Design of experiment exercise

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Describing the experiment

I generated a dataset of 25 entries by modifying the 11 xi values and getting the output value corresponding to them. The goal is to get the function F like F(X)=Y, X is a vector of 11 elements. We store it in a csv file library(dplyr)

```
##
  Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
##
  The following objects are masked from 'package:base':
##
      intersect, setdiff, setequal, union
df
##
             x2
                  x3
                                    x6
                                                              x10
        x1
                        x4
                             x5
                                           x7
                                                   x8
                                                         x9
                                                                     x11
     0.101 0.90 0.25 0.1600 0.39 0.3500 0.50000 0.70000 0.800 0.9000 1.0000
## 1
    0.100 0.10 0.90 0.2500 0.16 0.3900 0.35000 0.50000 0.700 0.8000 0.9000
     0.100 0.10 0.90 0.2500 0.60 0.9000 0.35000 0.50000 0.500 0.8000 0.9800
     0.100 0.10 0.00 0.2500 0.60 0.7900 0.34500 0.89500 0.500 0.2000 0.8200
     0.000 0.01 0.00 0.0525 0.06 0.0769 0.01345 0.04895 0.095 0.0182 0.0852
     1.000 1.00 1.00 1.0000 1.00 1.0000 1.00000 1.00000 1.000 1.0000 1.0000
     0.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.000 0.0000 0.0000
     0.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.000 0.000 1.0000
     0.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.000 1.0000 0.0000
## 10 0.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 1.000 0.0000 0.0000
## 11 0.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 1.00000 0.000 0.0000 0.0000
## 12 0.000 0.00 0.00 0.0000 0.00 0.0000 1.00000 0.00000 0.000 0.0000 0.0000
## 13 0.000 0.00 0.00 0.0000 0.00 1.0000 0.00000 0.00000 0.000 0.0000 0.0000
## 14 0.000 0.00 0.00 0.0000 1.00 0.0000 0.00000 0.00000 0.000 0.0000 0.0000
## 15 0.000 0.00 0.00 1.0000 0.00 0.0000 0.00000 0.00000 0.000 0.0000 0.0000
## 16 0.000 0.00 1.00 0.0000 0.00 0.0000 0.00000 0.00000 0.000 0.000 0.0000
## 17 0.000 1.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.000 0.0000 0.0000
## 18 1.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.0000 0.0000 0.0000
## 19 1.000 1.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.0000 0.000 0.0000
## 20 0.000 0.00 1.00 1.0000 0.00 0.0000 0.00000 0.00000 0.000 0.0000 0.0000
## 21 0.000 0.00 0.00 0.0000 1.00 1.0000 0.00000 0.00000 0.000 0.0000 0.0000
```

22 0.000 0.00 0.00 0.0000 0.00 0.0000 1.00000 1.00000 0.000 0.0000 0.0000

```
## 23 0.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 1.000 1.000 0.0000
## 24 0.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.000 1.0000 1.0000
## 25 1.000 0.00 0.00 0.0000 0.00 0.0000 0.00000 0.00000 0.0000 0.000 1.0000
##
## 1
     -0.4281779
## 2
     -0.1386140
## 3
       0.2632307
## 4
       0.2611612
## 5
       0.8832912
## 6
     -0.8763420
## 7
       1.0152508
       1.0145791
## 8
## 9
       1.0131179
## 10 -0.9812617
## 11
       1.0135006
## 12
       1.0130075
## 13
       1.0156932
## 14
       1.0118228
## 15
       2.0126428
## 16
       1.0140150
## 17
       1.0161708
## 18
       0.4207322
       0.4248749
## 19
## 20
       2.0143936
## 21
      1.0154428
      1.0107968
## 22
## 23 -0.9832606
       1.0147940
## 24
## 25 0.4172822
```

First, we figure out that the intercept F(0) is 1.0152508.

We can use a linear regression for a sanity check and we see that we obtain exactly the same result. This linear regression will also allow us to predict.

```
form <- as.formula(paste("y~", paste0("x", 1:11, collapse="+")))</pre>
reg=lm(form,data=df)
reg
##
## Call:
## lm(formula = form, data = df)
##
## Coefficients:
   (Intercept)
##
                                         x2
                                                       xЗ
                                                                      x4
                                                                                    x5
                           x1
##
      1.044933
                   -0.663815
                                  -0.011483
                                                 0.004691
                                                               0.933063
                                                                             -0.039211
##
             x6
                           x7
                                         x8
                                                        x9
                                                                     x10
                                                                                   x11
##
      0.003296
                   -0.050583
                                   0.010876
                                                -1.998210
                                                              -0.026140
                                                                             0.035827
plot(df)
```

