



Pointers

Q. Why do we need pointer?

- * it stores address in Hexadecimal number
0x7ff593fe:

Variable stores address of other variables.

$$P = \&i$$

→ int *P = &i; → int type aka address

P is a pointer of an integer → which stores address of i;

cout << P << endl → address

cout << *P << endl → value

Note

64 bit

int 32bit

$$\text{int } *q = P;$$

it means *q *p i

same will print same

Concept

→ When address is provided to pointer then it points garbage address and it also contains garbage value as well as

→ If you not initializing value to pointer then assign it null value.

Pointer Arithmetic

Size of all pointer is same (8 byte, 4 byte)

5. Operators on pointer

1. $\text{int } i = 10$

$\text{int } *p = &i;$

10. $\text{cout} \ll p \ll \text{endl};$

$p = p + 1;$

11. $\text{cout} \ll *p \ll \text{endl};$

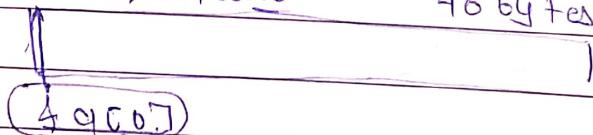
$\rightarrow +4 \text{ byte}$

$p + 1 \rightarrow$ next integer \rightarrow point to next add

15. $p - 1 \rightarrow$ previous integer
 $\downarrow -4 \text{ byte}$

* Array & pointer

20. $\text{int } q[10];$ for these ↓
 \hookrightarrow name 40 bytes



25. int main ()

$\text{int } q[10];$

$\text{cout} \ll q \ll \text{endl};$

$\text{cout} \ll *q \ll \text{endl};$

$q[0] = 5;$

30. $q[1] = 10;$

\rightarrow 1st element
at address

$\text{cout} \ll &q \ll \text{endl}$ \rightarrow 1st element

$\text{cout} \ll *(q+1) \ll \text{endl}$ \rightarrow next element

$$i[a] \rightarrow * (i+a)$$

$$a[i] \rightarrow * (a+i) \rightarrow \text{Same}$$

- * ① size of
- ② 4 op.

Concept

In case of array $\rightarrow a[10]$

containing

address of 1st elem

size of (a)

whole size \rightarrow 40 byte

$$\text{int } *p = 4 a[0];$$

add 700

$p \rightarrow$ add at 890

now can change

$$*p = 4 a[3]$$

\rightarrow +8 byte (708 byte)

$a+i$ not allowed

Array

$$(a = a + i)$$

a correspond to other memory
 \rightarrow can't change

\rightarrow array can't be assigned.

Character & Pointers

- * it behaves diff in character

```
int main()
{
```

```
int a[3] = {1, 2, 3}
```

```
char b[3] = {'a', 'b', 'c'}
```

```
cout << a << endl;
```

```
cout << b << endl;
```

→ a b c print karayega
null character dekh
kuch jayega

```
Char + c = A b [0]
```

```
cout << c;
```

→ phir se abc print
karayega jab tak null char
na milen

```
Char c1 = 'a';
```

```
Char *pc = &c1;
```

```
cout << c1 << endl;
```

```
cout << pc << endl;
```

- * array jab initialize karte hain Tab.
Ek temporary memory create hoga
and ~~iska~~ wo temporary memory
ki copy banegi

- * pointer mai usq kuch nahi hota
vo temp memory ko point karta hota

Pointer & functions

Print f^y

```
5 void print (int * p)
{
    cout << *p << endl;
}
```

```
10 int main()
{
```

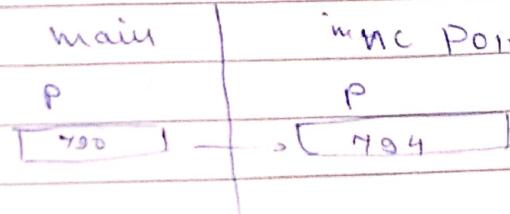
```
    int i = 10;
    int * p = &i;
    print (p);
}
```

```
15 cout << p << endl,
    increment Pointer (p);
    cout << p << endl;
```

A address same

```
void increment (int * p)
{
    (*p)++;
}
```

value change



Array Passed as pointer

```
int sum (int * a, int size)
```

```
{
```

```
    int ans = 0;
```

```
    for (int i = 0; i < size; i++)
    {
```

```
        ans += a[i];
    }
```

```
    return ans;
}
```

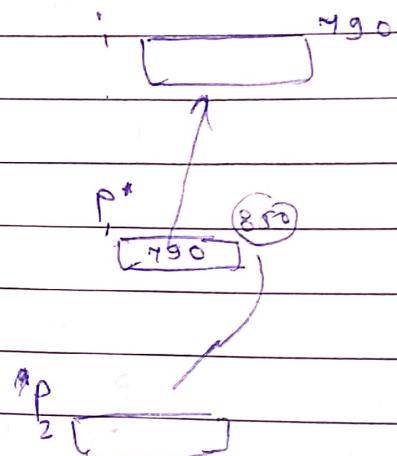
```
15 int main()
```

```
{ int a[10];
```

```
cout << "size of array: " << (a + 3, 7) << endl;
```

Double Pointer.

int *P = &i



int **P2 = &P

int main()

{

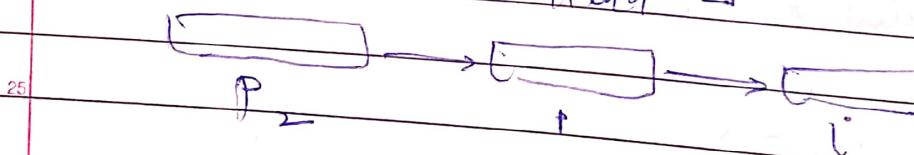
int i = 10;

int *P = &i;

int **P2 = &P;

cout << P2 << endl;

cout << *P2 << endl; } same



Dynamic Allocation

Type casting

Why we write pointer with * ?

like why we have to initialize datatype

like - why `int * p;`

why not `pointer * p;`

* because we have to read byte and
how to interpretate

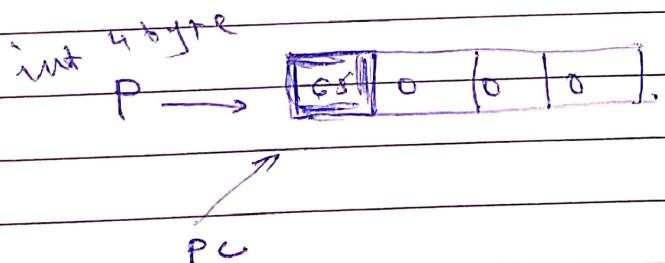
```
int i = 65;
char * c = i;
cout << c << endl;
```

Implicit

```
int * p = 45;
char * pc = p;
```

Explicit

```
int * p = 45;
char * pc = (char *) p;
cout << * p << endl;
cout << *(p+1) << endl;
cout << *(p+2) << endl;
cout << *(p+3) << endl;
```



(1) direct

(2) pointer to byte

Reference & Pass by reference

Reference Variable

int main()

{

int i = 10;

int& j = i; \rightarrow j mai i ka address

i++;

Store so jo change

cout << j << endl; J mai vo i mai koi

j++.

versa

cout << i << endl;

int k = j;

cout << k.

int t; \rightarrow

t = i \times wrong

is when declared you have to also
initialized

Pass by Reference in fn.

Void increment (int& n) $\overset{2}{\textcircled{2}}$ shared same memory

{

n++;

}

main ()

{

increment (i)

cout << i << endl;

}

* benefit → - value ref of Jaisakhte hai
→ same memory use Jaisakhte hai.

Camlin Page
Date

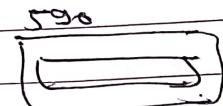
What if? (Return by reference)

int & f(int n)

5 ()
Created local var. int a = n;
 } return = q;
 }

fu created memory
for some time

q → 580
JK → 590



Similarly fu se int point.

int * f2(); {

Created local var. int i = 10;
 } return &i; i → 580

580
local memory

int main()

{

int & K = f2();

↑

it may
clear.
memory after
fu call.

int & p = f2();

}

basically {,

EK fu ok Jaise bhi local variable

kg reference ya pointer return karwaya gaya
to problem hoga because it will

vanished
y

Dynamic Memory Allocation

bad things

`int a[20];` → fixed size array

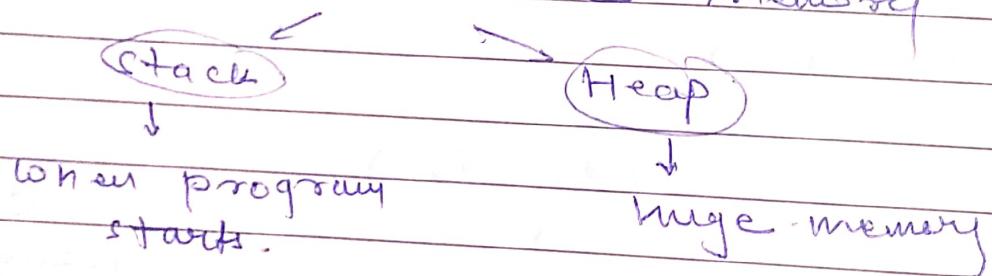
`int n;` → decided at runtime

`array;`

`int a[n];`

What DMA do. → drawbacks of

- * Whenever we allocate memory



When you write

`int i = 10;` → stored in Stack;

`int a[20]`

`int a[2000];`

In Heap → we can allocate memory in runtime.

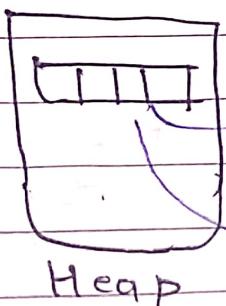
→ giving dynamic allocation

How D MA works

HA! HA! HA!

new

newint



it will creat 4 byte
in Heap

Heap

we do not give name
to new

Eye memory ka address
tak dega

Then how use?

pointer mai

save kar lega

like

`int *p = new int;`

`(*p = 10)`

→ if you want to change

Step

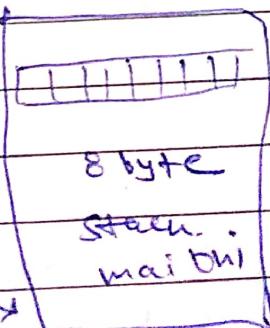
Store Kar lega

Address aayegi

`int *p = new int;`

`*p = 10;`

`cout << *p << endl;`



How to Create Array Dynamically

`{new int[50]}`

`int *p = new int [50];`

8 byte in ~~stack~~
heap

[50]

200 byte in heap

→
`int n;
cout << " " ->> n;`

`int *p[2] = new int[n];`

`for (int i=0; i<n; i++)`

{

`cin >> p[2][i];`

}

`int man = -1;`

`for (int i=0; i<n; i++)`

`if (man < p[2][i])`

{

`man = p[2][i];`

}

`}`

`cout << man << endl;`

25

30

* Major diff b/w static & dynamic memory

```
5    pn → int main () {
        while (true)
        {
            int * p = new int;
        }
}
```

```
10   while (true)
        {
            int i = 10;
        }
}
```

15 during this iteration

the memory will creat
in stack and automatic
delete

20 But when this called
the memory is not deleted
you have to delete the
memory by

25 { We don't
deleted p. }

30 { we deleted the
element which p } → { delete P }

35 { 8 byte pointer
in stack. }

40 This automatic
deleted

45 { 4 byte
by delete P.
it will delete
the memory of p }

What's About 2-D Array?

for 1-D array we define

int arr[5]; // meant [0:4]

arr[0]

arr[1]

arr[2] for storing 1-D pointers

int *arr = new int[5];

truly way

arr[0] = new int[10];

other pointer

arr

p(0) = new int[10];

p(1) = new int[10];

now we access (0,1)

is

Code

in main()

{

This is called

int *p = int new int[10];

int w[10];

cin >> w;

for (i = 0; i < n; i++)

p[i] = new int[10];

for (i = 0; i < n; i++)

{ cin >> p[i][j]; }

How much memory allocate in (T, 10)

Q. How to deallocate the memory?

For (int i=0; i<m; i++)

{

delete [] P[i];

}

delete [] P;

array ↗ uses and array ki
memory.delete

Why don't we create like int C[m][n]
in pointer;

15

20

25

30

20]

Macros & Global Variables

1. #define

ex:- #define PI 3.14

→ doesn't take
storage memory

→ compile time se pehle
he ye PI ko find kar k
3.14 Kar dega.

No extra memory.

2. Global Variables.

int g;

→ globally defined

void g() {

 ++;

 cout << g();

}

If value in one

fn change then the

value changed in

all fn.

(X) bad to
use

void f() {

 cout << g();

 g();

}

int main()

{

 g();

 f();

 f();

 cout << g();

Inline fn

(1) Ternary operators

int c = (a > b) ? a : b.

agar True to c mai a
agar False to c mai b.

[inline] int man (int a, int b)

{
 return (a > b) ? a : b;
}

int main ()

{
 int a, b;

 cin >> a >> b;

 int c = man (a, b);

 int x, y;

 x = 12;

 y = 34;

 int z = man (x, y);

copy

copy

* means koye fn nahi hui to pura code
uthi ke mein mai aayega;

* How to make Four "f" from Single "f"

-> Make it default arguments

Note :- You can only start making arguments default from right side.

int sum 2 (int a, int b = 0, int c = 0, int d = 0)
 { return a + b + c + d
 } what it mean?

int main()

{
 int a[20]

cout << sum(a, 20). <new

① sum (int a)
 {

 return a + a;

Making Arguments.

sum 2 (int a, int b)

{
 return a + b;

Optional

sum 3 (int a, int b, int c)

{
 return a + b + c;

exp.

Constant Variables

int main ()

{

Wahi hi

Wahi initialize

karo

const int i = 10;

int j = 12;

const int & k = j;

k++;

j++;

→ we can also write
int const

}

Const laga deyq matlab only read kar
sakte bhiya!

Storage constant not main only
path constant.

Pointers

int const i = 10;

int const * p = &i;

int j = 12;

int const * p2 = &j;

cout << *p2 << endl;

j++

cout << *p2 << endl;

Recursion

f_n calling itself

Let,

$$n! = n \cdot n-1 \cdot n-2 \cdots$$

$$n! = n \cdot (n-1)!$$

$$\text{fact}(n) = n + \text{fact}(n-1)$$

Program for factorial

int factorial (int n)

{

 cout << n << endl;

 if (n == 0)

{

 return 1;

}

 int smallOutput = factorial (n - 1);

 return n + smallOutput;

}

int main ()

{

 int n;

 cin >> n;

 int output = fact(n);

 cout << output << endl;

Principle of Mathematical Induction (PMI)

To prove some facts.

Let,

some fact of $f(n)$ is true $\forall n$.

PMI says,

① Prove $f(0)$ or $f(1)$ is true (Base case)

② Induction hypothesis (Assume)

$f(k)$ is true.
Assume

③ Induction step (using ② prove
 $f(k+1)$ is true)

Prove sum of n natural numbers $\frac{n(n+1)}{2}$

① Base case: $f(0)$ i.e. $\sum 0 = 0$ (LHS)

$$\text{RHS} \cdot \frac{n(n+1)}{2} = 0$$

$$② \sum 1 = 1 \quad \text{LHS}$$

$$\frac{1((1+1))}{2} = 1 \quad \text{RHS}$$

③ Induction hypothesis $\sum k = \frac{k(k+1)}{2}$

$$\sum k+1 = \frac{(k+1)(k+2)}{2}$$

$$k+1 + \sum k = \frac{(k+1)}{2} + \frac{(k+1)(k+2)}{2}$$

$$\left(\frac{k+1}{2}\right)(k+2)$$

fibonacci number

0 1 1 2 3 5 8 13 21 34

$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$

Base Case : Prove $\text{f}(0)$ & $\text{f}(1)$ is true.IH : Assume $\text{f}(i)$ is true $\forall i \leq k$ Tc : Use (2) to prove $\text{f}(k+1)$ is true

int fib(7n+4)

if (n == 0)
 f
 return 0;

}

if (n == 1)

f
 return 1;

}

int smallOutput1 = fib(n-1);

int smallOutput2 = fib(n-2);

{ return smallOutput1 + smallOutput2; }

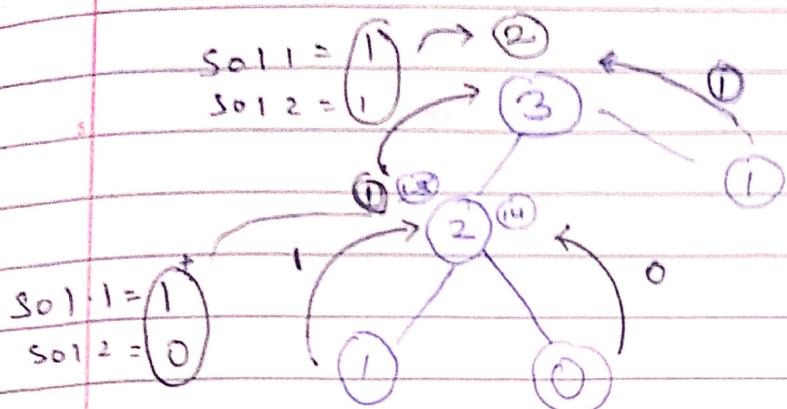
int main()

{

cout << fib(3) << endl;

}

dry run



Q Check if array is sorted or not use Recursion?

bool is_sorted(int arr[], int size)

if (size == 0 || size == 1)

{

return true;

}

if ($arr[0] > arr[1]$)

{

return false;

}

bool isSmallestSorted = is_sorted(arr + 1, size - 1)

{

return isSmallestSorted;

dry run

true (3 4 5 6) (5)

true (3 4 5 6) (4)

true (4 5 6) (3)

true (5 6) (2)

true (6) (1)

Same problem from q+1

bool isSmaller (q+1, size-1)

{

if (l is smaller or not)

{

return false;

}

if ($q[i] > q[i]$)

{

return false;

else

{ return true;

}

Q1 Problem ① (1st index). by Rec.

int index (a⁺, n, x)

{

 if (n == 0)

{

 return -1;

}

 if (a⁺ == x)

{

 return 0;

}

 base case

15 int ind = index (a+1, n-1, x);

 if (ind == -1)

{

 return -1

}

 else

{

 return ind + 1;

}

25

int main()

{ int i, n, x, k;

cin > n;

for (i = 0; i < n; i++)

{

 cin > a[i];

}

cin > x;

cout << index(a, n, k);

30

Problem ② Last index.

Same process followed but Reca is in second step then small calc per.

```
int index(int a[], int n, x)
```

```
{
```

base case

```
if (n == 0)
```

```
{
```

return -1

```
}
```

```
int ind = index(a[], n-1, x)
```

```
{ return ind+1;
```

~~```
if (*a == x)
```~~~~```
{
```~~~~```
return i
```~~~~```
}
```~~

else,

~~```
{ return -1
```~~~~```
}
```~~~~```
if (ind == -1)
```~~~~```
{
```~~~~```
if (a[] == n)
```~~~~```
{
```~~~~```
return 0;
```~~~~```
}
```~~

else

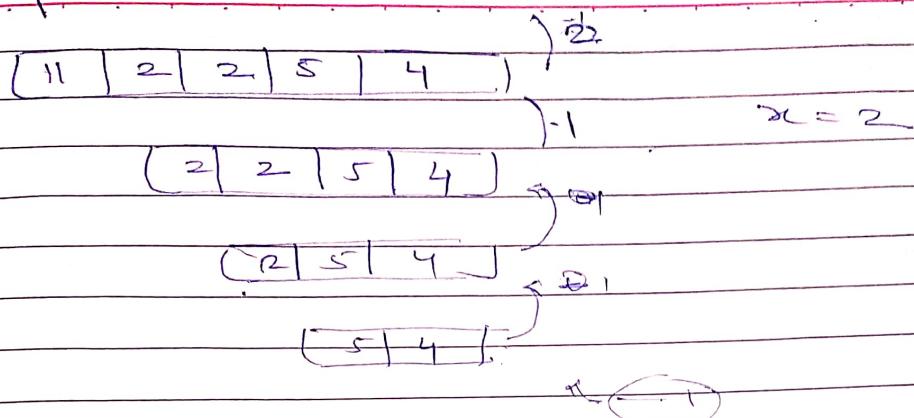
```
{
```

return -1;

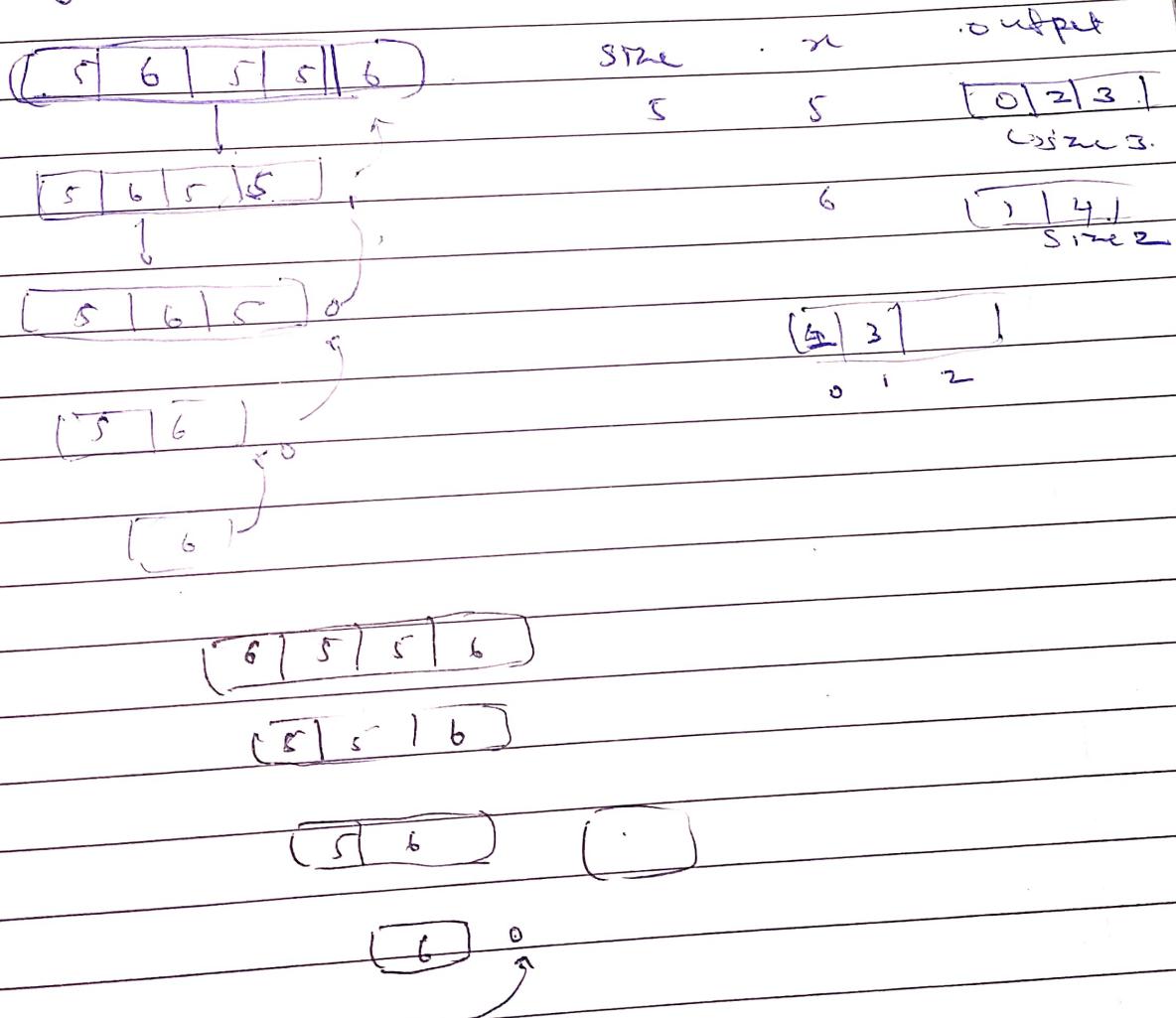
```
}
```

return ind+1;

dry run



(Q) # Return all index. of given num in array. also in sorted form



Q. finding length of string using recursion

```
#include < ->
```

```
5 int length (char s[])
```

```
{
```

```
if (s[0] == 'X')
```

```
return 0;
```

```
10 }
```

```
int small string length = length(s+1);
```

```
return 1 + small string length;
```

```
int main ()
```

```
{
```

```
char str [100];
```

```
cin >> str;
```

```
int l = length (str)
```

```
cout << l << endl;
```

```
}
```

dry run

7 (i) a b c d l o

6 (ii) b c d l o

5 (iii) c d l o

4 (iv) d l o

3 (v) l o

2 (vi) o

1 (vii) o

0 (viii) o

Remove Duplicates from String Using Recc.

#include <iostream>
using namespace std;

int length (char s[])

{

 if (s[0] == '\0')

 +

 return 0;

}

 int smallStringLength = length (s+1);

 return smallString;

else {

}

Void duplicate (char

{

 l = length (s[])

 if (l < 1)

{

 return 0;

}

 else if (s[0] != s[1])

 duplicate (s+1);

}

 else {

 int i = 1;

 for (i; s[i] != '\0'; i++)

 s[i-1] = s[i];

 }

$s[i-1] = s[i]$;
 duplicate(s);
 {
 5

int main()

{

int s[100];
 cin >> s;

duplicate(s);
 cout << s;

}

dry run

(k | a | q | q | b | c | c | d | d | s | l | o)

let l = 10.

(q | a | q | b | c | c | d | d | s | l | o)

(q | q | b | c | c | d | d | s | l | o) ✓

q | b | c | c | d | d | s | l | o

b | c | c | d | d | s | l | o

(k | a | q | b | c | c | d | d | s | l | o)

c | c | d | d | s | l | o

k | (a | a | q | b | c | c | d | d | s | l | o)

c | d | d | s | l | o

k | (c | a | q | b | c | c | d | d | s | l | o)

c | d | s | l | o

k | (c | c | d | d | s | l | o)

c | s | l | o

~~a | q | b | c~~

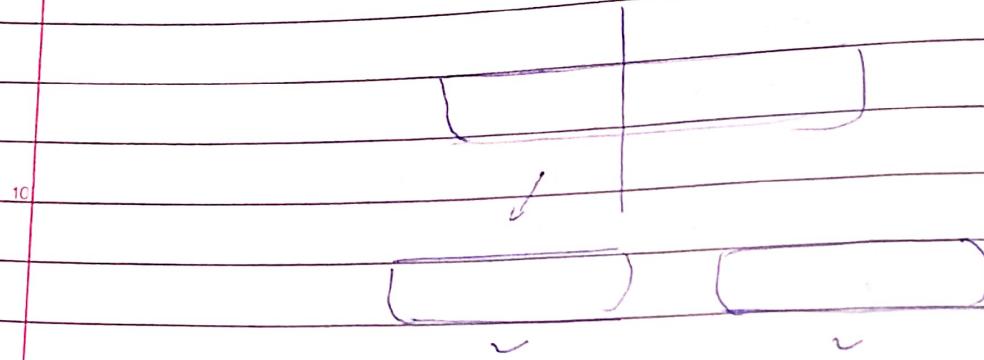
k | a | b | (c | c | d | d | s | l | o)

k | a | b | c | c | d | d | s | l | o

(k | a | b | c | d | s | l | o)

Merge Sort And Recursion

base case. $\rightarrow l \rightarrow 0 \rightarrow$ already sorted
return



or

Eadhne eadhne pai recursive

How it works?

Void mergeSort (int a[], int si, int ei)

if ($ei > si$)

{
 // return;

int mid = $\frac{si + ei}{2}$

for (i = si; i < mid; i++)

{
 if ($a[si] > a[si+1]$)

"Swap"

```

void smaller (int a[], int si, int mid)
{
    for (int i = si; si <= mid; si++)
    {
        if (a[si] < a[si + 1])
            swap (a[si], a[si + 1])
    }
}

```

void merge^{sort} (int low, int high)

```

{
    if (low < high)
    {
        int middle = (high + low) / 2;
        mergesort (low, middle);
        mergesort (middle + 1, high);
        merge (low, middle, high);
    }
}

```

void merge } (int low, int middle, int high)

```

{
    for (int i = low; i <= high; i++)
    {
        helper[i] = number[i];
    }
}

```

int i = low;

int j = middle + 1;

int k = low;

while ($i \leq \text{middle}$ & $i \leq \text{high}$)

if ($\text{helper}[i] \leq \text{helper}[j]$)

{

$\text{numbers}[k] = \text{helper}[i];$

$i++;$

}

else {

$\text{numbers}[k] = \text{helper}[j];$

$j++;$

}

$k++;$

}

while ($i \leq \text{middle}$)

f

$\text{numbers}[k] = \text{helper}[i];$

$i++;$

$j++;$

}

Quick Sort

$[5 | 9 | 8 | 3 | 12 | 7 | 1]$

$[3 | 9 | 8 | 5 | 12 | 7 | 1]$

$\begin{array}{|c|c|} \hline 3 & 1 & 12 \\ \hline \end{array} \quad \begin{array}{|c|c|} \hline 5 & 8 | 7 | 9 \\ \hline \end{array}$

Soot Soot

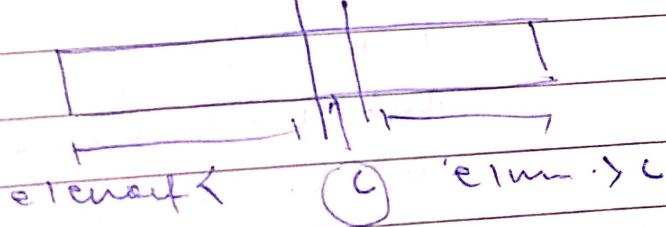
1st void qs(int a[], int si, int ei)

{

base case (i, <= 0)

return

c = partition (a, si, ei)



qs (a, si, e - 1)

qs (a, c + 1, ei);

}

Q) Understanding MergeSort using Recursion

Code

```

#include <bits/stdc++.h>
using __;

Void mergesort( int q[], int low, int middle, int high )
{
    int helper[high];
    for ( i = low ; i <= high ; i++ )
        helper[i] = q[i];
    int i = low;
    int j = middle + 1;
    int k = low;
    while ( i <= middle && j <= high )
        if ( helper[i] <= helper[j] )
            q[k] = helper[i];
            i++;
            k++;
        else
            q[k] = helper[j];
            j++;
            k++;
}

```

int main()

{

int n;

5

cin >> n;

int a[n];

for (int i=0; i<n; i++)

{

cin >> a[i];

10

mergesort(a, 0, n-1);

for (i=0; i<n; i++)

{

cout << a[i];

15

}

20

while (i <= middle)

a[k] = helper(i);

k++;

i++;

}

}

25

void merge sort (int a[], int low, int high)

{ if (low > high)

{ int middle = low + (high - low) / 2;

mergesort(a, low, middle);

mergesort(a, middle+1, high);

merge(a, low, middle, high);

30

}

dry run

4 0 6 1 5 2 3

4 0 6 1

4 0

4 0

1 6 1

1 6 1

(0, 0)
(0, 1)
(0, 2)
w.s (0, 6)

2, 2, 2

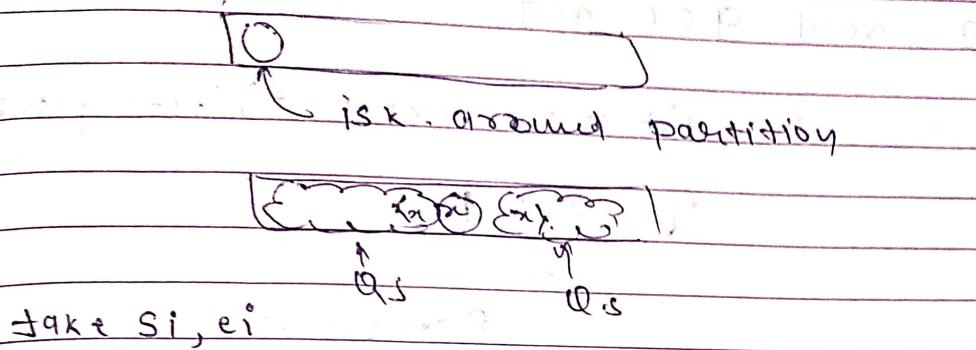
(3, 2)
(2, 3)
(0, 2)
(0, 6)

25

last step

30 last step

Algorithm for Q.S.



10 void qs (int a[], int si, int ei)

base case: $a[si] = a[ei]$

\Rightarrow sorted.

partition.(a, si, ei) \rightarrow a.ko c pair

count of smaller elements =

$s_i + \text{count_smaller_element}$.

partition(a, si, ei) \rightarrow a.ko c pair

$i = 1$
 $j = 8$

void qs(int a[], int si, int ei)

{ int n = size(a)/size(int);
 if (n < p)
 {
 Return 0;
 }

int c = Partition(a, si, ei)

qs(a, si, c-1);

qs(a, c+1, ei);

}

void Partition(int a[], int si, int ei)

for (i = 1; i <= ei; i++)
{

if (a[i] < a[c])

for (j = 0; j < m; j++)

{

m = count + 1;

}

~~Temporary Swap~~

swap(a[si], a[si+m])

i = si;
 j = ei.

if ($a[i] < a[j]$)

{

$i++;$

}

elseif ($a[i] > a[j]$)

{

$j--;$

}

else

{

swap ($a[i], a[j]$)

15

20

25

30

Strings in Rec.

- Substring O
- S.substring(2,3) «
- S.find()
- S.find("clif")

Q. How to find all subsequence of string

ex - "abc"

may be 2ⁿ subseq

| | |
|-----|----|
| .. | .. |
| ab | a |
| bc | b |
| c | |
| ab | |
| bc | |
| ac | |
| abc | |

int sub(string input, vector<string> output[])

{

 if (input.size() == 0)

 {

 output[0] = "";
 return;

}

(int smallOutput = sub(input, output),
string smallString = input.substring(0, i))

 for (int j = 0; j < smallOutput; j++)

 output[j + smallOutput] =

 * input[i] + output[j];

}

```
int main()
{
    string input;
    cin >> input;
    string * output = new string[1000];
    int count = sub(input, output);
    for(int i = 0; i < count; i++)
    {
        cout << output[i] << endl;
    }
}
```

Q. Keypad Problem

2 → "abc"

3 → "def"

4 → "ghi"

5 → "jkl"

6 → "mnoyz"

#include <iostream.h>

int keypad(int num, string output[], string digits[])

if (num == 0)

{

 output[0] = " ";

 return 1;

}

234

int lastdigit = num % 10;

int smallinput = num / 10;

string smalloutput[10000];

(1)

(24)

int smalloutputsiz = keypad(smallinput,

smalloutput,

digits)

24

string op = digits[lastdigit];

int k = 0;

for (int i = 0; i < op.size(); i++)

{

 for (int j = 0; j < smalloutputsiz; j++)

{

 output[k + i] = smalloutput[j] + op[i];

}

Keypad

3

int keypad (int num, string output[2])

{

string digits [3] = {

"0", "1", "2",
"3", "4", "5",
"6", "7", "8",
"9"

}

return keypad (num, output, digits)

int main ()

{

int num;

cin >> num;

string output [1000];

int count = keypad (num, output);

for (int i = 0; i < count + 1; i++)

{

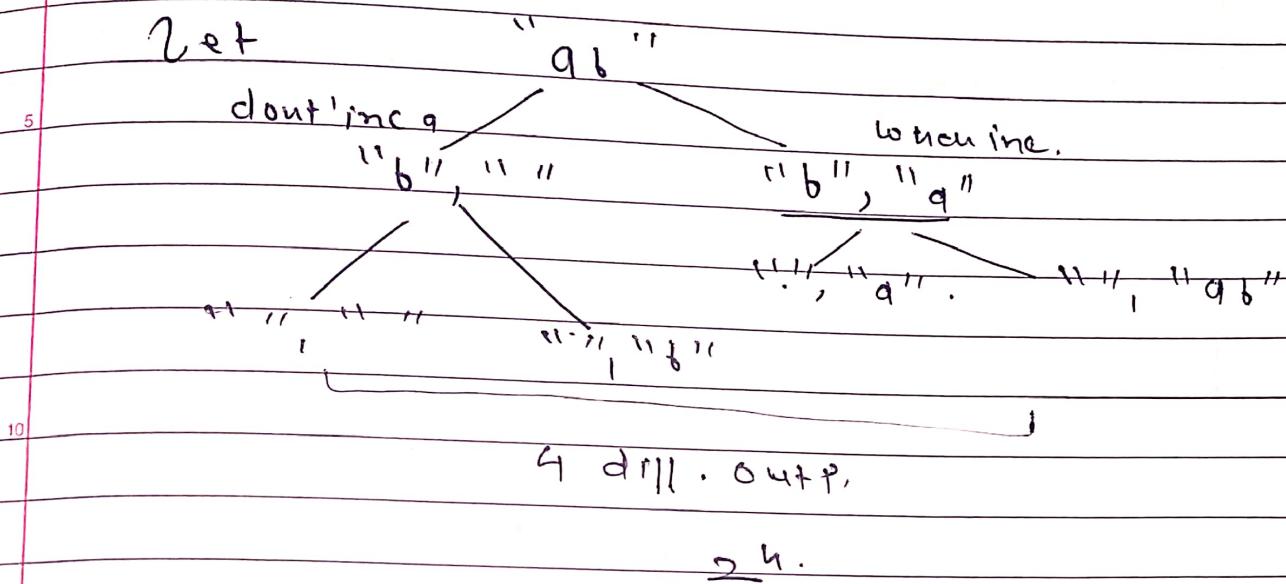
cout << output [i] << endl;

}

return 0;

}

How it Print ., string in Recc



15. void print_subs(string input, string output)

{ if (input.length() == 0)

cout << output << endl;

return;

}

print_subs(input.substr(1), output);
 print_subs(input.substr(1), output + input[0])

25. ?

int main()

{

string input;

cin >> input;

string output = " ";

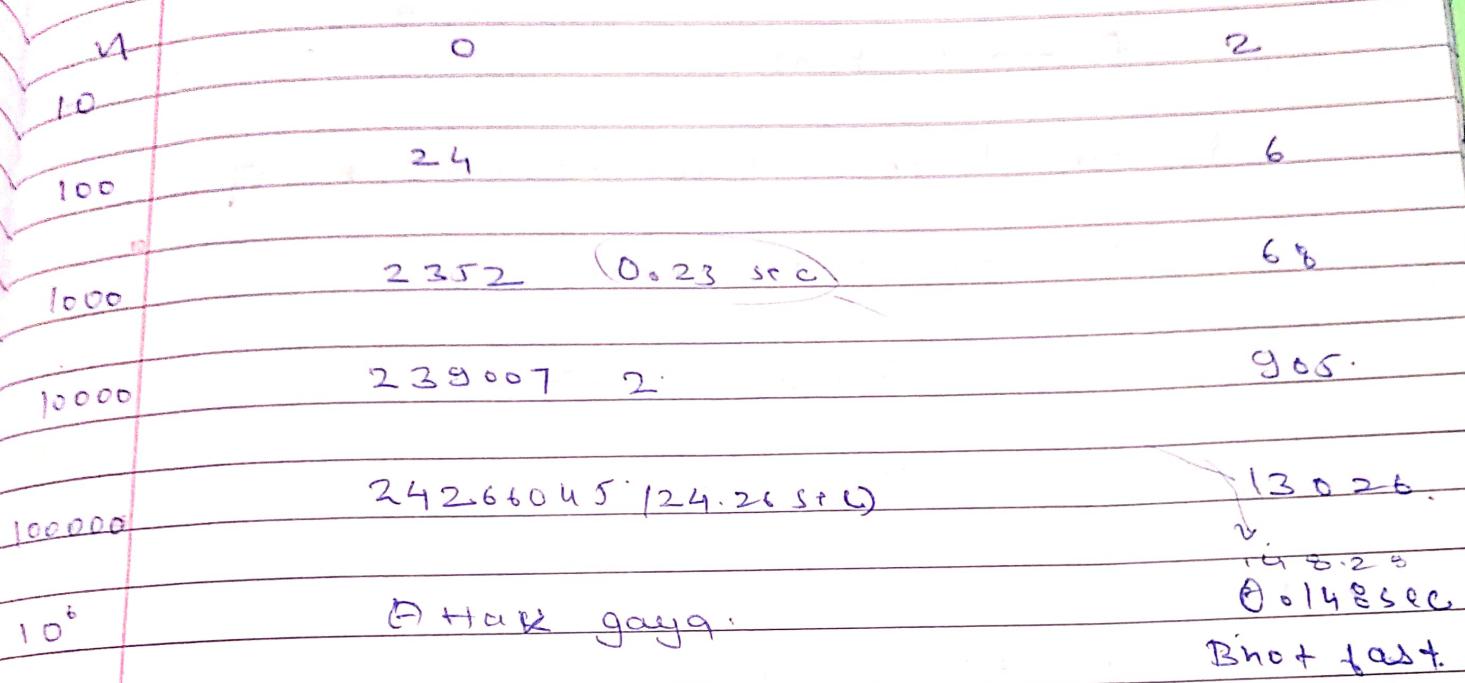
print_subs(input, output);

print_subs (input, output)

}

Time Complexity

Selection sort vs merge sort.



Problem to EXP. Analysis

- (1) Run again
- (2) Test case (we generally consider ~~worst case~~)
- (3) Code each step
- (4) Time consuming

∴ Points to remember :-

1. no of unit operation & not time
2. ³⁰ Highest power
3. we don't care
4. don't care abt efficient

Big O Notation

Time taken by algorithm to run

Number of operations

If time taken by P depends on n

$$T(n) = k_1 n^2 + k_2 n + k_3$$

Total steps

$$T(n) = \Theta(n^2)$$

Worst case

④ Largest element in array

Time complexity

Worst: $\Theta(n)$

Best: $\Theta(1)$

if ($\max - \delta(n)$)

Worst: $\Theta(n)$

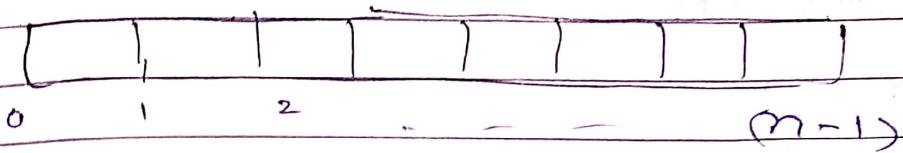
I

$\Theta(n)$

During each number performing B number of operations.

Time taken by algorithm

Bubble Sort



1st iteration

$\downarrow k \leftarrow (n-1)$

$+ \downarrow k \leftarrow (n-2)$

$+ \downarrow k \leftarrow (n-3)$

⋮

⋮

$\downarrow k \leftarrow (1+2+3+\dots+n-1)$

$\frac{k(n-1)n}{2}$

2

$$T(n) = \frac{kn(n-1)}{2}$$

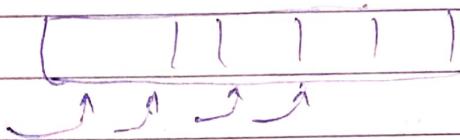
$$\frac{kn^2}{2} - \frac{kn}{2}$$

$$T(n) = \left(\frac{k}{2}\right) n^2$$

$$T(\text{Bubble sort}, n) = cn^2$$

{ Bubble sort is $O(n^2)$ }

Linear Search



② check whether x present.

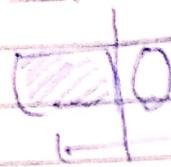
if present return i else go next.

$k=0 \rightarrow$ if element at 0^{th} position
(Best case)

Worst case to find all element

[Linear search $O(n)$]

Insertion Sort



0)

+ (n-1)

Compare them swap the present m,
selected actual



- 1

compare ① then if small the swap the
compare ② then swap. if small

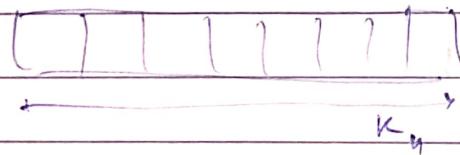
$$\therefore k + 2k + 3k = \dots + (n-1)k$$

$$k(1+2+3+\dots+(n-1))$$

$$\frac{k(n)(n-1)}{2} = \frac{kn^2 - kn}{2}$$

2.s in worst case $\mathcal{O}(n^2)$

Selection Sort ("go to each element & find min")



min = 0 Int_Man

Compare to & iterate to all
element then update min to
smallest and place to 1st pos

$$k_1 + k(n-1) + k(n-2) + \dots + 2$$

$$n(1+2+3+\dots+n)$$

$$\frac{k(n)(n+1)}{2} = \frac{kn^2}{2}$$

$\mathcal{O}(n^2)$ → Best &
Worst Case

Recursive Algo

```
int factorial( int n )
```

{

```
if ( n == 0 )
```

{

```
return 1;
```

}

```
return n * factorial( n - 1 );
```

}

$$T(n) = \underbrace{k_1 + k_2}_{\text{Small work}} + T(n-1)$$

+ f^n.

JK.

$$T(n) = T(n-1) + k$$

$$T(n-1) = T(n-2) + k$$

$$T(n-2) = T(n-3) + k$$

$$T(1) = T(0) + k.$$

$$T(0) = k.$$

n+1

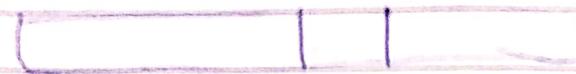
$$T(n) = k + k + k + \dots + k = (n+1)k$$

$$T(n) = k(n+1) = kn + k$$

$$T(n) = kn.$$

{ Fact is $O(n)$ }

Binary Search



go on middle

Boundary Update

$$T(n) = k + T(n/2)$$

go on middle

$$T(n/2) = k + T(n/4)$$

$$T(n/4) = \dots k + T(n/8)$$

⋮ T(1)

$$T(1) = k.$$

$$T(n) = k + k + \dots$$

$$n + \frac{n}{2} + \frac{n}{4} + \frac{n}{8} + \dots - - - - - I\left(\frac{n}{2^m}\right)$$

n

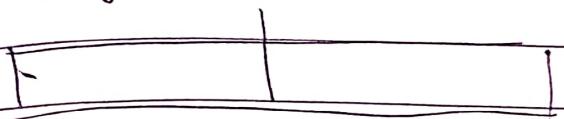
1 pair per level

$$2^m = n$$

$$\boxed{n = \log n}$$

$$\Theta(\log n)$$

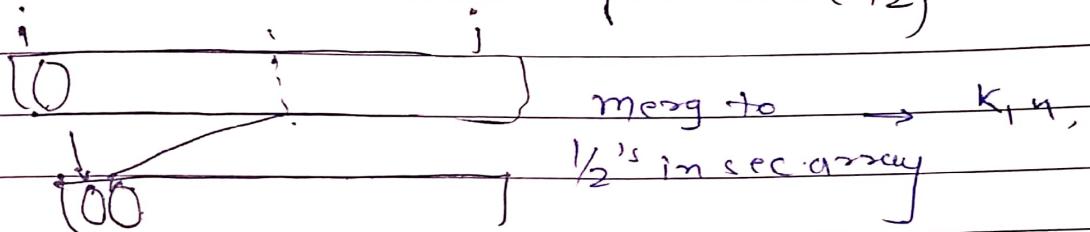
Merge Sort



Base case:

Call on $\frac{1}{2}n$ half $\rightarrow T(n/2)$

Call on $\frac{1}{2}n$ half $\rightarrow T(n/2)$



$$k_1n + k_2n = k_3n \quad \text{copy element from second to input} \rightarrow k_2n$$

$$\therefore T(n) = k + 2T(n/2) + k_1n + k_2n$$

by.

$$\begin{aligned} T(n) &= 2T(n/2) + n(k_1 + k_2) \\ &= 2T(n/2) + nk. \end{aligned}$$

$$\begin{aligned} T(n) &= 2T(n/2) + kn. \rightarrow k_n \\ 2 \star (T(n/2) &= \frac{1}{2}T(n/4) + k(n/2)) \rightarrow k_n \\ 4 \star (T(n/4) &= 8T(n/8) + k(n/4)) \rightarrow k_n. \end{aligned}$$

x.

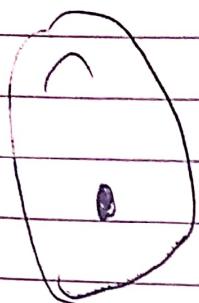
$T(1) = k_n$

$$n = \frac{n}{2} \dots \frac{n}{2^n} \dots \frac{n}{2^n}$$

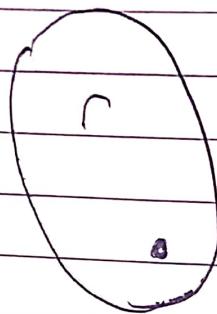
$$\frac{n}{2^n} = 1$$

$O(n \log n)$

$$n = \log n + k_n$$



object



oriented



Programming



Opps!

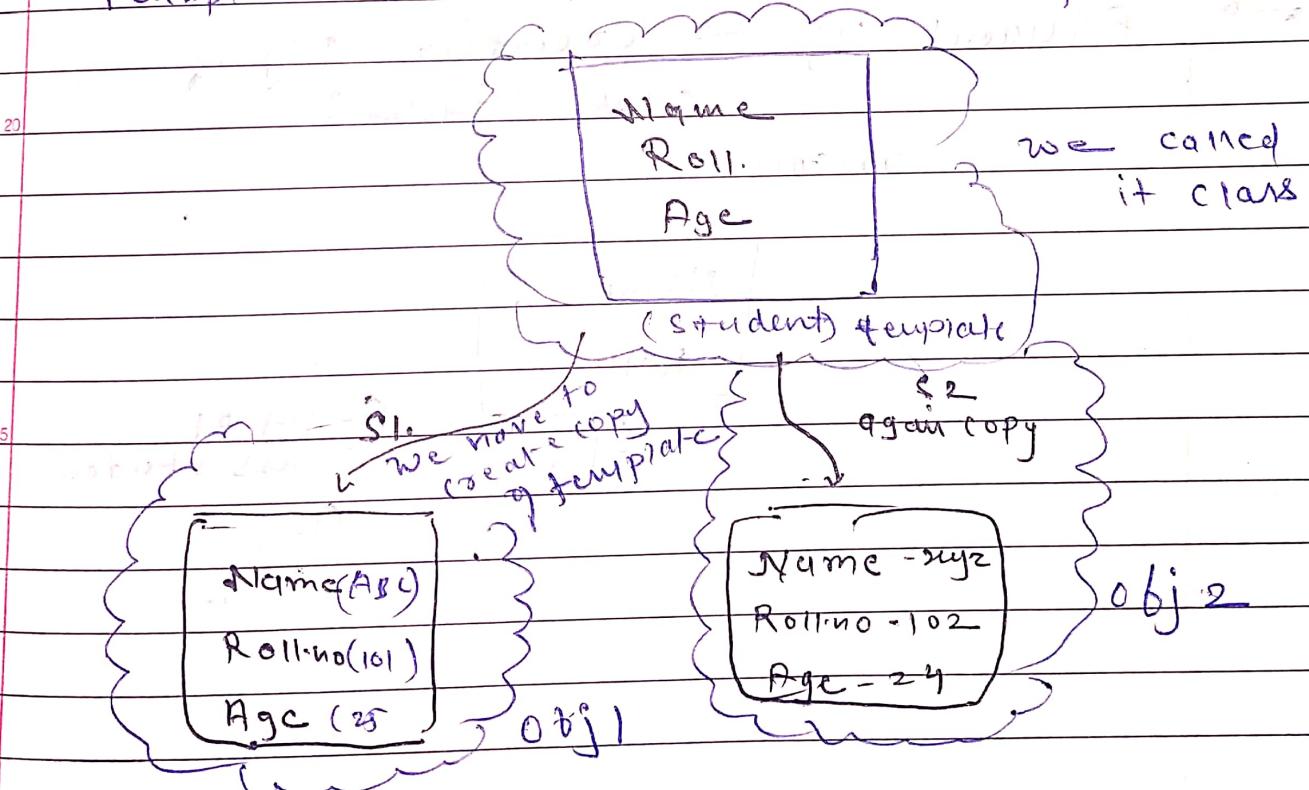
Let student is object it has some prop

- name
- Roll.no
- Age
- Address
- contact.no

If we want to perform operation like

Change Address → we have to make
set Roll.no fn

Let we have to take property of 20 student
Then we can use obj to and make
"Template" which indicate several properties



Class is a temp that defin Property & fn
of object.

Classes are user defined data type

How to make class

E₁₁

class Student → class name,

{

int rollNumber;

int age;

}

E₁₂

Class product

{

int id; and float

int weight;

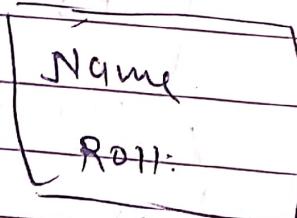
char name[100];

}



Student s1; → creating obj of
class Student

means



s1.

copy of
class studen

qs

s1.

Memory After 5+ Years

Statistically

Student A:

Student A's:

Age 27

Rn 30

S.

Age 27

Rn 30

S.

Cross Section

rat Remanence,

Mr. Roy,

Grade 6 (Bilingual)

Using Remanence & Roy

Female Student 100

1987 Mean (?)

Student A,

Student B,

Student C,

Age = 27

1987 Mean = 103

(Std 16.8, Age 27, Roy)

(Std 16.8, Mean 27, Roy)

S1: age 27,

* 26 age = 27,

* S2: 1987 Mean = 103

Dynamically

not a random

Student A has 100

free Student

Student type

no big - 100

Big - 100

Small - 100

Medium - 100

Large - 100

Access Modifier

- Public
- Private
- Protected

By default Access modifier → Private

We can access the private member outside the class.

within class we can access public data members

Getters & Setters

How to access private data member of class outside of class?

We can make member f in public and call f outside of class.

Public:

```
int getAge()
```

```
{
```

```
    return age;
```

```
}
```

```
int main()
```

```
{
```

```
cout << "age is " << s1.getAge();  
cout << "age is " <<
```

Making Getters & setters

Class Student {

Public:

int rollNumber;

Private:

int age;

Public:

Void display()

{

cout << age << " " << rollNumber
endl;

}

int getAge() → getter.

{

return age;

}

Void setAge(int a) → setter.

{

age = a;

}

} ;

int main()

Student s1;

Student *s2 = new Student;

s1.setAge(20);

s2 → setAge(24);

s1.display();

s2 → display();

Constructors

The fn which has name of the class;

ex → Class student;

student()

default const
constructor no Arguments

→ Same name

→ No return type

→ No input arguments

- * we never create a default constructor when class is made the default const. is automatically created.

struct.

student() {

}

When we made object constructor(default) is automatically created.

student s2;

student * s3 = new student;

* s3, student;

s3 → Student;