

## Converting an NFA to a DFA

Given:

A non-deterministic finite state machine (NFA)

Goal:

Convert to an equivalent deterministic finite state machine (DFA)

Why?

Faster recognizer!

Approach:

Consider simulating a NFA.

Work with sets of states.

**IDEA:** Each state in the DFA will correspond to a set of NFA states.

Worst-case:

There can be an exponential number  $O(2^N)$  of sets of states.

The DFA can have exponentially many more states than the NFA  
... but this is rare.

## NFA to DFA

Input: A NFA

$S = \text{States} = \{s_0, s_1, \dots, s_N\} = S_{\text{NFA}}$

$\delta = \text{Move function} = \text{Move}_{\text{NFA}}$

$\text{Move}'(S, a) \rightarrow \text{Set of states}$

Output: A DFA

$S = \text{States} = \{?, \dots, ?\} = S_{\text{DFA}}$

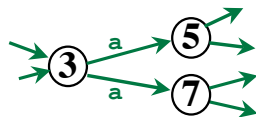
$\delta = \text{Move function} = \text{Move}_{\text{DFA}}$

$\text{Move}(s, a) \rightarrow \text{Single state from } S_{\text{DFA}}$

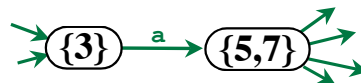
Main Idea:

Each state in  $S_{\text{DFA}}$  will be a set of states from the NFA

$S_{\text{DFA}} = \{ \{ \dots \}, \{ \dots \}, \dots, \{ \dots \} \}$

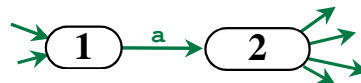


NFA



DFA

*(The names of the states is arbitrary and can be changed later, if desired.)*



## Algorithm: Convert NFA to DFA

### We'll use...

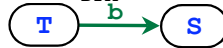
$\text{Move}_{\text{NFA}}(\mathbf{S}, \mathbf{a})$  the transition function from NFA  
 $\epsilon\text{-Closure}(\mathbf{s})$  where  $\mathbf{s}$  is a single state from NFA  
 $\epsilon\text{-Closure}(\mathbf{S})$  where  $\mathbf{S}$  is a set of states from NFA

### We'll construct...

$\mathbf{S}_{\text{DFA}}$  the set of states in the DFA  
 Initially, we'll set  $\mathbf{S}_{\text{DFA}}$  to  $\{\}$   
 Add  $\mathbf{X}$  to  $\mathbf{S}_{\text{DFA}}$  where  $\mathbf{X}$  is some *set of* NFA states  
*Example:* "Add  $\{\mathbf{3}, \mathbf{5}, \mathbf{7}\}$  to  $\mathbf{S}_{\text{DFA}}$ "  
 We'll "mark" some of the states in the DFA.  
 Marked = "We've done this one" (✓)  
 Unmarked = "Still need to do this one"

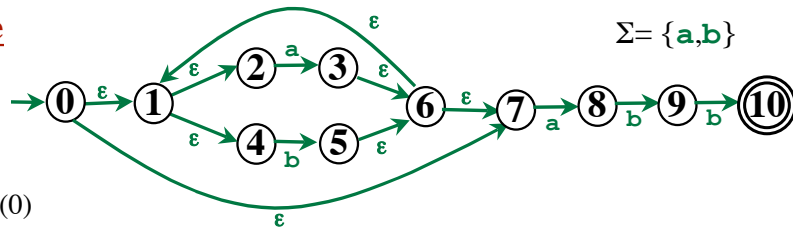
$\text{Move}_{\text{DFA}}(\mathbf{T}, \mathbf{b})$  The transition function from DFA  
 To add an edge to the growing DFA...

Set  $\text{Move}_{\text{DFA}}(\mathbf{T}, \mathbf{b})$  to  $\mathbf{S}$

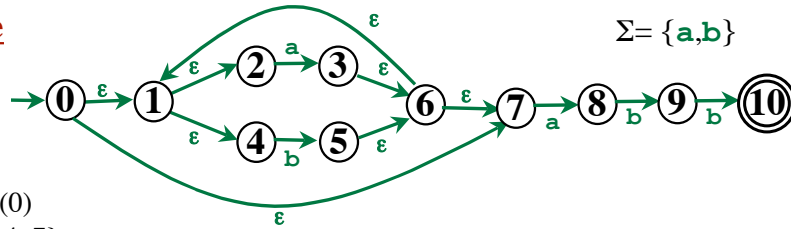


...where  $\mathbf{S}$  and  $\mathbf{T}$  are sets of NFA states

## Example



**Example**

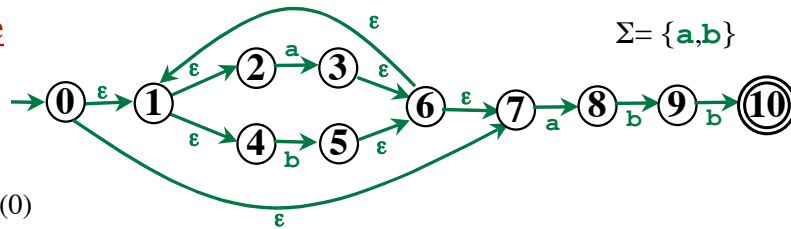


Start state:

$\epsilon$ -Closure (0)

$= \{0, 1, 2, 4, 7\}$

**Example**

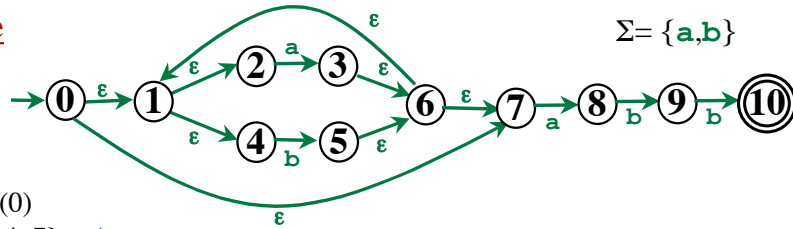


Start state:

$\epsilon$ -Closure (0)

$= \{0, 1, 2, 4, 7\} = A$

**Example**



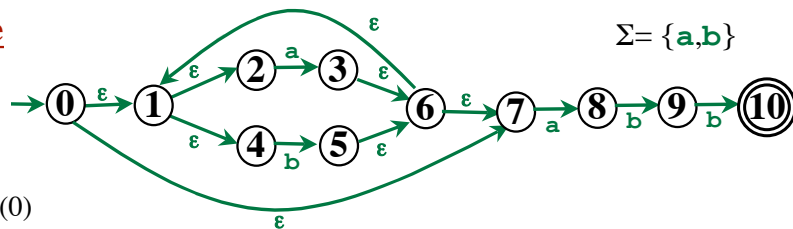
Start state:

$\epsilon$ -Closure (0)  
 $= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$   
 $=$

$\text{Move}_{\text{DFA}}(A, b)$   
 $=$

**Example**



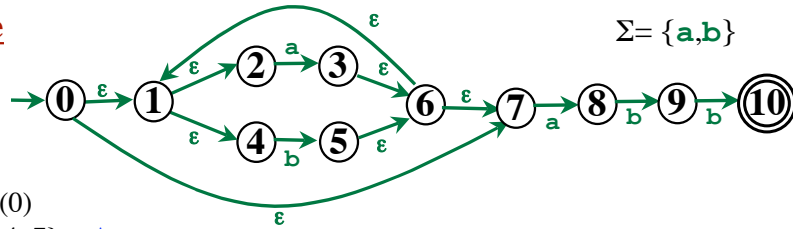
Start state:

$\epsilon$ -Closure (0)  
 $= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, a))$   
 $=$

$\text{Move}_{\text{DFA}}(A, b)$   
 $=$

### Example



Start state:

$\epsilon$ -Closure (0)

$= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$

$= \epsilon$ -Closure ( $\text{Move}_{\text{NFA}}(A, a)$ )

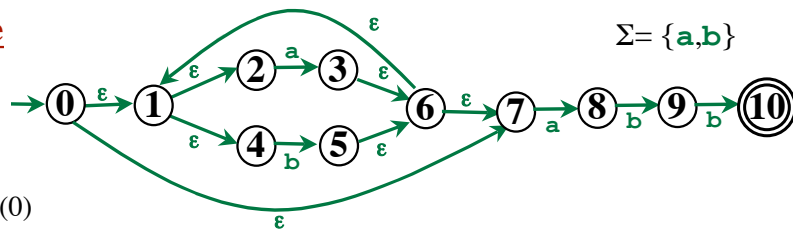
$= \epsilon$ -Closure ( $\{3, 8\}$ )

$=$

$\text{Move}_{\text{DFA}}(A, b)$

$=$

### Example



Start state:

$\epsilon$ -Closure (0)

$= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$

$= \epsilon$ -Closure ( $\text{Move}_{\text{NFA}}(A, a)$ )

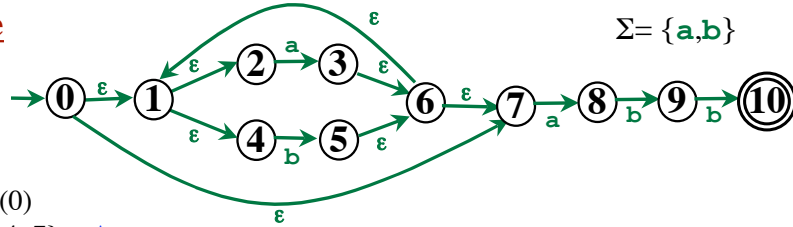
$= \epsilon$ -Closure ( $\{3, 8\}$ )

$= \{1, 2, 3, 4, 6, 7, 8\}$

$\text{Move}_{\text{DFA}}(A, b)$

$=$

**Example**



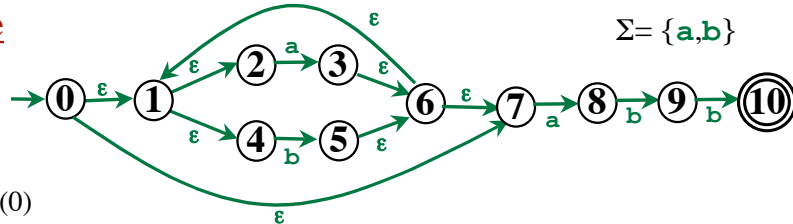
Start state:

$\epsilon$ -Closure (0)  
 $= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(A, b)$   
 $=$

**Example**



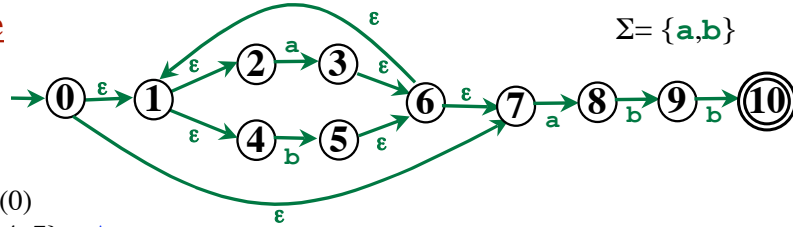
Start state:

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 $= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(A, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, b))$   
 $=$

**Example**



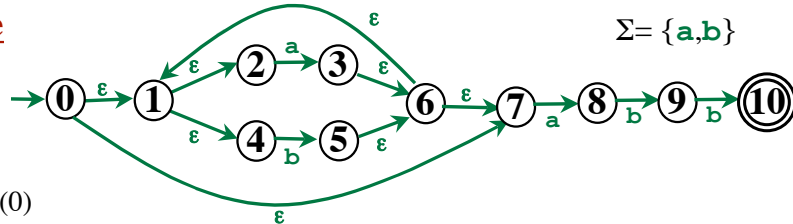
Start state:

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 $= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, a))$   
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$\text{Move}_{\text{DFA}}(A, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, b))$   
 $= \epsilon\text{-Closure}(\{5\})$   
 $=$

**Example**



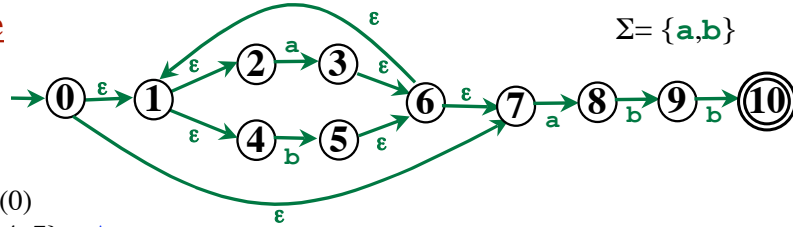
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$\text{Move}_{\text{DFA}}(A, a)$   
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 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(A, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, b))$   
 $= \epsilon\text{-Closure}(\{5\})$   
 $= \{1, 2, 4, 5, 6, 7\} = C$

**Example**

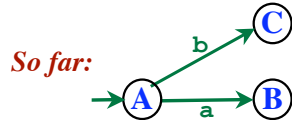


Start state:

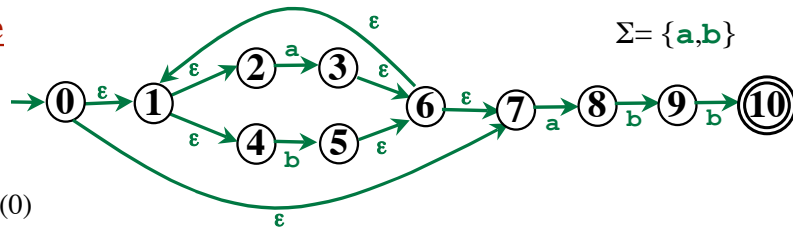
$\epsilon$ -Closure (0)  
 $= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(A, b)$   
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 $= \epsilon\text{-Closure}(\{5\})$   
 $= \{1, 2, 4, 5, 6, 7\} = C$



**Example**

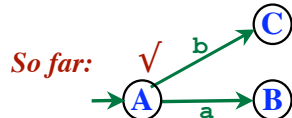


Start state:

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 $= \{0, 1, 2, 4, 7\} = A$

$\text{Move}_{\text{DFA}}(A, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

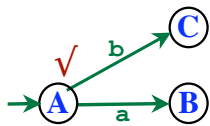
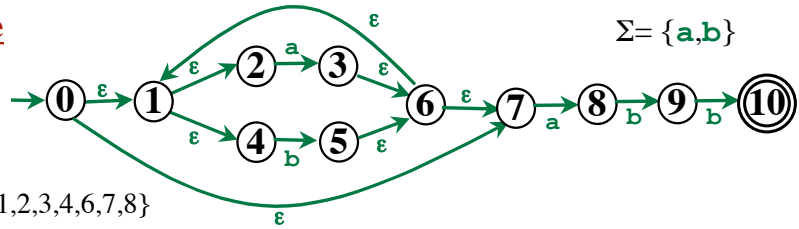
$\text{Move}_{\text{DFA}}(A, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, b))$   
 $= \epsilon\text{-Closure}(\{5\})$   
 $= \{1, 2, 4, 5, 6, 7\} = C$



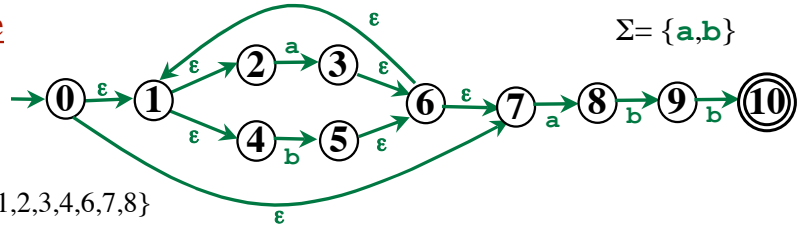
A is now done; mark it!  
 B and C are unmarked.  
 Let's do B next...



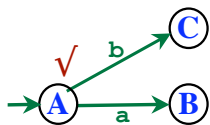
**Example**



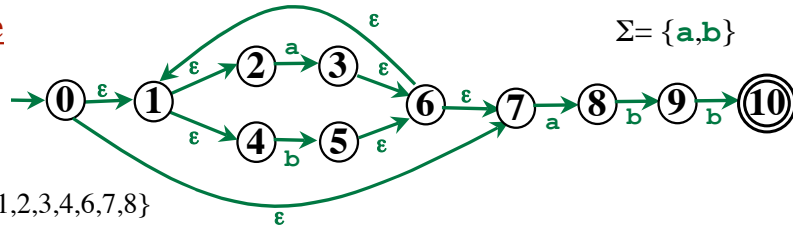
**Example**



$\text{Move}_{\text{DFA}}(B, a)$   
=

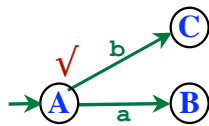


**Example**

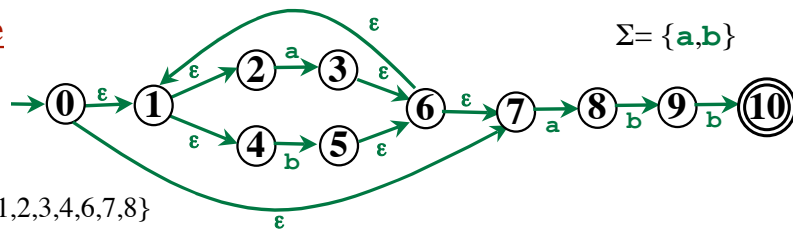


Process  $B = \{1, 2, 3, 4, 6, 7, 8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
 $=$

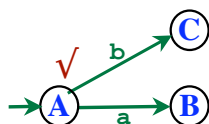


**Example**

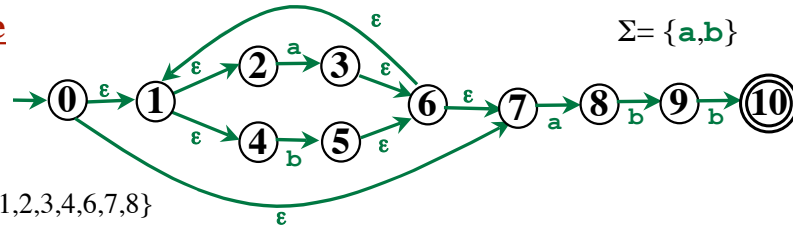


Process  $B = \{1, 2, 3, 4, 6, 7, 8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $=$

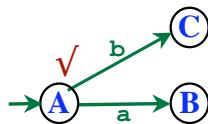


### Example

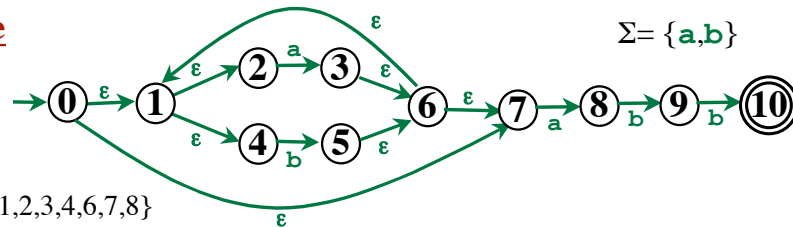


Process  $B = \{1, 2, 3, 4, 6, 7, 8\}$

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 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
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 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

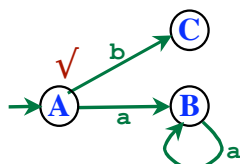


### Example

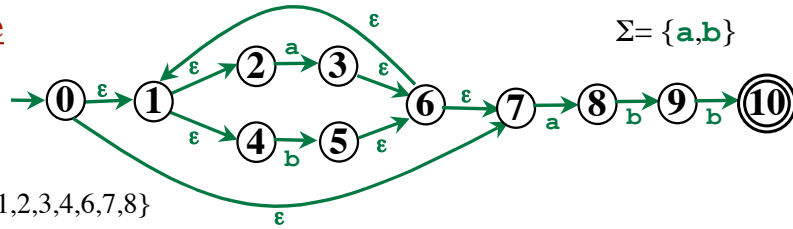


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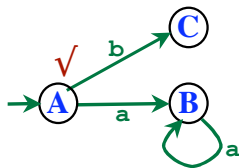
**Example**



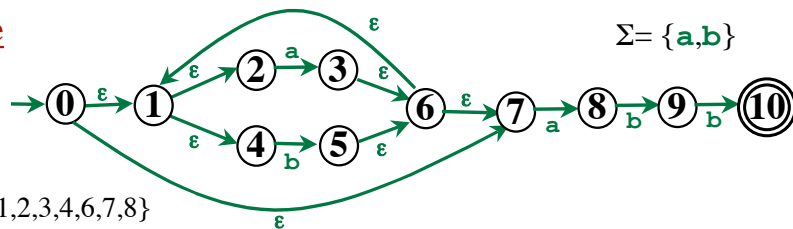
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 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(B, b)$   
 $=$



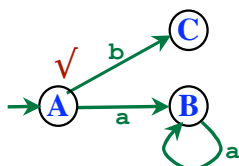
**Example**



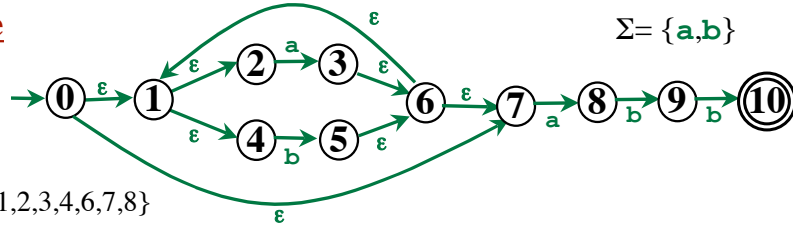
Process  $B = \{1, 2, 3, 4, 6, 7, 8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
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 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(B, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, b))$   
 $=$



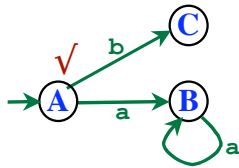
**Example**



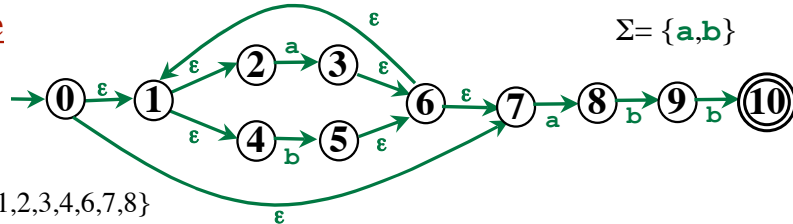
Process  $B = \{1,2,3,4,6,7,8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(B, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, b))$   
 $= \epsilon\text{-Closure}(\{5, 9\})$   
 $=$



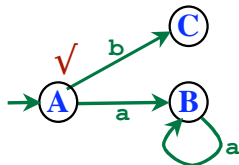
**Example**

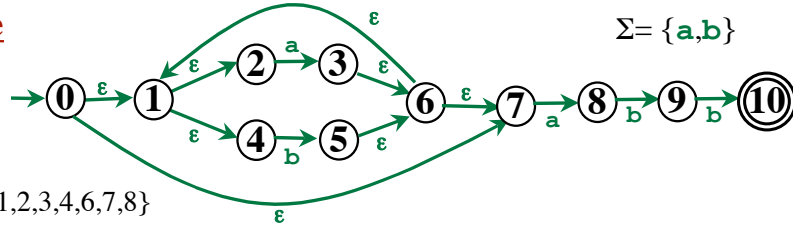


Process  $B = \{1,2,3,4,6,7,8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(B, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, b))$   
 $= \epsilon\text{-Closure}(\{5, 9\})$   
 $= \{1, 2, 4, 5, 6, 7, 9\} = D$

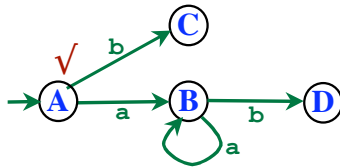
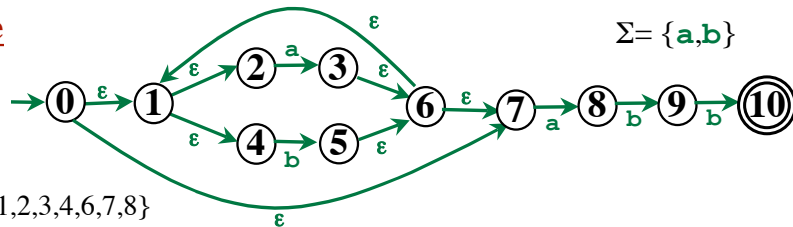


**Example**

Process  $B = \{1, 2, 3, 4, 6, 7, 8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

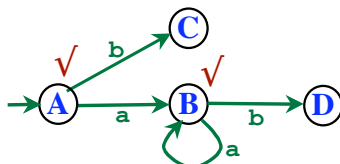
$\text{Move}_{\text{DFA}}(B, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, b))$   
 $= \epsilon\text{-Closure}(\{5, 9\})$   
 $= \{1, 2, 4, 5, 6, 7, 9\} = D$

**Example**

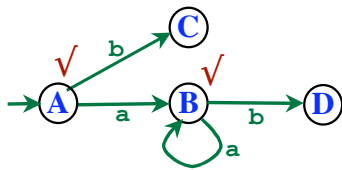
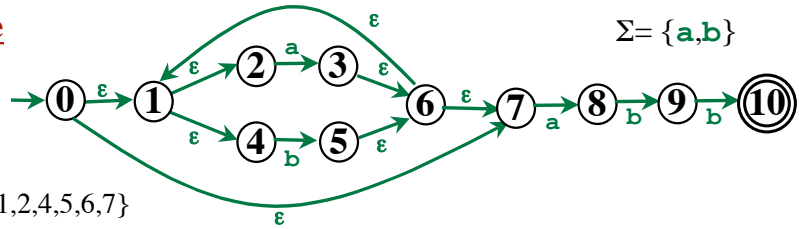
Process  $B = \{1, 2, 3, 4, 6, 7, 8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, a))$   
 $= \epsilon\text{-Closure}(\{3, 8\})$   
 $= \{1, 2, 3, 4, 6, 7, 8\} = B$

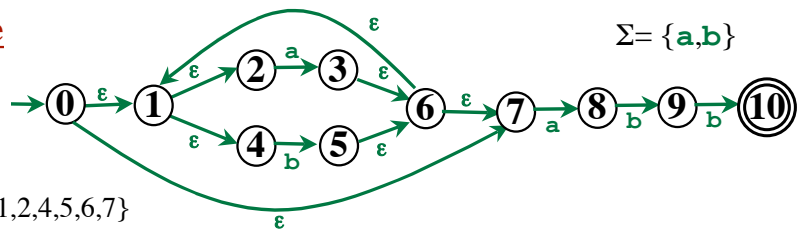
$\text{Move}_{\text{DFA}}(B, b)$   
 $= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(B, b))$   
 $= \epsilon\text{-Closure}(\{5, 9\})$   
 $= \{1, 2, 4, 5, 6, 7, 9\} = D$



**Example**

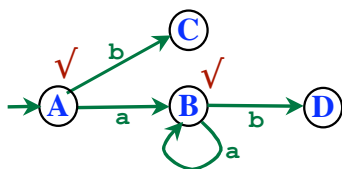


**Example**

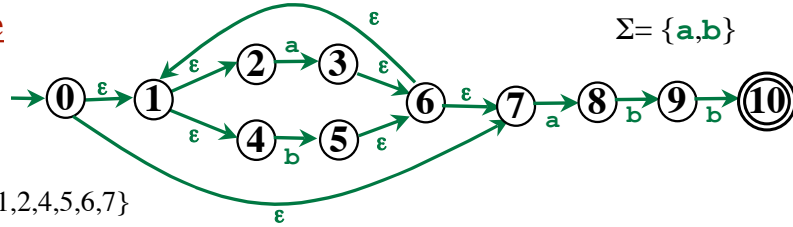


$\text{Move}_{\text{DFA}}(C, a) =$

$\text{Move}_{\text{DFA}}(C, b) =$



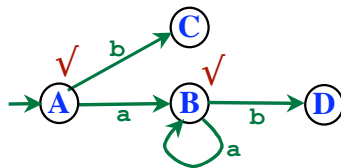
**Example**



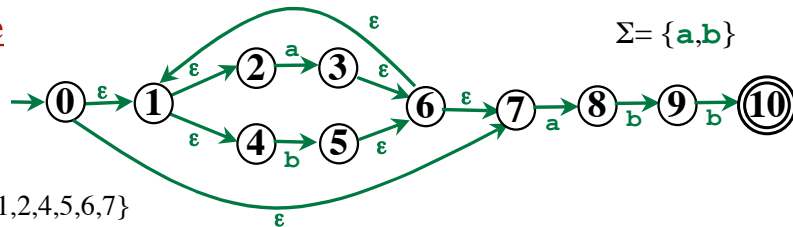
Process  $C = \{1, 2, 4, 5, 6, 7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) =$



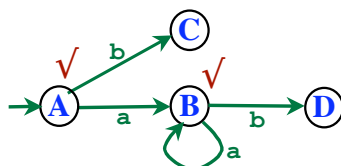
**Example**



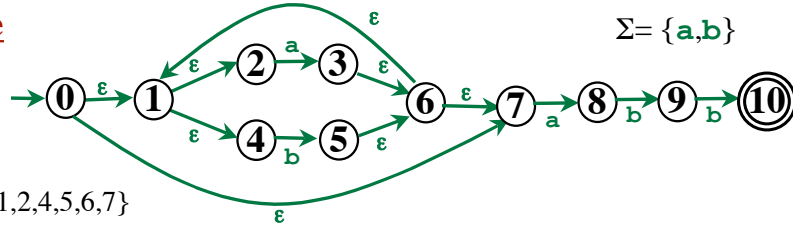
Process  $C = \{1, 2, 4, 5, 6, 7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$



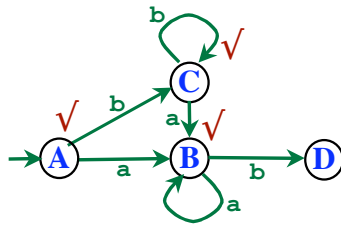
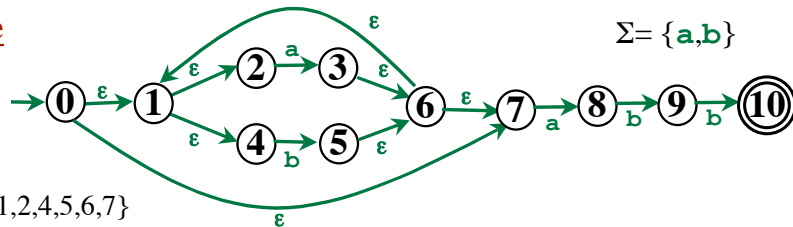


**Example**

Process  $C = \{1, 2, 4, 5, 6, 7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$

**Example**

Process  $C = \{1, 2, 4, 5, 6, 7\}$

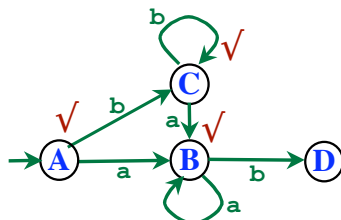
$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$

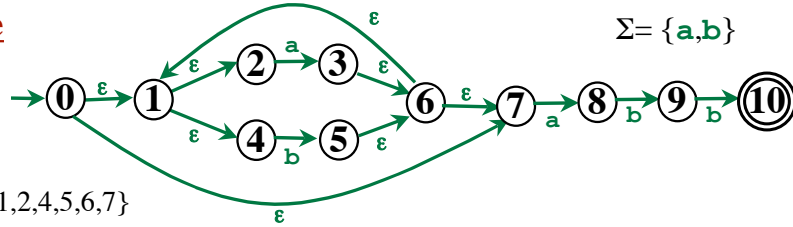
Process  $D = \{1, 2, 4, 5, 6, 7, 9\}$

$\text{Move}_{\text{DFA}}(D, a) =$

$\text{Move}_{\text{DFA}}(D, b) =$



**Example**



Process  $C = \{1, 2, 4, 5, 6, 7\}$

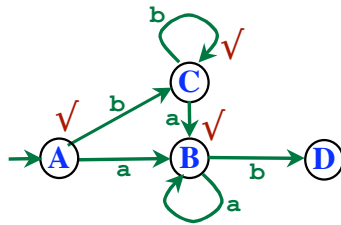
$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$

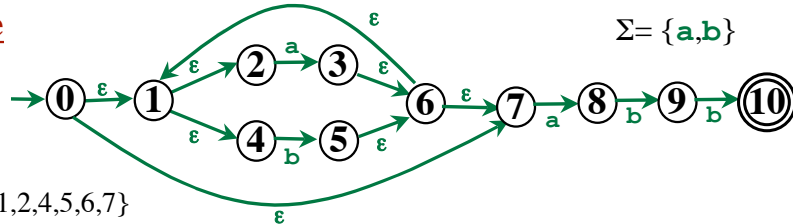
Process  $D = \{1, 2, 4, 5, 6, 7, 9\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(D, b) =$



**Example**



Process  $C = \{1, 2, 4, 5, 6, 7\}$

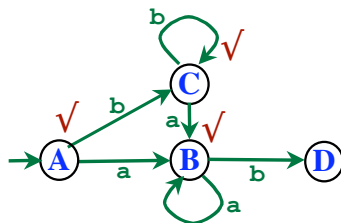
$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$

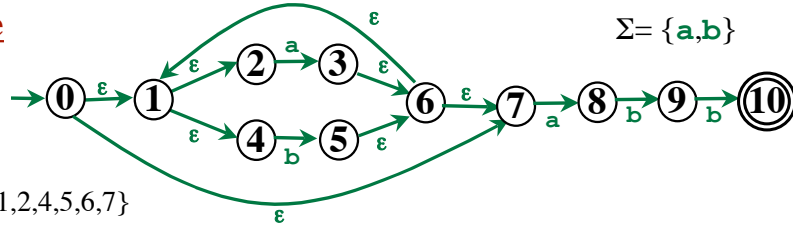
Process  $D = \{1, 2, 4, 5, 6, 7, 9\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(D, b) = \{1, 2, 4, 5, 6, 7, 10\} = E$



**Example**



Process  $C = \{1,2,4,5,6,7\}$

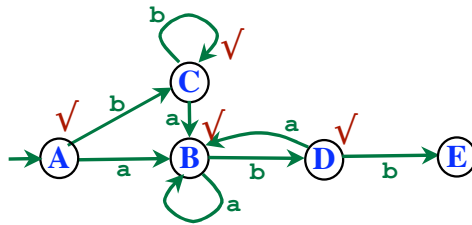
$\text{Move}_{\text{DFA}}(C, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1,2,4,5,6,7\} = C$

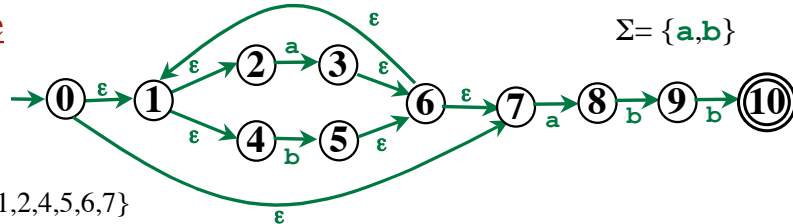
Process  $D = \{1,2,4,5,6,7,9\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(D, b) = \{1,2,4,5,6,7,10\} = E$



**Example**



Process  $C = \{1,2,4,5,6,7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1,2,4,5,6,7\} = C$

Process  $D = \{1,2,4,5,6,7,9\}$

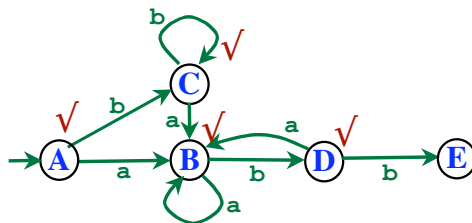
Process  $E = \{1,2,4,5,6,7,10\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1,2,3,4,6,7,8\} = B$

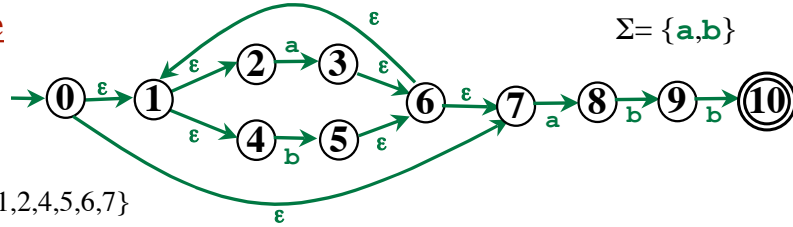
$\text{Move}_{\text{DFA}}(E, a) =$

$\text{Move}_{\text{DFA}}(D, b) = \{1,2,4,5,6,7,10\} = E$

$\text{Move}_{\text{DFA}}(E, b) =$



**Example**



Process  $C = \{1,2,4,5,6,7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1,2,4,5,6,7\} = C$

Process  $D = \{1,2,4,5,6,7,9\}$

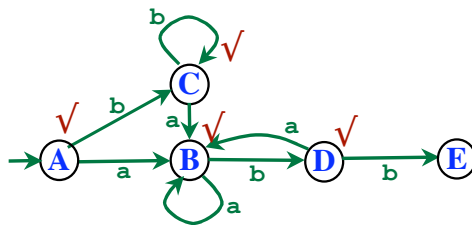
Process  $E = \{1,2,4,5,6,7,10\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1,2,3,4,6,7,8\} = B$

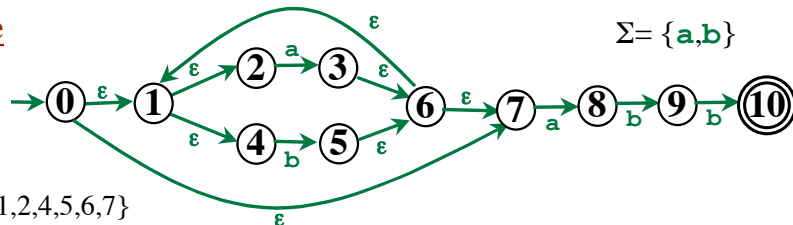
$\text{Move}_{\text{DFA}}(E, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(D, b) = \{1,2,4,5,6,7,10\} = E$

$\text{Move}_{\text{DFA}}(E, b) =$



**Example**



Process  $C = \{1,2,4,5,6,7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1,2,4,5,6,7\} = C$

Process  $D = \{1,2,4,5,6,7,9\}$

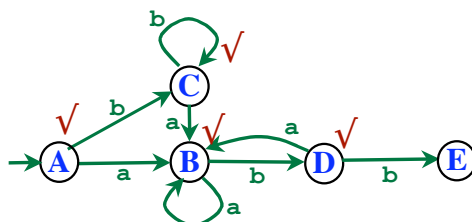
Process  $E = \{1,2,4,5,6,7,10\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1,2,3,4,6,7,8\} = B$

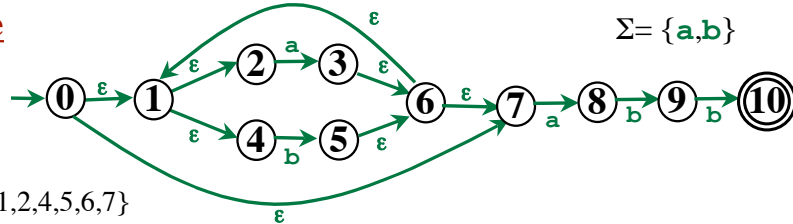
$\text{Move}_{\text{DFA}}(E, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(D, b) = \{1,2,4,5,6,7,10\} = E$

$\text{Move}_{\text{DFA}}(E, b) = \{1,2,4,5,6,7\} = C$



**Example**



Process  $C = \{1, 2, 4, 5, 6, 7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$

Process  $D = \{1, 2, 4, 5, 6, 7, 9\}$

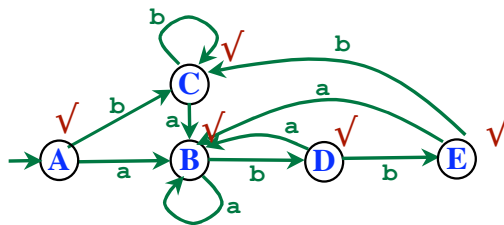
$\text{Move}_{\text{DFA}}(D, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(D, b) = \{1, 2, 4, 5, 6, 7, 10\} = E$

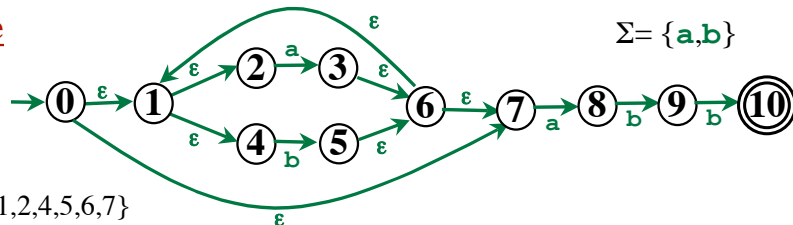
Process  $E = \{1, 2, 4, 5, 6, 7, 10\}$

$\text{Move}_{\text{DFA}}(E, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(E, b) = \{1, 2, 4, 5, 6, 7\} = C$



**Example**



Process  $C = \{1, 2, 4, 5, 6, 7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$

Process  $D = \{1, 2, 4, 5, 6, 7, 9\}$

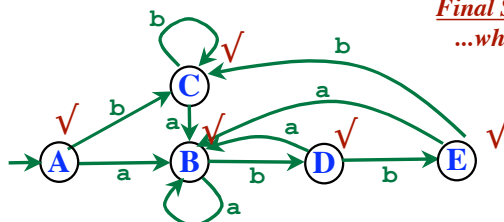
$\text{Move}_{\text{DFA}}(D, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(D, b) = \{1, 2, 4, 5, 6, 7, 10\} = E$

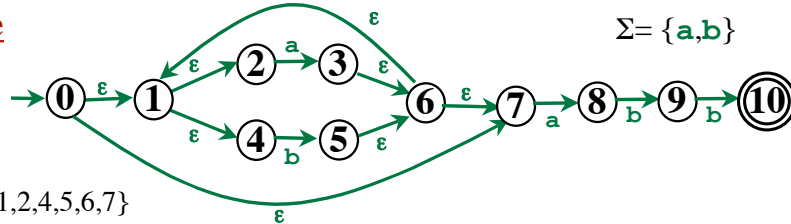
Process  $E = \{1, 2, 4, 5, 6, 7, 10\}$

$\text{Move}_{\text{DFA}}(E, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(E, b) = \{1, 2, 4, 5, 6, 7\} = C$



**Final States in DFA?**  
...which state(s) contain 10?

**Example**

Process  $C = \{1,2,4,5,6,7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1,2,4,5,6,7\} = C$

Process  $D = \{1,2,4,5,6,7,9\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1,2,3,4,6,7,8\} = B$

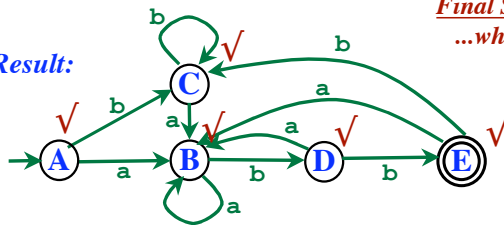
$\text{Move}_{\text{DFA}}(D, b) = \{1,2,4,5,6,7,10\} = E$

Process  $E = \{1,2,4,5,6,7,10\}$

$\text{Move}_{\text{DFA}}(E, a) = \{1,2,3,4,6,7,8\} = B$

$\text{Move}_{\text{DFA}}(E, b) = \{1,2,4,5,6,7\} = C$

**Final Result:**



**Final States in DFA?**

...which state(s) contain 10?

**Algorithm: Convert NFA to DFA**

$S_{\text{DFA}} = \{\}$

Add  $\epsilon$ -Closure( $s_0$ ) to  $S_{\text{DFA}}$  as the start state

Set the only state in  $S_{\text{DFA}}$  to "unmarked"

**while**  $S_{\text{DFA}}$  contains an unmarked state **do**

Let  $T$  be that unmarked state

Mark  $T$

**for each**  $a$  in  $\Sigma$  **do**

$S = \epsilon$ -Closure( $\text{Move}_{\text{NFA}}(T, a)$ )

**if**  $S$  is not in  $S_{\text{DFA}}$  already **then**

Add  $S$  to  $S_{\text{DFA}}$  (as an "unmarked" state)

**endif**

Set  $\text{Move}_{\text{DFA}}(T, a)$  to  $S$

**endFor**

**endWhile**

**for each**  $S$  in  $S_{\text{DFA}}$  **do**

**if** any  $s \in S$  is a final state in the NFA **then**

Mark  $S$  as a final state in the DFA

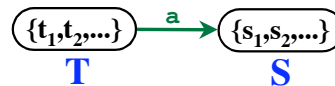
**endif**

**endFor**

A set of NFA states

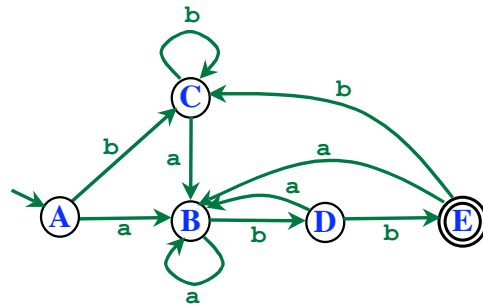
Everywhere you could possibly get to on an  $a$

i.e., add an edge to the DFA...



### Lexical Analysis - Part 3

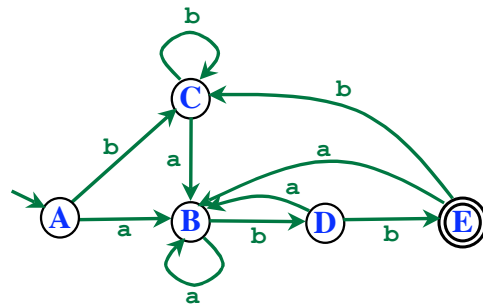
Resulting DFA for  $(a|b)^*abb$



Is it minimal?

### Lexical Analysis - Part 3

Resulting DFA for  $(a|b)^*abb$

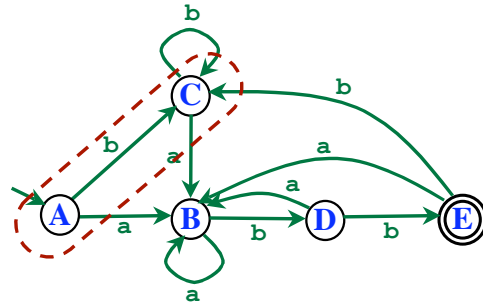


Is it minimal?

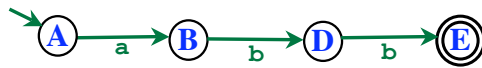


### Lexical Analysis - Part 3

Resulting DFA for  $(a|b)^*abb$

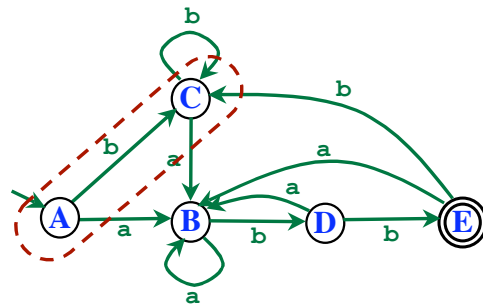


Is it minimal?

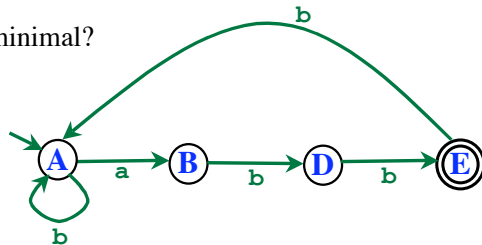


### Lexical Analysis - Part 3

Resulting DFA for  $(a|b)^*abb$

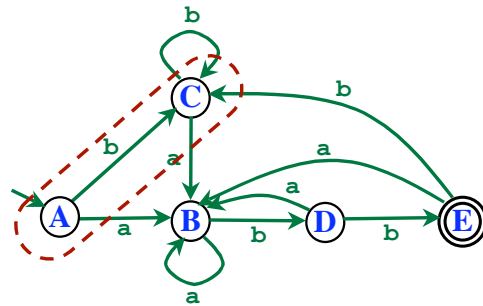


Is it minimal?

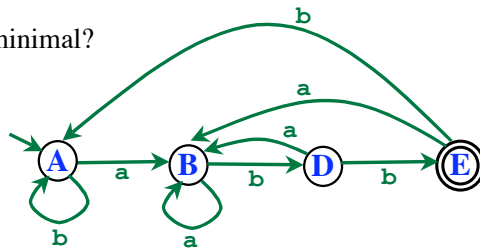




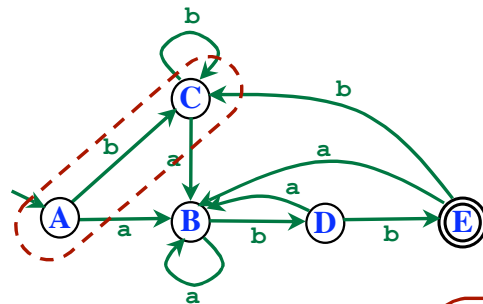
Resulting DFA for  $(a|b)^*abb$



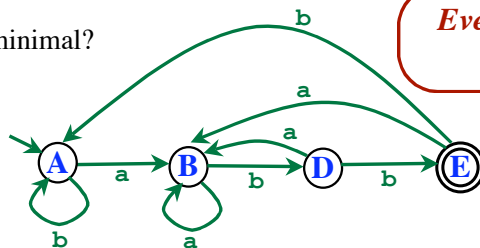
Is it minimal?



Resulting DFA for  $(a|b)^*abb$

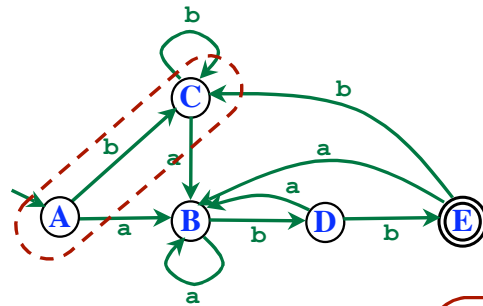


Is it minimal?

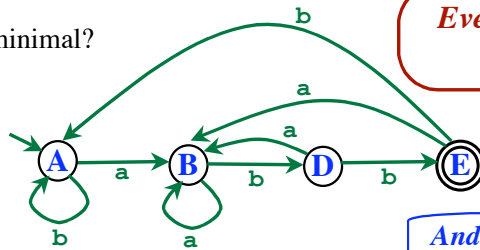


*Every Regular Set is recognized by a minimal DFA!*

Resulting DFA for  $(a|b)^*abb$



Is it minimal?



*Every Regular Set is recognized  
by a minimal DFA!*

*And it is unique, up to renaming of states*