Relational Database Design

Functional Dependencies

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Informal Design Guidelines for Relational Databases

- · What is relational database design?
 - The grouping of attributes to form "good" relation schemas
- Design is concerned mainly with base relations
- What are the criteria for "good" base relations?
- We first discuss informal guidelines for good relational design.

Semantics of the Relation Attributes

- GUIDELINE 1: Informally, each tuple in a relation should represent one entity or relationship instance.
 - Attributes of different entities (EMPLOYEEs, PROJECTs etc.) should not be mixed in the same relation
 - Foreign keys should be used to refer to other entities
 - Entity and relationship attributes should be kept apart as much as possible.
- <u>Key point</u>: Design a schema that can be explained easily relation by relation. The semantics of attributes should be easy to interpret.

Redundant Information in Tuples

- · The Evils of Redundancy
 - Wastes storage
 - Causes problems with update anomalies
 - Insertion anomalies
 - Deletion anomalies
 - Modification anomalies

EXAMPLE: AN UPDATE ANOMALY

· Consider a table: student_activity

SID	Activity	Place	Fee	
100	Skiing	Mt. Dora	200.00	Note that: Activity> Place
100	Golf	Orlando Links	50.00	and
150	Swimming	Lake Beatrice	100.00	Activity> Fee
175	Squash	UCF Courts	100.00	
175	Swimming	Lake Beatrice	100.00	

- If SID 100 drops golf, we lose the cost of golf. (Delete anomaly)
- If the fee for swimming changes, it must be changed in several places. (Update anomaly)
- The cost of an activity may not be added until a student participates in it. (Insertion anomaly)

Solution of UPDATE ANOMALY

· Solution ??

- · Main refinement technique:
 - decomposition
 - Example:
 - replacing ABCD with, say, AB and BCD

EXAMPLE: AN UPDATE ANOMALY

SID	Activity	Place	Fee
100	Skiing	Mt. Dora	200.00
100	Golf	Orlando Links	50.00
150	Swimming	Lake Beatrice	100.00
175	Squash	UCF Courts	100.00
175	Swimming	Lake Beatrice	100.00

Decompose the relation student_activity:

ENROLLMENT		ACT		
SID	Activity	Activity	Place	Fee
100	Skiing	Skiing	Mt. Dora	200
100	Golf	Golf	Orlando Links	50
150	Swimming	Swimming	Lake Beatrice	100
175	Squash	Squash	UCF Courts	100
175	Swimming			
200	Swimming			
200	Golf			A. P.

EXAMPLE: AN UPDATE ANOMALY

ENROLLMENT		ACT		
SID	Activity	Activity	Place	Fee
100	Skiing	Skiing	Mt. Dora	200
100	Golf	Golf	Orlando Links	50
150	Swimming	Swimming	Lake Beatrice	100
175	Squash	Squash	UCF Courts	100
175	Swimming			
200	Swimming			
200	Golf			

- · If SID 100 drops skiing, we still know the cost of skiing.
- If the fee for golf changes, it must be changed in only one place.
- · We can add an activity without a student.

The Evils of Redundancy

- · Decomposition should be used judiciously:
 - Is there reason to decompose a relation?
 - What problems (if any) does the decomposition cause?
- Functional dependency constraints are utilized to identify schemas with such problems and to suggest refinements.

Reducing the Redundant Values in Tuples

· GUIDELINE 2:

- Design a schema that does not suffer from the insertion, deletion and update anomalies.
- If there are any anomalies present, then note them so that applications can be made to take them into account.

Reducing Null Values in Tuples

- Many attributes may be grouped together into a flat relation
 - If many of attributes do not apply to all tuples in the relation??

- · Reasons for nulls:
 - Attribute not applicable or invalid
 - Attribute value unknown (may exist)
 - Value known to exist, but unavailable

Reducing Null Values in Tuples

· Problems:

- Space wastage
- Understanding the meaning of the attributes & specifying join operations at the logical level
- How to take aggregate operations in account
- Having same representation for all NULLs
 compromises the different meanings they may have

· GUIDELINE 3:

- Relations should be designed such that their tuples will have as few NULL values as possible
- Attributes that are NULL frequently could be placed in separate relations (with the primary key)

Spurious Tuples

- Bad designs for a relational database may result in erroneous results for certain JOIN operations
- The "lossless join" property is used to guarantee meaningful results for join operations
- The relations should be designed to satisfy the lossless join condition.
- No spurious tuples should be generated by doing a natural-join of any relations.

- Consider relation
 EMP_PROJ(Eno, Pnumber, Hours, Ename, Pname, Plocation)
- Decomposition of EMP_PROJ into relations
 EMP_LOCS (Ename, Plocation)
 and
 EMP_PROJ1 (Eno, Pnumber, Hours, Pname, Plocation)

```
Eno
      Pno
             Hours Pname Ploc
                                  Ename
11 1
                           Ank
                    X
11 2
                    У
                           Ist
                                  a
12 1
                    X
                           Ank
12 3
             10
                           Esk
```

 Decomposition of EMP_PROJ into relations EMP_LOCS (Ename, Plocation)

EMP_PROJ1 (Eno, Pnumber, Hours, Pname, Plocation)

ENa	me Ploc	
a	Ank	
a	Ist	
b	Ank	
b	Esk	

_					
	Eno	Pno	Hours	Pname	Ploc
	11 1		3	X	Ank
	11 2		4	У	Ist
	12 1		1	X	Ank
	12 3		10	Z	Esk

EName Ploc a Ank a Ist b Ank b Esk

Eno	Pno	Hours	Pname	Ploc
11 1		3	X	Ank
11 2		4	У	Ist
12 1		1	X	Ank
12 3		10	z	Esk

Eno	Pno	Hours	Pname	Ploc	Ename
11 1		3	X	Ank	a
<u>11 1</u>		<u>3</u>	X	<u>Ank</u>	<u>b</u>
11 2		4	У	Ist	a
<u>12 1</u>		<u>1</u>	X	<u>Ank</u>	<u>a</u>
12 1		1	X	Ank	b
12 3		10	Z	Esk	b

- Consider relation
 EMP_PROJ(Eno, Pnumber, Hours, Ename, Pname, Plocation)
- Natural Join of relations results in spurious tuples EMP_LOCS (Ename, Plocation)

and

EMP_PROJ1 (Eno, Pnumber, Hours, Pname, Plocation)

Problem:

Join attribute Plocation is neither a primary key nor a foreign key in either EMP_LOCS or EMP_PROJ1

Spurious Tuples

· GUIDELINE 4:

- Design relation schemas so that they can be joined with equality conditions on attributes that are either primary keys or foreign keys
 - This guarantees that no spurious tuples are generated
- Avoid relations that contain matching attributes that are not (foreign key, primary key) combinations
 - Joining on such attributes may produce spurious tuples

Spurious Tuples

- There are two important properties of decompositions:
 - a) Non-additive or losslessness of the corresponding join
 - b) Preservation of the functional dependencies.

- · Functional dependencies (FDs)
 - used to specify formal measures of the "goodness" of relational designs
 - constraints that are derived from the meaning and interrelationships of the data attributes

- X -> Y holds if whenever two tuples have the same value for X, they must have the same value for Y
 - For any two tuples t1 and t2 in any relation instance r(R): If t1[X]=t2[X], then t1[Y]=t2[Y]
- X -> Y in R specifies a constraint on all relation instances r(R)
- FDs are derived from the real-world constraints on the attributes

- · Given a value for attribute x:
 - If there is only one corresponding value for attribute y, then x determines y.
 - y is said to be functionally dependent on x.
 - x is called a **determinant**.
 - y may or may not determine x.
 - Candidate keys are determinants.
 - Determinants are candidate keys for the things they determine.

Example Determinants

- EmployeeID determines EmployeeName
 written as EmployeeID → EmployeeName
- · Why does EmployeeName NOT determine EmployeeID?
- · ProductID → Product Name
- Everyone in the same dorm pays the same fee, Dorm → Fee
 Do you think Fee would determine Dorm?
- If a student may not repeat a course
 CourseNo. + StudentNumber → Grade

Concatenated Determinants

- · FacultyID + CourseNo. + Section → Room, Time
- · FacultyID + Time → Room, CourseNo., Section

Functional Dependencies: Example

COMPANY (SSN, PNO, HOURS, BONUS, ENAME, PHONE, PNAME, {PLOCATIONS})

- SSN → ENAME, PHONE
- PNO → PNAME, {PLOCATIONS}
- HOURS → BONUS
- {SSN, PNO} → HOURS (not BONUS)

FD constraint

- An FD is a property of the attributes in the schema R
- The constraint must hold on every relation instance r(R)
- If K is a key of R, then K functionally determines all attributes in R
 - (since we never have two distinct tuples with t1[K]=t2[K])

Full Functional Dependency

- Attribute y is fully functionally dependent on attribute x, if it is functionally dependent on x and not functionally dependent on any proper subset of x.
- A FD x -> y where removal of any attribute from x means the FD does not hold any more
- · Example:

R (SSN, PNO, HOURS, ENAME)

FD: {SSN, PNO} → HOURS (full)

FD: {SSN, PNO} -> ENAME (not a full FD)

(a partial dependency as SSN -> ENAME also holds)

Inference Rules for FDs

- · Given a set of FDs F, we can infer additional FDs that hold whenever the FDs in F hold
- · Armstrong's inference rules:
 - IR1. (Reflexive) If Y subset-of X, then X -> Y
 - IR2. (Augmentation) If X -> Y, then XZ -> YZ
 - (Notation: XZ stands for X U Z)
 - IR3. (Transitive) If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$
- IR1, IR2, IR3 form a sound and complete set of inference rules

Inference Rules for FDs

- · Some additional and useful inference rules:
 - IR4. (Decomposition)

```
If X \rightarrow YZ, then X \rightarrow Y and X \rightarrow Z
```

- IR5. (Union) If X -> Y and X -> Z, then X -> YZ
- IR6. (Psuedotransitivity)

```
If X -> Y and WY -> Z, then WX -> Z
```

 The last three inference rules, as well as any other inference rules, can be deduced from IR1, IR2, and IR3 (completeness property)

Inference Rules: Example

· Given F = {A->B, C->X, BX->Z}, derive AC->Z

A->B: AX->BX (Augmentation)

AX->BX and BX->Z: AX->Z (transitivity)

C->X: AC->AX (Augmentation)

AC->AX and AX->Z: AC->Z (transitivity)

• Given $F = \{A \rightarrow B, C \rightarrow D\}$, with C is subset of B, show that $A \rightarrow D$

B->C (C is subset of B)

A->B and B->C so A->C (Transitivity)

A->C, C->D so A->D (Transitivity)

Inference Rules for FDs

 Closure of a set F of FDs is the set F⁺ of all FDs that can be inferred from F

 Closure of a set of attributes X with respect to F is the set X⁺ of all attributes that are functionally determined by X

 X⁺ can be calculated by repeatedly applying IR1, IR2, IR3 using the FDs in F

Problem: Finding FDs

· Approach 1: During Database Design

- Designer derives them from real-world knowledge of users
- Problem: knowledge might not be available

· Approach 2: From a Database Instance

- Analyze given database instance and find all FD's satisfied by that instance
- Useful if designers don't get enough information from users
- Problem: FDs might be artificial for the given instance

Problem: Finding FDs

- DB designers first specify the set of FDs, F that can easily be determined from the semantics of the attributes of R.
- Then IR1, IR2, IR3 are used to infer additional FDs that will also hold in R.
- · A systematic way:
 - Determine each set of attributes X that appears as a L.H.S. of some FD in F and then determine the set of all attributes that are dependent on X
 - For each set of attribute X, determine X⁺ of attributes that are functionally determined by X based on F (X⁺: closure of X under F)

Closure of a set of Attributes

· Example:

```
F = { ENO -> ENAME,
PNUMBER -> {PNAME, PLOCATION},
{ENO, PNUMBER} -> HOURS}
```

Closure sets wrt F
 {ENO}+ = {ENO, ENAME}
 {PNUMBER}+ = {PNUMBER, PNAME, PLOCATION}
 {ENO, PNUMBER}+ = {ENO, PNUMBER, ENAME, PNAME, PLOCATION, HOURS}

Equivalence of Sets of FDs

- · Two sets of FDs F and G are equivalent if:
 - Every FD in F can be inferred from G, and
 - Every FD in G can be inferred from F
 - Hence, F and G are equivalent if F+ =G+
- · Definition (Covers):
 - F covers G if every FD in G can be inferred from F
 - (i.e., if G^+ subset-of F^+)
- · F and G are equivalent if F covers G and G covers F
- · Algorithm for checking equivalence of sets of FDs

Minimal Sets of FDs

- · Minimal set of dependencies
- Set of dependencies in a standard or canonical form with no redundencies

Minimal Sets of FDs

- A set of FDs F is minimal if it satisfies the following conditions:
 - Every dependency in F has a single attribute for its RHS. (every dependency is in canonical form)
 - We cannot replace any dependency X -> A in
 F with a dependency Y -> A, where Y proper subset-of X and still have a set of dependencies
 that is equivalent to F. (F is left reduced)
 - We cannot remove any dependency from F and have a set of dependencies that is equivalent to F. (F is non redundant)

Minimal Sets of FDs

- · Every set of FDs has an equivalent minimal set (called Minimal Cover)
- · There can be several equivalent minimal sets
- There is no simple algorithm for computing a minimal set of FDs G that is equivalent to a set F of FDs
- To synthesize a set of relations, we assume that we start with a set of dependencies that is a minimal set

Computing Minimal Sets of FDs

Given set of FDs be $E: \{B \rightarrow A, D \rightarrow A, AB \rightarrow D\}$. Find the minimum cover of E.

- All above dependencies are in canonical form; (step 1 completed)
- In step 2, determine, if $AB \rightarrow D$ has any redundant attribute on the left-hand side; that is, can it be replaced by $B \rightarrow D$ or $A \rightarrow D$?
- Since B -> A, by augmenting with B on both sides (IR2), we have $BB \rightarrow AB$, or $B \rightarrow AB$ (i). However, $AB \rightarrow D$ as given (ii).
- By the transitive rule (IR3), we get from (i) and (ii), $B \rightarrow D$. Hence $AB \rightarrow D$ may be replaced by $B \rightarrow D$.
- A set equivalent to original E, say E': $\{B \rightarrow A, D \rightarrow A, B \rightarrow D\}$. No further reduction is possible in step 2 since all FDs have a single attribute on the left-hand side.
- In step 3, we look for a redundant FD in E'. By using the transitive rule on $B \to D$ and $D \to A$, we derive $B \to A$. Hence $B \to A$ is redundant in E' and can be eliminated.
- Hence the minimum cover of E is $\{B \rightarrow D, D \rightarrow A\}$.

Exercise

- Consider a relation R (A, B, C, D, E) with FDs:
 AB -> C, B -> D, and C -> E.
 What is/are the key(s) for R?
- Consider a relation R(A,B,C,D,E) with functional dependencies: $A \rightarrow B$, $BC \rightarrow E$, and $D \rightarrow A$ Find the key for R.
- Consider a relational schema R(A, B, C, D, E) with FDs $AB \rightarrow C$; $D \rightarrow A$, $C \rightarrow D$, $C \rightarrow E$, $E \rightarrow B$ Find all the (minimal) keys for R.