## Universität Duisburg-Essen

#### **BACHELOR THESIS**

# Development and Comparison of Overview Techniques for Extreme Resolution Datasets

Author: Danyun LEI

Supervisor: Prof. Dr. Jens KRÜGER

Examiners: Prof. Dr. Jens KRÜGER Prof. Dr. Josef PAULI

A thesis submitted in fulfillment of the requirements for the degree of Bachelor of Science

in

Computer Engineering International Studies in Engineering (ISE) PO08 Fakultät für Ingenieurwissenschaften

for

The High Performance Computing Group Department Engineering

September 22, 2019

## Versicherung an Eides Statt

Ich, Danyun LEI, versichere an Eides statt durch meine untenstehende Unterschrift,

- dass ich die vorliegende Arbeit mit Ausnahme der Anleitung durch die Betreuer selbstständig ohne fremde Hilfe angefertigt habe und
- dass ich alle Stellen, die wörtlich oder annähernd wörtlich aus fremden Quellen entnommen sind, entsprechend als Zitate gekennzeichnet habe und
- dass ich ausschließlich die angegebenen Quellen (Literatur, Internetseiten, sonstige Hilfsmittel) verwendet habe und
- dass ich alle entsprechenden Angaben nach bestem Wissen und Gewissen vorgenommen habe, dass sie der Wahrheit entsprechen und dass ich nichts verschwiegen habe.

Mir ist bekannt,	dass eine falsche	Versicherung a	n Eides Statt	nach §156	und nach
§163 Abs. 1 des	Strafgesetzbuches	mit Freiheitsstr	afe oder Geld	lstrafe besti	aft wird.

Ort, Datum	Unterschrift

"To see a world in a grain of sand, hold infinity in the palm of your hand. "  $\,$ 

William Blake

#### UNIVERSITÄT DUISBURG-ESSEN

## **Abstract**

Fakultät für Ingenieurwissenschaften
International Studies in Engineering (ISE) PO08
Computer Engineering

Bachelor of Science

# Development and Comparison of Overview Techniques for Extreme Resolution Datasets

by Danyun LEI Matr. No. 2265625 danyun.lei@stud.uni-due.de

In this thesis, three main overview techniques and two secondary preview techniques of the overviews are developed and implemented using the Mandelbrot set as the source of extreme resolution datasets. For these datasets, a hierarchical structure is used to present the index information of the current region of interest. Using the developed software in this thesis, it is possible to intuitively understand the hierarchical state of the current observing area with the whole. This thesis also compares the different overview techniques which in combination consists of six different ways.

It is worth mentioning that the Mandelbrot set that are implemented in this thesis is a very good example for extreme high resolution datasets because it is a dataset that can theoretically provide infinitely high resolution.

The technology stack used in this thesis is pure web technology, a classic combination of HTML / JavaScript / CSS, and the program offers the possibility to adapt and replace the pure front-end technology with front and back end separation solution easily.

# Acknowledgements

Foremost, I hereby express my deep sense of gratitude and indebtedness to Prof. Dr. Jens Krüger, for your valuable guidance, encouragement and support. Your patience and faith in me was a key reason that I could finish the work.

I would like to also express my thanks to Mr. Andrey Krekhov, Mr. Michael Michalski, Mr. Sebastian Cmentowski, and all colleagues in the group who have willingly helped me and offered valuable advices with their excelled abilities.

Also I express my thanks to Prof. Dr. Yunqi Lei, Dr. Bixia Wu and Dr. Franz-Josef Schmitz, in no particular order. Without your support, I could not have finished the task successfully.

# **Contents**

Ve	rsich	erung an Eides Statt	i
Al	ostrac	et e e e e e e e e e e e e e e e e e e	iii
A	knov	wledgements	iv
1	Intr	oduction and Motivation	1
	1.1	Introduction	1
	1.2	Motivation For More Complicated Situations	2
	1.3	Inspirations for the Arrangements of Context Views	5
		1.3.1 Dock And Scrollbar	6
		1.3.2 Stacked Cards	7
		1.3.3 Tabs	7
		1.3.4 Previews Of Contexts	8
	1.4	Related Work	11
2	Bacl	kground	13
	2.1	Web Technology Stack	13
	2.2	Web, HTML5 And Canvas API	14
		2.2.1 Browsers	14
		2.2.2 Markup Language	15
		2.2.3 HTML5	15
		2.2.4 Canvas API	17
	2.3	Mandelbrot Set	17
2	A 4101	hitaatuuni Daalama	21
3		hitectural Designs	
	3.1	Basic Structure	21
	3.2	Front End UI	
	3.3	Back End Resolver	25
4	Imp	lementation	26
	4.1	Files And Folders	26
		4.1.1 Folders	26
		4.1.2 Top Level Files	
	4.2	Start the Project	29
	4.3	Front End	31
	1.0	4.3.1 HTML Entry index.html	31
		4.3.2 Main JavaScript index.js	31
		4.3.2.1 Class MandelWorker	32
			34
		<u>.</u>	3 <del>4</del>
		4.3.2.3 Class MinimapManager	
		4.3.2.4 Class EffectManager	41
		4.3.2.5 Instantiation, Variables and the Rest	41

		4.3.3	CSSs for Overview Effects	42
		4.3.4	Scrollbar + Dock Effect	42
		4.3.5	Stacked Cards Effect	42
		4.3.6	Tabs Effect	42
	4.4	Back E	End Calculation	42
		4.4.1	Global Scope	42
		4.4.2	Message Reception	43
		4.4.3	Iteration Limit	43
		4.4.4	Iteration Count for One Point	43
		4.4.5	Image Generation	43
		4.4.6	High Precision Version	43
	4.5	Utility	Assets	
		4.5.1	Folder ./js	43
		4.5.2	Folder ./fa	44
		4.5.3	Folder ./bs	44
		4.5.4	Folder ./css	44
5	Rest	ılts and	l Comparison	45
	5.1	Genera	al Results	45
	5.2		arison Between Different Arrangement Methods	
	5.3	_	e Work	
A	Freq	uently	Asked Questions	46
	A.1 Where can I find the source code of this project?			46
	A.2		re LATEX source code for this thesis?	
Bi	Bibliography			

# **List of Figures**

1.1	Overview Plus Details On Map	1
1.2	Overview Plus Details In Photoshop	2
1.3	Overview Plus Details In Computer Games	3
1.4	Focus Region Becomes A Dot On Context Region	3
1.5	Multiple Levels of Overview Plus Details	4
1.6	Zoomed-in Fractal Image	4
1.7	Occupied Screen	5
1.8	MacOS Dock	6
1.9	MacOS Dock Hover	6
1.10	MacOS Dock With More Apps	6
1.11	Modern-looking Scrollbar	7
1.12	Means of Arrangements On iOS Safari	8
	How Google Chrome Arranged Objects of Interest	8
1.14	"Preview" Mechanism on Windows 10	9
1.15	Fade-in Effect in jQuery	10
1.16	Moving Preview Plane On Context Views	10
2.1	Mandelbrot Set Graphical Presentation	19
3.1	Basic Structure	21
3.2	Different Reponse Types	22
3.3	A Pair of Focus + Context	23
3.4	Manager of All The F+Cs	24
3.5	Manager of Effects	25
4.1	File Structure	26
4.2	DOM Body Structure	
4.3	Magnification Level	
4.4	Map Visual Pair	
4.5		
4.6	Message Exchange	

# **List of Tables**

# **List of Algorithms**

1	Algorithms for Simple Visualization	18
2	Algorithms for Grayscale Visualization	20

## List of Abbreviations

## **Acronyms**

**API** Application Programming Interface.

**CPU** Central Processing Unit.

**CSS** Cascading Style Sheets.

**DOM** Document Object Model.

**GIS** Geographic Information System.

**GPU** Graphics Processing Unit.

**HTML** Hypertext Markup Language.

**HTTP** Hypertext Transfer Protocol.

IT Information Technology.

JS JavaScript.

JSON Java Script Object Notation.

**LOD** Level of Detail.

**PC** Personal Computer.

**UI** User Interface.

**URL** Uniform Resource Locator.

## Glossary

- **CSS3** In latest evolution of the standard that defines **HTML**, comes together with the extended **CSS**, which is often referred as CSS3..
- **F + C** Focus + context, overview + details, mini-map or **minimap**, same concept as the entry **Map**.
- Full HD 1920 x 1080 px; also known as Full HD or FHD and BT.709.
- HTML5 Latest evolution of the standard that defines HTML.
- **Map** Overview + details, focus + context, mini-map or **minimap**.
- **O + D** Overview + details, focus + context, mini-map or **minimap**, same concept as the entry **Map**.

# **List of Symbols**

- natural number set
- $\mathbb{C}$ C complex number setM Mandelbrot set

Special thanks to Dr. Zhonghua Xu, Ms. Meng Wang and Mrs. Vivian E. Rice, I wish I could share the joy of this achievements with all of you - here or in Azeroth.

## **Chapter 1**

## Introduction and Motivation

#### 1.1 Introduction

In many modern-day applications and computer programs, we may encounter frequently a situation where users have to browse or interact with a large set of data or information, however, only focusing only on a certian part of them. In many situations, this part is usually a lot smaller than the original dataset relatively. The most commonly seen scenario would be a Geographic Information System (GIS) programs on computers, for example an O + D display shown in Figure 1.1 Overview Plus Details On Map. These type of applications usually have a zoomable interface to allow users to zoom into a specific region of the original dataset. Also they usually allow users to browse around the dataset from the current focus region and navigate and interact with the whole large dataset with the sense of the "large picture" by the mechanism of O + D techniques.

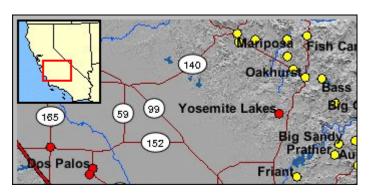


FIGURE 1.1: From http://wildfire.usgs.gov, an overview of the graphics next to a zoomed "detail view".

Other examples besides GIS include also some image processing, image generation applications such as Photoshop shown in Figure 1.2 Overview Plus Details In Photoshop, because usually the resolution of the image being processed or generated are larger than the resolution of one single screen monitor. Another interesting example would be in the modern computer gaming industry, that the concept of *Mini-maps* were invented, illustrated in Figure 1.3 Overview Plus Details In Computer Games, with the same concepts due to the fact that the virtual world of digital games are mostly a lot larger than how much one single screen can contain.

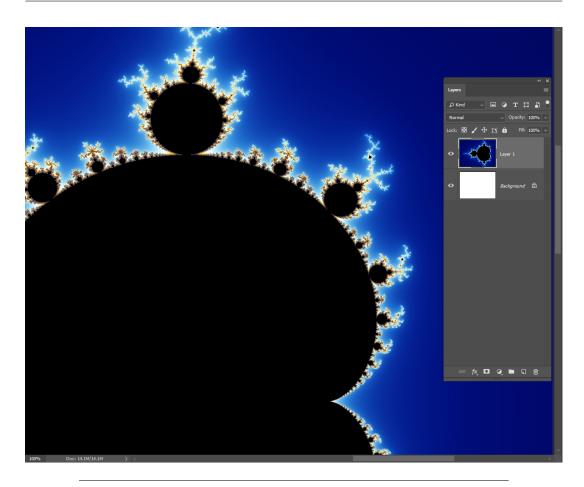


FIGURE 1.2: The basic mechanism in the application Photoshop, layers, offering an overview functionality, with detailed focus area on the main visual area.

Note that the term of *Overview* + *Details* sometimes are also referred to as *Focus* + *Context*, *Mini-map* or some other terms, however, they are referring to a similar techniques or concepts.

## 1.2 Motivation For More Complicated Situations

Most of these techniques and examples above are feasible and can improve how human comprehend the information or datasets is because the whole context area, although larger than how much one screen can hold, comparing to the focus area, is still not so much bigger. If you're looking at a street plan of a city, the focus area can still be visibly represented as a rectangle if the context area is only as large as a city. If you're looking at an image with the resolution of twice as wide and tall as your screen monitor, the focus area still has a quarter of the size of the context area.

However, there are situations when these techniques will not be able to improve our comprehension of the whole dataset in a very good way, that is when the resolution of the original dataset is getting too high and the focus area is zoomed in into an extremely detailed state. That way, the focus region becomes a "dot" instead of a region to be represented on the context view, losing its width and height properties



FIGURE 1.3: The computer game *Freeciv* has a mini-map in the bottom left corner. This is a similar concept as O + D. On this mini-map the white rectangle represents the area of the map currently visible on the main screen. The different colors represent land and ocean and the territories of the different players. The white dots are the position of cities and the blackness are the unexplored areas (the "fog of war")[25].

and stops giving intuitive information. A simple example is shown in Figure 1.4 Focus Region Becomes A Dot On Context Region indicating that when the resolution of the dataset is extreme, new approaches need to be taken in order to let the users able to "grab the whole picture".

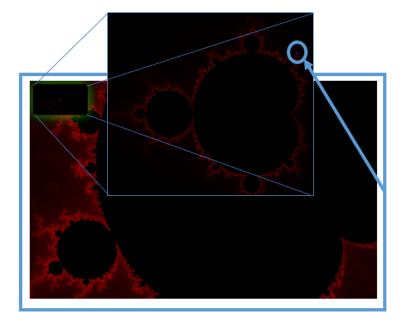


FIGURE 1.4: Traditional O + D techniques stop to provide intuitive information on a highly zoomed-in fractal image.

In these situations, a new level of the O + D techniques is introduced, which is to provide more levels of overviews to the user. Take what's shown in Figure 1.5 Multiple Levels of Overview Plus Details as an example, multiple levels of information of objects are presented as overviews for the users to browse and search. For a similar solution as shown previously in Figure 1.4 Focus Region Becomes A Dot On Context Region, a solution shown in Figure 1.6 Zoomed-in Fractal Image is to give multiple hierarchical overviews to the user to preserve the intuitiveness of the techniques.

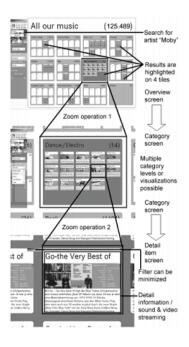


FIGURE 1.5: ZEUS from overview to detail view by zoom in[8].

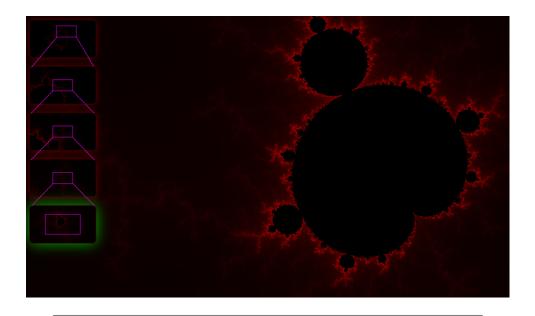


FIGURE 1.6: A graphical representation of Mandelbrot set zoomed in for around 35 thousand times compared to the original.

This solution is straightforward, however, we can still raise questions to push the topic into new levels — what happens when the resolution of the dataset increases even more?

In this case, more overviews need to be added and presented to the users. When more overviews are added providing more Levels of Detail (LODs) and contexts and put to the screen, the original problem emerges again — these overviews are going to occupy a large portion even the entire screen monitor so the most zoomed-in detail area, the most important area of interest, is not going to be easily comprehended or even not able to be seen, as shown in Figure 1.7 Occupied Screen.

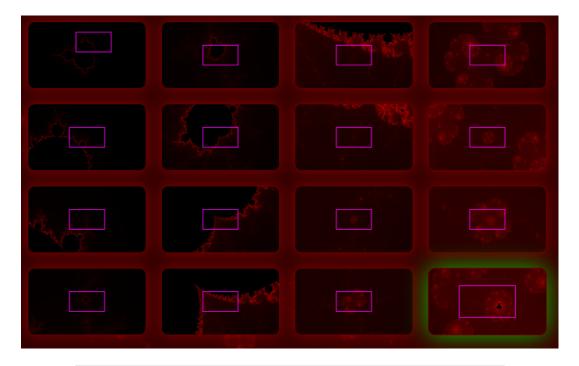


FIGURE 1.7: Too many overviews occupying entire screen monitor.

Therefore, the topic of this thesis is focused on solving this problem, to arrange these overviews in certain ways that they can all provide hierarchies of overviews of information with respect to the original extreme resolution dataset, at the same time, being intuitive enough for human users to understand the LODs as well as the most detailed region with the help of all these arrangements.

## 1.3 Inspirations for the Arrangements of Context Views

As we mentioned above, in order to prevent situations like shown in Figure 1.7 Occupied Screen that all tiled context views occupying the entire focus view from happening, we figured out several ways of arranging these context views, and the inspirations of which came from various ways of how we interact with IT related objects.

#### 1.3.1 Dock And Scrollbar

First thing that came into my mind was the state-of-the-art designs from *Apple*. They invented the concept of macOS Dock or *Dock* as shown in Figure 1.8 MacOS Dock, which can be used as an idea of arranging multiple objects of interest on one screen. Not that as shown in Figure 1.9 MacOS Dock Hover, that it adds an eye-catching visual effect to the current focused object and some other coherent objects.



FIGURE 1.8: Apple gives users the ability to put interested Apps on one side of the screen, which can be the interested contexts in our project.



FIGURE 1.9: When user hovers over an object of interest on the Dock, the Dock can show a visually distinguishable effect.

However, in situations that when user tries to add more interested objects to the Dock, this design only shrinks the sizes of the objects and cannot provide capabilities to embody more objects and advance further, as shown in Figure 1.10 MacOS Dock With More Apps.



FIGURE 1.10: Apple Dock has certain limitations of holding more objects inside.

At the same time, to display more object in a smaller container, there is an obvious way of putting a scrollbar beside it, as shown in Figure 1.11 Modern-looking Scrollbar. Therefore, the first idea of combining a scrollbar together with the visual effects of the macOS Dock were formed.



FIGURE 1.11: An example of using a scrollbar on the side of a container to allow users to browse through more information inside this container.

#### 1.3.2 Stacked Cards

We all browse through different web pages for some information nowadays, and we all had the necessity to keep several web pages open at the same time at some point. The amount of opened websites can easily grow out of hand and how the modern web browsers are handling these web pages of interest can easily catch our attention. The next thing that caught my attention is the *iOS Safari* browser. It is a famous browser installed by default on a popular mobile phone which is a device that has limited amount of space for visual area. How it's displaying the opened web pages are shown in Figure 1.12 Means of Arrangements On iOS Safari.

Visually, they look like cards stacked upon each other. What if we arrange it in a way that this stack of cards can dynamically adjust their positions on screen and the angles they pile up with as their numbers grow? This can be the next good way of arranging these context views of our project.

#### 1.3.3 Tabs

As mentioned before, how browsers arrange the open web pages can be really good examples for our project, therefore, we can't neglect the conventional way of arranging the open web pages on the top of the visual area as "opened tabs", like shown in Figure 1.13 How Google Chrome Arranged Objects of Interest. This is the third idea of cases we make in this project.



FIGURE 1.12: How iOS Safari arranges multiple open web pages on an iPhone.

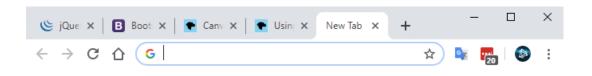


FIGURE 1.13: The way Google Chrome handles the open web pages are to put a so-called "tab" on top of visual area shaped like a tag, with informative titles which sometimes are shortened with ellipsis at the end.

#### 1.3.4 Previews Of Contexts

As shown in Figure 1.6 Zoomed-in Fractal Image, the context views can be relatively small when put to action. Therefore, we need some sort of mechanism to let the user "preview" the shrunk context views, in a similar sense where *Windows 10* users can hover their cursor over the bottom right corner of their screen monitor to have a "glance" of how their desktop looks like shown in Figure 1.14 "Preview" Mechanism on Windows 10, hiding the User Interface (UI) of the current open applications.



FIGURE 1.14: When users hover their mouse cursor on bottom right corner of a Windows PC and have a glance of what is on their Desktop.

A most natural preview setup would be like this, when the user hovers over one of the context view, display an enlarged image in Full HD that shows the context. That is in fact the default setting of this project.

As inspired by the same Windows effect, the second visual effects type becomes a fade-in and fade-out effect. This effect, as shown in Figure 1.15 Fade-in Effect in jQuery, is adding a small transition in the transparencies of the context to be displayed on screen — smoother and can give positive user experience in the comprehension of the F+C problem.





FIGURE 1.15: Illustration of the fadeIn() effect in *jQuery*, a transparency change of objects to be displayed.

Another way of giving previews of the contexts is inpired by some modern graphics and video work, such as a deep zooming video of Mandelbrot set<sup>1</sup> or some special scenes in a movie such as Limitless<sup>2</sup> or Man In Black<sup>3</sup>.

As shown in Figure 1.16 Moving Preview Plane On Context Views, it would be really nice if we implement this visual feature that when user wants to preview one of the contexts, instead of magically showing that context, we show this process of letting the preview image raise or sink from the "current" depths to the "intented" depths of the context. Therefore, this second ways of previewing the contexts got to be implemented into this project.

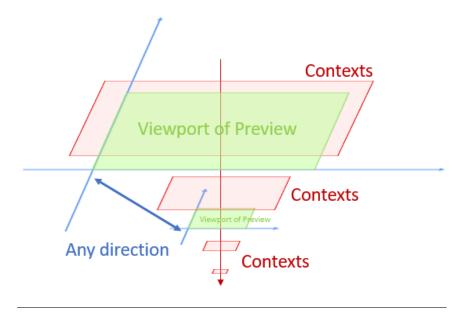


FIGURE 1.16: The viewport of preview is like a plane raising or sinking to the desired depths on the z axis.

<sup>&</sup>lt;sup>1</sup> See https://www.youtube.com/watch?v=pCpLWbHVNhk for more information.

<sup>&</sup>lt;sup>2</sup> See https://www.youtube.com/watch?v=xqv1maJaDtQ&t=37 for more information

<sup>&</sup>lt;sup>3</sup> See https://www.youtube.com/watch?v=OKnpPCQyUec for more information.

#### 1.4 Related Work

There are many researchers who have already done plenty of work related to the topic of O + D, F + C or LOD.

Some researchers did work on a single level of F + C techniques:

Cockburn et al. [4, 5] reviewed and compared O + D, zooming, and F + C interfaces. They described that O + D uses a spatial separation between focused and contextual views, zooming is temporal separation of views and F + C displays the focus within the context.

Hornbæk et al. [11] compared zoomable user interfaces with and without an overview by experiments to understand the navigation patterns and usability of these interfaces. In a later work, Hornbæk et al. [12] extensively reviewed papers that used the notion of overview and developed a model which highlights the awareness that makes up an overview, the process, by which users acquire it, the usefulness of overviews, and the role of user-interface components in developing an overview.

Baudisch et al. considered mainly the technique focus plus context screens.[2] They experimented and compared this technique with the other two techniques overview plus detail and zooming/panning. They noted, for interaction with dynamic views, the technique focus plus context screens alone seems not to be enough and needs an additional monitor. In a related work, Baudisch et al. [1] present the technique focus plus context screens and implemented a system with this technique by combining multiple display units of different resolution. Their means is particularly suitable for situations where all information is shown in only one view and switching between multiple views should be avoided.

Roto et al. [18] developed a Web page visualization method minimap for mobile phones that shows pages in a modified original layout and navigates a Web page with a mini map view.

Gutwin et al. [9] compared three techniques: fisheye, zoom and panning, to find out what is the best ways to redesign a large UI to fit a smaller screen of mobile devices.

Holmquist [10] developed a flip zooming as a new focus+context technique: Mini Pages are placed in a simple left-to-right, top-to-bottom ordering on the display. When a page is brought into focus, it is enlarged and placed approximately in the middle of the display, with the other Mini Pages arranged around it.

There are also some researchers did work related with multiple LODs:

Pan et al. [26] present a summary on the mesh simplification techniques which they used for creating models at multiple LOD. In this paper they also compared typical methods.

Clark [3] proposed hierarchical geometric models for visible surface algorithms for producing computer pictures. He described the benefits of using more than one representation of a model for image rendering and pointed out that objects that cover a small area of the screen can be rendered from a simplified version of the object and that this allows more efficient rendering of a scene.

Crow described the benefits of having both simple and complex representations of an object in his paper on an image generation environment.[6] He gave an example of a chair that is represented in high detail, medium detail and very low detail. These models with three level of detail were created by hand. He suggested that creating the lower levels of detail is a process that should be automated.

Gundelsweiler et al. [8] developed a system of hierarchical information structure. Objects and categories are organized in groups on different hierarchy level visualized as tiles on the screen by the user. The search is supported by zooming/panning navigation.

## **Chapter 2**

# **Background**

In this chapter, we'll introduce some necessary background knowledge in order to let the user understand better how this project came into its form.

Not only the technology stack that this project is using is important to further understanding of this project, but also some theoretical part that's behind them. We'll be introducing them gradually.

### 2.1 Web Technology Stack

Before starting to program on the software that shows the different ways to show an interface providing F + C with many LOD, we must first choose the nature and language of the program. A web technology stack program stands out easily and as a matter of fact, was also the first choice for the development of the immature prototype in the first place. There are several reasons behind it. For web technology stack developed programs:

- Compatibility Code once, it works everywhere. It saves lots of time for users
  and testers to read a long manual. All we need is a working browser with loose
  requirements to it.
- **Simple Installation** Almost nothing to be installed in order to see the project up and running. Besides a browser of some version specifications, only a web server of *any kind* is required, as described in Section § 4.2 Start the Project.
- **Appearance** Can look modern with almost zero code. Can have cool visual effects a lot easier than desktop development.
- **Successful Case** If it works for Google Maps, it should work for our project as well.
- **Performance** Slower in a sense because hardware resources are not easily fetched for browser-based **UI** heavy applications.

On the other hand for desktop development:

- **Compatibility** Really common to be "working on my computer" but not on users'.
- **Simple Installation** Lots of preconditions and require lots of planning before the delivery of a standalone package. If not planned and all aspects chosen

carefully, applications might not work on Macs and gives pop-ups to require "vcredist" dependencies on other operating systems.

- **Appearance** Requires lots of coding to have the most basic appearance. Visual effects need to be programmed manually one by one, not to mention the planning of the software structure.
- **Successful Case** Works also fine with lots of deep zooming applications such as *Ultra Fractal* and *Kalles Fraktaler*.
- **Performance** Can be a lot faster than web applications if choosing *C* / *C*++ or similar languages since they can access directly your hardware resources.

Since this project is focused a lot on the front end UI, web technologies is chosen even when performance can sometimes hinder the advancement of some applications. If planned well, performance on the deep zooming part of the project can be improved by coding techniques and algorithms, however, on the other hand, programming front end UI effects together with planning a good structure to use the advantages of calculation speed of desktop applications would not be productivity efficient.

Some other approaches were also considered, for example to use an intermediate solution like Python because it can be easily structured and coded, however, most of them were not as good choices as web technologies. Taking Python as an example, it cannot do conventional iterations over pixels fast enough unless complicated techniques are used, which actually brings it back on the same level with desktop programming, not to mention the invocation of hardware GPU / CPU resources and fast image manipulations — they all bring lots of complications to the implementation of the project.

### 2.2 Web, HTML5 And Canvas API

After the choice of web technology stack, we'll be talking about the equipments that are used in the project.

Technically speaking, web wechnologies are focused on UI and communications between servers and computers since the computers and servers on the internet can't communicate with each other the way people do, however, the communication part is not hugely focused in this project. First thing to know is that web technology stack includes the markup languages and multimedia packages servers and computers use to communicate, however, it's the markup languages and multimedia packages that we focus on, not the communication part, since the communication involved currently is still on local machines.

#### 2.2.1 Browsers

Web technology runs on browsers. Browsers are the tools that request information and then they show us users in the way we can understand, as the interpreters of the web programs. There are many famous web browsers around:

- Google Chrome Currently the most popular browser by Google
- Safari Apple's web browser

- Firefox Open-source browser supported by the Mozilla Foundation
- Internet Explorer Microsoft's browser

And since Google Chrome has the most popularity and supports all of our requirements for the project, we chose Google Chrome as our browser for the project.

#### 2.2.2 Markup Language

There are some fundamental things for web programming. The first things we need to know about are Hypertext Markup Language (HTML), Cascading Style Sheets (CSS) and JavaScript (JS).

HTML is one of the first thing to be introduced in this section. Thanks to HTML, the browsers can know what to present when we hit them we a request. It is the standard markup language for documents designed to be displayed in a web browser. It can be assisted by technologies such as CSS and scripting languages such as JS.[22]

CSS The technology assisting HTML describes how HTML elements are to be displayed on the screen, if to be put straightforward. It is a style sheet language used for describing the presentation of a document written in a markup language like HTML.[20] CSS is a cornerstone technology of the web technologies, alongside HTML and JavaScript (JS).[7]

**JavaScript** Alongside HTML and CSS, JavaScript (JS) is one of the core technologies of the World Wide Web.[7] JavaScript enables interactive web pages and is an essential part of web applications. The vast majority of websites use it,[19] and major web browsers have a dedicated JavaScript engine to execute it.[23]

#### 2.2.3 HTML5

It is worth mentioning that there is more to the technologies this project is using than the traditional HTML / CSS / JS, which is the larger set — HTML5. HTML5 is the latest evolution of the standard that defines the original. The term HTML5 represents two different concepts:

- It is a new version of the markup language HTML, with new elements, attributes, and behaviors
- A larger set of new web technologies that allows the building of more diverse and powerful applications.

Therefore, this set is sometimes called *HTML5* and friends and often shortened to just HTML5.

There are lots of new features that HTML5 brings to the original HTML, but we're not describing all them there in full<sup>1</sup>. The core features we care about and using in this project are the following two:

<sup>&</sup>lt;sup>1</sup> See https://en.wikipedia.org/wiki/HTML5 to know more details

**Graphics and Effects** Allowing a much more diverse range of presentation options, with respect to 2D / 3D graphics and effects.

**Performance and Integration** Providing greater speed optimization and better usage of computer hardware.

**Styling** Allowing more sophisticated themes and **UI** experience.

Solving exactly the problems of our focus points in this thesis. Some more specific details to each of the above points and their applications in this project will be shortly described.

In the graphics part, the new element <canvas> element that allows delicate drawing on web pages are heavily used.

In the performance and integration part, *Web Workers* are used allowing delegation of JS evaluation to background threads, and allowing these activities to prevent slowing down interactive events. The separation used in the project can also be easily advanced by replacing this multithreading calculation part with the new *XMLHttpRequest* allowing fetching information asynchronously, also allowing it to display dynamic content, varying according to the time and user actions<sup>2</sup>.

In the styling part, since the new CSS in HTML5, CSS3, has been extended to be able to style elements in a much more complex way, many new features of CSS3 are used, such as:

**Background Styling** The possibility to put shadows on elements using box-shadow and CSS filters. These advanced box effects are used in this project for the display of halos of the context views and also internally in the dependencies of this project,  $jQuery^3$  and  $Bootstrap^4$ .

**Animating of Styles** Using CSS Transitions to allow the animation between different states or using *CSS Animations* to animate parts of the page without a triggering event, for example some movement animations of the context views in this project.

**New Presentational Layouts** Two new layouts have been added to CSS3: the CSS multi-column layouts and CSS flexible box layout, and the latter is used in multiple places in this project, for example, the default layouts for the context views and the tabs layouts for the conext views. The dependency *Bootstrap* also relies largely on this new feature.

<sup>&</sup>lt;sup>2</sup> This is the technology behind *Ajax*. To know more information about *Ajax*, see https://en.wikipedia.org/wiki/Ajax\_(programming).

<sup>&</sup>lt;sup>3</sup> jQuery is an open-source, fast, small, and feature-rich JavaScript library. It makes things like HTML document traversal and manipulation, event handling, animation, and Ajax much simpler with an easy-to-use API that works across a multitude of browsers. See https://jquery.com/ for more information.

<sup>&</sup>lt;sup>4</sup> Bootstrap is an open source toolkit for developing with HTML, CSS, and JS. See https://getbootstrap.com/ for more information.

#### 2.2.4 Canvas API

HTML5 brought exciting new advantages to the HTML coding world as mentioned above. Amongst them all, one of the most thrilling one, the new <canvas>, allows us to render delicate graphics powered by JS. We'll be talking about what it is and then the Application Programming Interface (API) that supports its usages.

<canvas> is an HTML element which can be used to render graphics via scripts<sup>5</sup>, here in our project JS. It can, for instance, be used to draw graphs or create simple (and not so simple) animations. In our project, <canvas> is used for the graphical representation of the extreme resolution datasets.

It's also worth mentioning that after first introduced in *WebKit* by *Apple* for the *OS X Dashboard*, <canvas> has since been implemented and supported in all major browsers and today.

The Canvas API itself is a sense of how to use scripts to draw on this newly introduced HTML element. It is largely focuses on 2D graphics. The reason to bring it up here together with the <canvas> element is that there are many other APIs that come together with it, for example the WebGL API, which also uses the <canvas> element, draws hardware-accelerated 2D and 3D graphics. In another word, the context of the <canvas> element<sup>6</sup> is "2d" through the Canvas API, not "webgl" context or any other.

#### 2.3 Mandelbrot Set

As for the datasets themselves, we use a kind of computable dataset instead of a static and deep zoomable image information dataset. The advantage is obvious that by using a dataset that can be computed for its information of any specific point in the set, we don't have to store the information anywhere anymore, as if we did, it would require a lot of investment and investigation for the storage or fetching of the dataset for this project. The downside of it is also clear that we'll have to trade time for space, since the calculation is usually going to take more time than only querying from a static set of data. It is proved to be solid to do this trade, since in this project, the visually inspected results shows that the waiting time is still inside human tolerable margins.

The dataset we chose is the Mandelbrot set. The Mandelbrot set is a famous example of a fractal in mathematics. It is named after Benoît Mandelbrot, a Polish-French-American mathematician<sup>7</sup>. The reason this thesis is using Mandelbrot set as the source of extreme resolution dataset is because Mandelbrot set can provide theoretically infinitely high resolution datasets. In this section, we'll introduce briefly Mandelbrot set, its algorithms ideas for visualization.

 $<sup>^{5}</sup>$  To know about the <canvas> element, see https://en.wikipedia.org/wiki/Canvas\_element.

<sup>&</sup>lt;sup>6</sup> Here not the same concept as the "context" in the previously mentioned term F + C.

<sup>&</sup>lt;sup>7</sup> Its definition and name are due to Adrien Douady, in tribute to the mathematician Benoît Mandelbrot[24].

#### What Is Mandelbrot Set

Firstly, we recursively define a sequence  $(z_n)_{n\in\mathbb{N}}$ ,  $z_n\in\mathbb{C}$  as follows:

$$z_0 = 0 \tag{2.1}$$

$$z_n = z_{n-1}^2 + c, \ c \in \mathbb{C}$$
 (2.2)

For different constant c, the absolute value of  $z_n$  could remain bounded, could also be divergent, if n is increased.

The Mandelbrot set  $\mathbb{M}$  is the set of c in the complex plane for which the sequence  $(z_n)_{n\in\mathbb{N}}$ ,  $z_n\in\mathbb{C}$  remains bounded.

#### Important Properties of the Mandelbrot Set

A property of Mandelbrot set is as follows:

A complex number c belongs to the Mandelbrot set  $\mathbb{M}$ , if and only if the absolute value of  $z_n$  is not larger than 2, for all n = 0, 1, 2, ...

#### Simple Graphical Presentation

The following figure Figure 2.1 Mandelbrot Set Graphical Presentation is a simple graphical representation of Mandelbrot set. A point *c* in the complex plane is conventionally colored *black* if it belongs to the Mandelbrot set M, and *white* if not.

#### Algorithms for Visualization

A simple algorithm is introduced for visualization of black and white in Algorithm 1 Algorithms for Visualization.

**foreach** c in complex plane **do** 

**Algorithm 1:** Algorithms for Simple Visualization

In Algorithm 1 Algorithms for Visualization, the variable *max* can be treated as a constant for each complete cycle of the execution of the algorithm. The larger *max* 

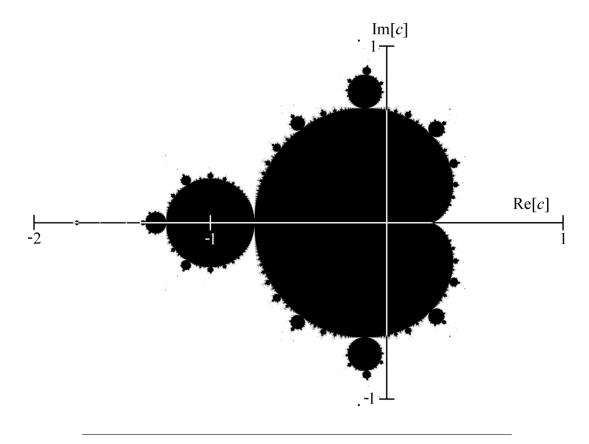


FIGURE 2.1: A simple graphical representation of Mandelbrot set.

is, the more accurate the image generated will be. However, it should not be set infinitely large as a point belonging to the Mandelbrot set will cause the algorithm to loop infinitely. A simple equation is used for the determination of this value *max*:

$$(50 \cdot log_{10} \, magnif)^{1.08}$$
 (2.3)

Where *magnif* is the magnification level, a number representing the number of pixels that together has a length of 1 on the mathmatical axis, shown in Figure 4.3 Magnification Level.

#### Algorithms Idea for Graphical Representation with Grayscale

In the above algorithm in Section § 2.3 Algorithms for Visualization, c is set to either black or white. If the iteration number n is equal to the maximum iteration number m and the value of  $z_n$  still less than 2, then c has the color black. If the iteration number n is smaller than m at then at this moment the absolute value of  $z_n$  becomes larger than 2. In this case, we cannot set the color of c to black, because c dose not belong to Mandelbrot set. However, we set a color with a portion of black, to indicate how close c is to be in black area, as shown in Algorithm 2 Algorithms Idea for

#### Graphical Representation with Grayscale.

Algorithm 2: Algorithms for Grayscale Visualization

The value *max* is determined in the same way as described in Equation 2.3 Algorithms for Visualization.

<sup>&</sup>lt;sup>a</sup> In the current implementation, this color is set to be grayscaled red, rgb( $grayscale\% \times 255, 0, 0$ ).

## Chapter 3

# **Architectural Designs**

Before starting to talk about the implementations of the project, we'll first describe the architecture of the project on a design level, without describing the details on the tech ends.

#### 3.1 Basic Structure

The basic structure of this project is fairly simple, as shown in Figure 3.1 Basic Structure.

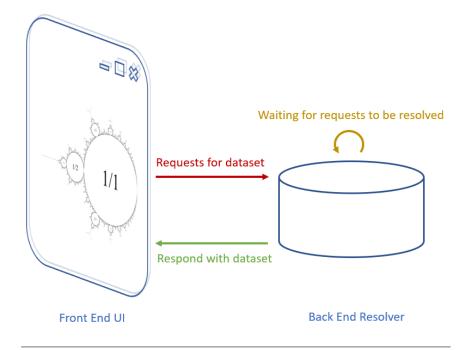


FIGURE 3.1: An illustration of the basic structure of the project, a front end that makes requests and a resolver that responds to the connected front end.

First of all, a front end UI that organizes the content of the project, handling user interactions and so on, and making requests when some actual data of the extreme resolution dataset is needed.

Secondly, a back end resolver that resolves the requests coming from the connected front end, through necessary methods such as fetching an image from the database

or calculate some values out of an equation. In the current state, however, this back end resolver should "resolve" the "problem" by calculation and not data fetching, calculating a portion of the dataset Mandelbrot set. It should return an image as an answer together with some necessary parameters so the front end can verify and use them as either a complete result image or as a intermediate buffer image, as shown in Figure 3.2 Different Reponse Types.

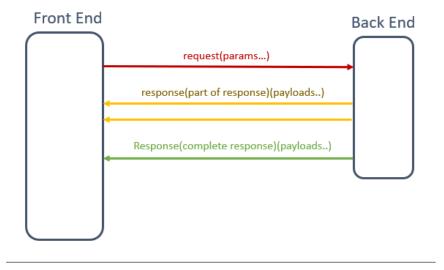


FIGURE 3.2: Responses of different types that the resolver can answer to the front end.

#### 3.2 Front End UI

For starters, the front end should consist of three major parts: models of the F + C, a manager to manage all these F + Cs and a effect manager to manage the effects to be displayed and some other UI interactionss and controls from the user which in turn results to more effects.

First of all, let's look at the model of a pair of F + C. This model should represent a tiny manager that manages one focus view together with a context view, as shown in Figure 3.3 A Pair of Focus + Context. It's connected with these two targets and when it's being instructed to send messages to the outside world(not inside front end criteria), requests and receives responses and handle the render event, putting them on corresponding canvases.

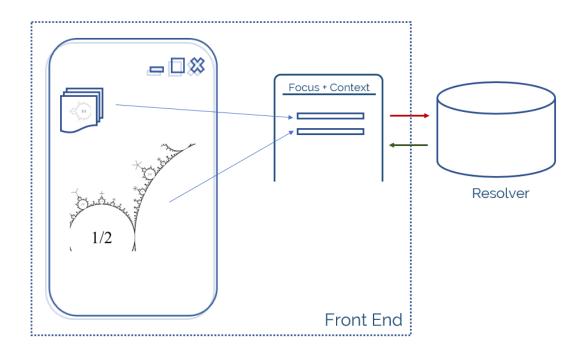


FIGURE 3.3: Model of a pair of **F** + **C**, a tiny manager that connects a focus view(the one in the center of the browser in this illustration) with a context view(the smaller view displaying dataset information), as well as sending pings to the outside.

And then a single instance of that model is not enough, let's look at the manager that manages all generated F + C models shown in Figure 3.4 Manager of All The F+Cs. We can see that this manager should manage the connections between each F + C model with their corresponding canvases, as well as controlling them when to send or receive requests to the outside world, in turn controls the message exchange between the entire front end with the outside world resolver.

Note that from a insider point of view, this manager controls all the message exchange for all the F+C models, however, to the outside world, this resolver is still handling all the different connections like treating multiple clients and don't have knowledge of the presence of this manager. Another thing that worth mentioning is that this manager should also handle the initializations of all the F+C models. Non-effect based UI events should also be handled here as some user interactions like zooming and panning require data exchange between the front end side and the outside world.

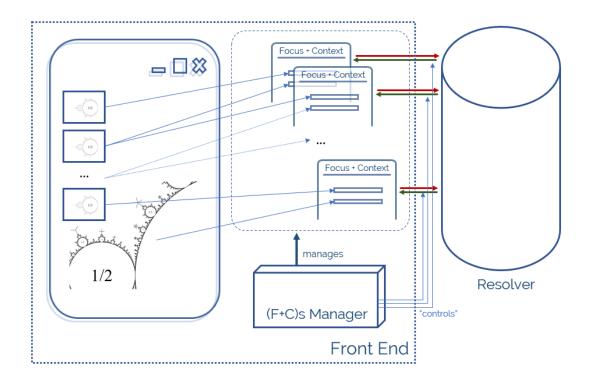


FIGURE 3.4: A manager that manages all the F + C models that are connected properly with corresponding views and outside world, in turn controls the data exchange between the front end  $\overline{UI}$  with outside world.

Finally we need a manager that manages only the visual effects. All related affairs should be within the criteria of not requiring data exchange with the outside world, as shown in Figure 3.5 Manager of Effects. This manager will manage the arrangements of the F + C models but only on the front end, for example the activation / deactivation of effects, the positions and visual effects occurring during these processes, and user interactions with the control panel that triggers rearrangements of the on-screen canvases, and the mechanics of previews.

It is worth mentioning that the preview mechanics, since it being purely on front end, is managed by this effect manager. This manager detects this user interaction when trying to activate one of the previews, and then goes into its storage and find corresponding recorded dataset data, finally instruct corresponding F + C model to render them on the canvas that's for previewing purpose.

#### To summarize:

- Manages F + C models with respect to effects.
- Manages user interactions on F + C models with respect to their context canvases and preview mechanics.
- Manages user interactions on control panels.
- Manages everything else that stays in front end criteria.

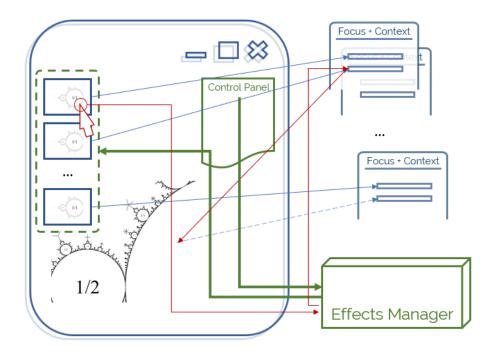


FIGURE 3.5: A manager that manages all effects related routines, including: (green) getting feedback of first hand user interactions from control panel and reflect back to the arrangements of the pile of F + C models; (red) some other user interactions such as mouse hovering event triggering the preview mechanics of putting preview image data onto the browser.

## 3.3 Back End Resolver

As for the back end resolver, it can be fairly simple or can be a complete cluster of servers or supercomputers to solve the response.

In the current state of the project, however, is a relatively simple script that compute for the required dataset with a given solution and location information, and send the results back to the front end, gracefully with the help of modern technology HTML5 introduced in Section § 2.2.3 HTML5.

The structure of it can be narrowed down to three essential part:

- Kickstarting of the idle state.
- Reception of requests, necessary parsing of the requests and sending them to calculation instances.
- Responses during the calculation / fetching process of the extreme resolution dataset, and / or at the end of the calculation / fetching as final results.

## Chapter 4

# **Implementation**

In this chapter, the overall structure of the project, how the files are arranged and the functionalities of each components, will be described in details.

## 4.1 Files And Folders

The folder names and file names are mostly self-explanatory or conventional in this project. They'll be described briefly in this section.



FIGURE 4.1: A glimpse of files and folders.

## 4.1.1 Folders

**Folder** ./.vscode The configured Visual Studio Code workspace settings file. This file is included and stored inside the workspace and only apply when the workspace

is opened which overrides Visual Studio Code's default user settings. The author tweaked this file to make some parts of VS Code's editor, user interface, and functional behavior more fitting to review or to base future work upon this project<sup>1</sup>.

VS Code provides two different scopes for settings:

- User Settings Settings that apply globally to any instance of VS Code you open.
- Workspace Settings Settings stored inside your workspace and only apply when the workspace is opened.

Workspace settings override user settings[13].

**Folder** ./js All the third-party open source JS dependencies are stored in this folder. Sometimes third-party open source projects include a bundle of JavaScript (JS) and CSS files, here only the pure JS projects' files are included.

**Folder** ./css The CSS files of the projects are included. Firstly there is a ./css/common.css file, which sets the overall styles of the project, basically whatever the users can see at the very first glance when they open this project. Then there are several other CSS files, each sets a specific portion of the styles in this project. These files include:

- CSS File ./css/dock.css sets the iOS-Dock look-like styles, making the focused item larger with larger margins and adjacent items smaller and smaller margins with their corresponding nearby items.
- CSS File ./css/minibar.css sets the customed scrollbar styles that's being added upon the default styles of the dependency *MiniBar* which is used to create custom scrollbars.
- CSS File ./css/stacked.css sets the styles of the stacked cards effect.
- CSS File ./css/tabs.css sets the related styles of the tabs effect.

Note that most of the effects require not only the CSS stylings but also JS actions in order to work.

**Folder** ./fa Assets of the dependency *Font Awesome*, including all resources of the open source part. This dependency is used for the fonts of the icons in this project.

**Folder** ./bs Assets of the open source project *Bootstrap* by *Twitter*. This dependency is used for the stylings of the web elements inside the control panel, such as input boxes, dropdown menus and font styles in control panel. It also comes with some nice utilities for general web elements style setting.

<sup>&</sup>lt;sup>1</sup> To learn more about this file, see https://code.visualstudio.com/docs/getstarted/settings.

**Folder** ./node\_modules Packages pulled from the JS dependency management tool  $npm^2$  are stored in this folder. The required dependency here is the package minibarjs under this folder - in folder ./node\_modules/minibarjs. Conventionally this folder shouldn't be included or committed to the version control system<sup>3</sup>, because all the packages info are recorded in the file package.json and package-lock.json and if any dependencies are missing, running the npm command npm install should be able to pull all necessary dependencies into this folder, however, considering this project sometimes can be run in an environment without internet connection, this folder is included in the final static zipped package.

**Folder** ./exp Some trivial *Python*, **JS** and **HTML** codes left from the prototypes of implementation at the beginning of this project. Some of them are using different algorithms and different scripts trying to achieve similar results to this project. They are not in use anymore and only kept for future references.

## 4.1.2 Top Level Files

File index.html This entry HTML file of this project. When a server is being run on the local machine, this is the first file getting executed. When a different implementation of the back end using techniques other than a web worker, for example a WebSocket, is developed and being adapted to this project, double-clicking on this file should also start this project.

File index.js The main JS script file of the project. This file gets included at the very end of the HTML file index.html.

**File** naive-worker.js The back end calculation JS script. The only job of this script is to receive information of the image the front end is asking for, and post the result message back to the front end. This piece of scripts not only post the complete results back, but also slices of results when the calculation takes longer than a certain amount of time and let the front end decide what to do with the partial results<sup>4</sup>.

**File** package.json A description file of the JS package management tool *npm*. This file can have many descriptions about what *npm* should do for this workspace<sup>5</sup> but here it most importantly specifies which packages to pull from the global repository, in the Java Script Object Notation (JSON) field 'dependencies'. Dependencies are specified in a simple object that maps a package name to a version range. The version range is a string which has one or more space-separated descriptors. Dependencies can also be identified with a tarball or git URL[17].

<sup>&</sup>lt;sup>2</sup> Build amazing things — Essential JavaScript development tools that help you go to market faster and build powerful applications using modern open source code[16]. Too know more about *npm*, see https://www.npmjs.com/.

<sup>&</sup>lt;sup>3</sup> This is actually also what this project is following.

<sup>&</sup>lt;sup>4</sup> In this project, what the front end will do after receiving partial results is that it will still render the slices of images onto the canvas and high light the painted partial image with green borders.

<sup>&</sup>lt;sup>5</sup> For for detailed information, see https://docs.npmjs.com/files/package.json.

**File** package-lock.json A generated file from *npm* package manager which locks the version of the dependencies of this specific workspace. Take the current project as an example, in file package.json there is this part in the JSON body:

```
{
    ..
    "dependencies": {
        ..
        "minibarjs": "^0.4.0",
        ..
},
    ..
}
```

This piece of code only specified that the version of the package minibarjs that we require will match all 0.x.x releases including 0.5.x, but will hold off on 1.x.x. This file package-lock.json will "lock" the version inside current workspace to a specific version with a hashed fingerprint of the files, in the current project with a version number of 0.4.0 and a hash fingerprint sha512-iCUE/YVWn+Oht+NV2fLBS8bAVxED/916A5i1qJ20csCrcOtXHamgpWCo7uL+23HQOUyFPvpw1izw213vzVKkXg==.

**File** README.md A brief introduction file for the global version control system *GitHub*. Trivial.

**File** .gitignore Version control settings file, telling which files should not be committed to *Git* system. Not relavant to the project but the version control during the development phase of this project. Trivial.

## 4.2 Start the Project

Although this project is a pure web project, it cannot be started by simply double-clicking on the entry file index.html, because modern browsers usually don't not allow local scripts to directly start *Web Workers*<sup>6</sup> for security concerns. However, *Web Worker* is being used in this project as simple means for doing heavy calculations in background threads without interfering with the UI, therefore, in order to start the project, a simple Hypertext Transfer Protocol (HTTP) server must be up and running on the local machine.

It is also worth mentioning that this project should be running with Google Chrome browser as it supports most of the advanced visual effects and modern web technology syntax, known as  $HTML5^7$ . The recommended version of Google Chrome is 76.0.x.

To start and keep a HTTP server running, the simplest and recommended way would be to use *Python*'s http.server. To do that[14]:

<sup>&</sup>lt;sup>6</sup> Web Workers are a simple means for web content to run scripts in background threads.[15]

<sup>&</sup>lt;sup>7</sup> See https://developer.mozilla.org/en-US/docs/Web/Guide/HTML/HTML5 for more detailed information.

**Install Python** If you are using *Linux* or *macOS*, it should be available on the system already. If you are a *Windows* user, *Python* installer can be downloaded from the *Python* homepage and the instructions can be followed to install it:

- Go to python.org
- Under the *Download* section, click the link for Python 3.xxx.
- At the bottom of the page, choose the *Windows x86 executable installer* and download it.
- When it has downloaded, run it.
- On the first installer page, make sure you check the "Add Python 3.xxx to PATH" checkbox.
- Click *Install*, then click *Close* when the installation has finished.

**Verification** Open a *Command Prompt* (Windows) / *Terminal* (macOS / Linux). To check *Python* is installed, enter the following command:

```
python -V
```

**Navigation** The above command should return a version number. If this is OK, navigate to the directory that the files of this project is inside, using the cd command.

```
# include the directory name to enter it, for example
cd Desktop/fractals
```

**Start the Server** Enter the command to start up the server in that directory:

```
# If Python version returned above is 3.X:
python -m http.server

# Or simply:
py -m http.server

# If Python version returned above is 3.X
# and on non-Windows machines:
python3 -m http.server

# If Python version returned above is 2.X,
# or if on macOS using the default Python
# installed:
python -m SimpleHTTPServer
```

By default, the above actions will run the contents of the directory where the files of this project are located on a local web server, on port 8000. In order to view this project now, simply go to this server by going to the Uniform Resource Locator (URL) localhost:8000 in your web browser, to be specific and recommended in Google Chrome. Here the project entry index.html will be run by default and users can see directly the result.

## 4.3 Front End

Since this project is a pure web project, the front end occupies a large portion of the codes.

## 4.3.1 HTML Entry index.html

The entry of the project is where this program gets started, in similar concept of the main() function in C or the public static void main(String[] args) function in Java. The entry point is a HTML file and as expected named index.html. It introduces the front end structure of the project in raw.

First part of the HTML file is the <head> part. In this part, the character set of this web page is defined as *UTF-8*, the size of the entire HTML document as fullscreen size, scaling not allowed and not shrinking to display its content.

```
<meta charset="utf-8">
<meta name="viewport" content="width=device-width,
    initial-scale=1, shrink-to-fit=no">
```

And then all the needed CSS files are included to end the <head> part. Besides the CSS files which will be described in Section § 4.3.3 CSSs for Overview Effects, the necessary CSS files from third-party open source vendors are also included, including Bootstrap's CSS part, FontAwesome and MiniBar CSS assets.

The <body> part is the essential part of the HTML entry, which describes the structure of what users can "actually see". It begins first with three <div> tags for the most important three parts of this project, the container for main background canvases, the container for mini-maps, and the container for the control panel floating on the top right corner of the UI screen. The positioning, sizes and container behaviours of these <div>s are defined in the CSS files which are already included. Before users set any effects up, these properties mostly come from the file ./css/common.css.

After the visual <div> part, several <script> tags come after it to include what's necessary for the essential coding part. Here firstly are the dependencies of the project, including *jQuery*, *Bootstrap*'s JS part, and *MiniBar*'s JS part. And then at the very end the main JS file index.js is included and all the core programs of this project goes in there.

Worth noting that conventionally all JS files should be included at the very end of the page as what we are doing now, unless the JS file is needed before the render phase of the web page. This way if the JS file is a little bit bigger than usual, the loading of the JS files won't affect the rendering process of the DOM documents.

### 4.3.2 Main JavaScript index. js

The main JS file index.js is where the core codes are. In this file there is firstly the definition of required classes from bottom level to the top, then the instantiation of them and putting the front end HTML elements into action to display the overall results.

There in total four classes defined.

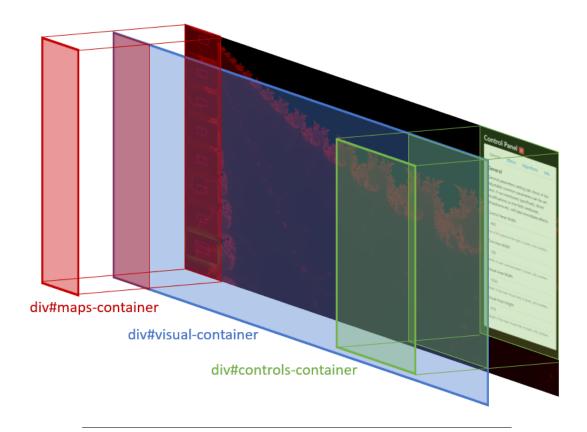


FIGURE 4.2: Document Object Model (DOM) structure in <body> tag.

#### 4.3.2.1 Class MandelWorker

The class MandelWorker is in charge of sending a message to the back end and when a result is sent back, handle it by executing a preset function(or say callback). This class is the red and green arrows shown in Figure 3.3 A Pair of Focus + Context.

When instantiated, an instance of a native *Web Worker* will also be created as a private property of this class. MandelWorker instantiates the *Web Worker* by the script naiveworker.js, which means that the script naiveworker.js will be the core of the worker and this worker will be doing whatever in that script when it is asked to<sup>8</sup>.

#### Function work (params...)

The function work(params...) is the interface between MandelWorker and the outside invoker. To get an image from the source, one must invoke this function with the needed parameters as follows:

- magnif The magnification level of the result image to be expected from the Web Worker.
- centerX The x component of the center coordinates on the mathmatical plane of the result image to be expected from the worker.
- centerY The y component of this coordinates.

<sup>&</sup>lt;sup>8</sup> See https://developer.mozilla.org/en-US/docs/Web/API/Web\_Workers\_API/Using\_web\_workers#Spawning\_a\_dedicated\_worker for more detailed information of the process of instantiating a *Web Worker*.

- width The width in pixels of the result image.
- height The height in pixels of the result image.
- callback The function to execute when a result message is received.
- callbackThis The "this" context where the callback function should be executed under.

Here what's worth mentioning is the parameter magnif. The magnification level is a number representing the number of pixels that together has a length of 1 on the mathmatical axis. As shown in Figure 4.3 Magnification Level is an image with the magnification level of 2, since 2 pixels have the length of 1 on the mathmatical axis.

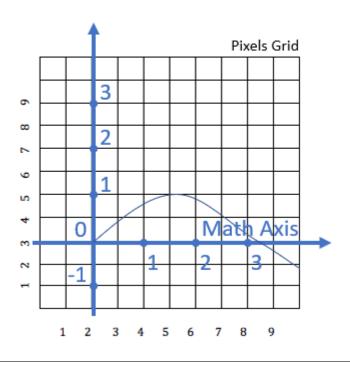


FIGURE 4.3: Magnification level in aspect of mathmatical axis.

Once this function is invoked, MandelWorker will tell its own Web Worker to start working on datasets fetching<sup>9</sup>, and if any sorts of results come through that worker, hit the workerResponse(e) function of the current MandelWorker.

## Function workerResponse(e)

The function workerResponse(e) will be called when a response from the Web Worker is sent back. It basically does one thing: checking if the parameters of callback and callbackThis were set when function work(params...) got invoked in the first place. If they were set to any function, call it under the conext of the parameter callbackThis.

#### Function destroy()

The function destroy() as the name implies is the method to destroy and release the resources for current MandelWorker. It terminates the Web Worker, sets the response

<sup>&</sup>lt;sup>9</sup> In the context of the current project, is actually image generation.

method to null so no responses will be dealt furthermore and sets all other references to null as well so the internal JS engine can garbage collect<sup>10</sup> all these instance to avoid memory leakage when the calculation gets heavy.

## 4.3.2.2 Class MapVisualPair

An abstract concept of pairing a minimap  $^{11}$  with an active focus region with higher resolution, as Figure 4.4 Map Visual Pair is an example of what they actually are respectively. This class is realizing the model of a pair of F + C shown in Figure 3.3 A Pair of Focus + Context.

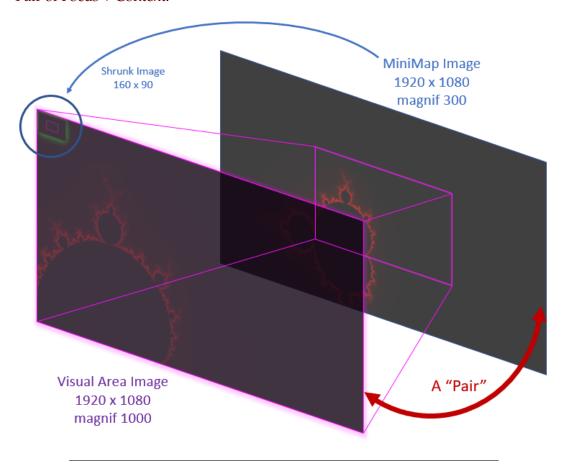


FIGURE 4.4: Map area image and visual area(current focus region) image.

The minimap representing a relatively "larger" area in the dataset and the visual area, which represents the active observing region, actually have both same resolution so they can both be displayed on a Full HD screen. Although the visual area seems "smaller" in comparison with the Map area, since it's an active region that is being observed by the user, the size of this visual area only represents its dimensions on the mathmatical plane and not smaller pixels-wise.

<sup>&</sup>lt;sup>10</sup> In computer science, garbage collection (GC) is a form of automatic memory management. The garbage collector, or just collector, attempts to reclaim garbage, or memory occupied by objects that are no longer in use by the program[21].

<sup>&</sup>lt;sup>11</sup> Same concept in current project as an *overview*.

The Map image, however, will normally be shrunk and put on the left side of the screen, till the user hovers over a specific Map that will trigger the preview process of this program so he can have a glance of this image in a Full HD way.

The reason to pair up a visual area with a Map area is that whenever the user wants to browse around the dataset, the focusing coordinates on the visual area should also reflect back to the Map area, and the rectangle representing the current observing area should also get updated automatically. When there are more hierarchies of Maps present, this pairing mechanism becomes extremely helpful because the changes on the active region will flow all the way up to all levels of Maps necessary. Here Figure 4.5 Pairing Multiple Levels of Maps is a simple illustration of it.

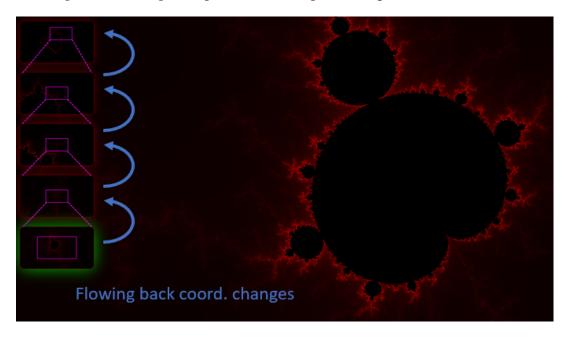


FIGURE 4.5: When multiple hierarchies of Maps present, visual area changes, all Maps changes.

Function init(mapCanvas, previewCanvas, visCanvas = null)

This function will initialize the current MapVisualPair, bounding a mapCanvas, a previewCanvas and a visCanvas all of type <canvas> element to this class. When internally a drawing action should be performed, related images will be drawn on corresponding canvas.

The canvas mapCanvas will be used to draw the shrunk version of the Map image. previewCanvas will be used to draw the normal(Full HD) version of the Map image. And visCanvas will be used to draw the visual area image in Full HD if set.

After bounding the canvases, this function will also check if any event handlers are bound to the events mouseover and mouseout to the mapCanvas element, and record corresponding info to the element to avoid attemps to rebound event handlers to the same <canvas> element. In this way, only one event handler for mouseover and mouseout will be triggered when the user hovers their mouse on the <canvas> and when the user put their cursor out of the element.

The handlers this function is going to bound to the mapCanvas element are going to first add CSS class .nearby to adjacent siblings of this canvas, and check if any additional callbacks this class should call. The callbacks, if any, which are set in the private properties mouseOverCallback and mouseOutCallback, will be called under set context mouseOverCallbackThis and mouseOutCallbackThis when user performs corresponding actions. As mentioned before, they will also be called only once because the bounding information is recorded. In the project, these callbacks and the contexts of them are set by a manager class Section § 4.3.2.4 Class EffectManager.

### Function destroy()

This function as the name implies releases all in-use resources, including Workers, unbinding bound event handlers, clearing references to the canvases and their 2d contexts.

```
Function drawMapHoverArea(offsetRealX = 0, offsetRealY = 0)
```

When the class is told to draw images on corresponding canvas elements, it will not automatically draw the purple rectangle indicating the current observing visual area, since the cached image data does not include this rectangle — it doesn't belong to the extreme resolution dataset itself, therefore, this function exists to draw this current focus area using a purple rectangle to indicate it, drawing this rectangle on the mapCanvas whenever invoked. Note that whenever the image from the calculation side is fetched, without invoking this function, no current obeserving area rectangle will be shown, since the newly fetched image data will cover the old one also the old drawn rectangle.

The parameters offsetRealX and offsetRealY can also be set, as the purple rectangle to be drawn will then have an offset of (offsetRealX, offsetRealY) with respect to the center of the current observing area on the mathmatical complex plane.

```
Function drawPreviewHoverArea(offsetRealX = 0, offsetRealY = 0)
```

Like the function drawMapHoverArea, this function will also draw a rectangle representing the current observing visual area, but on another canvas previewCanvas. The reason to separate these two functions is that the canvas previewCanvas isn't always visible and if these two functions are combined, it'll draw unintended purple rectangles on wrong canvases.

```
Function moveTo(x = null, y = null)
```

This function is used to move the current MapVisualPair around. The parameters of coordinates are on the mathmatical complex plane, i.e. with respect to the entire datasets.

Note that these two parameters can be omitted and when omitted, the current MapVisualPair will simply send a ping to the calculation side and grab new image data for current observing coordinates, like a "refresh" action.

#### Properties visMagnif and mapMagnif

The magnification for the pair of these two canvases. See Figure 4.3 Magnification Level for the explanation of magnification level.

## Properties visCenterX and visCenterY

The coordinates of the center point of the current observing visual area, with respect to the mathmatical complex plane.

## Properties visCanvasWidth and visCanvasHeight

The width and height in **pixels** of the image data of the whole visual area. In Figure 4.4 Map Visual Pair, they're the dimensions of the whole visual area image. These properties have to exist because the dimensions of this area cannot always be fetched from the visCanvas property, as it is an optional parameter during the init(params..) phase and sometimes is absent.

## Properties visImgOffsetX and visImgOffsetY

These two properties are set for the dragging actions that are realized in Section § 4.3.2.3 Class MinimapManager. They represents the current dragging offset with respect to the top left corner of the visCanvas. The reference point being top left corner not the center point is because in web canvas drawing system, the (0, 0) point is the top left corner, unlike in mathmatical complex plane it being the center.

## Properties mapCenterX and mapCenterY

Like the properties visCenterX and visCenterY, these two properties represents the coordinates of the center point of the current Map area, with respect to the mathmatical complex plane. In Figure 4.4 Map Visual Pair, they're the center coordinates of the Map image.

## 4.3.2.3 Class MinimapManager

The manager class of all the minimaps, controlling all their behaviours on the top level. This class is described in Figure 3.4 Manager of All The F+Cs, the manager of all the F + C models, plus a Full HD visual area.

#### **Inits**

Function initMaps(visCanvas, previewCanvas, mapsContainer, visualContain
er, hoverX = 0, hoverY = 0)

This function initializes the states of all the MapVisualPairs that should be displayed, as well as initializing its own requird properties.

The properties visCanvas and previewCanvas are the canvases bound to this manager. visCanvas is the canvas for the main visual area and the details image is rendered on this canvas. previewCanvas is the canvas that's initially hidden, but will be shown when the EffectManager described in Section § 4.3.2.4 Class EffectManager instructs, designed for the presentation of the preview images. These two canvases have exactly the same dimensions, covering the entire UI viewport, and on the most bottom layer of the page hence being laid over by the Maps and control panels. previewCanvas in turn lays over visCanvas since when a preview instruction is issued, it has to be displayed over the original visual area.

The property mapsContainer is the container holding all the canvases for the display of Maps. It's bound to this manager during this initialization phase. During this phase, step one, basic DOM structure of one Map, consisting of one <cavans> element and one <span> element for the purpose of showing the magnif number, will be created and appended to this container. The center coordinates of the Map will be from the parameters hoverX and hoverY, and 0 if not designated. The magnif level of

the first Map comes from the variable mapMagnif in the global scope of index.js<sup>12</sup>. Based on the magnif of the first Map and the visMagnif variable defined in global scope, the initial dimensions of the focus area projected on the Map can be calculated.

With the dimensions of the first Map, this manager then decides whether additional Maps are required, based on the results of whether this projected area on Map is too small. If this area is too small, additional DOM structure consisting of one <canvas> and one <span> will be created and appended to the container. The criteria of whether this area is too small is defined by the private property this.minStrokeW<sup>13</sup> of this manager. After the new DOM is created, we then will have two canvases. The first one will be the Map canvas and the one created after the calculation of the projection area will be the "visual" area. These two areas will then be paired up, forming an object of MapVisualPair. The magnif value of the visual area will be determined by the magnif value of the Map area, the minimal dimensions allowed for the projection area preset in this.minStrokeW and the dimensions of the dimensions of previewCanvas.

Since the model of F + C are hierarchical, we can easily see that the new magnif value of the next Map area will be the value of the magnif value of the previous visual area. After the pairing of these two Maps and forming a first MapVisualPair, we can repeat this process described in above paragraph until the projection area on the current Map area is big enough then set in this.minStrokeW. When this happens, we bind the most recent Map canvas with the main visual area canvas and form the final MapVisualPair. This pair is named this.pairMain in this manager.

And the end of the initialization process, we put all these generated MapVisualPairs in an array called this.pairs and also bind visualContainer which holds visCanvas and previewCanvas with this manager. Later this container will be used for the events binding of UI interactions.

## Function initPairMainDrag()

This function is called after the process in initMaps(params..) is complete. It registers necessary event handlers for mouse dragging related events that allows for browsing around the center of the focus view like Google Maps, including:

- pairMainMouseDown(e) is bound with what was set in visContainer property, responding to single mouse pressing event without releasing the button.
- pairMainMouseMove(e) is bound with what was set in visContainer property, responding to single mouse moving event without releasing the button.
- pairMainMouseUp(e) is bound with what was set in properties visContainer
  or anywhere on the web page, responding to single mouse button releasing
  event.

All the handlers are bound under the context of the current class, a.k.a this or MinimapManager.

#### Function initPairMainWheel()

 $<sup>^{12}</sup>$  Technically not the global scope of entire <code>index.js</code> file per se, but the "global scope" of entire anonymous function that envelops all the codes.

<sup>&</sup>lt;sup>13</sup> In pixels.

This function can be called after the process in initMaps(params..) is complete. In the project it is called after initPairMainDrag(). It registers necessary event handlers for mouse wheeling related events that allows zooming into the dataset on the fly like Google Maps. It binds the event handler pairMainWheel(e) to the mouse wheel event with the root document of the web page, which means when user tries to scroll the middle button of thier mouse, this handler will be triggered.

This handler is also bound under the context of the current class, a.k.a this or MinimapManager.

## Handlers and Functions Related with Mouse Dragging

#### Function pairMainMouseDown(e)

As mentioned before, this function handles the event when user presses the left mouse button before releasing it.

When this event happens on the target, we first records the current position of the user's cursor on the attributes dragStartX, dragStartY, dragCurrentMouseX and dragCurrentMouseY, and use window.requestAnimationFrame(callback) to activate an animation with max frame rates allowed. The callback parameter in window.requestAnimationFrame(callback) is the method pairMainStepDrag(timestamp) of this manager and will be called every time when a new frame should be rendered to the screen and we use this mechanism to repaint the dragged image of the current focus area in the correct place.

This function also sets a dragGlobalID property to the class to mark that this process has been marked started.

#### Function pairMainMouseMove(e)

This function handles the situation when the user, while not releasing the left mouse button, moves the mouse around.

This function does one simple thing: if the dragGlobalID attribute is set on the class meaning the process of mouse dragging being started, set the current postion of user's cursor to the attributes dragCurrentMouseX and dragCurrentMouseY to be used by pairMainStepDrag(timestamp).

#### Function pairMainStepDrag(timestamp)

During the phase of dragging, since this function is triggered every time a new frame is needed to be rendered, we simply grab the values in dragCurrentMouseX and dragCurrentMouseY, and compare them with dragStartX and dragStartY, and see how much the user has moved their mouse since the last frame rendered.

We then paint the image based on the offsets we calculated from these two pairs of values on the correct position.

#### Function pairMainMouseUp(e)

When user releases the mouse button after the series of the previous events, this handler gets triggered.

We repaint the image of the focus area one last time on the correct place, and put this final offset on the properties visImgOffsetX and visImgOffsetY of this.pairMain, and stop the animation using window.cancelAnimationFrame(this.dragGlobalID) with the help of the recorded dragGlobalID.

At this point, new coordinates of the current center of visual view will be calculated and check how many of the MapVisualPairs need updates. All of those that need updates will be instructed to send requests to back end resolver and fetch new image data.

The properties visImgOffsetX and visImgOffsetY are set on this. pairMain so next time when user starts to drag the mouse, the image of the visual area will start from the current offset and not jump back to the initial offset of this drag which is (0, 0), even if the calculation from the resolver hasn't completed yet. This mechanism can be compared with this situation of Google Maps: when user is looking at location A and the loading is completed, and drags the map around and stops at another location B, the map will start to fetch the data around location B. However, if the user refuses to wait and starts to drag again to a new location C, the second drag starts from location B and not location A.

## Handlers and Functions Related with Zooming In and Out

### Function pairMainWheel(e)

This function handles the event when user scrolls the middle button of their mouse.

In this handler, we first check if this process is already ongoing or not.

If this process hasn't been started yet, we set a property wheelCurrentRatio representing how much user has zoomed in to 1, and records the current magnif value of the visual area, visMagnif. We then request a same rendering mechanism trigger by window.requestAnimationFrame and pass on the frame executor pairMainStepWheel (timestamp) to start an animation for zooming in. After that, while the zooming animation of the current visual area image is ongoing, we set a timer of 500 milliseconds that detects if the scrolling on the mouse button is still happening. When the timer hits, meaning within 500 milliseconds the user hasn't scrolled the mouse button, we should consider that user wants to stop the zooming at current depth.

If this process is started already, meaning this process is still ongoing, we only refresh the counter of the timer, and reset it back to 500 milliseconds and let the pairMainStepWheel(timestamp) to keep working on each frames of the animation.

#### Function pairMainStepWheel()

During the phase of zooming in or out of the dataset, this function is triggered every time a new frame is needed to be rendered. We check if the zooming direction is in or out, then repaint the zoomed image and calculate the new visMagnif<sup>14</sup>.

## Function pairMainTimeoutWheel()

If this function gets triggered, it means the timer has timed out and user wants to stop at current depth. Since each frame we have the value of visMagnif calculated, we now have a new magnif value for the visual area in the system.

To make the current system has the clear resolution again, two situation can happen: user has either zoomed deeper into the dataset, or has zoomed out shallower.

When the first situation is the case, we start from the most zoomed in Map, and check whether with its magnif value new Maps are needed. This process is the same as described in initMaps(params...) since we're here also initializing new Maps, adding more to the pile of this.pairs.

<sup>&</sup>lt;sup>14</sup> As mentioned before, the magnif value of the main visual area.

When the second situation is the case, we do the reverse way of the initializing process. If the current projection area is larger than the most zoomed in Map entirely, this Map is no longer needed and needs to be removed. We delete this Map, invoking all the destroy() methods on MapVisualPair and their MandelWorkers, and move one level upper. We stop at the level where the projection area is small enough within one Map, and reconnect the current most zoomed in map with the canvas of the main visual area.

After the increment or decrement of the Maps, MapVisualPair that needs to get updates will be instructed to send requests to resolvers.

## 4.3.2.4 Class EffectManager

This class manages the behaviours, activation and deactivation of the overview effects and the preview effects of the overviews.

General functions: init(), getInfo(el)

Fade in / out related functions: fadeMouseOver(e, currentPair), fadeMouseOut(e, currentPair)

Zoom in / out through related functions: zoomMouseOver(e, currentPair), zoomStep(timestamp), zoomMouseOut(e, currentPair)

General preview effects functions: updatePreview(), updateFadePreview(), updateZoomPreview(), destroyPreview()

General overview effects functions: destroy(), update()

Scrollbar + Dock effects specific functions: initScrollbar(), destroyScrollbar(),
updateScrollbar()

Stacked Cards effects specific functions: initStacked(), destroyStacked(), updateStacked()

Tabs effects specific functions: initTabs(), destroyTabs(), updateTabs()

#### 4.3.2.5 Instantiation, Variables and the Rest

- screenWidth
- screenHeight
- mapWidth
- mapHeight
- controlPanelWidth
- visMagnif
- mapMagnif
- hoverX
- hoverY
- mainCanvas
- previewCanvas

- \$('#visual-container')
- \$('#maps-container')

### 4.3.3 CSSs for Overview Effects

Folder . /css includes five CSS files, each setting up some visual effects of the project.

File ./css/common.css first sets up all general appearance of the elements on the web page when no parameters or effects are set. File ./css/dock.css sets up the appearance when *Scrollbar* + *Dock* is activated, only the iOS Dock part and file ./css/minibar.css sets up the scroll bar part. File ./css/stacked.css sets up the effects of stacked cards. File ./css/tabs.css sets up the effects of the tab selection on the top.

- 4.3.4 Scrollbar + Dock Effect
- 4.3.5 Stacked Cards Effect
- 4.3.6 Tabs Effect

## 4.4 Back End Calculation

The back end calculation is done in the JS file naive-worker.js. This file is being used for initializing the WebWorkers inside index.js dynamically. Whenever a calculation or extraction for a specific region of a dataset is needed, the main JS file index.js is going to send a message to naive-worker.js with desired parameters and this back end will respond with corresponding image data.

### 4.4.1 Global Scope

In the global scope of this file, the following things were done.

**Includes** The decimal.js dependency is included for high-precision floating points calculation. Default parameters for the dependency is set.

**Constants** Constants of default screen width and default screen height are defined in case the front end doesn't give these parameters.

Canvas An OffscreenCanvas instance is created and instantiated with the dimensions of by default the values of the defined constants. The OffscreenCanvas will be used as the canvas to generate the desired image on, and since it's not being shown on the screen, will occupy less system resources and boost the calculation speed. Corresponding variables is declared after the instantiation, respectively canvas for the OffscreenCanvas itself and ctx as the 2d context of the canvas.

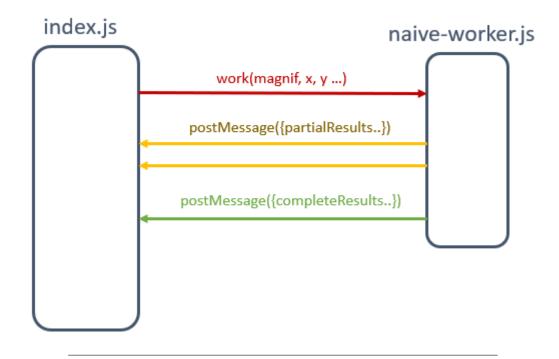


FIGURE 4.6: Message exchange between index.js and naive-worker.js.

## 4.4.2 Message Reception

See Figure 4.6 Message Exchange.

- 4.4.3 Iteration Limit
- 4.4.4 Iteration Count for One Point
- 4.4.5 Image Generation
- 4.4.6 High Precision Version

## 4.5 Utility Assets

Other open source third-party utilities lie in different folders with corresponding names.

## **4.5.1** Folder ./js

In ./js folder, all JS third-party files are here, including:

- File decimal.min.js is for high-precision floating points calculation for JavaScript (JS).
- File jquery-3.4.1.min.js is for DOM traversal and manipulation, event handling and animation.

- File bootstrap.bundle.min.js is for some basic styling of the control panel sitting on top right corner of the screen.
- **4.5.2** Folder . /fa
- **4.5.3** Folder ./bs
- **4.5.4** Folder ./css

# **Chapter 5**

# **Results and Comparison**

- 5.1 General Results
- 5.2 Comparison Between Different Arrangement Methods
- **5.3** Future Work

# Appendix A

# **Frequently Asked Questions**

## A.1 Where can I find the source code of this project?

This source code of the project is hosted on *GitHub* as a private repository on https: //github.com/divyinfo/fractals.git. You could ask the author at danyun.lei@stud.unidue.de for further assitance such as asking for a view or collaboration access.

## A.2 Is there LATEX source code for this thesis?

Yes, it is hosted on *GitHub* as a private repository on https://github.com/divyinfo/fractals-report.git. You could contact the author at danyun.lei@stud.uni-due.de if further assitance is needed.

# **Bibliography**

- [1] Patrick Baudisch, Nathaniel Good, and Paul Stewart. "Focus plus context screens: combining display technology with visualization techniques". In: *Proceedings of the 14th annual ACM symposium on User interface software and technology*. ACM. 2001, pp. 31–40.
- [2] Patrick Baudisch et al. "Keeping things in context: a comparative evaluation of focus plus context screens, overviews, and zooming". In: *Proceedings of the SIGCHI conference on Human factors in computing systems*. ACM. 2002, pp. 259–266.
- [3] James H Clark. "Hierarchical geometric models for visible surface algorithms". In: *Communications of the ACM* 19.10 (1976), pp. 547–554.
- [4] Andy Cockburn, AMY Karlson, and Benjamin B Bederson. "A review of focus and context interfaces". In: *HCIL Tech Report* 2006-09 (2006).
- [5] Andy Cockburn, Amy Karlson, and Benjamin B Bederson. "A review of overview+detail, zooming, and focus+ context interfaces". In: *ACM Computing Surveys* (*CSUR*) 41.1 (2009), p. 2.
- [6] Franklin C Crow. "A more flexible image generation environment". In: *ACM SIGGRAPH Computer Graphics* 16.3 (1982), pp. 9–18.
- [7] David Flanagan. *JavaScript: the definitive guide*. 6 ed. "JavaScript is part of the triad of technologies that all Web developers must learn: HTML to specify the content of web pages, CSS to specify the presentation of web pages, and JavaScript to specify the behaviour of web pages." O'Reilly Media, Inc., 2006, p. 1.
- [8] Fredrik Gundelsweiler, Thomas Memmel, and Harald Reiterer. "ZEUS–zoomable explorative user interface for searching and object presentation". In: *Symposium on Human Interface and the Management of Information*. Springer. 2007, pp. 288–297.
- [9] Carl Gutwin and Chris Fedak. "Interacting with big interfaces on small screens: a comparison of fisheye, zoom, and panning techniques". In: *Proceedings of Graphics Interface* 2004. Canadian Human-Computer Communications Society. 2004, pp. 145–152.
- [10] Lars Erik Holmquist. "The Zoom Browser: Showing Simultaneous Detail and Overview in Large Documents". In: *Human IT: Journal for Information Technology Studies as a Human Science* 2.3 (1998).
- [11] Kasper Hornbæk, Benjamin B Bederson, and Catherine Plaisant. "Navigation patterns and usability of zoomable user interfaces with and without an overview". In: *ACM Transactions on Computer-Human Interaction (TOCHI)* 9.4 (2002), pp. 362–389.
- [12] Kasper Hornbæk and Morten Hertzum. "The notion of overview in information visualization". In: *International Journal of Human-Computer Studies* 69.7-8 (2011), pp. 509–525.
- [13] Microsoft. *User and Workspace Settings*. [Online; accessed 14-September-2019]. 2018. URL: https://code.visualstudio.com/docs/getstarted/settings.

Bibliography 48

[14] Mozilla and individual contributors. How do you set up a local testing server?

- Learn web development | MDN. [Online; accessed 14-September-2019]. 2019.

URL: https://developer.mozilla.org/en-US/docs/Learn/Common\_questions/set\_up\_a\_local\_testing\_server.

- [15] Mozilla and individual contributors. *Using Web Workers Web APIs* | *MDN*. [Online; accessed 14-September-2019]. 2019. URL: https://developer.mozilla.org/en-US/docs/Web/API/Web\_Workers\_API/Using\_web\_workers.
- [16] npm, Inc. npm | build amazing things. [Online; accessed 14-September-2019]. 2019. URL: https://www.npmjs.com/.
- [17] npm, Inc. npm-package.json | npm Documentation. [Online; accessed 14-September-2019]. 2019. URL: https://docs.npmjs.com/files/package.json#dependencies.
- [18] Virpi Roto et al. "Minimap: a web page visualization method for mobile phones". In: *Proceedings of the SIGCHI conference on Human Factors in computing systems*. ACM. 2006, pp. 35–44.
- [19] w3techs.com. Usage Statistics of JavaScript for Websites, March 2018. [Online; accessed 15-September-2019]. 2018. URL: https://w3techs.com/technologies/details/cp-javascript/all/all.
- [20] Wikipedia. Cascading Style Sheets Wikipedia. [Online; accessed 15-September-2019]. 2019. URL: https://en.wikipedia.org/wiki/Cascading\_Style\_Sheets.
- [21] Wikipedia. Garbage collection (computer science) Wikipedia. [Online; accessed 14-September-2019]. 2019. URL: https://en.wikipedia.org/wiki/Garbage\_collection\_(computer\_science).
- [22] Wikipedia. *HTML Wikipedia*. [Online; accessed 15-September-2019]. 2019. URL: https://en.wikipedia.org/wiki/HTML.
- [23] Wikipedia. *JavaScript Wikipedia*. [Online; accessed 15-September-2019]. 2019. URL: https://en.wikipedia.org/wiki/JavaScript.
- [24] Wikipedia. *Mandelbrot set Wikipedia*. [Online; accessed 14-September-2019]. 2019. URL: https://en.wikipedia.org/wiki/Mandelbrot\_set.
- [25] Wikipedia. *Mini-map Wikipedia*. [Online; accessed 14-September-2019]. 2019. URL: https://en.wikipedia.org/wiki/Mini-map.
- [26] Pan Zhigeng, Ma Xiaohu, and Shi Jiaoying. "Overview of Multiple Level of Detail Creation [J]". In: *Journal of Image and Graphics* 9 (1998).