

## Assignment 1 Image Filtering and Hybrid Images

### Part 1

#### 1.1

```
In [1]: import numpy as np

def boxfilter(n):
    #assertion statement for which n is not odd
    assert n%2!=0,"Dimension must be odd"
    #full n*n array with 0.04
    box = np.full((n,n),0.04)
    #sum up every element in the array
    sum = np.sum(box)
    #use the ratio of 0.04 and sum of the array elements
    #as the new array number
    result = box/sum
    return result

#tests
print boxfilter(3)
print boxfilter(5)
print boxfilter(4)

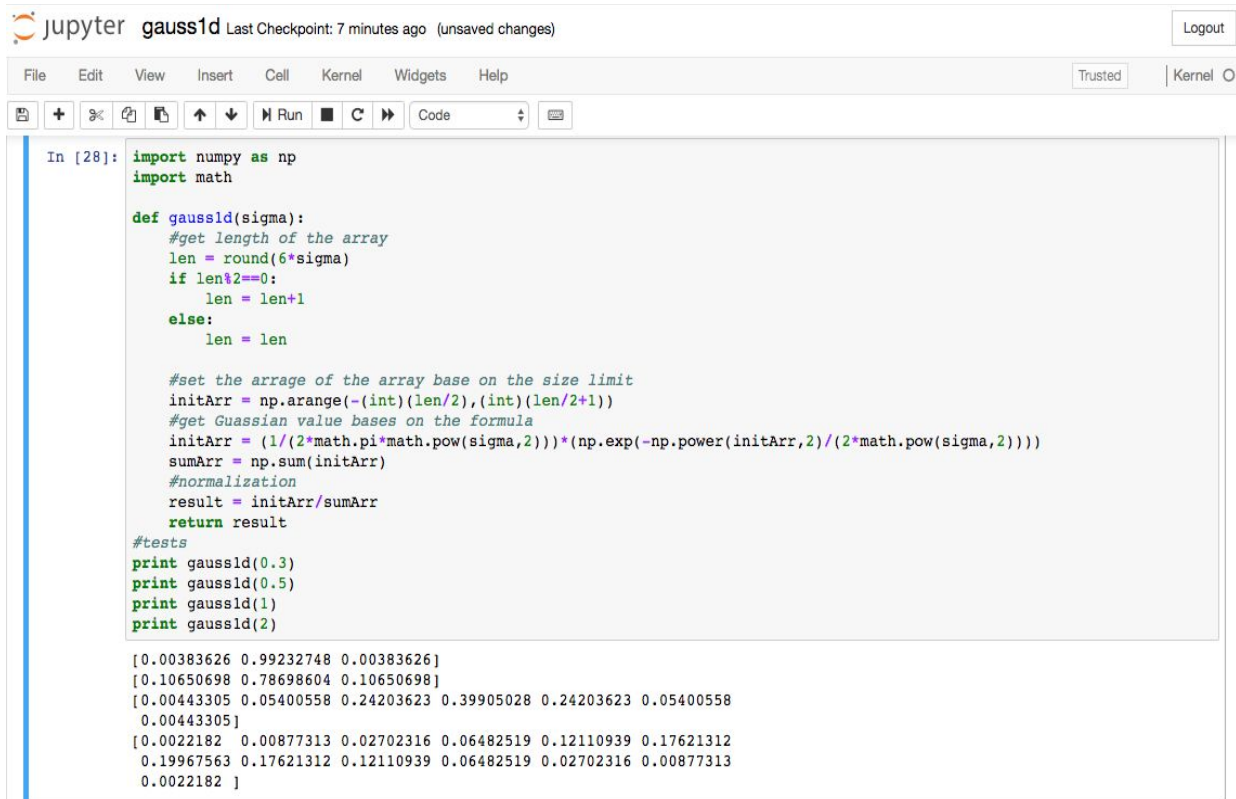
[[0.11111111 0.11111111 0.11111111]
 [0.11111111 0.11111111 0.11111111]
 [0.11111111 0.11111111 0.11111111]]
[[0.04 0.04 0.04 0.04 0.04]
 [0.04 0.04 0.04 0.04 0.04]
 [0.04 0.04 0.04 0.04 0.04]
 [0.04 0.04 0.04 0.04 0.04]
 [0.04 0.04 0.04 0.04 0.04]]

-----
AssertionError                                Traceback (most recent call last)
<ipython-input-1-bfca8b26f6c4> in <module>()
    16 print boxfilter(3)
    17 print boxfilter(5)
----> 18 print boxfilter(4)
    19
    20

<ipython-input-1-bfca8b26f6c4> in boxfilter(n)
     3 def boxfilter(n):
     4     #assertion statement for which n is not odd
----> 5     assert n%2!=0,"Dimension must be odd"
     6     #full n*n array with 0.04
     7     box = np.full((n,n),0.04)

AssertionError: Dimension must be odd
```

## 1.2



The image shows a Jupyter Notebook interface with a single code cell. The code defines a function `gauss1d` that calculates a 1D Gaussian distribution. It takes a `sigma` parameter and returns a 1D array. The function includes comments for each step: getting the array length, setting the array base, calculating the Gaussian value, summing the array, and normalizing the result. Below the function definition, there are four test calls to `gauss1d` with `sigma` values of 0.3, 0.5, 1, and 2. The output of the notebook shows the results of these calls as 1D arrays.

```
In [28]: import numpy as np
import math

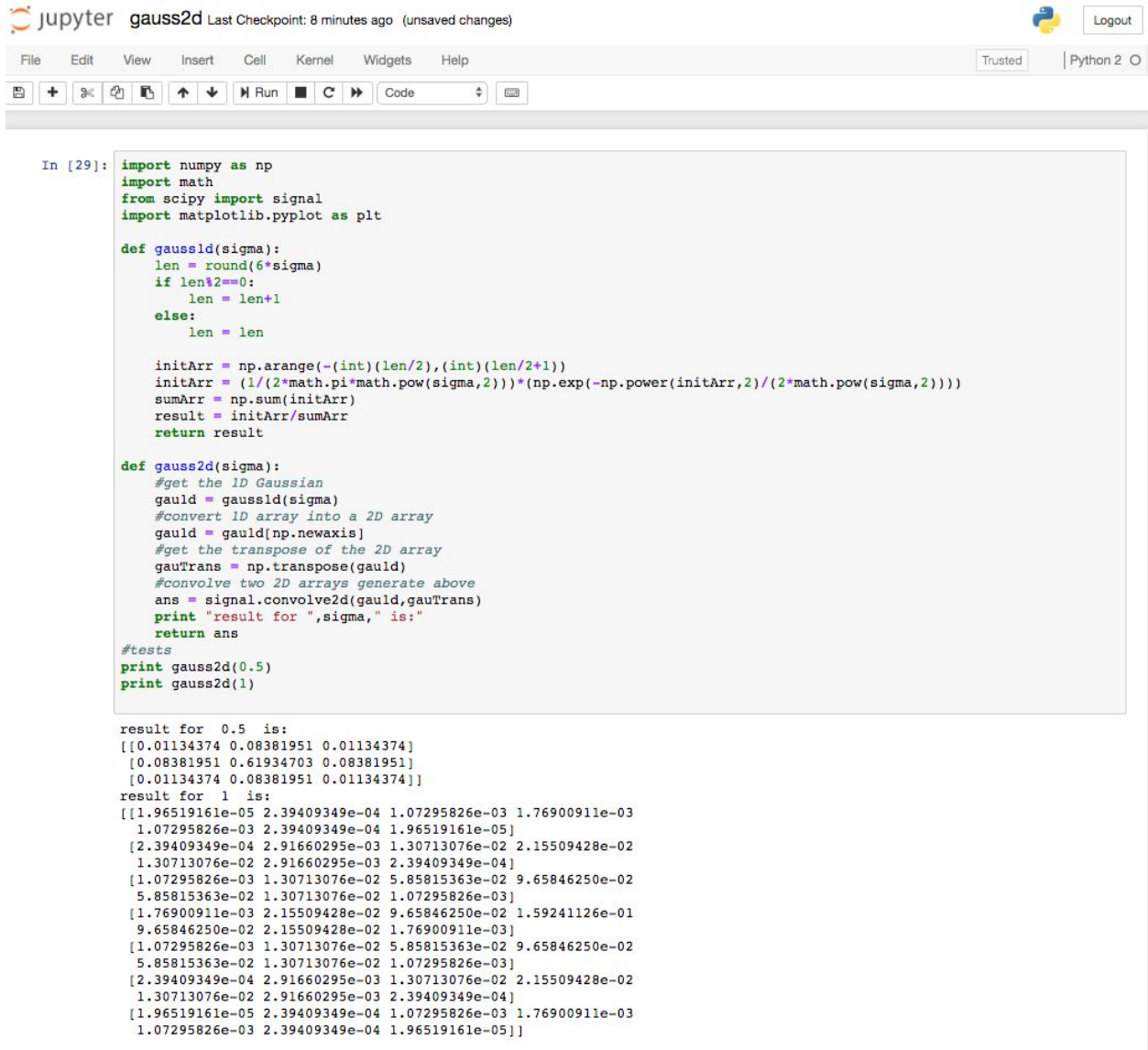
def gauss1d(sigma):
    #get length of the array
    len = round(6*sigma)
    if len%2==0:
        len = len+1
    else:
        len = len

    #set the arrage of the array base on the size limit
    initArr = np.arange(-(int)(len/2),(int)(len/2+1))
    #get Guassian value bases on the formula
    initArr = (1/(2*math.pi*math.pow(sigma,2)))*(np.exp(-np.power(initArr,2)/(2*math.pow(sigma,2))))
    sumArr = np.sum(initArr)
    #normalization
    result = initArr/sumArr
    return result

#tests
print gauss1d(0.3)
print gauss1d(0.5)
print gauss1d(1)
print gauss1d(2)
```

```
[0.00383626 0.99232748 0.00383626]
[0.10650698 0.78698604 0.10650698]
[0.00443305 0.05400558 0.24203623 0.39905028 0.24203623 0.05400558
 0.00443305]
[0.0022182  0.00877313 0.02702316 0.06482519 0.12110939 0.17621312
 0.19967563 0.17621312 0.12110939 0.06482519 0.02702316 0.00877313
 0.0022182 ]
```

## 1.3



The image shows a Jupyter Notebook interface with a single code cell. The code defines two functions: `gauss1d` and `gauss2d`. `gauss1d` calculates a 1D Gaussian distribution for a given sigma. `gauss2d` calculates a 2D Gaussian distribution by convolving two 1D Gaussians. The code includes imports for numpy, math, scipy, and matplotlib. The output shows the results of `gauss2d(0.5)` and `gauss2d(1)`.

```
In [29]: import numpy as np
import math
from scipy import signal
import matplotlib.pyplot as plt

def gauss1d(sigma):
    len = round(6*sigma)
    if len%2==0:
        len = len+1
    else:
        len = len

    initArr = np.arange(-(int)(len/2),(int)(len/2+1))
    initArr = (1/(2*math.pi*math.pow(sigma,2)))*(np.exp(-np.power(initArr,2)/(2*math.pow(sigma,2))))
    sumArr = np.sum(initArr)
    result = initArr/sumArr
    return result

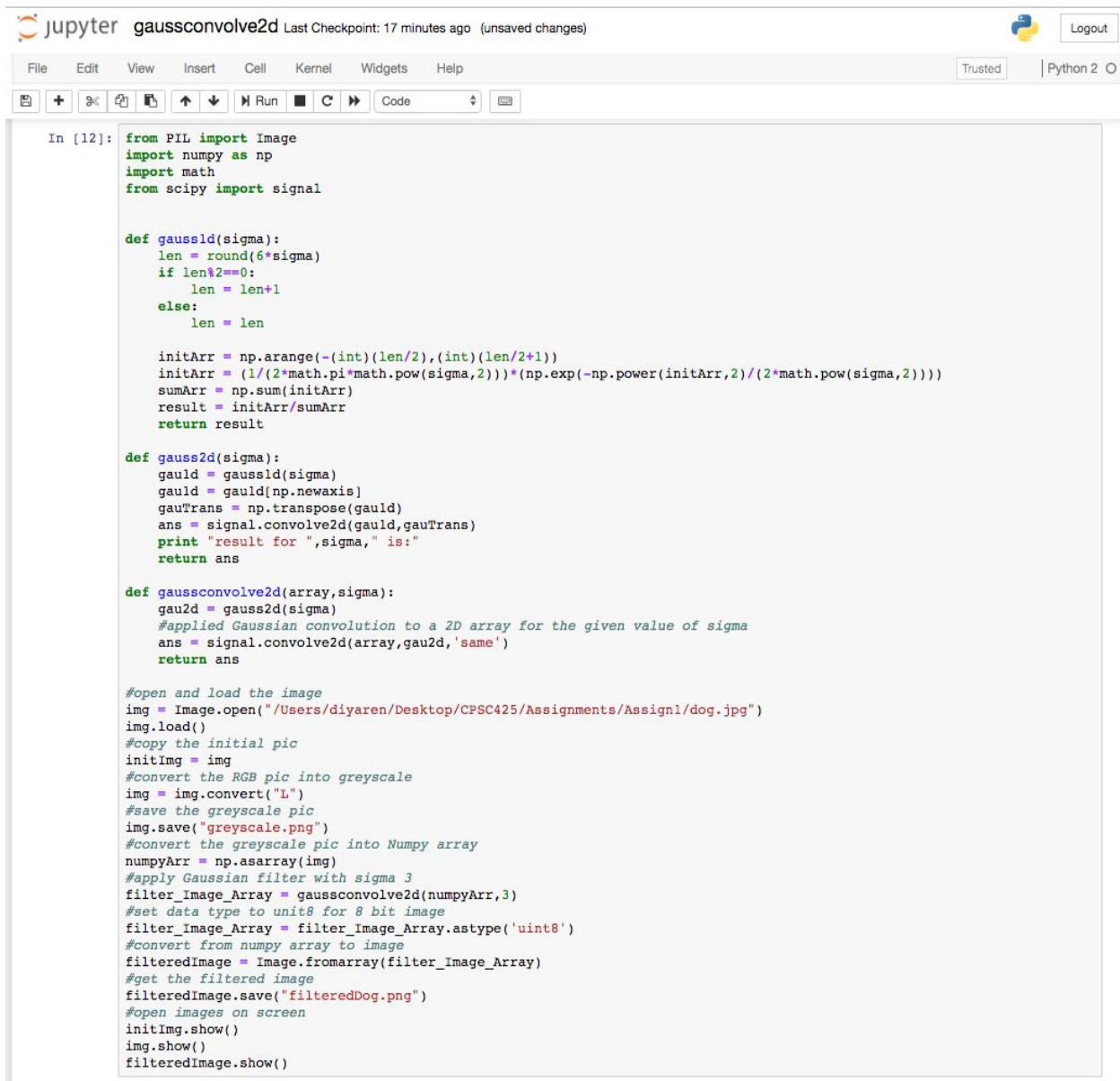
def gauss2d(sigma):
    #get the 1D Gaussian
    gauld = gauss1d(sigma)
    #convert 1D array into a 2D array
    gauld = gauld[np.newaxis]
    #get the transpose of the 2D array
    gauTrans = np.transpose(gauld)
    #convolve two 2D arrays generate above
    ans = signal.convolve2d(gauld,gauTrans)
    print "result for ",sigma," is:"
    return ans

#tests
print gauss2d(0.5)
print gauss2d(1)

result for 0.5 is:
[[0.01134374 0.08381951 0.01134374]
 [0.08381951 0.61934703 0.08381951]
 [0.01134374 0.08381951 0.01134374]]
result for 1 is:
[[1.96519161e-05 2.39409349e-04 1.07295826e-03 1.76900911e-03
 1.07295826e-03 2.39409349e-04 1.96519161e-05]
 [2.39409349e-04 2.91660295e-03 1.30713076e-02 2.15509428e-02
 1.30713076e-02 2.91660295e-03 2.39409349e-04]
 [1.07295826e-03 1.30713076e-02 5.85815363e-02 9.65846250e-02
 5.85815363e-02 1.30713076e-02 1.07295826e-03]
 [1.76900911e-03 2.15509428e-02 9.65846250e-02 1.59241126e-01
 9.65846250e-02 2.15509428e-02 1.76900911e-03]
 [1.07295826e-03 1.30713076e-02 5.85815363e-02 9.65846250e-02
 5.85815363e-02 1.30713076e-02 1.07295826e-03]
 [2.39409349e-04 2.91660295e-03 1.30713076e-02 2.15509428e-02
 1.30713076e-02 2.91660295e-03 2.39409349e-04]
 [1.96519161e-05 2.39409349e-04 1.07295826e-03 1.76900911e-03
 1.07295826e-03 2.39409349e-04 1.96519161e-05]]
```

## 1.4

### Part 1:



The image shows a Jupyter Notebook interface with a single code cell. The notebook title is "gaussconvolve2d" and it shows "Last Checkpoint: 17 minutes ago (unsaved changes)". The interface includes a menu bar (File, Edit, View, Insert, Cell, Kernel, Widgets, Help), a toolbar with icons for file operations and execution, and a status bar indicating "Trusted" and "Python 2". The code cell contains a Python script that defines three functions: `gauss1d`, `gauss2d`, and `gaussconvolve2d`. It then uses these functions to load an image, convert it to grayscale, and apply a Gaussian filter with a sigma of 3. The final filtered image is saved and displayed.

```
In [12]: from PIL import Image
import numpy as np
import math
from scipy import signal

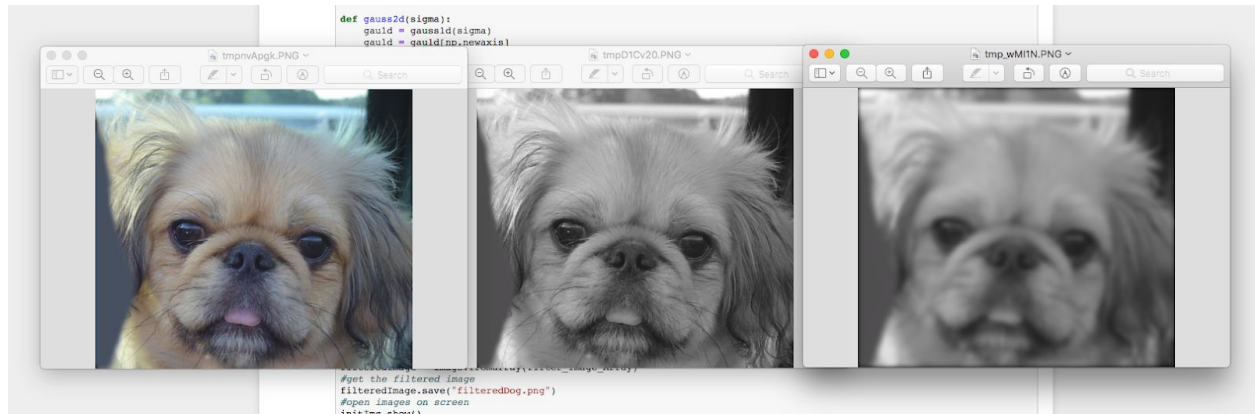
def gauss1d(sigma):
    len = round(6*sigma)
    if len%2==0:
        len = len+1
    else:
        len = len

    initArr = np.arange(-(int)(len/2),(int)(len/2+1))
    initArr = (1/(2*math.pi*math.pow(sigma,2)))*(np.exp(-np.power(initArr,2)/(2*math.pow(sigma,2))))
    sumArr = np.sum(initArr)
    result = initArr/sumArr
    return result

def gauss2d(sigma):
    gauld = gauss1d(sigma)
    gauld = gauld[np.newaxis]
    gauTrans = np.transpose(gauld)
    ans = signal.convolve2d(gauld,gauTrans)
    print "result for ",sigma," is:"
    return ans

def gaussconvolve2d(array,sigma):
    gau2d = gauss2d(sigma)
    #applied Gaussian convolution to a 2D array for the given value of sigma
    ans = signal.convolve2d(array,gau2d,'same')
    return ans

#open and load the image
img = Image.open("/Users/diyaren/Desktop/CPSC425/Assignments/Assign1/dog.jpg")
img.load()
#copy the initial pic
initImg = img
#convert the RGB pic into greyscale
img = img.convert("L")
#save the greyscale pic
img.save("greyscale.png")
#convert the greyscale pic into Numpy array
numpyArr = np.asarray(img)
#apply Gaussian filter with sigma 3
filter_Image_Array = gaussconvolve2d(numpyArr,3)
#set data type to uint8 for 8 bit image
filter_Image_Array = filter_Image_Array.astype('uint8')
#convert from numpy array to image
filteredImage = Image.fromarray(filter_Image_Array)
#get the filtered image
filteredImage.save("filteredDog.png")
#open images on screen
initImg.show()
img.show()
filteredImage.show()
```



Part 2:

Why does Scipy have separate functions 'signal.convolve2d' and 'signal.correlate2d'?

Ans:

Scipy.signal.correlate2d does a matched filtering( cross-correlation) of an N-dimensional signal and a N-dimensional template

Scipy.signal.convolve2d does a convolution of an N-dimensional signal and an N-dimensional kernel.

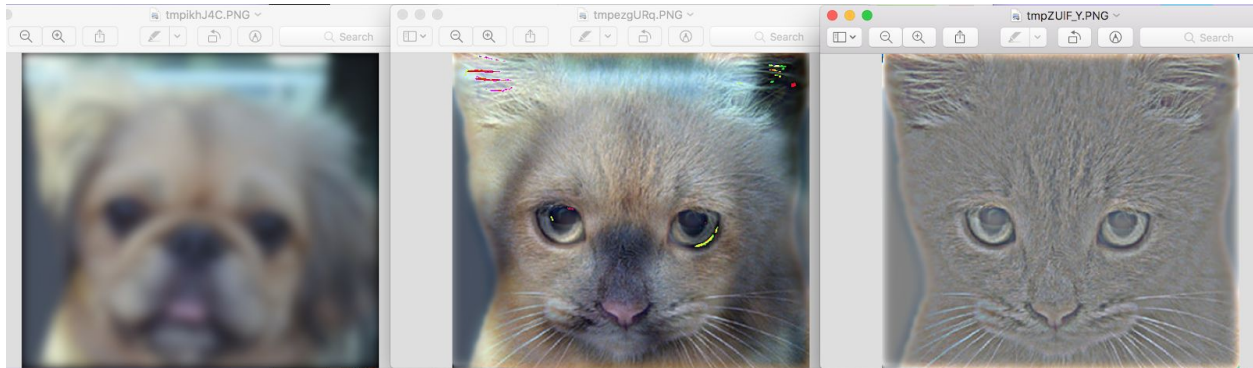
The matched filtering is done by correlating a known signal, or template, with an unknown signal to detect the presence of the template in the unknown signal. Scipy.signal.convolve2d and Scipy.signal.correlate2d will produce the same result only when convolve the unknown signal with a conjugated time-reversed version of the template. So when dealing with other cases, we still need to process them separately using different Scipy functions.

**1.5** Convolution with a 2D Gaussian filter is not the most efficient way to perform Gaussian convolution on an image. In a few sentences, explain how this could be implemented more efficiently taking advantage of separability and why, indeed, this would be faster. NOTE: It is not necessary to implement this. Just the explanation is required. Your answer will be graded for clarity.

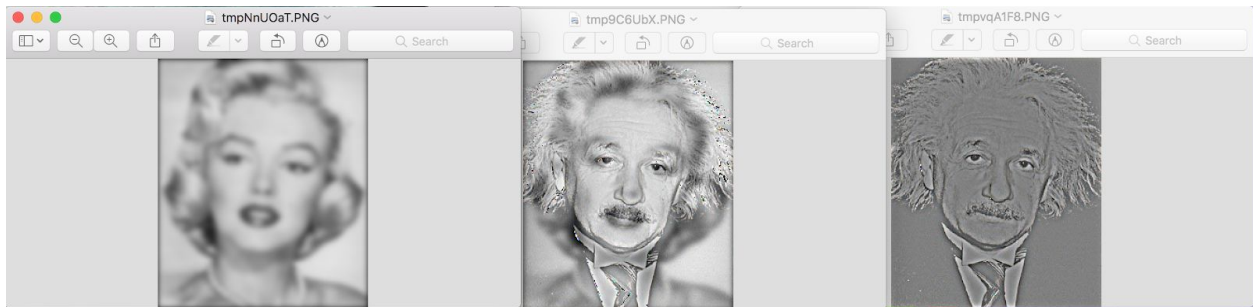
Ans: It is best to take advantage of the Gaussian separable property by dividing the process into two passes. In the first pass, a one-dimensional kernel is used to blur the image in only the horizontal or vertical direction. In the second pass, the same one-dimensional kernel is used to blur in the remaining direction. The resulting effect is the same as convolving with a two-dimensional kernel in a single pass, but requires fewer calculations.

## Part 2

Set 1: use 6 as sigma



Set 2: use 3 as sigma



Set 3: use 1 as sigma

