst(const std::vector<int>& vec) {
  if ( !vec.empty() ) return std::optional<int>(vec[0]);
  else return std::optional<int>();
}
```

- Ranges for the Standard Library
- C++ Ranges are Pure Monadic Goodness (Bartosz Milewski)

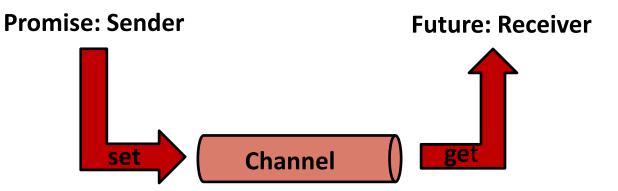


Pure functions

std::promise and std::future

- Are channels between a Sender and a Receiver.
- The Producer puts a value in the channel, the Consumer is waiting for.
- The Sender is called Promise, the Receiver Future.

```
int a= 2000, b= 11;
std::future<int> sum= std::async( [=] {return a+b;} );
std::cout << sum.get() << std::endl;</pre>
```



std::future improvements

std::promise and std::future

- Has a few serious short comings
 Futures are not composable
- Improvements for composability (TS 19571)
 - then: attach a continuation to a future fmap (Functor)
 - future<future<T>>: unboxing constructor join (Monad)
 - make_ready_future: produce a future that is ready immediately and holds a given value return (Monad)
 - when_any: produces a new future, when at least one of the futures is ready mplus (Monad Plus)
 - when all: produces a new future, when all futures are ready



C++17: I See a Monad in Your Future! (Bartosz Milewski)



Recursion

Recursion is the control structure in functional programming.

• A loop needs a running variable (for int i=0; i <= 0; ++i)

There are no variables in pure functional languages.

Recursion combined with list processing is a powerful pattern in functional languages.



Recursion

Haskell

```
fac 0=1
fac n=n * fac (n-1)
```

• C++

```
template<int N>
struct Fac{
   static int const value= N * Fac<N-1>::value;
};
template <>
struct Fac<0>{
   static int const value = 1;
};
```



fac(5) == Fac<5>::value == 120



Recursion

Fac<5>::value =

```
= 5 * Fac<4>::value

= 5 * 4 * Fac<3>::value

= 5 * 4 * 3 * Fac<2>::value

= 5 * 4 * 3 * 2 * Fac<1>::value

= 5 * 4 * 3 * 2 * 1 * Fac<0>::value

= 5 * 4 * 3 * 2 * 1 * 1

= 120
```



- LISt Processing is the characteristic for functional programming:
 - Transforming a list into another list.
 - Reducing a list to a value.
- The functional pattern for list processing:
 - 1. Processing the head of the list.
 - 2. Recursively processing the tail of the list.

```
mySum [] = 0

mySum (x:xs) = x + mySum xs

mySum [1,2,3,4,5] \longrightarrow 15
```



```
template<int ...>
struct mySum;
template<>struct
mySum<>{
  static const int value= 0;
};
template<int i, int ... tail> struct
mySum<i,tail...>{
  static const int value= i + mySum<tail...>::value;
};
                                            sum == 15
int sum= mySum<1,2,3,4,5>::value;
```

The key idea: Pattern matching

First match in Haskell

```
mult n 0 = 0

mult n 1 = n

mult n m = (mult n (m - 1)) + n

mult 3 2 = (mult 3 (2 - 1)) + 3

= (mult 3 1) + 3
```

= 3 + 3

= 6

Best match in C++

```
template < int N, int M >
struct Mult{
  static const int value= Mult<N,M-1>::value + N;
};
template < int N >
struct Mult<N,1> {
  static const int value= N;
};
template < int N >
struct Mult<N,0> {
  static const int value= 0;
};
std::cout << Mult<3,2>::value << std::endl;</pre>
```

Lazy Evaluation

- Evaluate only, if necessary.
 - Haskell is lazy

```
length [2+1, 3*2, 1/0, 5-4]
```

C++ is eager

```
int onlyFirst(int a, int) { return a; }
onlyFirst(1,1/0);
```

- Advantages:
 - Saving time and memory usage.
 - Working with infinite data structures.



Lazy Evaluation

Haskell

```
successor i= i: (successor (i+1))
take 5 (successor 1)
[1,2,3,4,5]
```

```
odds= takeWhile (< 1000) . filter odd . map (^2)
[1..]= [1,2,3,4,5,6,7,8,9,10,11,12,13,14,15 ... Control-C
odds [1..]

[1,9,25, ..., 841,961]
```

Lazy Evaluation

C++

Short circuit evaluation in logical expressions

```
if (true or (1/0)) std::cout << "short circuit evaluation" short circuit evaluation
```

- Expression Templates
 - Use Operator Overloading and Template Metaprogramming
 - A templated expression store the structure of some arbitrary sub-expression. The recursive evaluation of the expression-tree takes places at the assignment of the result.

```
Vec<int> a(LEN), Vec<int> b(LEN), Vec<int> c(LEN);
Vec<int> res= a*b + b*d;
```



Ranges

Ranges for the Standard Library (N4128) by Eric Niebler

- Algorithm for std::vector<int> v{1,2,3,4,5,6,7,8,9};
 - Classical with Iterators

```
std::sort( v.begin(), v.end() );
```

New with Ranges

```
std::sort( v );
```

Range Adaptors support pipelines and lazy evaluation



- List comprehension: Syntactic sugar for map and filter
- Like mathematic

```
\{v*v \mid v \in N , v \mu o \delta 2 = 0 \}: Mathematik [n*n \mid n < -[1..], n \mod 2 == 0]: Haskell
```

Example



Range Comprehension

Pythagorean triple in Haskell with List Comprehension

```
triples = [(x, y, z)|z <-[1..], x <-[1..z], y <-[x..z], x^2 + y^2 == z^2] triples = (>>=) [1..] x = -2 (>>=) [1..z] x = -2 (>>=) [1..z] x = -2 (>>=) [x..z] x = -2 (>>= z^2) >> return (x, y, z) take 5 triples
```

Pythagorean triple in C++ with Range Comprehension

```
auto triples =
  view::for_each(view::ints(1), [](int z) {
    return view::for_each(view::ints(1, z), [=](int x) {
        return view::for_each(view::ints(x, z), [=](int y) {
            return yield_if(x*x + y*y == z*z, std::make_tuple(x, y, z));
        });
    });
    for (auto triple: triples | view::take(5)) { ...
```



[(3,4,5),(6,8,10),(5,12,13),(9,12,15),(8,15,17)]

Syntactic sugar for Monads: do-Notation

```
triples = do
  z <-[1..]
  x <-[1..z]
  y <-[x..z]
  guard(x^2 + y^2 == z^2)
  return (x,y,z)

take 5 triples</pre>
```



[(3,4,5),(6,8,10),(5,12,13),(9,12,15),(8,15,17)]

Function composition: fluent interface

```
(reverse . sort) [10,2,8,1,9,5,3,6,4,7]

[10,9,8,7,6,5,4,3,2,1]

isTit (x:xs)= isUpper x && all isLower xs

sorTitLen= sortBy(comparing length) . filter isTit . words
sorTitLen "A Sentence full of Titles ."
["A","Titles","Sentence"]
```



Typeclasses are interfaces for similar types.

• Typeclass Eq

```
class Eq a where
    (==) :: a -> a -> Bool
    (/=) :: a -> a -> Bool
    a == b = not (a /= b)
    a /= b = not (a == b)
```

Type Bool as instance of the typeclass Eq.

```
instance Eq Bool where
True == True = True
False == False = True
_ == _ = False
```







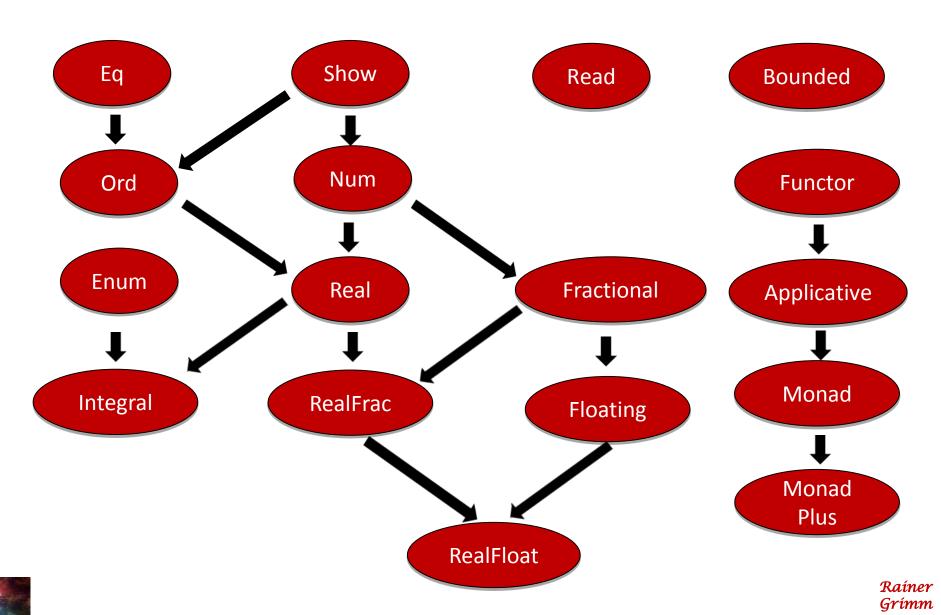
Datentyp Day as member of Eq and Show

```
data Day= Morning | Afternoon deriving (Eq,Show) isEqual a b = a == b
```

```
Prelude>
Prelude> Morning == Morning
True
Prelude> Morning == Afternoon
False
Prelude> Morning
Morning
Prelude> isEqual Morning Afternoon
False
Prelude> :type isEqual
isEqual :: Eq a => a -> a -> Bool
Prelude>
```

Userdefined typeclasses are supported.





- Concepts Lite are constraints for templates.
 - Models semantic categories rather then syntactic restrictions.
 - State requirements of templates at there declaration.
 - Support function overloading and class templates specialization based on constraints.
 - Integrates with automatic type deduction.
 - Improves error messages by checking template arguments at the point of template instanziation.



Additional benefit with no cost for the run time, compile time or code size.

Template declaration

```
template<Sortable Cont>
void sort(Cont& container);
```

equivalent

```
template<typename Cont>
  requires Sortable<Cont>()
void sort(Cont& container);
```

Sortable must be a predicate (constexpr)

```
template <typename T>
constexpr bool Sortable(){ . . .
```

```
std::list<int> lst = {1998,2014,2003,2011};
sort(lst); // ERROR: lst is no random-access container with <</pre>
```

- Concepts Lite works for any template
 - Function templates

```
template<LessThanComparable T>
const T& min(const T &x, const T &y) {
  return (y < x) ? y : x;
}</pre>
```

Class templates

```
template<Object T>
class vector;

vector<int> v1; // OK
vector<int&> v2 // ERROR: int& does not satisfy the constraint Object
```

Member functions of class templates

```
template <Object T>
class vector{

  void push_back(const T& x)
   requires Copyable<T>();
};
```

Automatic type deduction

```
auto func(Container) -> Sortable;
Sortable x= func(y);
```

- Concepts Lite supports
 - Multiple requirements for the template arguments.

Overloading of function and class templates specialization.

```
template<InputIterator I>
void advance(I& iter, int n);
template<BidirectionalIterator I>
void advance(I& iter, int n);
template<RandomAccessIterator I>
void advance(I& iter, int n);
```

```
std::list<int> lst{1,2,3,4,5,6,7,8,9};
std::list<int>:: iterator i= lst.begin();
std::advance(i,2);
BidirectionalIterator
```

Basic

- DefaultConstructible
- MoveConstructible
- CopyConstructible
- MoveAssigable
- CopyAssignable
- Destructible

Container

- Container
- ReversibleContainer
- AllocatorAwareContainer
- SequenceContainer
- ContinguousContainer
- AssociativeContainer
- UnorderedAssociativeContainer

Layout

- TriviallyCopyable
- TrivialType
- StandardLayoutType
- PODType

Iterator

- Iterator
- InputIterator
- OutputIterator
- ForwardIterator
- BidirectionalIterator
- RandomAccessIterator
- ContinguousIterator

Container element

Stream I/O functions

Random Number Generation

Library-wide

- EqualityComparable
- LessThenComparable
- Swappable
- ValueSwappable
- NullablePointer
- Hash
- Allocator
- FunctionObject
- Callable
- Predicate
- BinaryPredicate
- Compare

Concurrency

Other

```
includ
nt mais(){
 std::cout <<
 std::vector-
 std::iota(my
 std::cout
 for ( auto.
 std::cout
                                             ind( std::logical
 std::function< bool (an example ayBindPro
 myVec.erase(std: remove_if(myVec.
 std::cout << "my Vele:
 for ( auto i: myVec) std::cout <<
 std::cout << "\n\n";
                                        Rainer Grimm
 std::vector<int> myVec2(20);
                                        www.grimm-jaud.de
 std::iota(myVec2.begin()::yVec2
                                        rainer@grimm-jaud.de
 std::cout << 'nvVec2:
```